

The projectiles and the targets: cosmic rays, particle accelerators

Cosmic Rays - I

Distinction between “primary” and “secondary” cosmic rays. Primaries are: protons, light Nuclei and γ . (+ others like electrons/positrons...)

Table 28.1: Relative abundances F of cosmic-ray nuclei at 10.6 GeV/nucleon normalized to oxygen ($\equiv 1$) [7]. The oxygen flux at kinetic energy of 10.6 GeV/nucleon is $3.29 \times 10^{-2} \text{ (m}^2 \text{ s sr GeV/nucleon)}^{-1}$. Abundances of hydrogen and helium are from Refs. [3,4]. Note that one can not use these values to extend the cosmic-ray flux to high energy because the power law indices for each element may differ slightly.

Z	Element	F	Z	Element	F
1	H	540	13–14	Al-Si	0.19
2	He	26	15–16	P-S	0.03
3–5	Li-B	0.40	17–18	Cl-Ar	0.01
6–8	C-O	2.20	19–20	K-Ca	0.02
9–10	F-Ne	0.30	21–25	Sc-Mn	0.05
11–12	Na-Mg	0.22	26–28	Fe-Ni	0.12

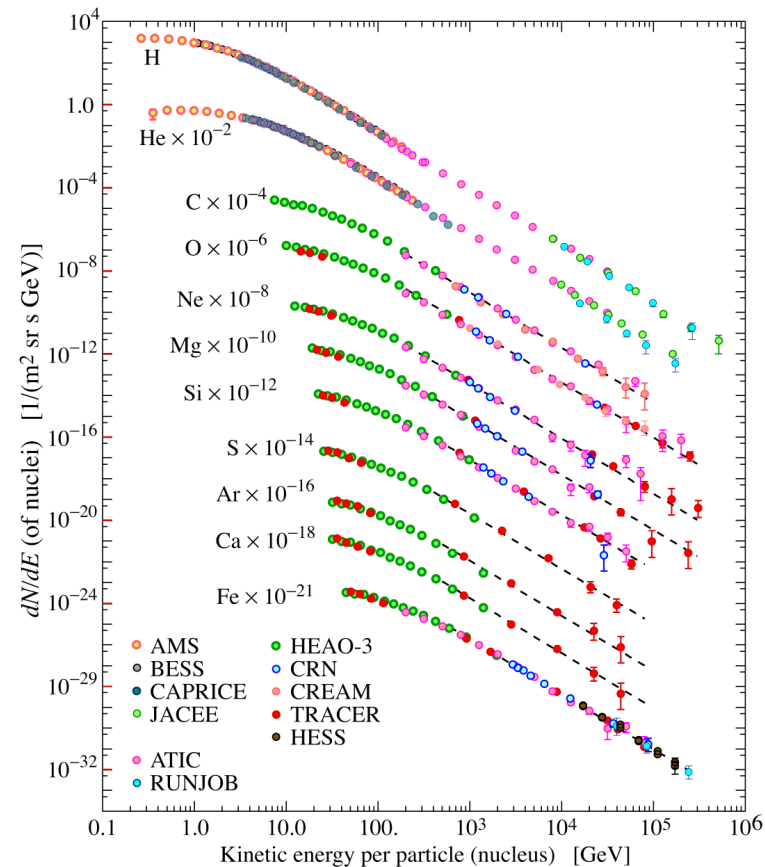
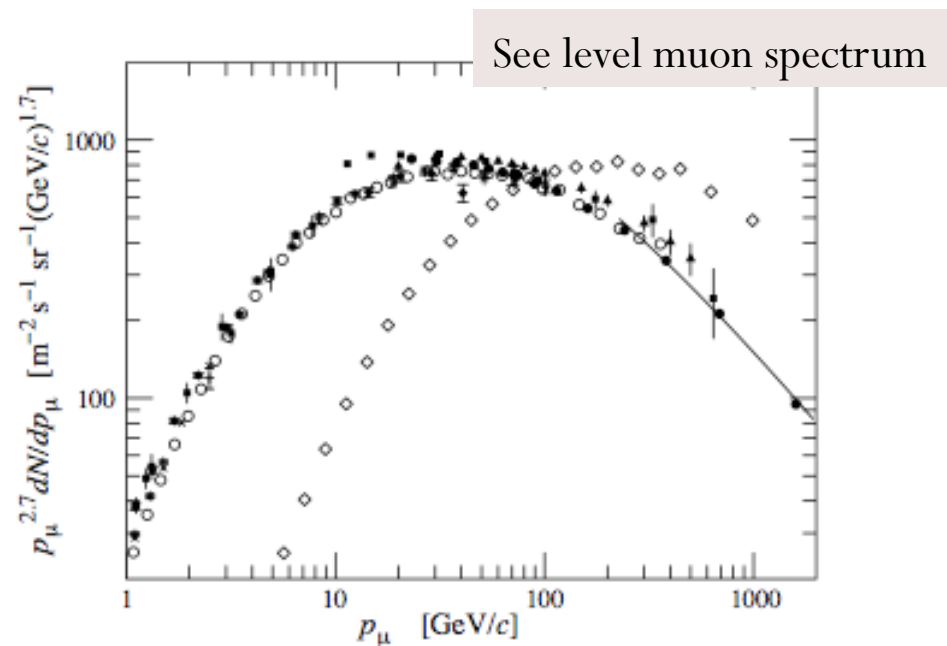


Figure 28.1: Fluxes of nuclei of the primary cosmic radiation in particles per energy-per-nucleus are plotted vs energy-per-nucleus using data from Refs. [2–13].

