

First CP Violation Measurements in B_s Mesons System at CDF



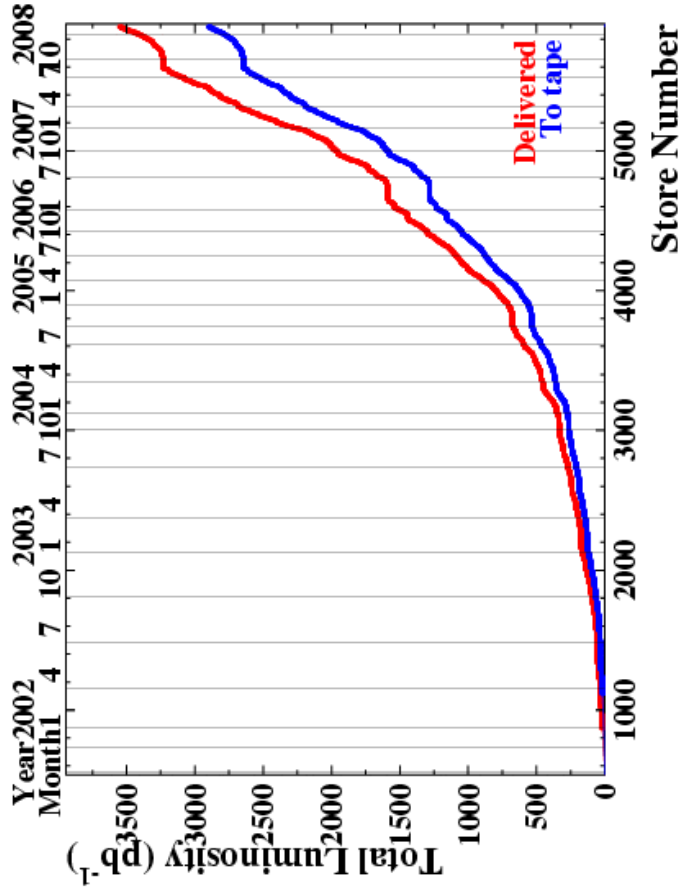
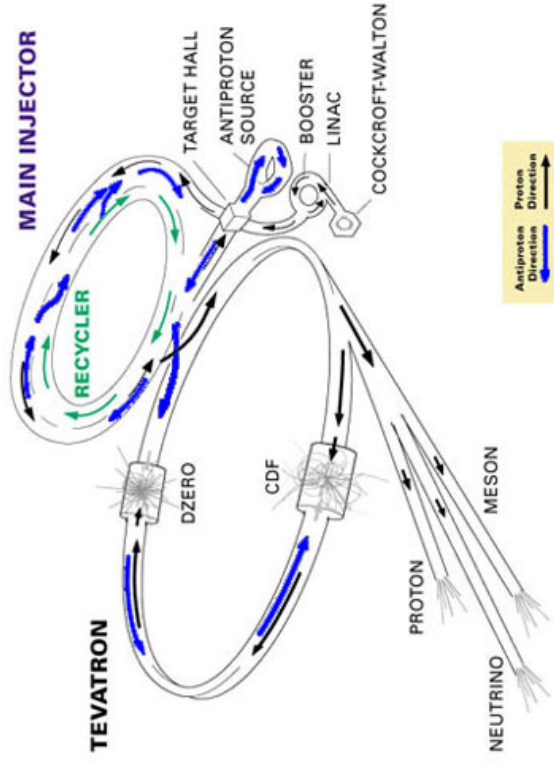
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Rome, 29th February 2008

- Theory and Motivations
- CDF Detectors
- Analysis Review:
 - Polarization Measurements on $B_d \rightarrow J/\Psi K^{*0}$ decays
 - [Sin\(2 \$\beta_s\$ \) measurement](#)
 - ✓ Untagged Analysis on $B_s \rightarrow J/\Psi \Phi$ decays
 - ✓ Flavor Tagged Analysis on $B_s \rightarrow J/\Psi \Phi$ decays
- Summary and Conclusions

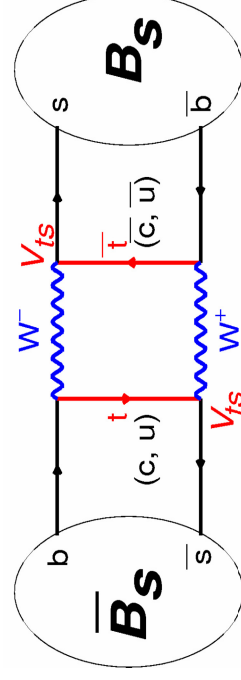
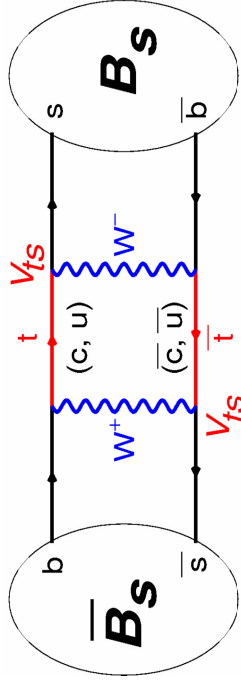
- $p\bar{p}$ collisions at 1.96 TeV
- Excellent Performance
- Peak Initial Luminosity: $3 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$
- Challenge for Detectors, Triggers and Reconstructions



- Tevatron detectors are the only one to have currently access to B_s mesons
- The analyses presented in this talk span from 1.35 to 1.7 fb⁻¹
- Currently on tape ~3 fb⁻¹

- CP Violation is the non-conservation of combined charge-parity quantum numbers
- CP Violation in SM is due to complex coupling of the W boson to quarks through the CKM mechanism:

$$\begin{array}{ccc}
 \begin{array}{c} \text{WEAK} \\ \text{EIGENSTATES} \end{array} & & \begin{array}{c} \text{STRONG} \\ \text{EIGENSTATES} \end{array} \\
 \begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} & = & V \begin{pmatrix} d \\ s \\ b \end{pmatrix} \\
 \\ \\
 V & = & \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}
 \end{array}$$



Flavor eigenstates:

$$|B_s\rangle = (b\bar{s})$$

$$|\bar{B}_s\rangle = (\bar{b}s)$$

⇒ Different Masses:

$$\Delta m_s = M_H - M_L \approx 2 |M_{12}| \quad \text{defines the Mixing Oscillation Frequency}$$

⇒ Different Lifetimes:

$$\Delta\Gamma_s = \Gamma_L - \Gamma_H \approx 2 |\Gamma_{12}| \cos\Phi_s,$$

Mass eigenstates are ($|p|^2 + |q|^2 = 1$):

$$|B_H(t)\rangle = p|B_s(t)\rangle + q|\bar{B}_s(t)\rangle;$$

$$|B_L(t)\rangle = p|B_s(t)\rangle - q|\bar{B}_s(t)\rangle$$

CPV phase:

$$\Phi_s = \arg\left(-\frac{M_{12}}{\Gamma_{12}}\right)$$

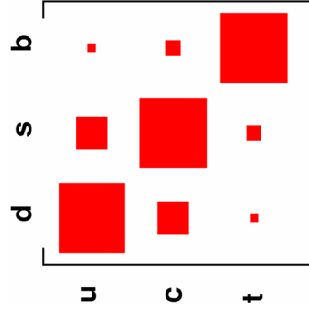
Sizeable $\Delta\Gamma_s$:

$$\Delta\Gamma_s > \Delta\Gamma_d$$

- Unitarity condition for CKM matrix $V^\dagger V = 1$:
 - ✓ Three families \Rightarrow 4 independent parameters
- Wolfenstein Parameterization:

$$V_{\text{CKM}} = \begin{pmatrix} \lambda & & & \\ 1 - \frac{1}{2}\lambda^2 - \frac{1}{8}\lambda^4 & \lambda & & \\ -\lambda + \frac{1}{2}A^2\lambda^5[1 - 2(\rho + i\eta)] & 1 - \frac{1}{2}\lambda^2 - \frac{1}{8}\lambda^4(1 + 4A^2) & A\lambda^3(\rho - i\eta) & \\ A\lambda^3[1 - (1 - \frac{1}{2}\lambda^2)(\rho - i\eta)] & -A\lambda^2 + \frac{1}{2}A\lambda^4[1 - 2(\rho + i\eta)] & A\lambda^2 & \\ & & 1 - \frac{1}{2}A^2\lambda^4 & + 0(\lambda^6) \end{pmatrix}$$

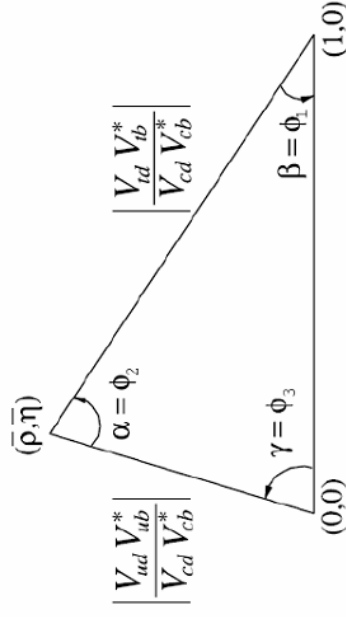
Large CPV Suppressed CPV



- Expansion in terms of $\lambda = \sin(\theta_c) \sim 0.23$
- η responsible for CP Violation $\Rightarrow \eta \neq 0$ implies CPV
 - \Rightarrow Standard Model does not predict values for CKM elements
 - \Rightarrow Experimental Input is crucial

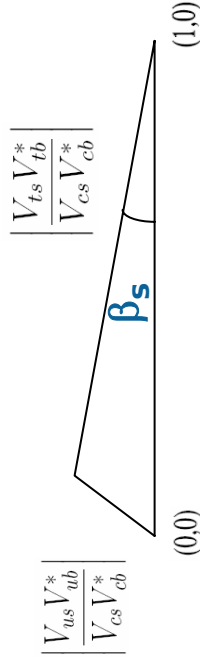
- Unitarity condition for CKM matrix $V^\dagger V = 1$:
 - ⇒ Can construct six unitarity relation between distinct columns or rows of CKM matrix

- Unitarity Triangle:



$$V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^* = 0$$

- Unitarity Triangle in B_s System:



$$V_{us} V_{ub}^* + V_{cs} V_{cb}^* + V_{ts} V_{tb}^* = 0$$

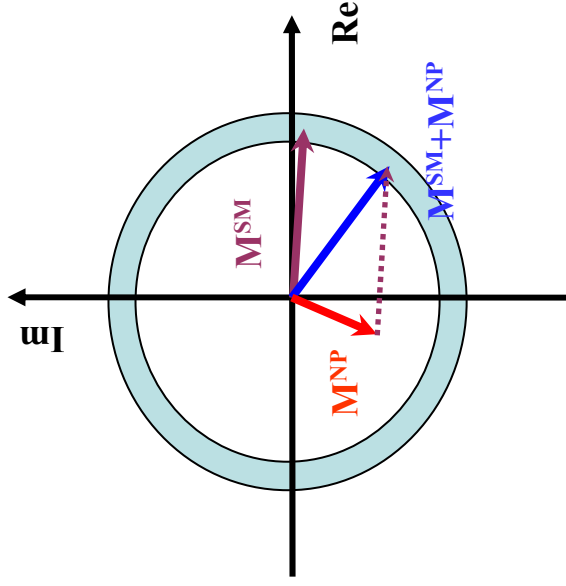
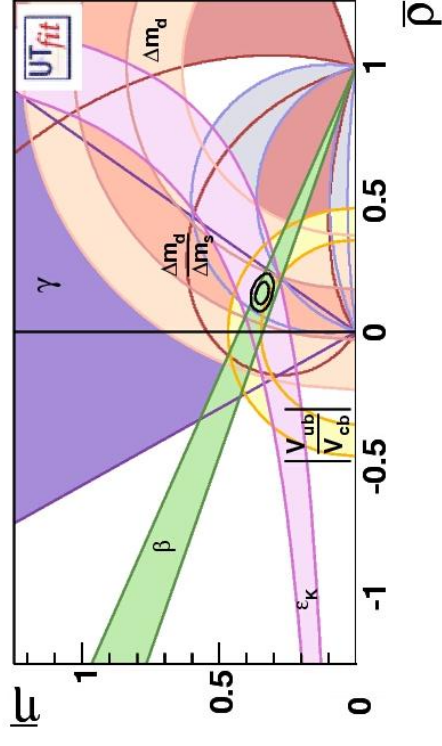
$$\beta_s^{\text{SM}} = \arg \left[-\frac{V_{ts} V_{tb}^*}{V_{cs} V_{cb}^*} \right] \sim 0.02 \text{ rad}$$

⇒ Evidence of non-unitarity would suggest presence of unknown physics contributions

- B_s mixing oscillation observed by **CDF**:

- ✓ $\Delta m_s = M_H - M_L \approx 2 |M_{12}|$ is well measured
- ✓ Precisely determines $|M_{12}|$ in good agreement with the Standard Model

$$\Delta m_s = 17.77 \pm 0.10 \text{ (stat)} \pm 0.07 \text{ ps}^{-1}$$



- Phase of the mixing amplitude is instead poorly determined
- Both are needed to constrain New Physics:

$$M_{12} = |M_{12}| e^{i\phi M}$$

- If New Physics present in mixing amplitude:
 - $\Phi_s = \Phi_s^{\text{SM}} + \Phi_s^{\text{NP}} \sim \Phi_s^{\text{NP}}$ [$\Phi_s^{\text{SM}} \sim 0.004$ rad]
 - Phase Φ_s can be measured directly using charge asymmetry in B_s semileptonic decays or through $\Delta\Gamma_s$ measurement
- CP violation phase β_s is also expected to be small in the Standard Model:
 - $\beta_s = \arg\left[-\frac{V_{ts}V_{tb}^*}{V_{cs}V_{cb}^*}\right] \sim 0.02$ rad
- Same New Physics phase Φ_s^{NP} would add to $\beta_s \Rightarrow 2\beta_s = 2\beta_s^{\text{SM}} - \Phi_s^{\text{NP}}$
- if NP dominates $2\beta_s = -\Phi_s$
 - \Rightarrow Sensitive to NP effect in $M_{12} = |M_{12}| e^{i\phi^{\text{M}}} = |M_{12}| e^{-i2\beta_s} = |M_{12}| e^{i\Phi_s}$
 - \Rightarrow Large CP violation phase in $B_s \rightarrow J/\Psi \Phi$ decay is unequivocal sign of physics beyond the Standard Model

1. Direct CP Violation in decay:

$$\Gamma(B \rightarrow f) \neq \Gamma(\bar{B} \rightarrow \bar{f})$$

$$A(B \rightarrow f) = \sum A_k e^{i(\delta_k + \phi_k)} \quad \xrightarrow{\text{from QCD}} \quad A(\bar{B} \rightarrow \bar{f}) = \sum A_k e^{i(\delta_k - \phi_k)} \quad \Rightarrow \quad |\bar{A}_f / A_f| \neq 1$$

from CKM

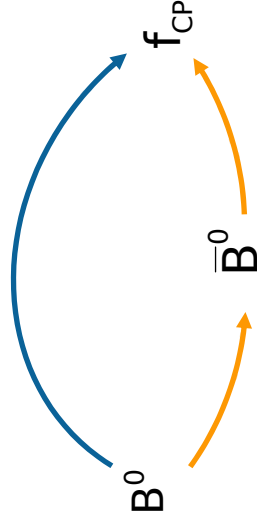
2. CP Violation in Mixing:

$$|B^0\rangle \dots t \dots (q/p)g_-(t)|\bar{B}^0\rangle$$

$$|\bar{B}^0\rangle \dots t \dots (p/q)g_-(t)|B^0\rangle$$

- If $|q/p|^2 \neq 1$ it is possible to measure CP violation in decays to final states accessible only to B^0 or \bar{B}^0