Cosmic rays - II

- At sea level cosmic rays are essentially muons. Rate $\approx 70 \text{ m}^{-2} \text{ s}^{-1} \text{ sr}^{-1} \rightarrow 1 \text{ cm}^{-2} \text{ min}^{-1}$ ($\approx 2 \text{ Hz/dm}^2$) horiz. detector.
- Angular distribution: $\approx \cos^2\theta$

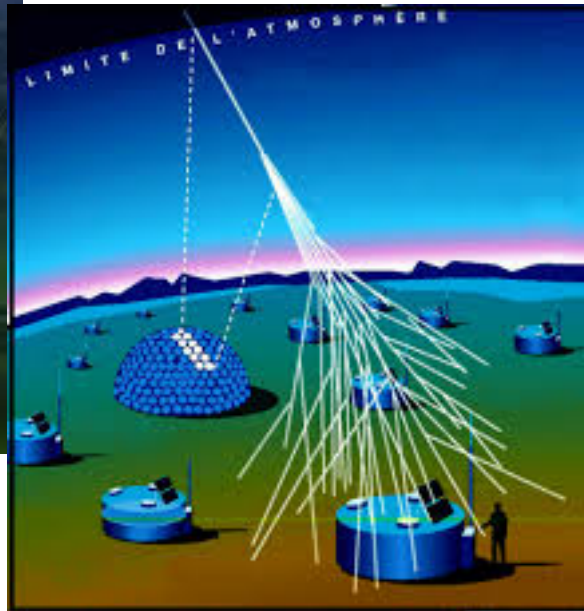
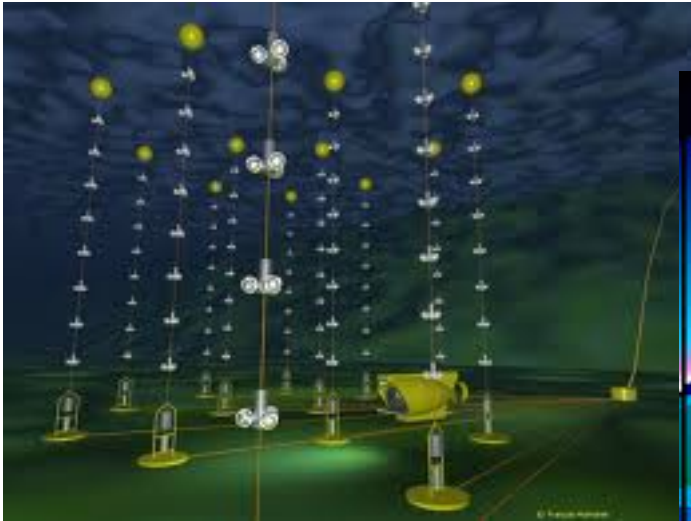


Cosmic rays - III

- Many discoveries of particles have been done in the past in experiments using cosmic rays as projectiles:
 - Positron
 - Muon
 - Pion
 - Kaon
- Today, large experiments use cosmic rays for specific studies:
 - Astrophysical objects (AGN, pulsars, anisotropies,...)
 - Fundamental physics phenomena (ZKP effect) profiting of the ultra high energy of the primary
 - Matter/Antimatter and Dark Matter
- Experiments located in the ground, underground (or deep in the oceans) and in the space

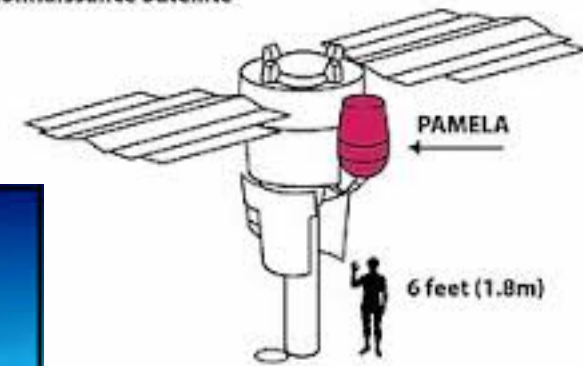
Present cosmic ray experiments

Underwater experiment: ANTARES



Ground based experiment: AUGER

Resurs-DK
Reconnaissance Satellite



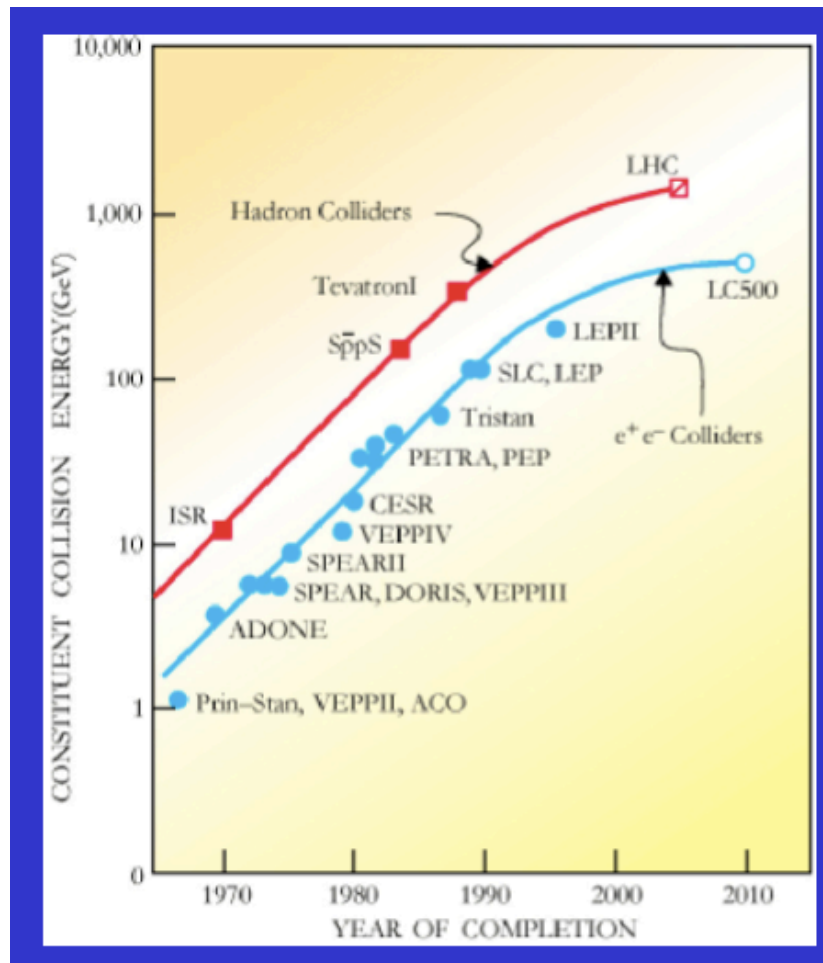
Satellite based experiment:
PAMELA

We will discuss AMS in a
specific lecture.

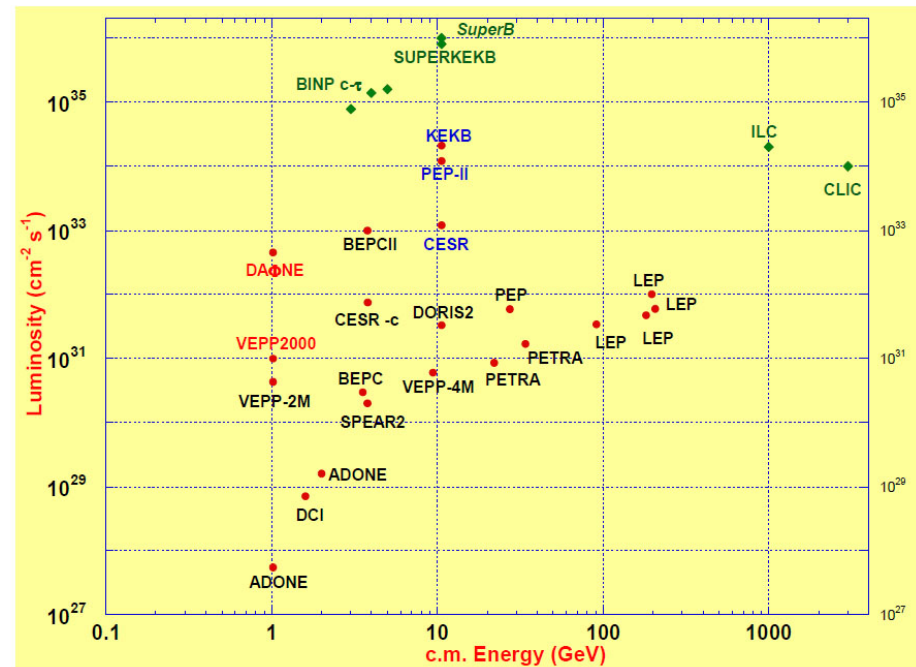
Particle Accelerator Physics

- A new discipline, separation of the communities;
- Many byproducts:
 - Beams for medicine
 - Beams for archeology and determination of age
- Two main quantities define an accelerator: the **center of mass energy** and the **beam intensity** (normally called luminosity)
- Few general aspects to be considered (we consider colliders here):
 - The **center of mass energy** is a “design” quantity: it depends on the machine dimensions, magnets and optics.
 - The **luminosity** is a quantity that has to be reached: it depends on several parameters. In many cases it doesn't reach the “design” value. It is the key quantity for the INTENSITY frontier projects.

Colliders: “Livingston” plots



Here it can be seen the separation
Between *Energy* and *Intensity* frontiers !



Colliders: general aspects - I

- **Storage rings:**

beams are accumulated in circular orbits and are put in collisions.