3. Indirect CP Violation in the interference of decays with and without mixing:



$$\Rightarrow \lambda_f = \frac{q \bar{A}_f}{p A_f} \neq 1 \quad \text{Today Physics Topic!}$$

- CP Violation arises from the interference between decay ($B \rightarrow f_{CP}$) and mixing ($B \rightarrow \bar{B} \rightarrow f_{CP}$) amplitudes:

$$A_{f_{CP}}(t) = \frac{\Gamma(\bar{B} \rightarrow f) - \Gamma(B \rightarrow f)}{\Gamma(\bar{B} \rightarrow f) + \Gamma(B \rightarrow f)} = \frac{2\text{Im}\lambda_f}{1 + |\lambda_f|^2} \sin(\Delta m t) - \frac{1 - |\lambda_f|^2}{1 + |\lambda_f|^2} \cos(\Delta m t)$$

In the limit of
 $|\lambda_f| = 1$
 (No direct CPV)

$$\lambda_f = \frac{q\bar{A}_f}{pA_f} = \eta_f e^{-i2\beta},$$

$$\eta_f = \pm 1 \text{ for } CP(f) = \pm 1$$

$$\Rightarrow A_{f_{CP}}(t) = \eta_f \sin(2\beta) \sin(\Delta m t)$$



- $\sin(2\beta_s) \approx 0$, compared to $\sin(2\beta) \approx 0.70$

Analysis Strategy

1. Reconstruct decays from stable products:

- $B_s \rightarrow J/\Psi[\mu^+\mu^-] \Phi[K^+K^-]$
- $B_d \rightarrow J/\Psi[\mu^+\mu^-] K^{*0}[K^+\pi^-]$
- B_d is used a control sample

2. Measure lifetime $ct = m_B * L_{xy}/p_T$

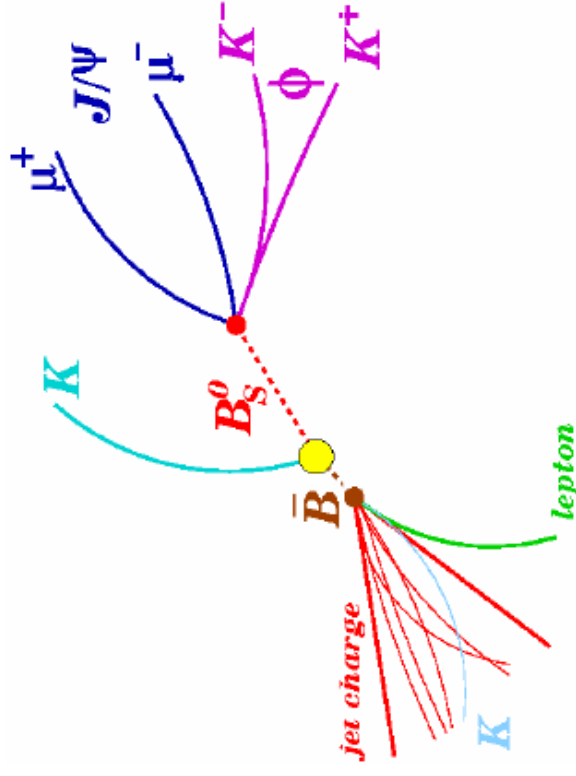
3. Measure decay angles $\vec{w} = (\theta, \Phi, \psi)$

4. Identify B_s / \bar{B}_s at production time:

- Flavor Tagging (Tag decision ξ)

5. Perform maximum likelihood fit:

- Likelihood in m, ct, \vec{w}, ξ



Overview of the decay:

- B_s travels $\sim 450 \mu\text{m}$ before decaying into J/Ψ and Φ

- Multi-purpose detector
- Classical layered structure
- Excellent momentum resolution $\sigma(p)/p < 0.1\%$
- Triggered Muon Coverage $|\eta| < 1.0$

- **Yield (S):**

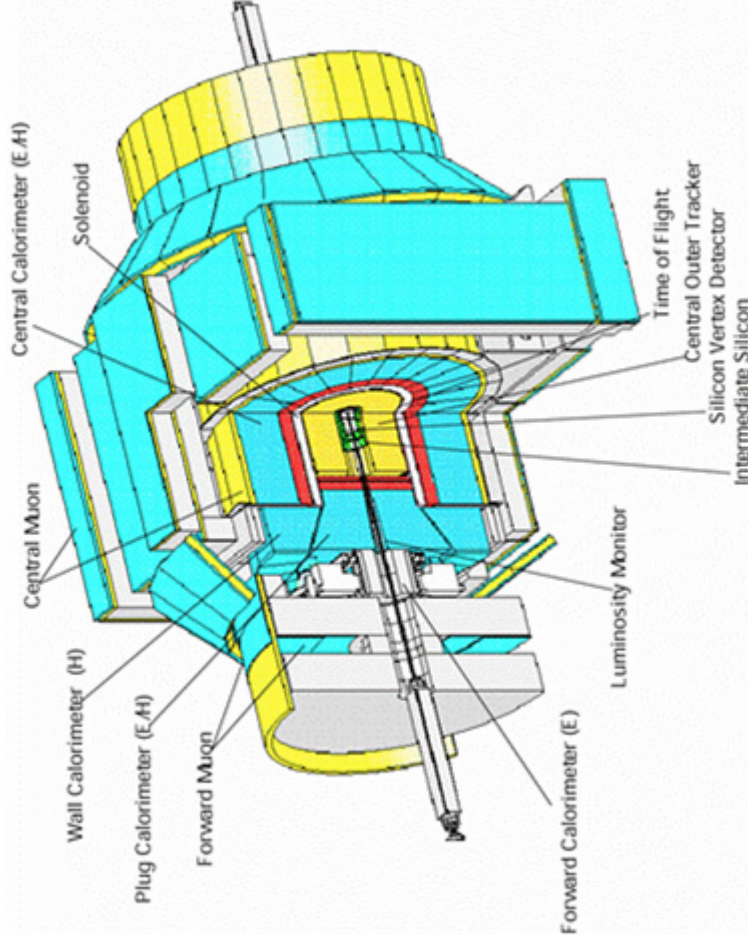
- ✓ Displaced Track Trigger
- ✓ **Di-muon** Trigger

- **Proper time resolution (σ_{ct}):**

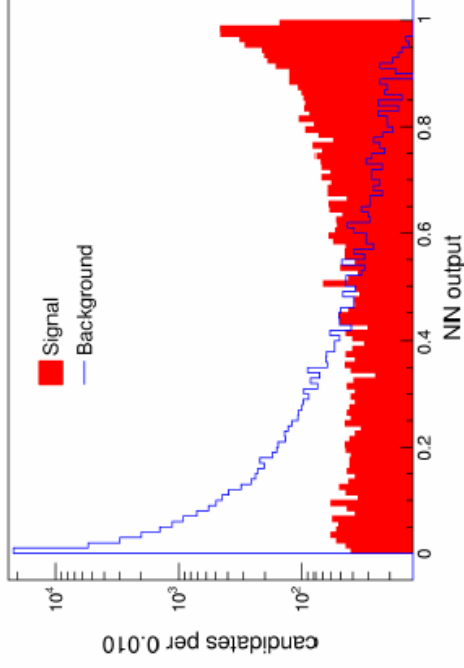
- ✓ ISL, SVXII, L00
(Silicon Strip Vertex Detector)

- **Particle Identification:**

- ✓ **TOF** (Time Of Flight)
- ✓ dE/dx in COT (Drift Chambers)
- ⇒ **Flavor Tagging Power (ϵD^2)**

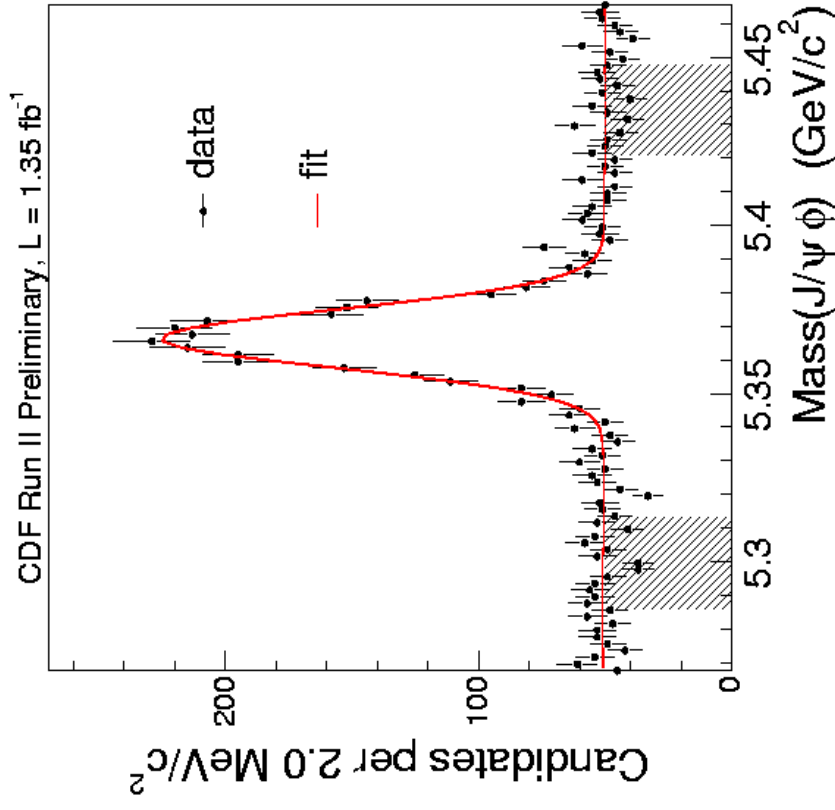


- Data with 1.35 fb^{-1} (1.7 fb^{-1})
- Di-muon trigger
- Soft preselection followed by neural network selection
- NN trained on:
 - ✓ Simulated events for signal
 - ✓ B_s mass sidebands for background
- Selection maximizes $S / \sqrt{S+B}$ under signal peak



NN Variables:

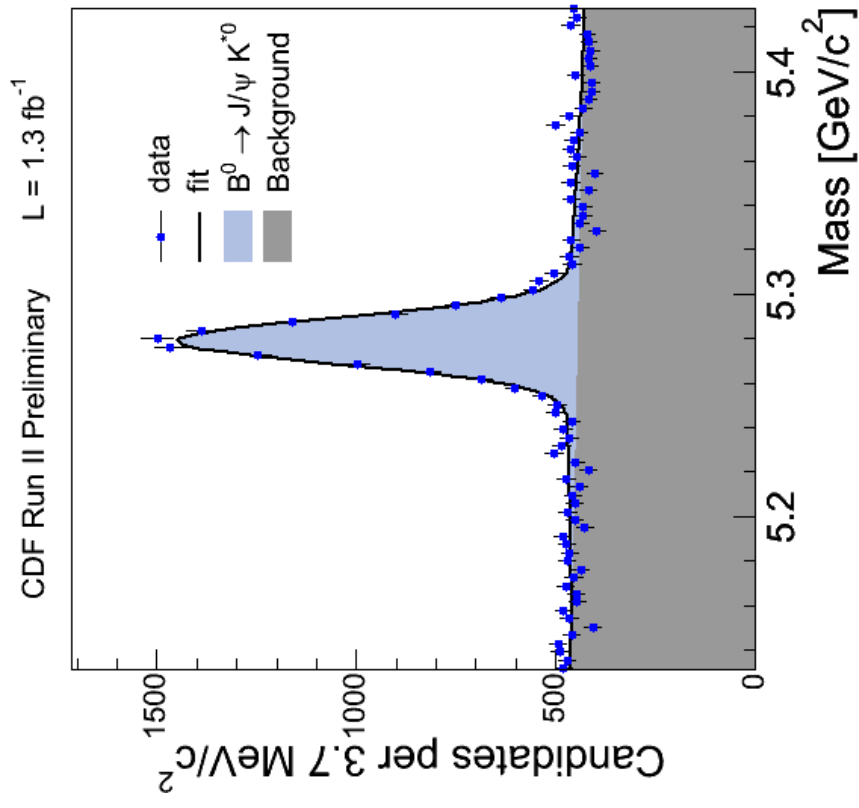
- B_s : p_T and vertex quality
- J/Ψ : p_T and vertex quality
- Φ : mass and vertex quality
- K^+/K^- : p_T and PID (TOF, dE/dx)



Signal Candidates:

- ~ 2000 in 1.35 fb^{-1} (Tagged analysis)
- ~ 2500 in 1.7 fb^{-1} (Untagged analysis)

$S/B \sim 2$

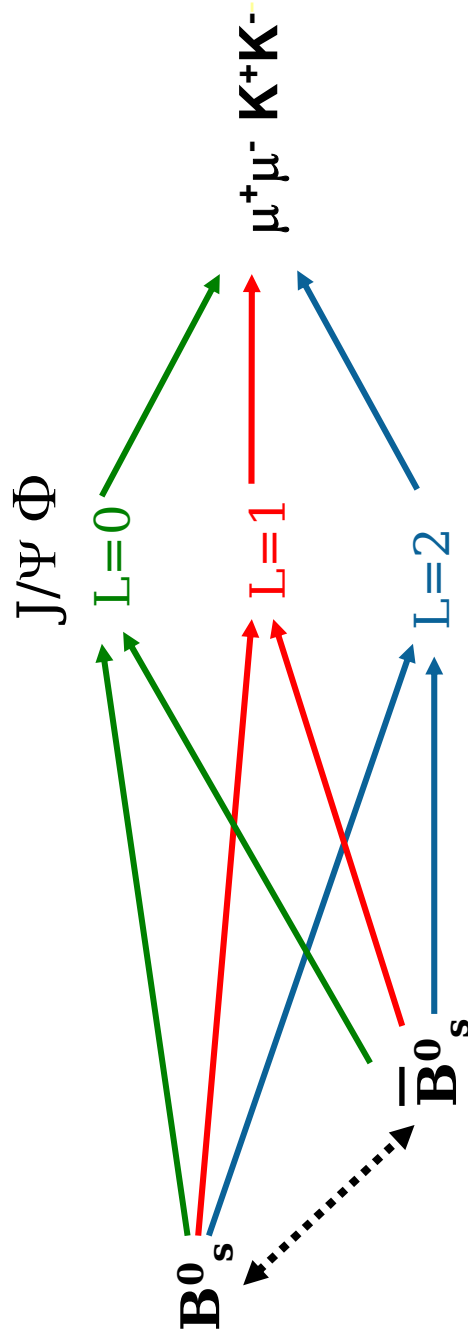


Signal Candidates:

- ~ 7800 in 1.35 fb^{-1}

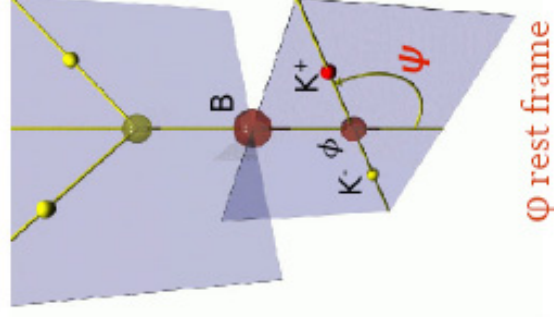
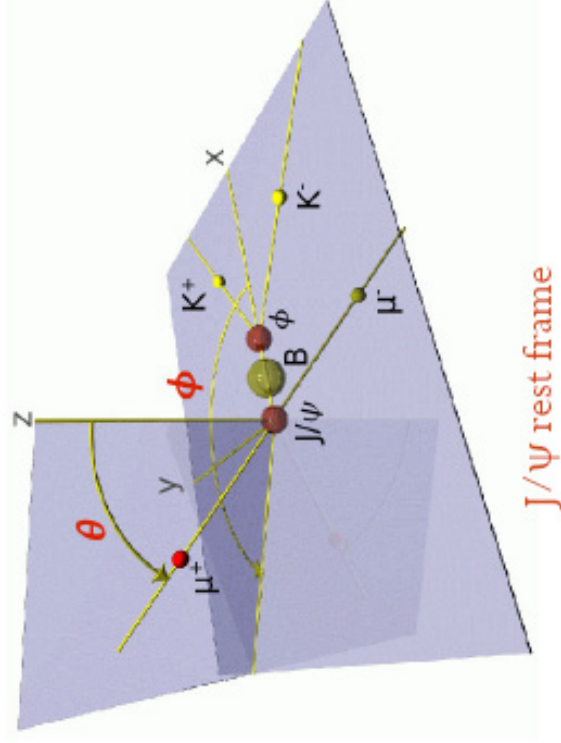
- $B_s \rightarrow J/\Psi \Phi$ ($B_d \rightarrow J/\Psi K^{*0}$) decays into admixture CP eigenstates
- Spin-0 B_s decays to spin-1 J/Ψ and spin-1 Φ three different angular momentum final states:

✓ $L=0$ (S-wave), $L=2$ (D-wave) \Rightarrow P-even
 ✓ $L=1$ (P-wave) \Rightarrow P-odd



- C-even \Rightarrow Different Parity \Rightarrow Separate CP contributions
- Different parity contributions disentangled by their different decay angle distributions

TRANSVERSITY BASIS



Angular momentum:

- $P \rightarrow VV$ decay:
 - ✓ $L=0$
 - ✓ $L=1$
 - ✓ $L=2$

Transversity Basis:

- 3 Angles $\vec{w} = (\theta, \Phi, \psi)$:
 - ✓ θ (J/ψ rest frame)
 - ✓ Φ (J/ψ rest frame)
 - ✓ Ψ (Φ rest frame)

- In the Transversity basis the vector mesons polarization w.r.t the direction of motion is:

- ✓ Longitudinal $\Rightarrow A_0$ [CP-even]
- ✓ Transverse and parallel to each other $\Rightarrow A_{||}$ [CP-even]
- ✓ Transverse and perpendicular to each other $\Rightarrow A_{\perp}$ [CP-odd]

General decay rate formula:

$$\begin{aligned} \frac{d^4P(t, \vec{w})}{dt d\vec{w}} &\propto |A_0|^2 T_+ f_1(\vec{w}) + |A_{\parallel}|^2 T_+ f_2(\vec{w}) \\ &+ |A_{\perp}|^2 T_- f_3(\vec{w}) + |A_{\parallel}| |A_{\perp}| U_+ f_4(\vec{w}) \\ &+ |A_0| |A_{\parallel}| \cos(\delta_{\parallel}) T_+ f_5(\vec{w}) \\ &+ |A_0| |A_{\perp}| V_+ f_6(\vec{w}) \end{aligned}$$

- Strong phases:
 $\checkmark \delta_{\parallel} \equiv \arg(A_{\parallel}^* A_0)$
 $\checkmark \delta_{\perp} \equiv \arg(A_{\perp}^* A_0)$

- Decay rate is a function of time, decay angles \vec{w} , initial B_s flavor and parameters $\Delta\Gamma_s, \beta_s$
- B_s decays into admixture of CP eigenstates ⇒ interference terms in general decay rate formula
- f_i ($i=1, \dots, 6$) encode the different angular distributions

General decay rate formula:

$$\begin{aligned} \frac{d^4P(t, \vec{w})}{dt d\vec{w}} &\propto |A_0|^2 T_+ f_1(\vec{w}) + |A_{||}|^2 T_+ f_2(\vec{w}) \\ &+ |A_{\perp}|^2 T_+ f_3(\vec{w}) + |A_{||}| |A_{\perp}| U_+ f_4(\vec{w}) \\ &+ |A_0| |A_{||}| \cos(\delta_{||}) T_+ f_5(\vec{w}) \\ &+ |A_0| |A_{\perp}| V_+ f_6(\vec{w}) \end{aligned}$$

- Strong phases:
 - ✓ $\delta_{||} \equiv \arg(A_{||}^* A_0)$
 - ✓ $\delta_{\perp} \equiv \arg(A_{\perp}^* A_0)$

$$T_{\pm} = e^{\mp t} \times [\cosh(\Delta\Gamma t / 2) \mp \cos(2\beta_s) \sinh(\Delta\Gamma t / 2)]$$

$$\mp \eta \sin(2\beta_s) \sin(\Delta m_s t)], \quad \eta = +1(-1) \text{ for } P(\bar{P})$$

$$U_{\pm} = \pm e^{\mp t} \times [\sin(\delta_{\perp} - \delta_{||}) \cos(\Delta m_s t)$$

$$- \cos(\delta_{\perp} - \delta_{||}) \cos(2\beta_s) \sin(\Delta m_s t)$$

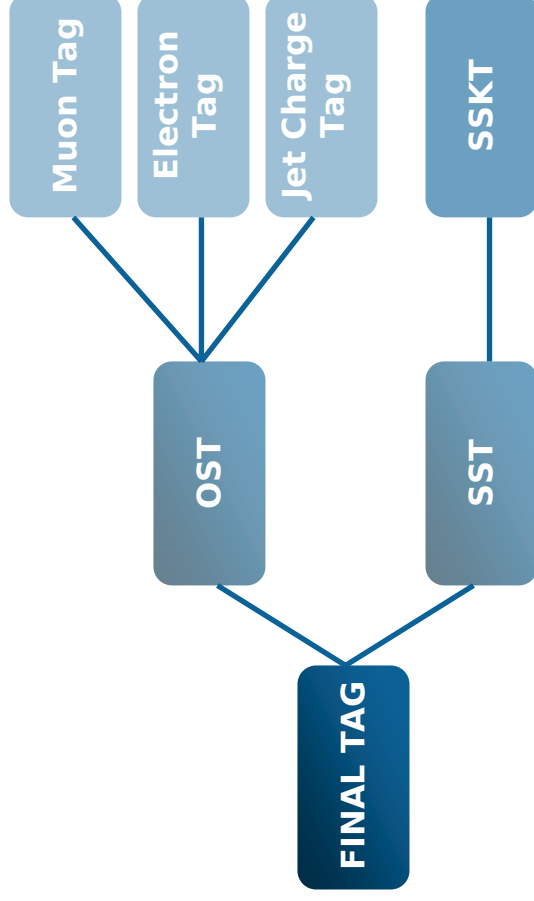
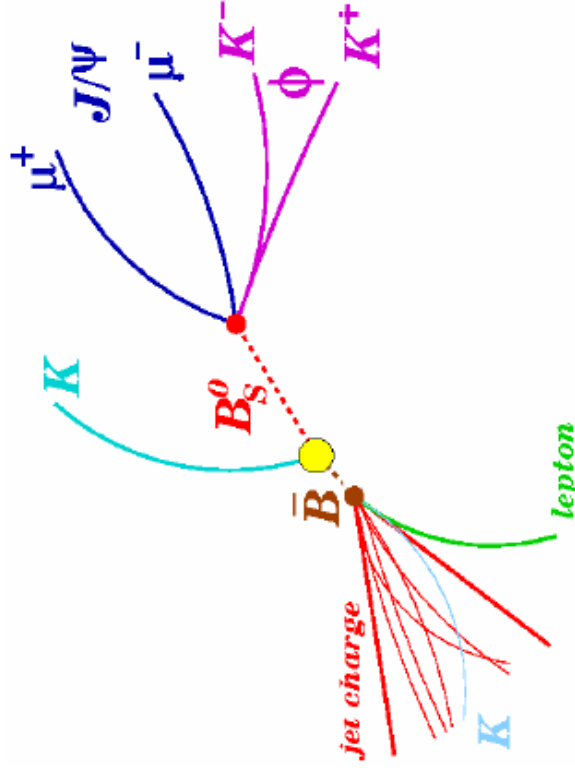
$$\pm \cos(\delta_{\perp} - \delta_{||}) \sin(2\beta_s) \sinh(\Delta\Gamma t / 2)]$$

$$V_{\pm} = \pm e^{\mp t} \times [\sin(\delta_{\perp}) \cos(\Delta m_s t)$$

$$- \cos(\delta_{\perp}) \cos(2\beta_s) \sin(\Delta m_s t)$$

$$\pm \cos(\delta_{\perp}) \sin(2\beta_s) \sinh(\Delta\Gamma t / 2)]$$

Terms with Δm_s dependence
flip sign for initial B_s flavor



- Two independent methods of tagging: same and opposite side
- Opposite Side Tagger is calibrated using data (high stat B^+ , B^0)
- Same Side Tagger is calibrated on Monte Carlo
- Efficiency $\epsilon = P(\text{tag decision})$
- Dilution $D = 1 - 2q$, q is mistag probability

Opposite Side Tagging

- Soft Lepton Taggers
- Jet Charge Tagger

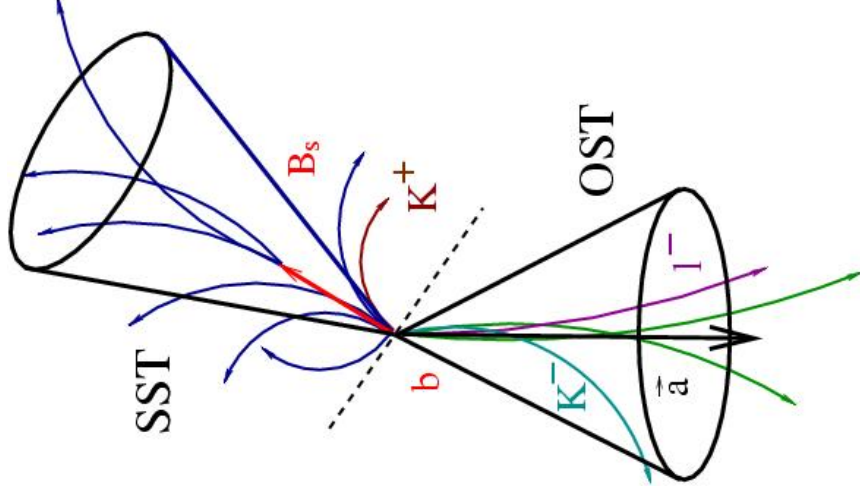
OST's perform identically in $B_{u,d,s}$:
 Calibrated in high statistics B^+/B^0 data

- Combined Performance:
 - ✓ Efficiency: $\epsilon = 0.96 \pm 0.01$
 - ✓ Average Dilution: $D = 0.11 \pm 0.02$

Same Side Kaon Tagging

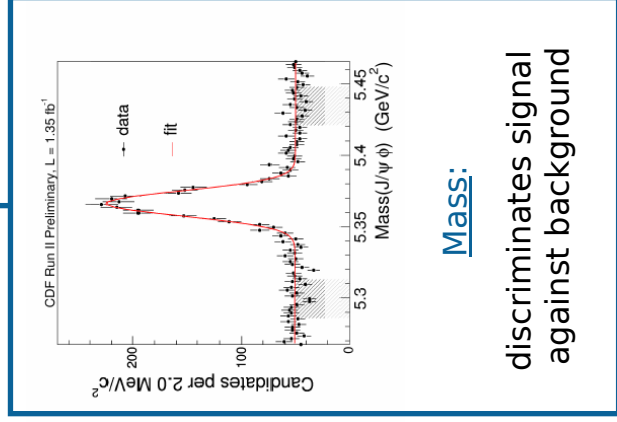
- Most powerful tagger available:
 - ✓ 2-3 times more effective than combined OST
- SSKT is different for B^0 , B^+ and B_s :
 SST needs to rely on MC simulation

- Performance:
 - ✓ Efficiency: $\epsilon = 0.50 \pm 0.01$
 - ✓ Average Dilution: $D = 0.27 \pm 0.04$



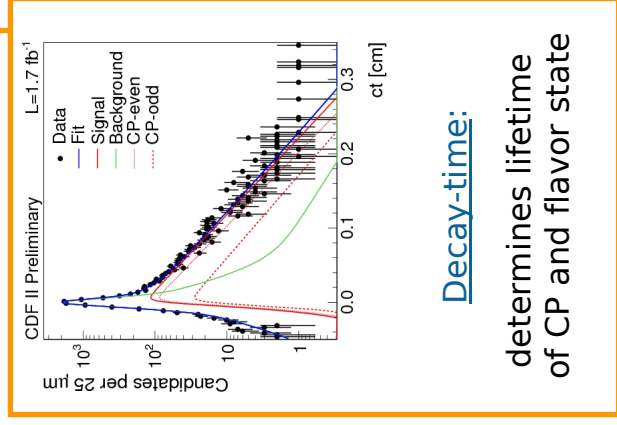
OST and SST
 combined
 independently

$$P_s = P_M(m | \sigma_m) P_L(ct, \vec{w}, \xi | D, \sigma_{ct}) P(D) \varepsilon(\vec{w})$$



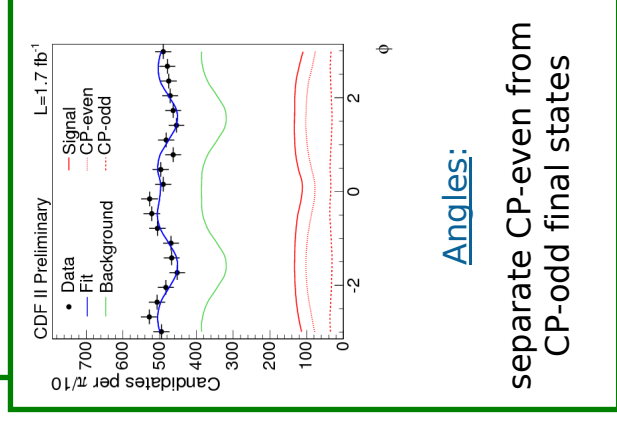
Mass:

discriminates signal against background



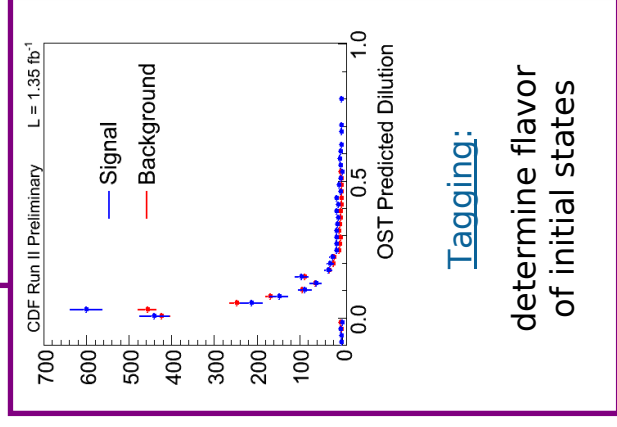
Decay-time:

determines lifetime of CP and flavor state



Angles:

separate CP-even from CP-odd final states

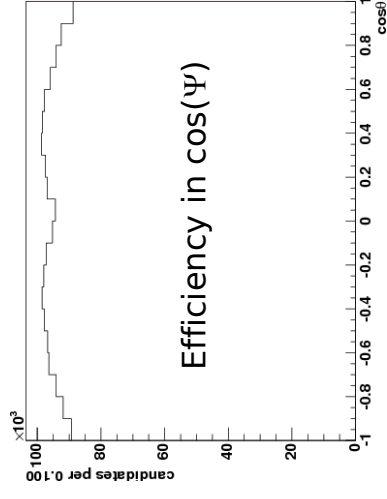
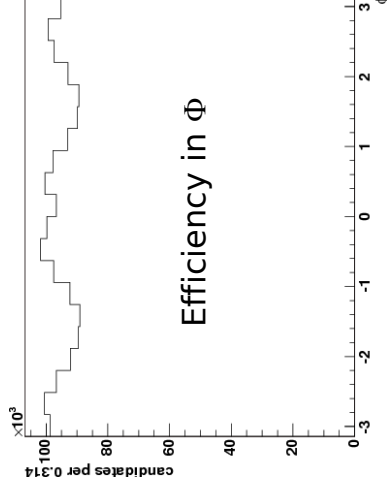
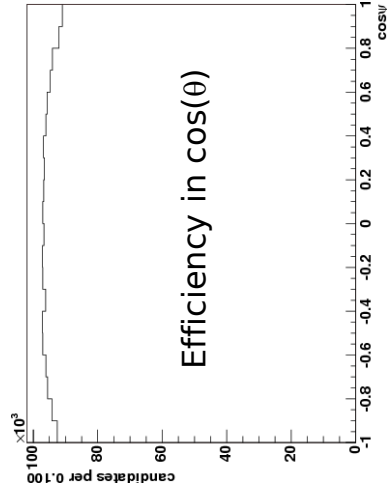