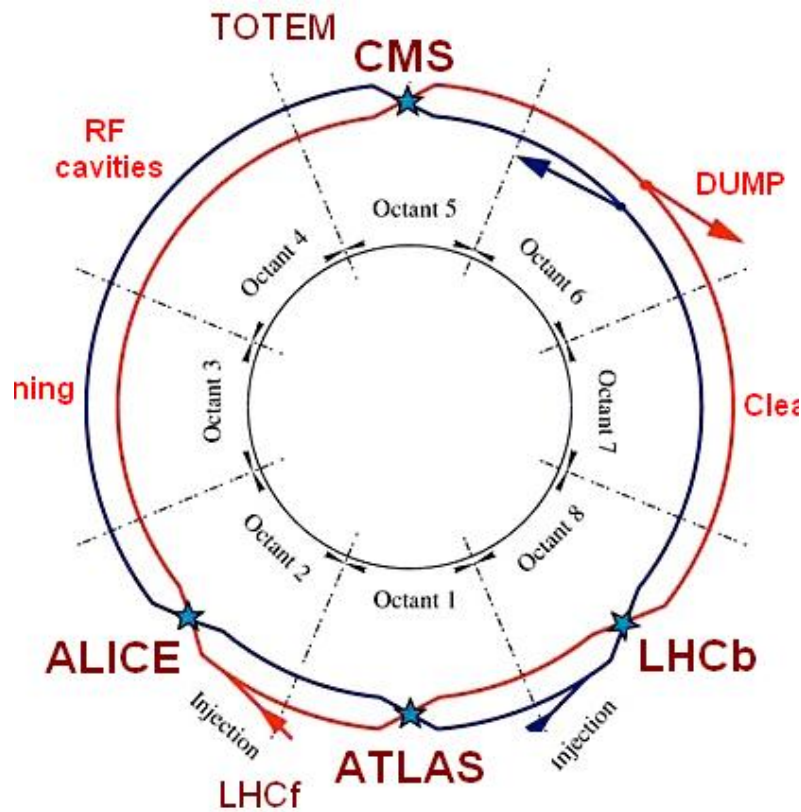
- “bunches” of particles (typically $N \approx 10^{10}$ - 10^{12} / bunch) in small transverse dimensions (σ_x, σ_y down to $<$ mm level) and higher longitudinal dimensions (σ_z at cm level) like *needles* or *ribbons*.
- the bunches travel along a \approx circular trajectory (curvilinear coordinate s)
 - magnetic fields to bend them (dipoles) and to focalize them (quadrupoles or higher order)
 - electric fields to increase their energies (RadioFrequency cavities)
- Multi-bunch operation n_b (increase of luminosity BUT reduction of inter-bunch time)
- One or more interaction regions (with experiments or not..)
- History:
 - e^+e^- : *Ada, Adone, Spear, ... Lep, flavour-factories*
 - pp : *ISR, LHC*
 - $ppbar$: *SpS, Tevatron*
 - ep : *HERA*
 - *muon colliders are considered today (never built)*

- **Linear colliders:**

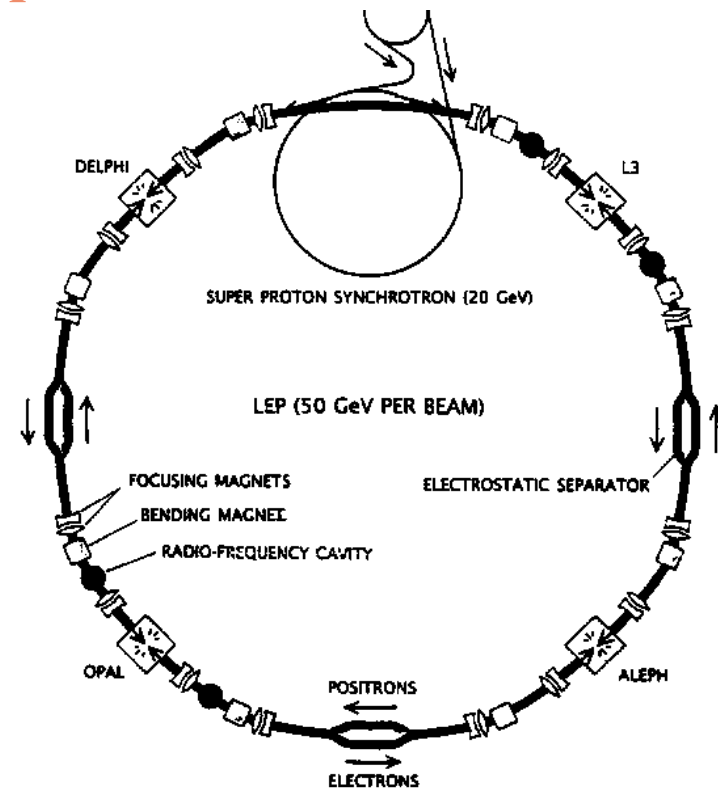
ambitious projects aiming to reach higher electron energies without the large energy loss due to synchrotron radiation.