Tagging:

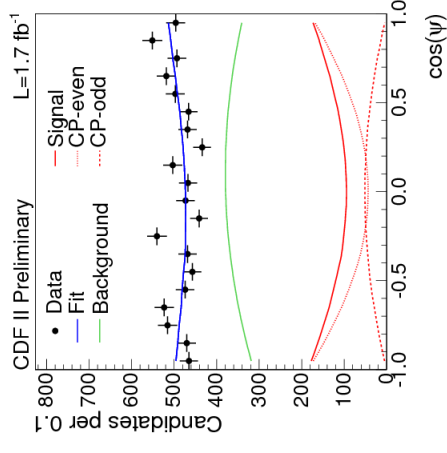
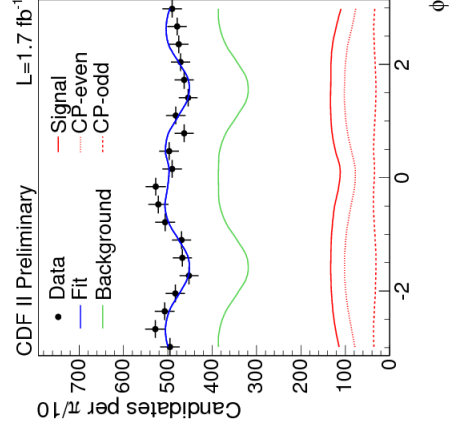
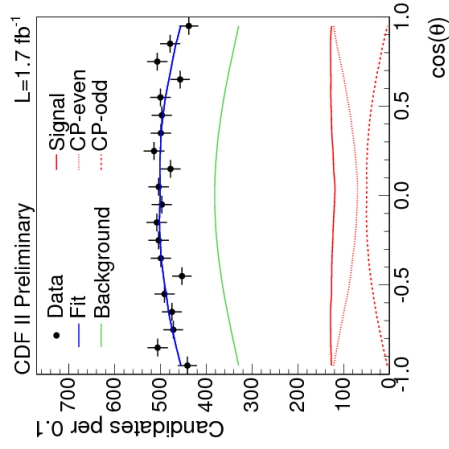
determine flavor of initial states

- $\varepsilon(\vec{w})$ is the sculpting of transversity angles due to detector acceptance

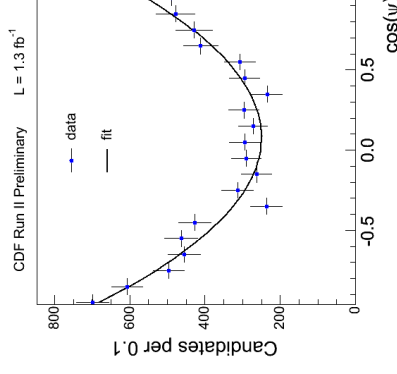
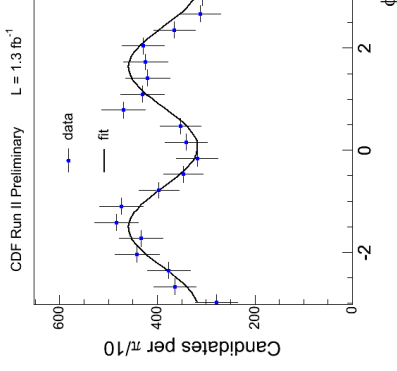
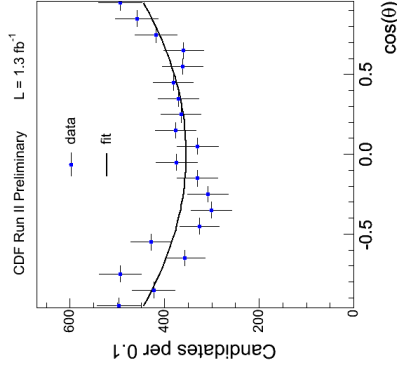
- Monte Carlo passed through detector simulation and to determine angular sculpting
- Deviation from flat distribution indicates detector effects



- Data projections uncorrected for detector sculpting



- Corrected distributions-fits agrees well: validates treatment of detector acceptance!



- Results for $B^0 \rightarrow J/\Psi K^{*0}$ in good agreement with BaBar and errors are competitive!

Phys. Rev. D 76, 031102 (2007)

$$c\tau = 456 \pm 6 \text{ (stat)} \pm 6 \text{ (syst)} \mu\text{m}$$

$$|A_0(0)|^2 = 0.569 \pm 0.009 \text{ (stat)} \pm 0.009 \text{ (syst)}$$

$$|A_{\parallel}(0)|^2 = 0.211 \pm 0.012 \text{ (stat)} \pm 0.006 \text{ (syst)}$$

$$\delta_{\parallel} = -2.96 \pm 0.08 \text{ (stat)} \pm 0.03 \text{ (syst)}$$

$$\delta_{\perp} = +2.97 \pm 0.06 \text{ (stat)} \pm 0.01 \text{ (syst)}$$

$$|A_0(0)|^2 = 0.556 \pm 0.009 \text{ (stat)} \pm 0.010 \text{ (syst)}$$

$$|A_{\parallel}(0)|^2 = 0.211 \pm 0.010 \text{ (stat)} \pm 0.006 \text{ (syst)}$$

$$\delta_{\parallel} = -2.93 \pm 0.08 \text{ (stat)} \pm 0.04 \text{ (syst)}$$

$$\delta_{\perp} = +2.96 \pm 0.05 \text{ (stat)} \pm 0.03 \text{ (syst)}$$

Untagged Analysis

- Drop the information on flavor tagging \Rightarrow several terms in the likelihood are canceled
- Simpler likelihood suited for precise measurements of $\Delta\Gamma$, width-difference and τ , average lifetime
- Reduced but still available sensitivity to phase β_s due to CP-even/CP-odd interference
- Sensitive to $|\cos(2\beta_s)|$ and $|\sin(2\beta_s)|$ (note absolute values)



4-fold ambiguity in the likelihood

General decay rate formula:

$$\begin{aligned} \frac{d^4P(t, \vec{w})}{dt d\vec{w}} &\propto |A_0|^2 T_+ f_1(\vec{w}) + |A_{\parallel}|^2 T_+ f_2(\vec{w}) \\ &+ |A_{\perp}|^2 T_- f_3(\vec{w}) + |A_{\parallel}| |A_{\perp}| U_+ f_4(\vec{w}) \\ &+ |A_0| |A_{\parallel}| \cos(\delta_{\parallel}) T_+ f_5(\vec{w}) \\ &+ |A_0| |A_{\perp}| V_+ f_6(\vec{w}) \end{aligned}$$

$$T_{\pm} = e^{-\Gamma t} \times [\cosh(\Delta\Gamma t / 2) \mp \cos(2\beta_s) \sinh(\Delta\Gamma t / 2)]$$

$$\mp \eta \sin(2\beta_s) \sin(\Delta m_s t)], \quad \eta = +1(-1) \text{ for } P(\bar{P})$$

$$U_{\pm} = \pm e^{-\Gamma t} \times [\sin(\delta_{\perp} - \delta_{\parallel}) \cos(\Delta m_s t) - \cos(\delta_{\perp} - \delta_{\parallel}) \cos(2\beta_s) \sin(\Delta m_s t)]$$

$$\pm \cos(\delta_{\perp} - \delta_{\parallel}) \sin(2\beta_s) \sinh(\Delta\Gamma t / 2)]$$

$$V_{\pm} = \pm e^{-\Gamma t} \times [\sin(\delta_{\perp}) \cos(\Delta m_s t) - \cos(\delta_{\perp}) \cos(2\beta_s) \sin(\Delta m_s t)]$$

$$\pm \cos(\delta_{\perp}) \sin(2\beta_s) \sinh(\Delta\Gamma t / 2)]$$

- Sizeable $\Delta\Gamma_s \Rightarrow$ CP-even and CP-odd contributions of the signal can be distinguished
- Results assuming no CP violation $\Rightarrow \beta_s = 0$
- **CDF:** ~ 2500 signal events (1.7 fb^{-1})

World Best Measurements (arXiv: 0712.2348)

$$\tau_s = 1.52 \pm 0.04 \text{ (stat)} \pm 0.02 \text{ (syst)} \text{ ps}$$

$$\Delta\Gamma_s = 0.076_{-0.063}^{+0.059} \text{ (stat)} \pm 0.006 \text{ (syst)} \text{ ps}^{-1}$$

Lifetime:

Decay Width:

$$|A_0(0)|^2 = 0.531 \pm 0.020 \text{ (stat)} \pm 0.007 \text{ (syst)}$$

$$|A_{\parallel}(0)|^2 = 0.230 \pm 0.026 \text{ (stat)} \pm 0.009 \text{ (syst)}$$

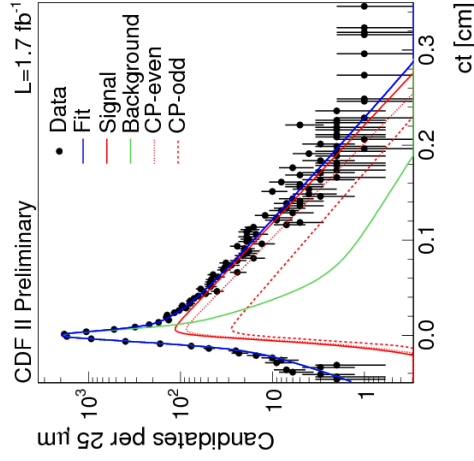
Theory:

$$\tau(B_s)/\tau(B_d) = 1.00 \pm 0.01$$

Using PDG:

$$\tau(B_d) = 1.530 \pm 0.009 \text{ ps}$$

$$\tau(B_s)/\tau(B_d) = 0.99 \pm 0.03$$



Systematics Evaluation:

- B_d decays reco'd as B_s : $O(3\%)$ contamination
- Signal Mass model
- Lifetime Mass Model
- Detector Angular acceptance
- Silicon detector alignment

- Allowing CP violation phase β_s to float in the fitter
- Biases: non-Gaussian estimates in pseudo-experiments
- Significant bias w.r.t statistical uncertainties and dependent on true values in the simulated experiment

⇒ Dependence on one parameter in the likelihood vanishes for some values of other parameters: Likelihood loses degrees of freedom

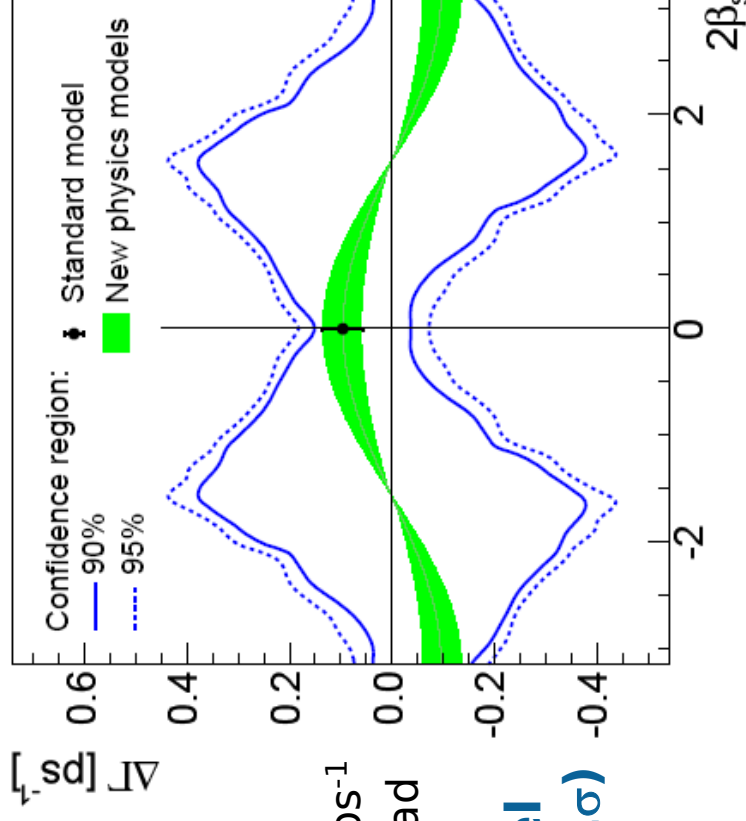
e.g., if $\Delta\Gamma=0$, δ_\perp is undetermined: $\cos(\delta_\perp) \sin(2\beta_s) \sinh(\Delta\Gamma_s t / 2)$

⇒ Two exact symmetries are present in $B_s \rightarrow J/\Psi \Phi$ untagged analysis:

- $2\beta_s \leftrightarrow -2\beta_s, \delta_\perp \leftrightarrow \delta_\perp + \pi$
 - $\Delta\Gamma \leftrightarrow -\Delta\Gamma, 2\beta_s \leftrightarrow 2\beta_s + \pi$
- } 4 equivalent minima

- Difficult to quote a central value with standard uncertainties!