Colliders: general aspects - II

LHC scheme: up to 7 TeV per beam

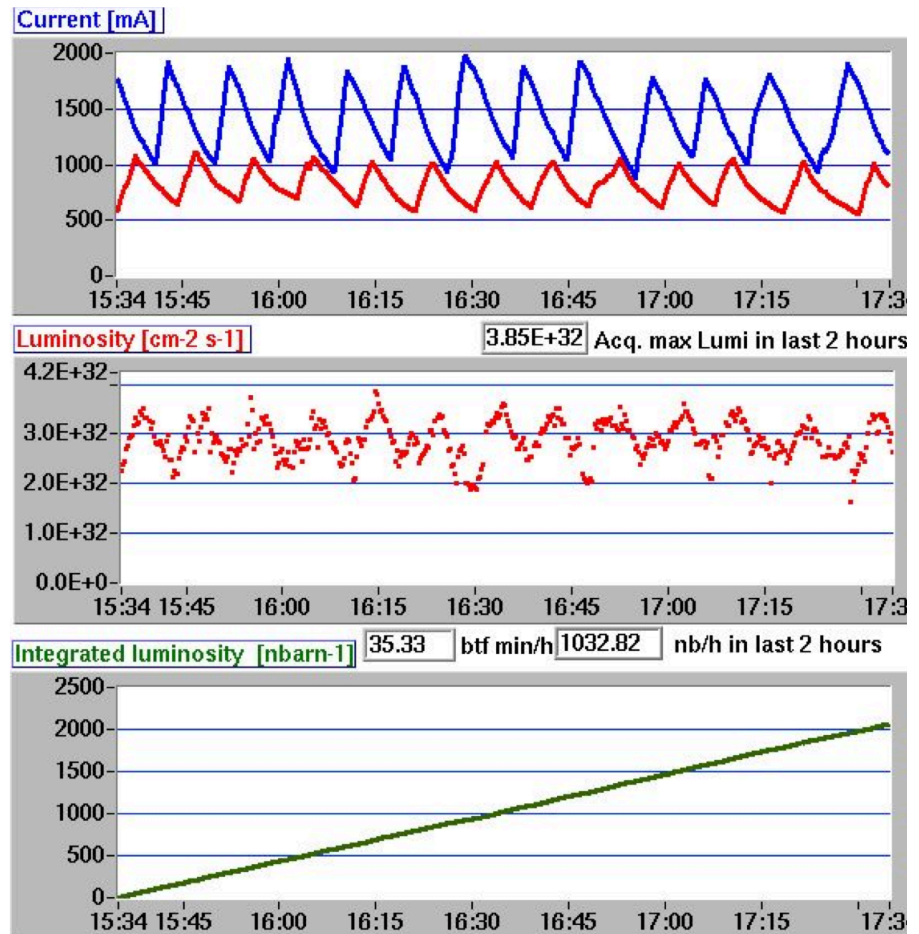


LEP scheme: up to 100 GeV per beam



Colliders: general aspects - III

- Two different operation modalities:
 - Single injection (LHC)
 - “top-up” injection, continuous mode.
- Important quantities for the experiment operation are:
 - Integrated luminosity
 - Machine background



LifeTime: 50% reduction in 10 minutes

Colliders: general aspects - IV

“Typical” LHC operation mode: single- injection



LifeTime: 25% reduction in 9 h

Collider parameters - I

Main parameters

Impact on detector operation

Technical parameters

	CESR (Cornell)	CESR-C (Cornell)	LEP (CERN)	ILC (TBD)	CLIC (TBD)
Physics start date	1979	2002	1989	TBD	TBD
Physics end date	2002	2008	2000	—	—
Maximum beam energy (GeV)	6	6	100 - 104.6	250 (upgradeable to 500)	1500 (first phase: 250)
Delivered integrated luminosity per exp. (fb^{-1})	41.5	2.0	0.221 at Z peak 0.501 at 65 – 100 GeV 0.275 at >100 GeV	—	—
Luminosity ($10^{30} \text{ cm}^{-2}\text{s}^{-1}$)	1280 at 5.3 GeV	76 at 2.08 GeV	24 at Z peak 100 at > 90 GeV	1.5×10^4	6×10^4
Time between collisions (μs)	0.014 to 0.22	0.014 to 0.22	22	0.55 [†]	0.0005 [‡]
Full crossing angle (μ rad)	± 2000	± 3300	0	14000	20000
Energy spread (units 10^{-3})	0.6 at 5.3 GeV	0.82 at 2.08 GeV	0.7→1.5	1	3.4
Bunch length (cm)	1.8	1.2	1.0	0.03	0.0044
Beam radius (μm)	H: 460 V: 4	H: 340 V: 6.5	H: 200 → 300 V: 2.5 → 8	H: 0.474 V: 0.0059	H: 0.045 * V: 0.0009
Free space at interaction point (m)	± 2.2 (± 0.6 to REC quads)	± 2.2 (± 0.3 to PM quads)	± 3.5	± 3.5	± 3.5
Luminosity lifetime (hr)	2–3	2–3	20 at Z peak 10 at > 90 GeV	n/a	n/a
Turn-around time (min)	5 (topping up)	1.5 (topping up)	50	n/a	n/a
Injection energy (GeV)	1.8–6	1.5–6	22	n/a	n/a
Transverse emittance ($10^{-9}\pi$ rad-m)	H: 210 V: 1	H: 120 V: 3.5	H: 20–45 V: 0.25 → 1	H: 0.02 V: 7×10^{-5}	H: 2.2×10^{-4} V: 6.8×10^{-6}
β^* , amplitude function at interaction point (m)	H: 1.0 V: 0.018	H: 0.94 V: 0.012	H: 1.5 V: 0.05	H: 0.01 V: 5×10^{-4}	H: 0.0069 V: 6.8×10^{-5}

Collider parameters - II

Main parameters

Impact on detector operation

Technical parameters

	KEKB (KEK)	PEP-II (SLAC)	SuperKEKB (KEK)
Physics start date	1999	1999	2015
Physics end date	2010	2008	—
Maximum beam energy (GeV)	e^- : 8.33 (8.0 nominal) e^+ : 3.64 (3.5 nominal)	e^- : 7–12 (9.0 nominal) e^+ : 2.5–4 (3.1 nominal)	e^- : 7 e^+ : 4
Delivered integrated luminosity per exp. (fb^{-1})	1040	557	—
Luminosity ($10^{30} \text{ cm}^{-2}\text{s}^{-1}$)	21083	12069 (design: 3000)	8×10^5
Time between collisions (μs)	0.00590 or 0.00786	0.0042	0.004
Full crossing angle ($\mu \text{ rad}$)	$\pm 11000^\dagger$	0	± 41500
Energy spread (units 10^{-3})	0.7	e^-/e^+ : 0.61/0.77	e^-/e^+ : 0.64/0.81
Bunch length (cm)	0.65	e^-/e^+ : 1.1/1.0	e^-/e^+ : 0.5/0.6
Beam radius (μm)	H: 124 (e^-), 117 (e^+) V: 1.9	H: 157 V: 4.7	e^- : 11 (H), 0.062 (V) e^+ : 10 (H), 0.048 (V)
Free space at interaction point (m)	+0.75/−0.58 (+300/−500) mrad cone	± 0.2 , ± 300 mrad cone	e^- : +1.20/−1.28, e^+ : +0.78/−0.73 (+300/−500) mrad cone
Luminosity lifetime (hr)	continuous	continuous	continuous
Turn-around time (min)	continuous	continuous	continuous
Injection energy (GeV)	e^-/e^+ : 8.0/3.5 (nominal)	e^-/e^+ : 9.0/3.1 (nominal)	e^-/e^+ : 7/4
Transverse emittance ($10^{-9}\pi \text{ rad}\cdot\text{m}$)	e^- : 24 (57*) (H), 0.61 (V) e^+ : 18 (55*) (H), 0.56 (V)	e^- : 48 (H), 1.8 (V) e^+ : 24 (H), 1.8 (V)	e^- : 4.6 (H), 0.013 (V) e^+ : 3.2 (H), 0.0086 (V)
β^* , amplitude function at interaction point (m)	e^- : 1.2 (0.27*) (H), 0.0059 (V) e^+ : 1.2 (0.23*) (H), 0.0059 (V)	e^- : 0.50 (H), 0.012 (V) e^+ : 0.50 (H), 0.012 (V)	e^- : 0.025 (H), 3×10^{-4} (V) e^+ : 0.032 (H), 2.7×10^{-4} (V)

Collider parameters - III

Main parameters

Impact on detector operation

Technical parameters

	HERA (DESY)	TEVATRON* (Fermilab)	RHIC (Brookhaven)	LHC (CERN)		
Physics start date	1992	1987	2001	2009	2012 (expected)	nominal
Physics end date	2007	2011	—	—		
Particles collided	ep	$p\bar{p}$	pp (polarized)	pp		
Maximum beam energy (TeV)	e : 0.030 p : 0.92	0.980	0.25 48% polarization	3.5	4.0	7.0
Delivered integrated luminosity per exp. (fb^{-1})	0.8	12	up to 0.14 at 100 GeV/n up to 0.15 at 200 GeV/n	up to 5.6	—	—
Luminosity ($10^{30} \text{ cm}^{-2}\text{s}^{-1}$)	75	431	145 (pk) 90 (avg)	3.7×10^3	5×10^3	1.0×10^4
Time between collisions (ns)	96	396	107	49.90	49.90	24.95
Full crossing angle (μ rad)	0	0	0	240	≈ 300	≈ 300
Energy spread (units 10^{-3})	e : 0.91 p : 0.2	0.14	0.15	0.116	0.116	0.113
Bunch length (cm)	e : 0.83 p : 8.5	p : 50 \bar{p} : 45	70	9	9	7.5
Beam radius (10^{-6} m)	e : 110(H), 30(V) p : 111(H), 30(V)	p : 28 \bar{p} : 16	90	26	20	16.6
Free space at interaction point (m)	± 2	± 6.5	16	38	38	38
Initial luminosity decay time, $-L/(dL/dt)$ (hr)	10	6 (avg)	5.5	8	8	14.9
Turn-around time (min)	e : 75, p : 135	90	200	≈ 180	≈ 180	≈ 180
Injection energy (TeV)	e : 0.012 p : 0.040	0.15	0.023	0.450	0.450	0.450
Transverse emittance ($10^{-9}\pi$ rad-m)	e : 20(H), 3.5(V) p : 5(H), 5(V)	p : 3 \bar{p} : 1	15	0.7	0.6	0.5
β^* , ampl. function at interaction point (m)	e : 0.6(H), 0.26(V) p : 2.45(H), 0.18(V)	0.28	0.6	1.0	0.6	0.55

The quest for high Luminosity

- Luminosity formula:
 - f is fixed by the collider radius
 - High N_1 and N_2 and n_b
 - Low σ_x, σ_y
- Integrated Luminosity L_{int} : [L_{int}]
 $= \text{l}^{-2} \rightarrow \text{nbarn}^{-1} = 10^{33} \text{ cm}^{-2}$
- Problems:
 - Increase number of particles / bunch ? \rightarrow beam-beam effects generate instabilities;
 - Increase number of bunches reduces the inter-bunch time T_{BC} ;
 - Decrease σ_x and σ_y ? (see next slides on beam dynamics).

$$L = n_b f \frac{N_1 N_2}{4\pi\sigma_x\sigma_y} = \frac{I_1 I_2}{4\pi n_b f e^2 \sigma_x \sigma_y}$$