- Quote instead [Feldman-Cousins](#) confidence region
- Use likelihood ratio to determine probability of result to fluctuate above a given value of input parameters (p-value)



Standard Model
expectations:

([arXiv:hep-ph/0612167](https://arxiv.org/abs/hep-ph/0612167))

$$\Delta\Gamma_s = 0.096 \pm 0.039 \text{ ps}^{-1}$$

$$2\beta_s = 0.04 \pm 0.01 \text{ rad}$$

Standard Model

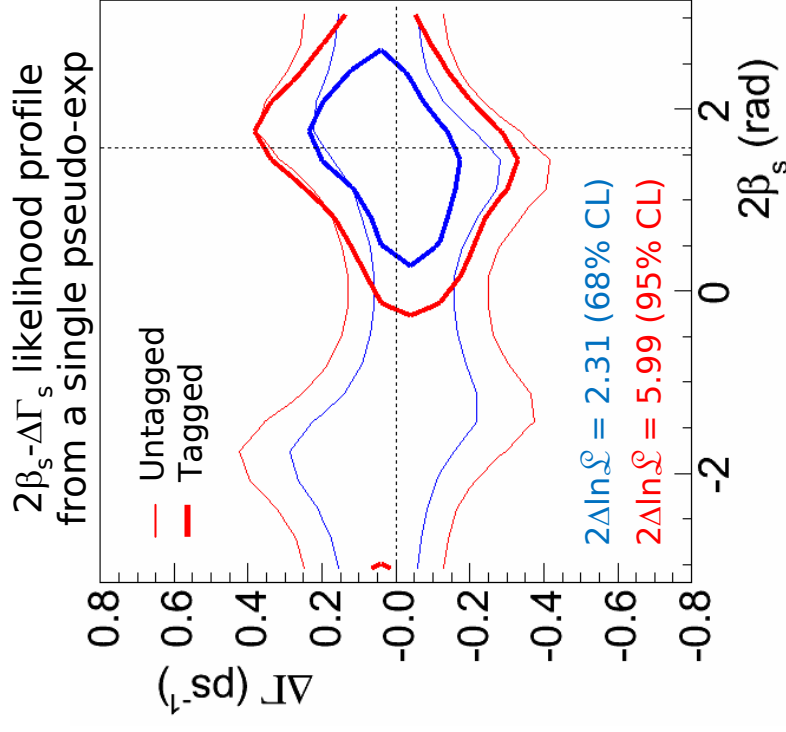
$p_{\text{value}} = 22\% (1.2\sigma)$

Accepted by PRL [arXiv:0712.2343](https://arxiv.org/abs/0712.2343) [hep-ex]

Tagged Analysis

- Tagging improves sensitivity to CP violation phase β_s
- Exact symmetry present in signal probability distribution
- Two minima in the likelihood
- Check $\beta_s - \Delta\Gamma_s$ likelihood profile with Toy MC to understand tagging effect
- Likelihood: with tagging, gain sensitivity to both $|\cos(2\beta_s)|$ and $\sin(2\beta_s)$, rather than only $|\cos(2\beta_s)|$ and $|\sin(2\beta_s)|$ (note absolute value)
- $\beta_s \leftrightarrow -\beta_s$ is no longer a likelihood symmetry:
 - \Rightarrow 4-fold ambiguity reduced to 2-fold
 - \Rightarrow allowed region for β_s is reduced to half

$2\beta_s \leftrightarrow \pi - 2\beta_s$
$\Delta\Gamma_s \leftrightarrow -\Delta\Gamma_s$
$\delta_{\parallel} \leftrightarrow \pi - \delta_{\parallel}$
$\delta_{\perp} \leftrightarrow \pi - \delta_{\perp}$



Likelihood contour does **not** have the correct coverage: the resulting confidence region do not contain the true value with desired CL independently of true value



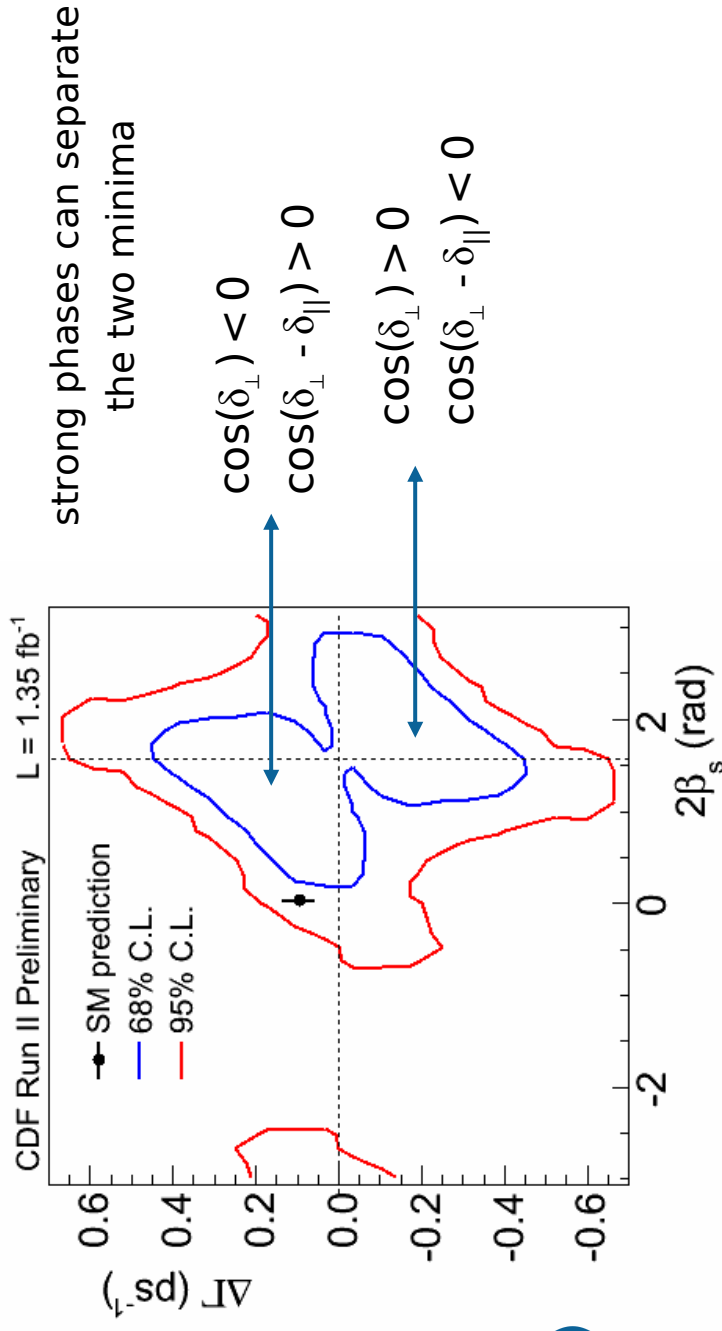
Feldman-Cousins likelihood ratio ordering

Standard Model expectations:

(arXiv:hep-ph/0612167)

$$\Delta\Gamma_s = 0.096 \pm 0.039 \text{ ps}^{-1}$$

$$2\beta_s = 0.04 \pm 0.01 \text{ rad}$$



Standard Model

$p_{\text{value}} = 15\% (1.5\sigma)$

Under PRL review arXiv:0712.2397 [hep-ex]

1-dim Feldman-Cousins procedure on CP violation phase β_s

1. Without External Constraints:

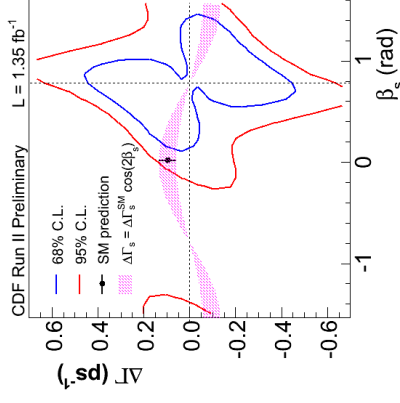
$2\beta_s$ in [0.32, 2.82] at the 68% C.L.



2. $\Delta\Gamma_s$ is theoretically constrained:

• Input $\Delta\Gamma_s \approx 2|\Gamma_{12}|\cos\Phi_s \approx 2|\Gamma_{12}|\cos(2\beta_s)$: ($\Gamma_{12} = 0.048 \pm 0.018$):

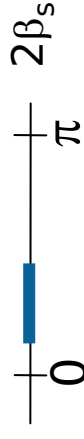
$2\beta_s$ in [0.24, 1.36] U [1.78, 2.90] at 68% C.L.



3. Strong phases from $B_d \rightarrow J/\Psi K^{*0}$ [PRD 71, 032005 (2005)],

B_s lifetime from B_d [PDG] and $\Delta\Gamma_s \approx 2|\Gamma_{12}|\cos(2\beta_s)$:

$2\beta_s$ in [0.40, 1.20] at 68% C.L.



- Inclusive dimuon charge asymmetry $A_{SL}^{\mu\mu} = \frac{N(b\bar{b} \rightarrow \mu^+\mu^+X) - N(b\bar{b} \rightarrow \mu^-\mu^-X)}{N(b\bar{b} \rightarrow \mu^+\mu^+X) + N(b\bar{b} \rightarrow \mu^-\mu^-X)}$

$$Z_q = \frac{1}{1 - [\Gamma_q / (2\Gamma_q)]^2} \frac{1}{1 + (\Delta m_q / \Gamma_q)^2}$$

$$A_{SL}^{\mu\mu} = \frac{1}{4} \left[A_{SL}^d + \frac{f_{s^s} Z_s A_{SL}^s}{f_d Z_d} \right]$$

f_q is the production rate of B_q mesons in the hadronization of the b quark

Combine this result with the measurement from $B_s \rightarrow J/\Psi\Phi$ to constrain the phase β_s

- Using world averages for f_q , the semileptonic asymmetry for B_d from B factories and the measured parameters Δm_q and $\Delta\Gamma_q$ we can extract A_{SL}^s
- if $\Delta m_s / \bar{\Gamma}_s \gg 1 \Rightarrow A_{SL}^s = \frac{\Delta\Gamma_s}{\Delta m_s} \tan\Phi_s$



- Tagged analysis of $B_s \rightarrow J/\psi \Phi$ decay from **DØ**

arXiv: 0802.2255

- **DØ**: ~ 2000 B_s events with 2.8 fb^{-1}
- Combined Tagging Power $\Rightarrow \epsilon D^2 = (4.68 \pm 0.54)\%$
- Quoting point estimate:

$$\tau_s = 1.52 \pm 0.06 \text{ (stat)} \pm 0.01 \text{ (syst)} \text{ ps}$$

$$\Delta\Gamma_s = 0.19 \pm 0.07 \text{ (stat)}^{+0.02}_{-0.01} \text{ (syst)} \text{ ps}^{-1}$$

$$\Phi_s = -2\beta_s = -0.57^{+0.24}_{-0.30} \text{ (stat)}^{+0.07}_{-0.02} \text{ (syst)} \text{ rad}$$

FIT inputs:

Δm_s fixed to 17.77 ps^{-1} ← **CDF**

Gaussian constraint on Strong phases:

$$\delta_{\perp} - \delta_{\parallel} = -0.46 \pm (\pi/5)$$

$$\delta_{\perp} = +2.92 \pm (\pi/5) \leftarrow \text{B Factories}$$

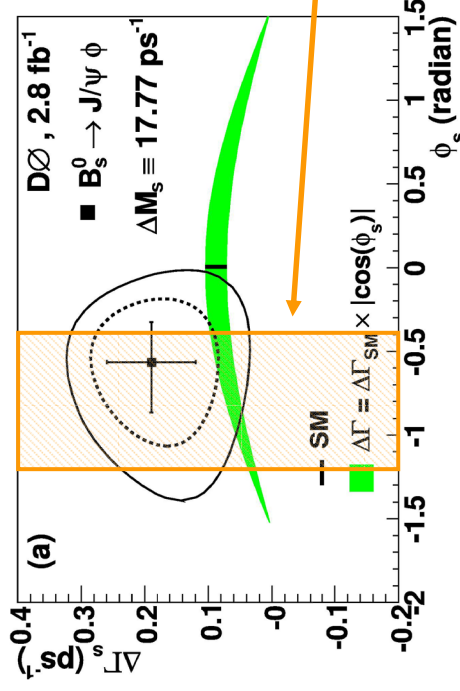
Standard Model expectations:

(arXiv:hep-ph/0612167)

$$2\beta_s = 0.04 \pm 0.01 \text{ rad}$$

Standard Model

$P_{\text{value}} = 6.6\%$



90% C.L. contours:

$$-1.20 < 2\beta_s < 0.06 \text{ rad}$$

$$0.06 < \Delta\Gamma_s < 0.30 \text{ ps}^{-1}$$

CDF 68% CL:

Constraining lifetime, strong phases and $\Delta\Gamma_s$

- **CDF:** 1.6 fb⁻¹ of data collected (di-muon charge asymmetry):

$$A_{\text{SL}}^{\text{S}} = 0.020 \pm 0.021 \text{ (stat)} \pm 0.016 \text{ (syst)} \pm 0.009 \text{ (inputs)}$$

(<http://www-cdf.fnal.gov/physics/new/bottom/070816.blessed-acp-bsemil/>)

- **DØ:** 1.0 fb⁻¹ of data collected (di-muon charge asymmetry):

$$A_{\text{SL}}^{\text{S}} = -0.0064 \pm 0.0101 \text{ (stat + syst)}$$

PRD 74, 092001 (2006)

- **DØ:** 1.3 fb⁻¹ of data collected (B_s semileptonic decays):

$$A_{\text{SL}}^{\text{S}} = [2.45 \pm 1.93 \text{ (stat)} \pm 0.35 \text{ (syst)}] \times 10^{-2}$$

PRL 98, 151801 (2007)

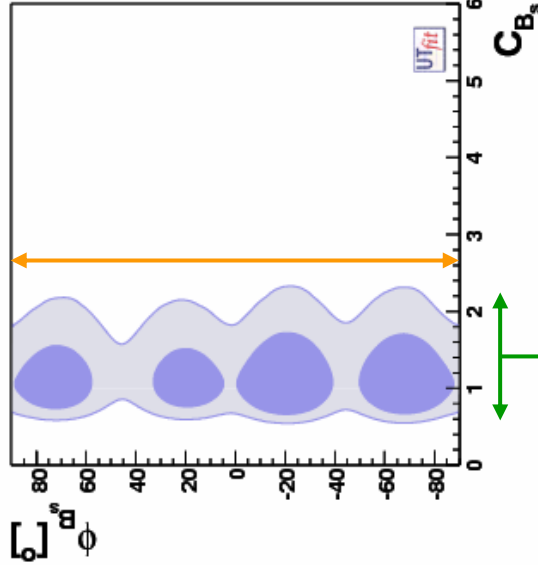
- **Unofficial Tevatron Average (Rescaled to common inputs):**

$$A_{\text{SL}}^{\text{S}} = [-0.0054 \pm 0.0072 \text{ (stat + syst)}]$$

UTfit inputs:

- Δm_s measurement (CDF)
- Lifetime τ_s (CDF and DØ)
 - $\Delta \Gamma_s$ (CDF on 200 pb⁻¹)
- $\Delta \Gamma_s$ and Φ_s (DØ on 1.1 fb⁻¹)
- Semileptonic A_{SL} (DØ)