$$L_{int} = \int_{Trun} L(t) dt$$

$$T_{BC} = \frac{1}{n_b f}$$

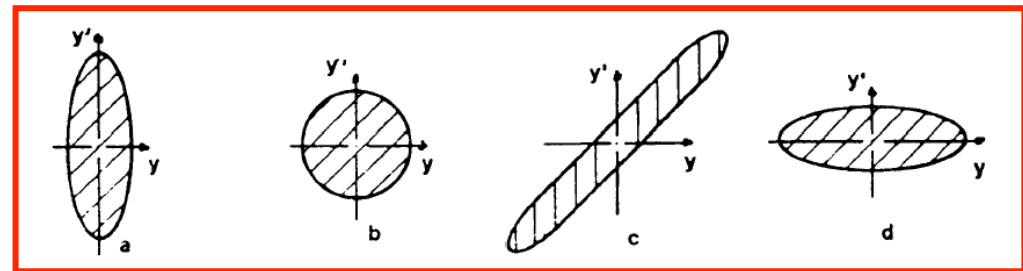
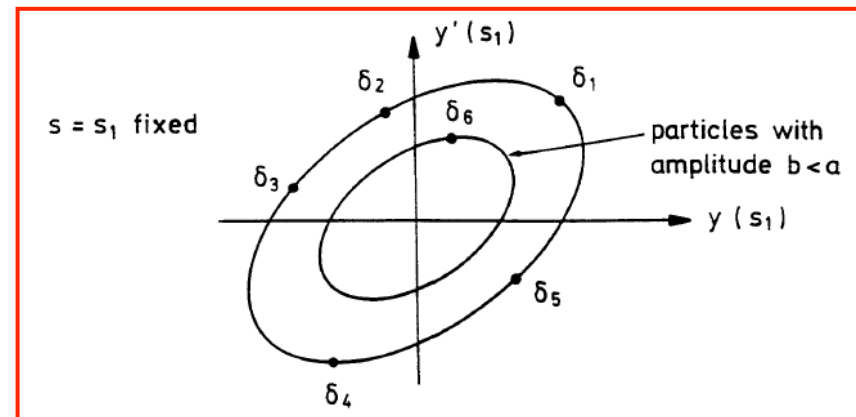
Beam dynamics - I

- Along s , the positions $x(s), y(s)$ ($\mathbf{u}(s)$) of the particles are characterized by oscillations wrt reference trajectory: “betatron” oscillations and “chromaticity” oscillations
- If we neglect momentum dispersion ($\delta p \approx 0$) only betatron oscillations are relevant:
 - $\beta(s)$ betatron function
 - $\phi(s)$ phase advancement function
 - A and ϕ_0 are constants of the motion
- $\mathbf{u}'(s)$ is the “inclination” angle of the trajectory ($\alpha(s)$ is a function of $\beta(s)$)
- At any given s the $\mathbf{u}(s) \% \mathbf{u}'(s)$ plane is the phase space plot. The “area” of the plot is called **emittance** ϵ . $A = \sqrt{\epsilon}$
- Emittances are conserved quantities due to the Liouville theorem \rightarrow small-size beam \Rightarrow large angular spread and viceversa

$$\mathbf{u}(s) = \mathbf{u}_\beta(s) + \eta(s) \frac{\delta p}{p}$$

$$u_\beta(s) = A \sqrt{\beta(s)} \cos(\phi(s) + \phi_0)$$

$$u'_\beta(s) = -\frac{A}{\sqrt{\beta(s)}} \left[\sin(\phi(s) + \phi_0) + \alpha(s) \cos(\phi(s) + \phi_0) \right]$$



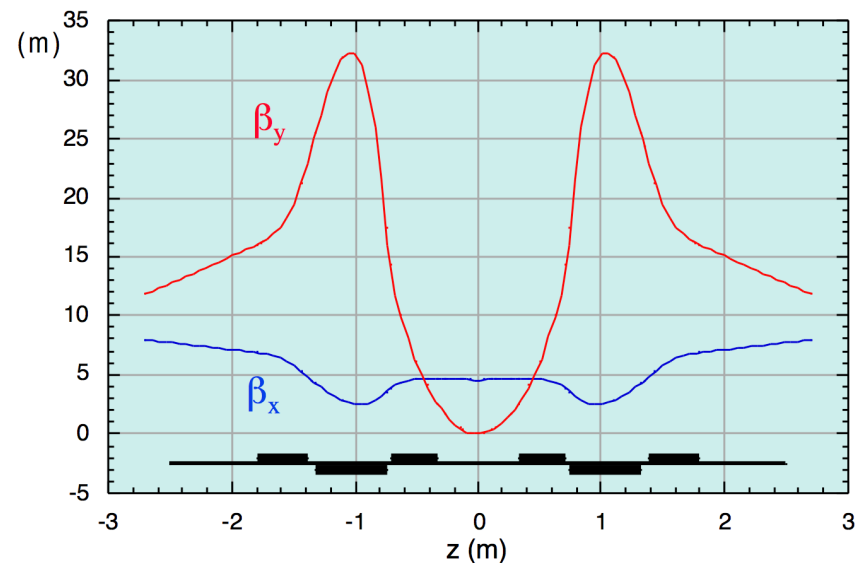
Beam dynamics - II

- **Emittance** is a length \times angle (measured in mm \times mrad)
- Beam dimensions and angular spread change along s . They depend on the emittance and on the betatron functions at the interaction point (IP): $\beta^* = \beta(s_{IP})$.
- Emittance has to be as low as possible
 - In e^+e^- the actual value is an equilibrium between radiation dumping and diffusion
 - In pp it depends on the way the beam is prepared (for anti-p specific cooling systems were invented)
- β^* has also to be as low as possible