B_s System

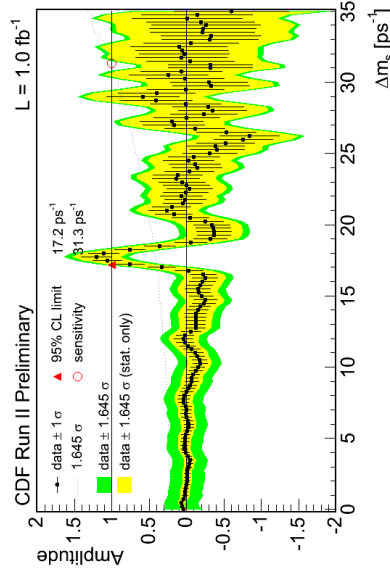


UTfit Group

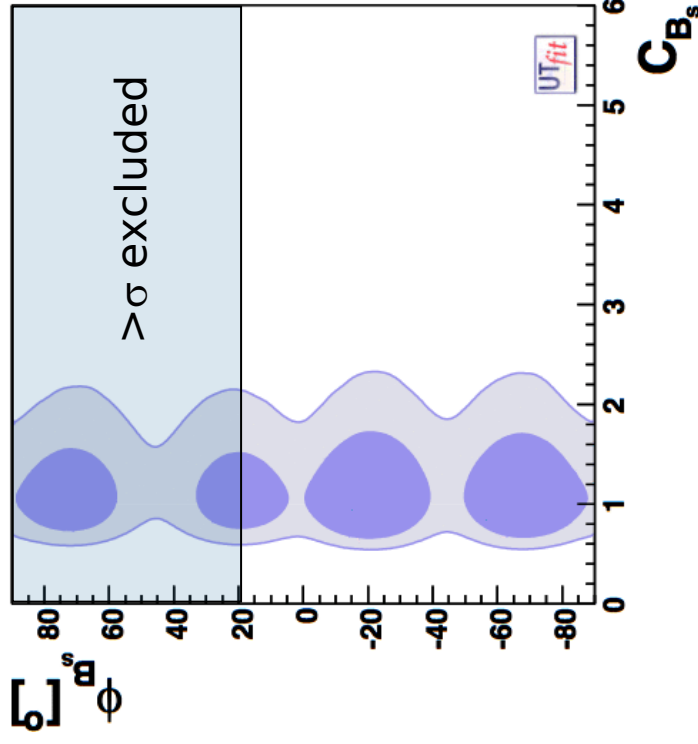
$\Delta m_s = C_{B_s} * \Delta m_s^{SM}$: Lattice-QCD dominated uncertainty

$$\frac{\langle B_s | H_{\text{eff}}^{\text{full}} | \bar{B}_s \rangle}{\langle B_s | H_{\text{eff}}^{SM} | \bar{B}_s \rangle} = C_{B_s} e^{2i\Phi_{B_s}}$$

$\beta_s = \beta_s^{SM} - \Phi_{B_s}$: Experimentally dominated uncertainty (today physics topic)



New Physics in B_s mixing

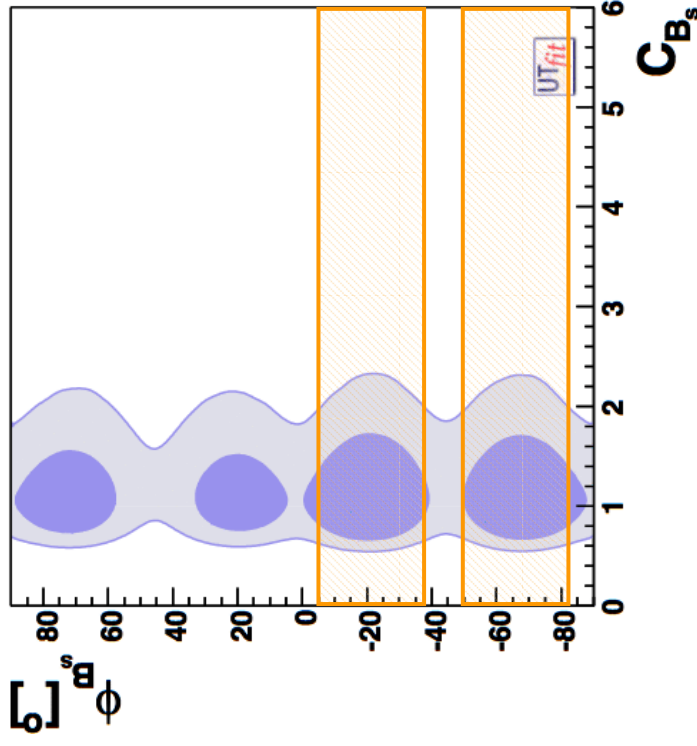


(<http://www.utfit.org/>)

$$C_{B_s} e^{2i\phi_{B_s}} = \frac{\langle B_s | H_{\text{eff}}^{\text{full}} | \bar{B}_s \rangle}{\langle B_s | H_{\text{eff}}^{\text{SM}} | \bar{B}_s \rangle}$$

$$\Delta m_s = C_{B_s} \cdot \Delta m_s^{\text{SM}}$$

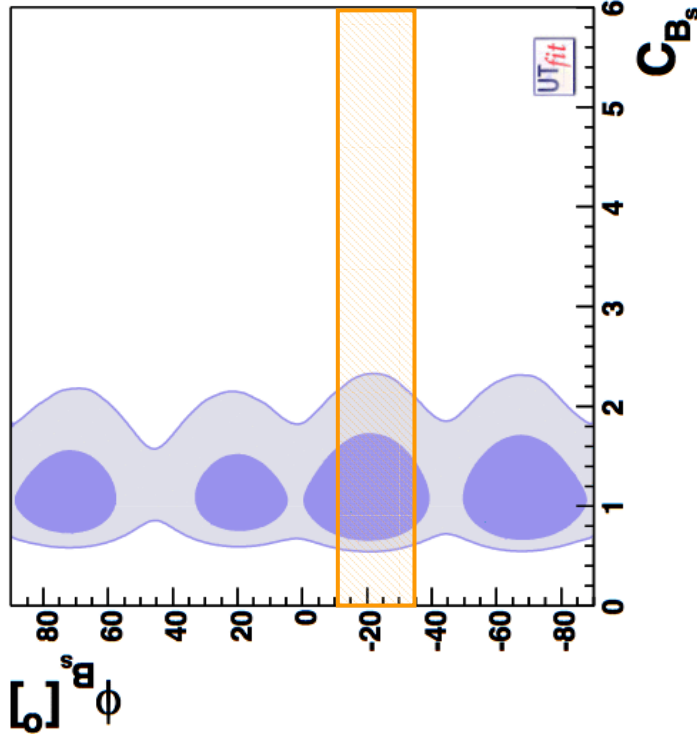
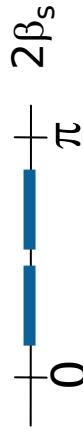
$$\beta_S^{\text{exp}} = \beta_S^{\text{SM}} - \Phi_{B_s}$$



- Constraint:

- ✓ $\Delta\Gamma_s = 2|\Gamma_{12}|\cos\Phi_s \approx 2|\Gamma_{12}|\cos(2\beta_s)$
with $(\Gamma_{12}=0.048\pm 0.018)$:

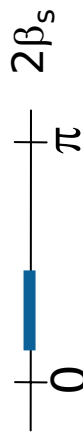
$$2\beta_s \in [0.24, 1.36] \cup [1.78, 2.90] \text{ at } 68\% \text{ C.L.}$$



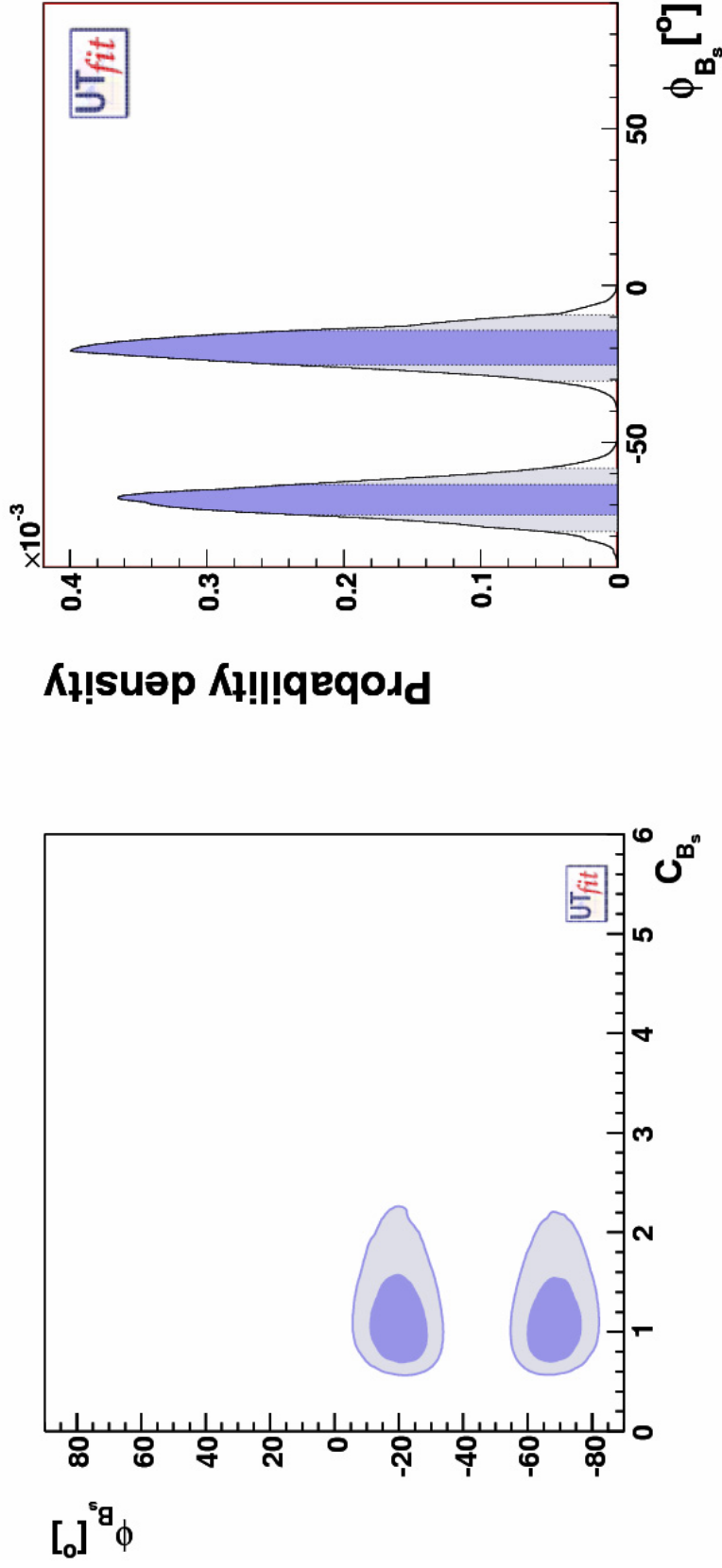
- Constraints:

- ✓ Strong phases from $J/\Psi K^{*0}$ [hep-ex/0411016],
 B_d lifetime [PDG] and $\Delta\Gamma_s \approx 2|\Gamma_{12}|\cos(2\beta_s)$:

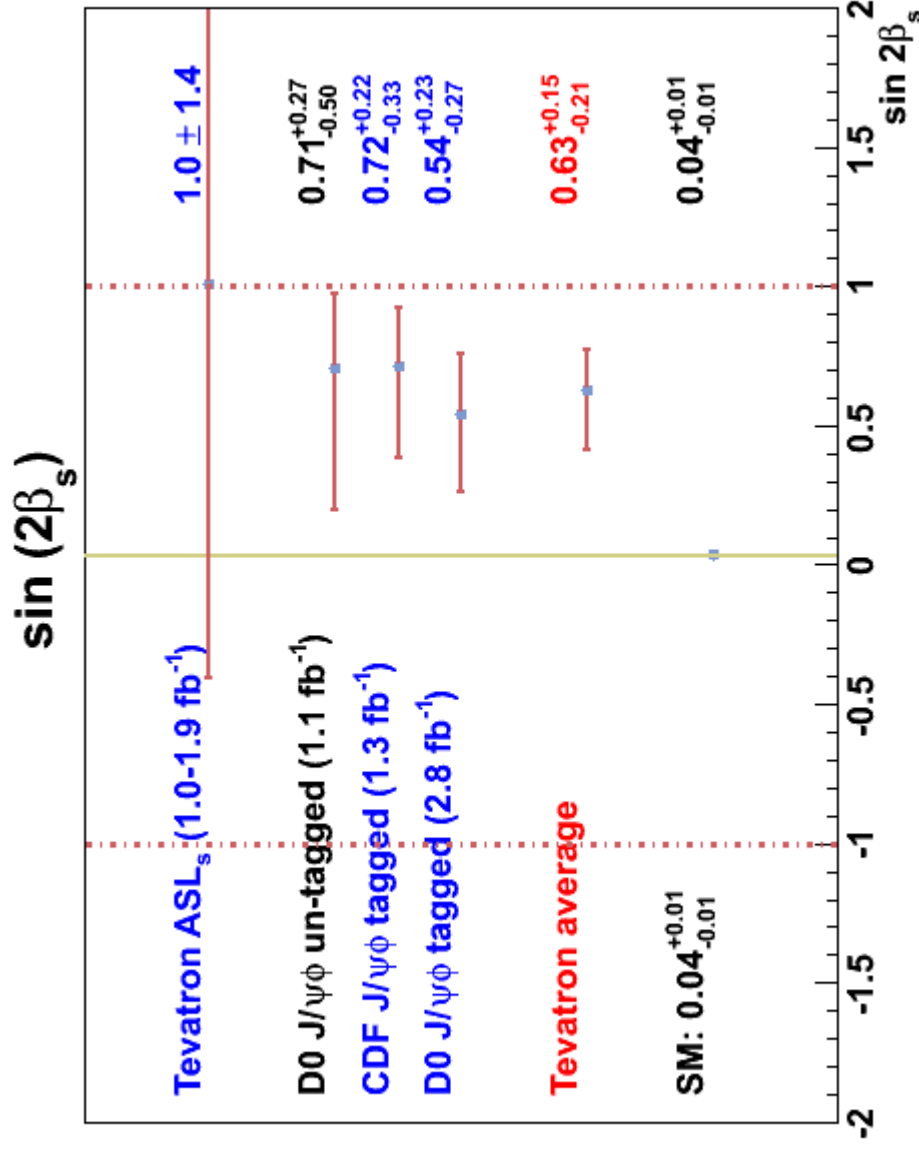
$$2\beta_s \in [0.40, 1.20] \text{ at } 68\% \text{ C.L.}$$



Thanks to Luca Silvestrini & Marco Ciuchini!



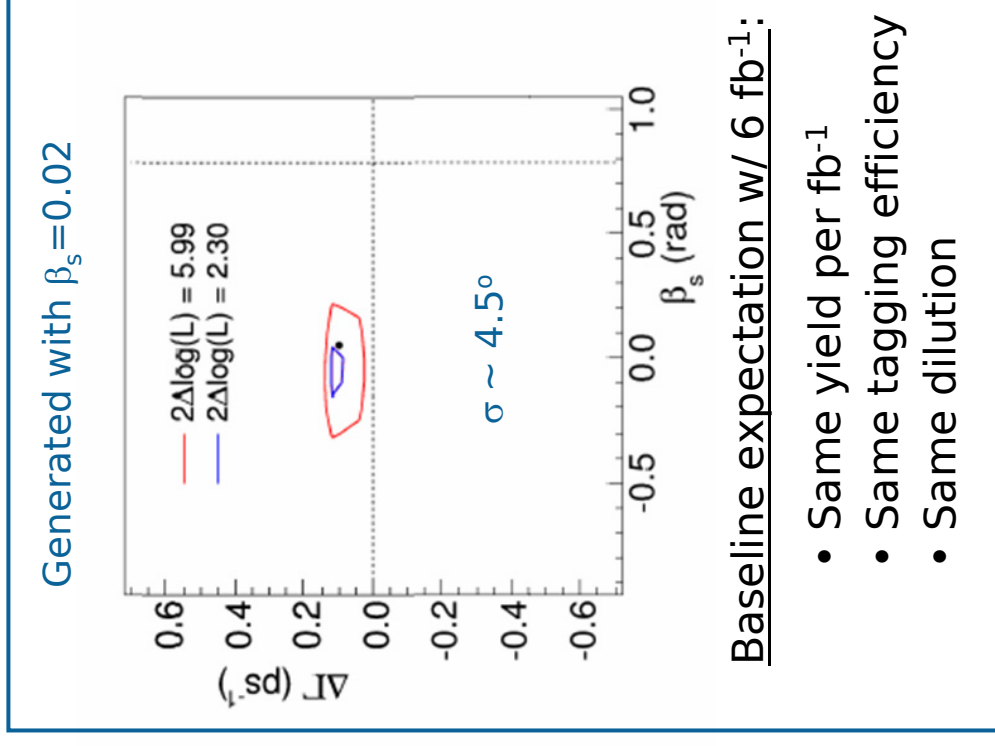
- CDF(DØ) searches for CP violation in B_s system:
 - ✓ Direct CP violation (e.g. $B_s \rightarrow K^- \pi^+$)
 - ✓ CP Violation in Mixing: precise A_{SL}^S measurement (to be compare in perspective with A_{SL}^d)
 - ✓ CP Violation in the interference between mixing and decay: $\sin(2\beta_s)$ measurement → [today topic](#)
- Interesting $\sin(2\beta_s)$ fluctuation at Tevatron experiments:
 - ✓ Both experiments, CDF and DØ
 - ✓ In both measurements, untagged and tagged
 - ✓ In the same direction of A_{SL}

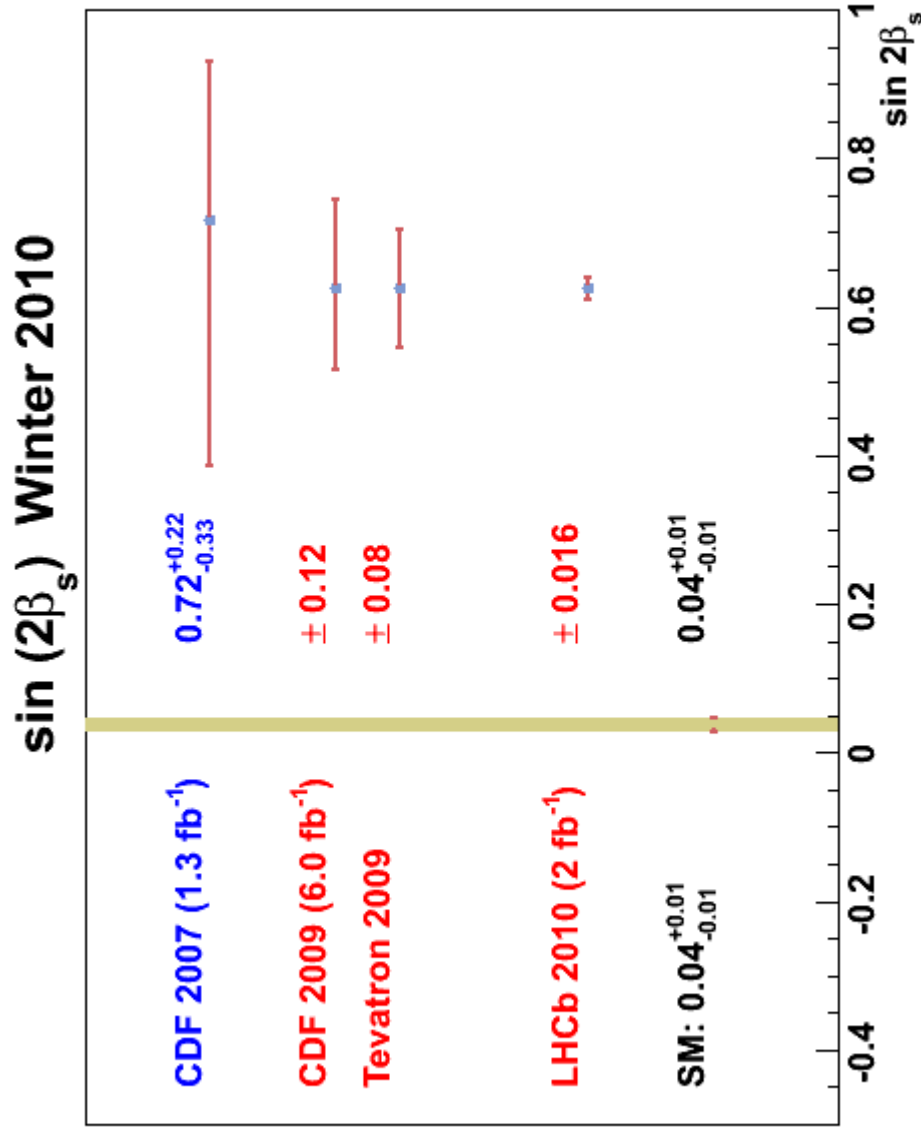


- Measurement of $\sin(2\beta_s)$ is a key part of the LHCb flavor program

Analysis improvements:

- Add more data: so far only 15% of available statistics at the end of next year
- Exploit additional 50% statistics from other triggers
- Better behaved likelihood at higher statistics
- Improve tagger performances





Backup Slides

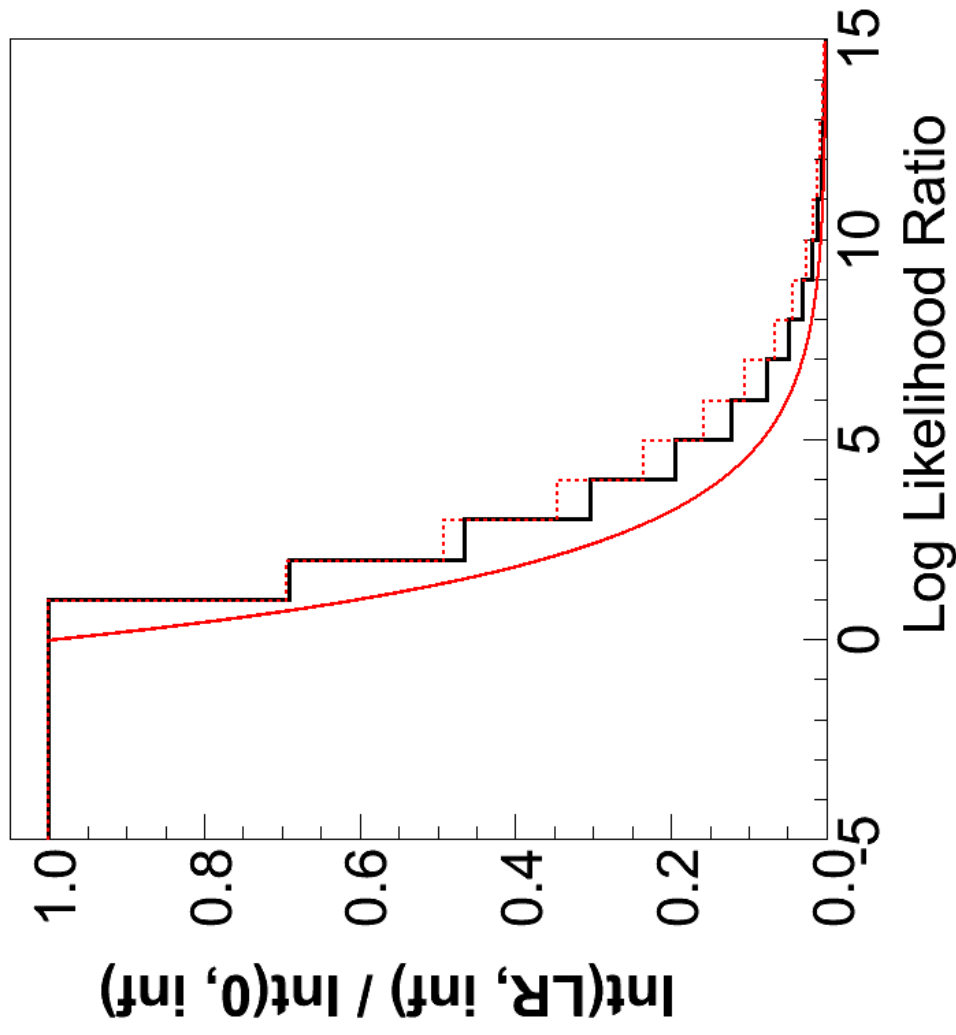
Likelihood Ratio:
$$R(\Delta\Gamma, \Phi) = \log \frac{L(\Delta\hat{\Gamma}, \hat{\Phi}, \hat{\theta})}{L(\Delta\Gamma, \Phi, \hat{\theta}')}$$

$\hat{}$ = parameters minimized by the likelihood L

θ' = parameters which minimize L for a specific choice of $\Delta\Gamma, \Phi$

1. For a specific choice of $\Delta\Gamma, \Phi$ pseudo-exp are generated using θ'
2. $p_{\text{value}} = \int_{R_{\text{data}}}^{\infty} f(R, \Delta\Gamma, \Phi) dR$ } Plug-In Method

Frequentist approach: probability to observe a result with $R \geq R_{\text{data}}$, if $\Delta\Gamma$ and Φ are the values predicted by some model



$B_s \rightarrow J/\Psi \Phi$ differential decay rate depends on 4 event variables:

- **ct**: Proper decay length
- \vec{w} : vector formed by the 3 angles that characterize the decay
- ξ : tag decision (+1 if B_s , -1 if \bar{B}_s , 0 if no tag)

... some other parameters describing the physics:

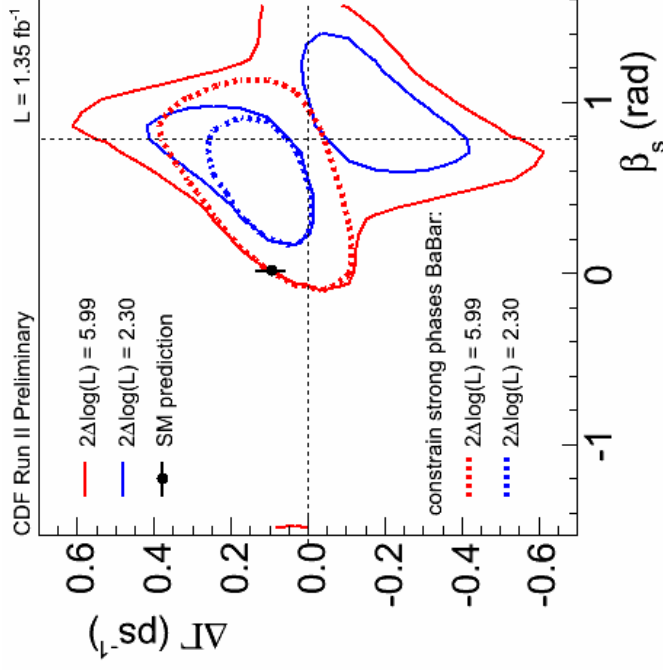
- ✓ $|A_\alpha|$, $\alpha = \{0, ||, \perp\}$: amplitudes for decay to longitudinal (CP-even), transverse and parallel to each other (CP-even) or perpendicular to each other (CP-odd) polarizations of $J/\Psi \Phi$
- ✓ δ_α : Strong phases associated with those amplitudes
- ✓ Γ , $\Delta\Gamma$: Average lifetime and lifetime difference
- ✓ β_s : CP violation phase in $b \rightarrow c\bar{c}s$ transition

$$P(\text{ct}, \vec{w} | \xi) = \frac{1 + \xi D}{1 + |\xi|} P_B(\text{ct}, \vec{w}) \varepsilon(\vec{w}) + \frac{1 - \xi D}{1 + |\xi|} P_{\bar{B}}(\text{ct}, \vec{w}) \varepsilon(\vec{w})$$

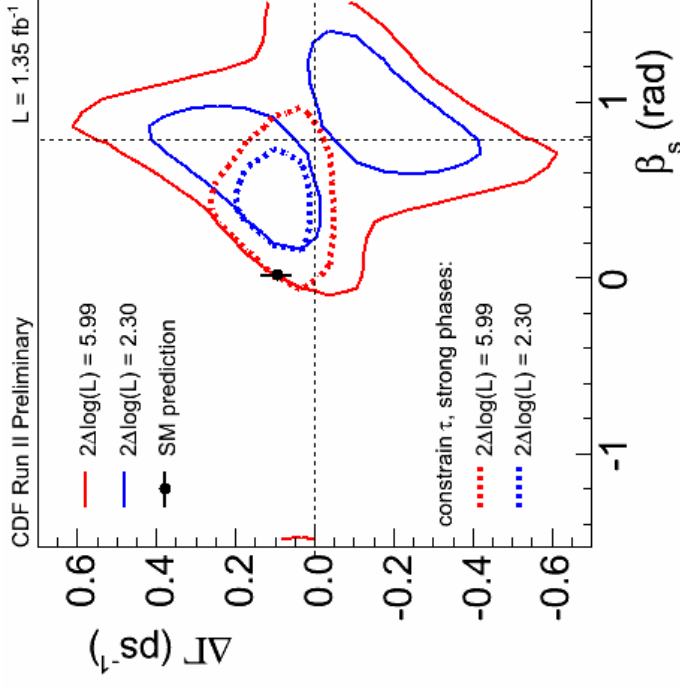
- $\varepsilon(\vec{w})$ is the sculpting of transversity angles due to detector acceptance

- SU(3) flavor symmetry suggests that B_s and B^0 have similar lifetimes and strong phases
- Likelihood profiles with external constraints from B factories
- Underestimated confidence regions when using $2\Delta\ln\mathcal{L} = 2.31$ (5.99) to approximate 68% (95%) C.L. regions

constrain strong phases



constrain lifetime and strong phases



⇒ External constraints on strong phases remove residual 2-fold ambiguity

Most powerful tagger available:

- ✓ 2-3 times more effective than combined OST

Exploit charge correlation between b and fragmentation tracks:

- ✓ B^+ , B^0 likely to have a π^- , π^+ nearby
- ✓ B_s likely to have K^+

Neural Network separates kaons and pions:

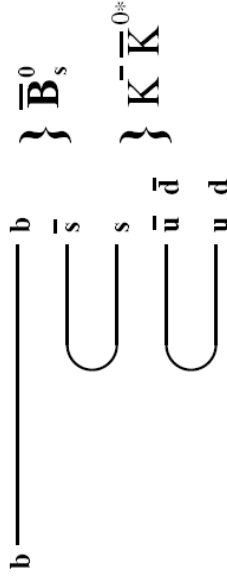
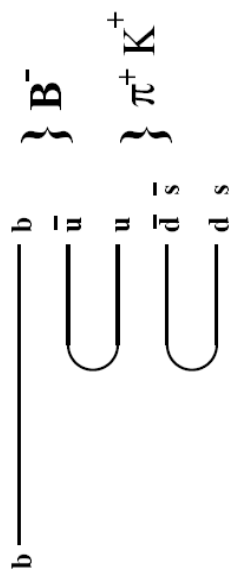
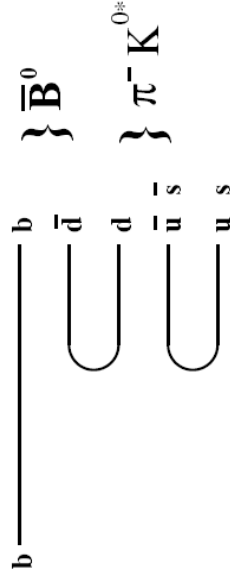
- ✓ **TOF and COT dE/dx** crucially important
- ✓ Kinematic of candidate provide additional separating power

Unlike OST, SSKT is different for B^0 , B^+ and B_s :