$$\sigma_x = \sqrt{\varepsilon_x \beta_x^*}$$

$$\sigma_{\vartheta_x} = \sqrt{\varepsilon_x / \beta_x^*}$$

Low Beta Scheme



Beam dynamics - III

$$Q = \frac{1}{2\pi} \oint_L \phi(s) ds$$

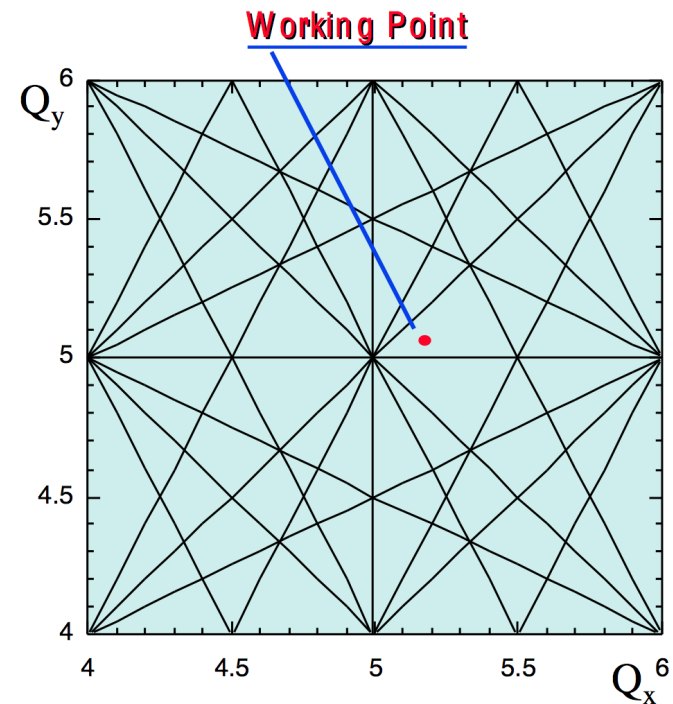
- Q is phase advancement, the number of oscillations per turn: it is the “**tune**”. If integer, at any passage in the same point the bias is the same and there are instabilities.
- Q has to be far from an “integer number”
- The beam-beam effect gives rise to a “**tune shift**” If, for small tune shifts, we have instabilities we have to reduce N_1 and N_2
- So the luminosity can be expressed in terms of β_y^* and of the maximum “acceptable” tune shift ξ

$$L = \pi \left(\frac{\gamma}{r_e} \right)^2 f_R \varepsilon (1 + \kappa) \frac{\xi^2}{\beta_y^*}$$

Tune Resonances

$$mQ_x + nQ_y = p \quad m, n, p \in \mathbf{N}$$

$$|m| + |n| = \text{resonance order}$$



The pile-up

- How many interactions take place per bunch crossing ? It depends on:
 - Interaction rate that in turns depends on:
 - Luminosity
 - Total Cross-section
 - Bunch crossing rate that depends on
 - Bunch frequency
 - Number of bunches circulating
- Pile-up μ = average number of interactions per bunch-crossing

$$\mu = \frac{L\sigma_{tot}}{fn_b}$$

Comparison: e^+e^- vs pp

- DAFNE: e^+e^- @ 1 GeV c.o.m. energy, $\sigma_{\text{tot}} = 5 \mu\text{b}$,
 $L = 10^{33} \text{cm}^{-2}\text{s}^{-1}$, $n_b = 120$, $f = c/100 \text{ m} = 3 \text{ MHz}$

$$\rightarrow \text{TBC} = , \mu =$$

- LHC: pp @ 13 TeV c.o.m. energy, $\sigma_{\text{tot}} = 70 \text{ mb}$,
 $L = 10^{34} \text{cm}^{-2}\text{s}^{-1}$, $n_b = 3000$, $f = c/27 \text{ km} = 10 \text{ kHz}$

$$\rightarrow \text{TBC} = , \mu =$$

Colliders: power needed

- Circulating beams loose energy
 - Synchrotron radiation;
 - Beam-gas and beam-beam interactions
 - → finite beam lifetime → need of RF to “push” beams.
- Comparison btw LEP and LHC (consider only synchrotron radiation loss)

$$Power = n_b \times N \times \frac{\delta E}{turn} \times \frac{c}{2\pi R}$$

$$\frac{\delta E}{turn} = \frac{4\pi}{3} \frac{e^2}{4\pi\epsilon_0} \frac{1}{R} \beta^3 \gamma^4 \propto \frac{E^4}{Rm^4}$$

$$Power(W) = n_b \times N \times 0.5 \cdot 10^{-19} \frac{\gamma^4}{R(m)^2}$$

$$\gamma(LHC) = 7 \cdot 10^3$$

$$\gamma(LEP) = 2 \cdot 10^5$$

$$R = 4300m$$

$$\Rightarrow Power(LHC) \approx 10kW$$

$$\Rightarrow Power(LEP) \approx 10MW$$

Heavy Ion collisions.

- Lead nuclei @ LHC:
 - $Z=82, A=208, M \approx 195 \text{ GeV}$
 - $\Delta E_K = ZeV$ (proton $\times Z$)
 - $p = ZeRB$ (proton $\times Z$)
 - $\rightarrow E_{Pb} = 574 \text{ TeV} = 82 \times 7 \text{ TeV}$
 - $\rightarrow E_{Pb}/\text{Nucleon} = 574/A = 2.77 \text{ TeV}$
 - $\sqrt{s_{NN}} = 5.54 \text{ TeV}$
- Luminosity: $\approx 10^{27} \text{ cm}^{-2}\text{s}^{-1}$
- $n_b = 600$
- $N_1 = N_2 = 7 \times 10^7$ ions/bunch
- Heavy ions program @ RHIC
 - Au, Cu, U ions up to 100 GeV/nucleon
 - Luminosity $\approx 10^{28} \div 10^{29} \text{ cm}^{-2}\text{s}^{-1}$
- Cross-sections:
 - $\sigma_{pp} \approx 70 \text{ mb}$
 - $\sigma_{pPb} \approx \sigma_{pp} \times A^{2/3}$
 - $\sigma_{PbPb} \approx \sigma_{pp} \times N_{\text{coll}} \approx 10 \text{ barn!}$
- How much is the pile-up ?