- ✓ SST needs to rely on MC simulation
- ✓ Data and MC thoroughly compared

Performance:

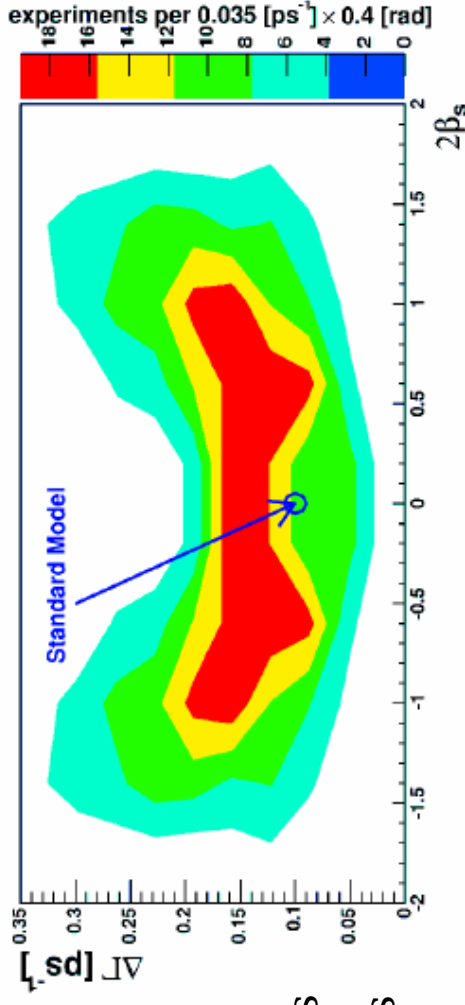
- ✓ Efficiency: $\epsilon = 0.50 \pm 0.01$
- ✓ Average Dilution: $D = 0.27 \pm 0.04$



OST and SST
combined
independently

Fits on simulated samples

generated with SM inputs for $\Delta\Gamma_s$ and β_s



- Biases
- Non-Gaussian estimates in pseudo-experiments
- Strong dependence on true values for biases on some fit parameters

⇒ Dependence on one parameter in the likelihood vanishes for some values of other parameters: Likelihood loses degrees of freedom

e.g., if $\Delta\Gamma=0$, δ_\perp is undetermined: $\cos(\delta_\perp) \sin(2\beta_s) \sinh(\Delta\Gamma_s t/2)$

⇒ Two exact symmetries are present in $B_s \rightarrow J/\Psi \Phi$ untagged analysis:

- $2\beta_s \leftrightarrow -2\beta_s, \delta_\perp \leftrightarrow \delta_\perp + \pi$
 - $\Delta\Gamma \leftrightarrow -\Delta\Gamma, 2\beta_s \leftrightarrow 2\beta_s + \pi$
- } 4 equivalent minima

- Direct CP asymmetry $A_{CP}(B_S \rightarrow K^- \pi^+)$ in a self tagging mode:

$$A_{CP} = \frac{N(\overline{B}_S^0 \rightarrow K^+ \pi^-) - N(B_S^0 \rightarrow K^- \pi^+)}{N(\overline{B}_S^0 \rightarrow K^+ \pi^-) + N(B_S^0 \rightarrow K^- \pi^+)}$$

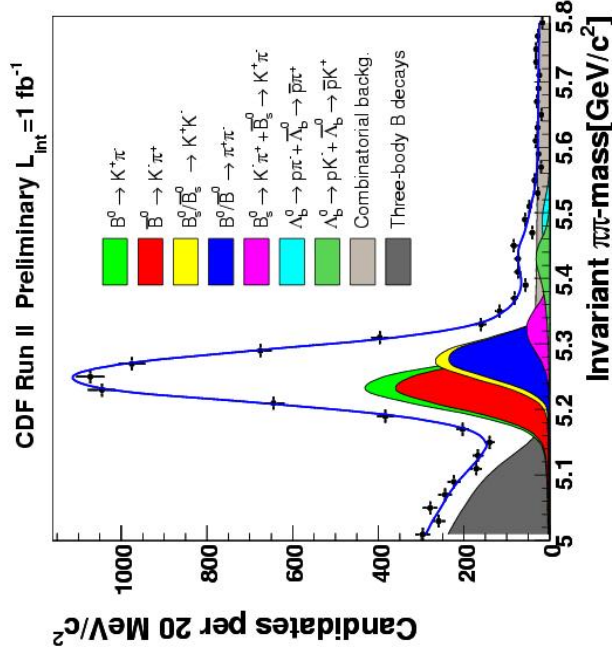
- Observed for the first time three new rare charmless modes:

$$N(B_S^0 \rightarrow K^- \pi^+) = 230 \pm 34 \text{ (stat)} \pm 16 \text{ (syst)} [8\sigma \text{ signif}]$$

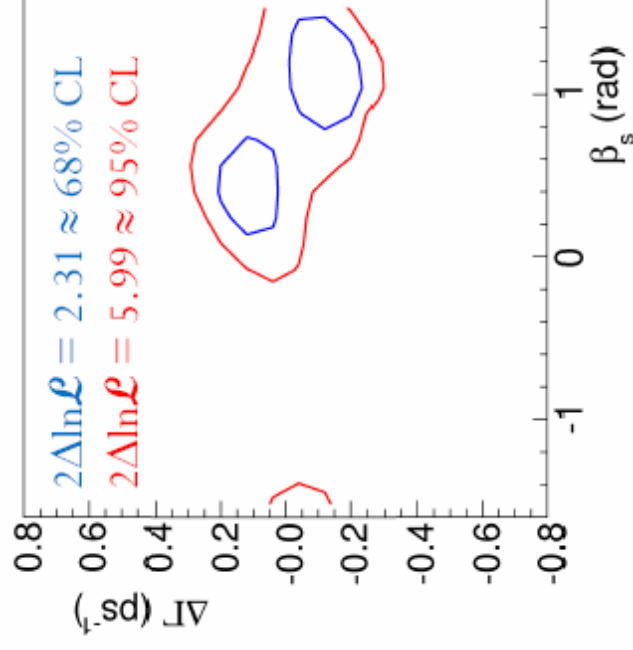
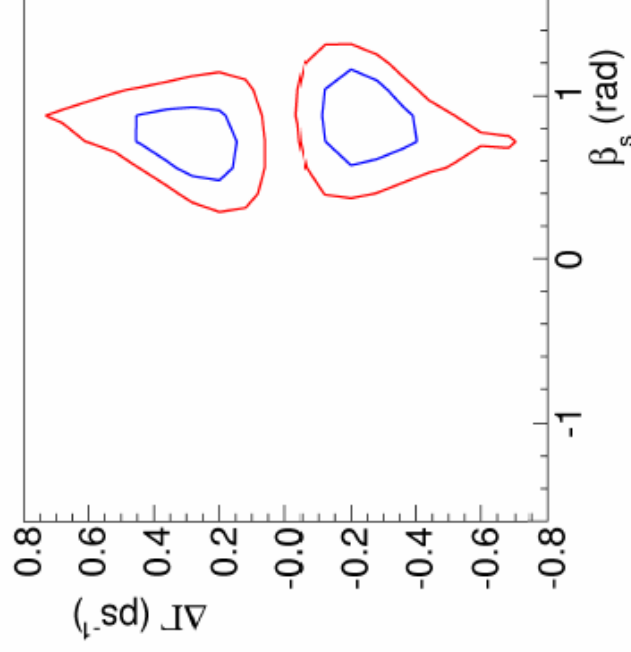
- Direct CP violation due to interference between penguin and tree diagrams:

$$A_{CP}(B_S^0 \rightarrow K^- \pi^+) = 0.39 \pm 0.15 \text{ (stat)} \pm 0.08 \text{ (syst)}$$

- A_{CP} is 2.5σ different from 0
- Compatible with SM expectation (~ 0.37) [H.J.Lipkin, Phys. Lett. B **621**, 126 (2005)]

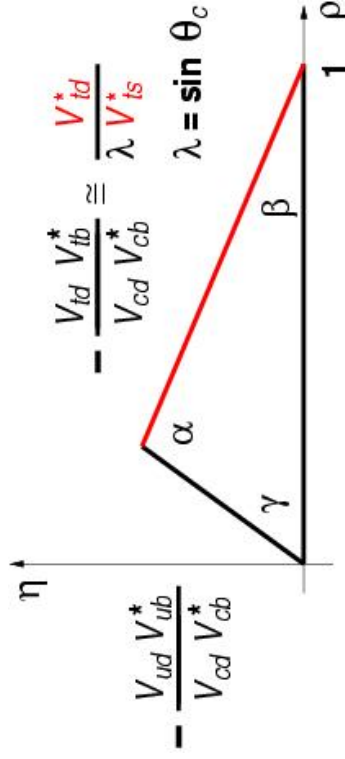


- Check β_s - $\Delta\Gamma$ likelihood profile on Toy MC
 - Likelihood profile is NOT parabolic
 - Shape strongly dependent on “true” values
- } Cannot reliably quote central values and uncertainties



CDF: World First Observation (5σ)

- Unitarity Triangle:



Ratio of frequencies for B⁰ and B_s

$$\frac{\Delta m_s}{\Delta m_d} = \frac{m_{B_s} f_{B_s} B_{B_s} |V_{ts}|^2}{m_{B_d} f_{B_d} B_{B_d} |V_{td}|^2} = \frac{m_{B_s} \xi^2}{m_{B_d}} \frac{|V_{ts}|^2}{|V_{td}|^2}$$

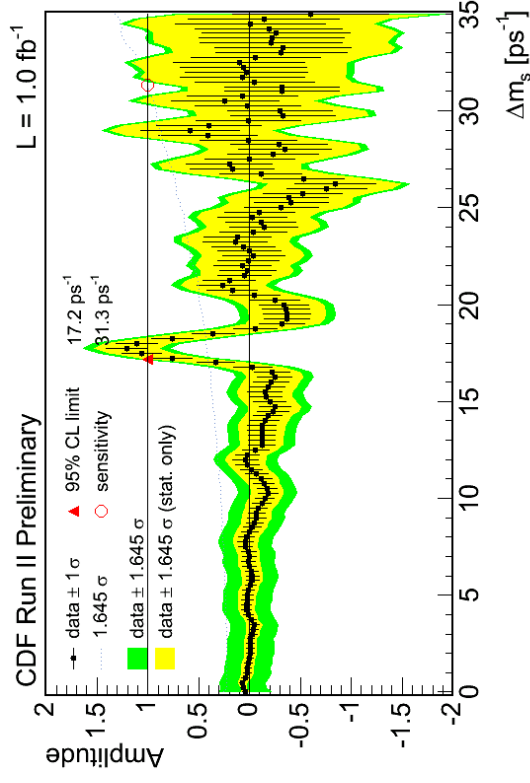
$\xi = 1.210^{+0.047}_{-0.035}$ from lattice QCD
(hep/lat-0510113)

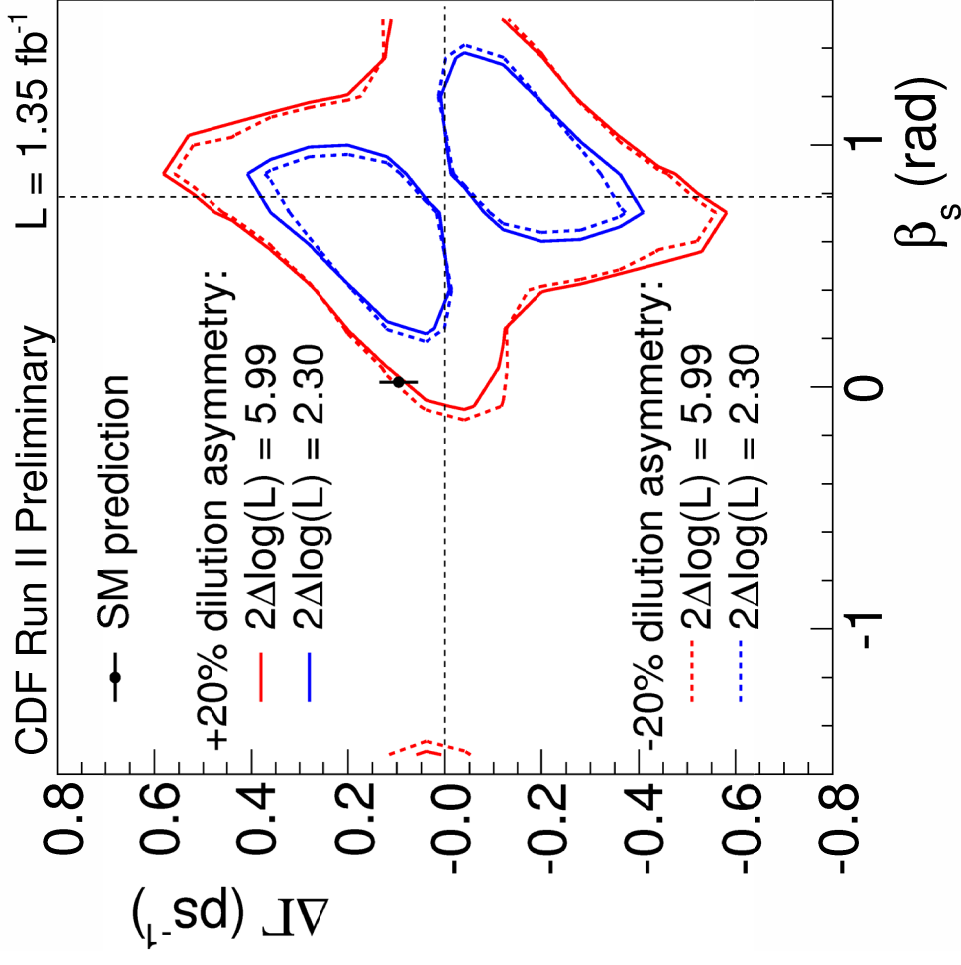
$$V_{ts} \sim \lambda^2, V_{td} \sim \lambda^3, \lambda = 0.224 \pm 0.012$$

- Integrated Luminosity: 1 fb⁻¹

$$\Delta m_s = 17.77 \pm 0.10 \text{ (stat)} \pm 0.07 \text{ ps}^{-1}$$

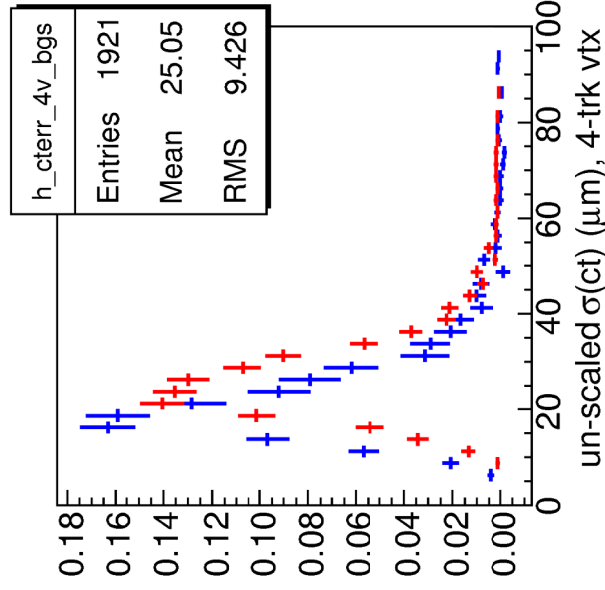
$$\left| \frac{V_{td}}{V_{ts}} \right| = 0.2060 \pm 0.0007 \text{ (exp)}^{+0.0081}_{-0.0060} \text{ (theor)}$$





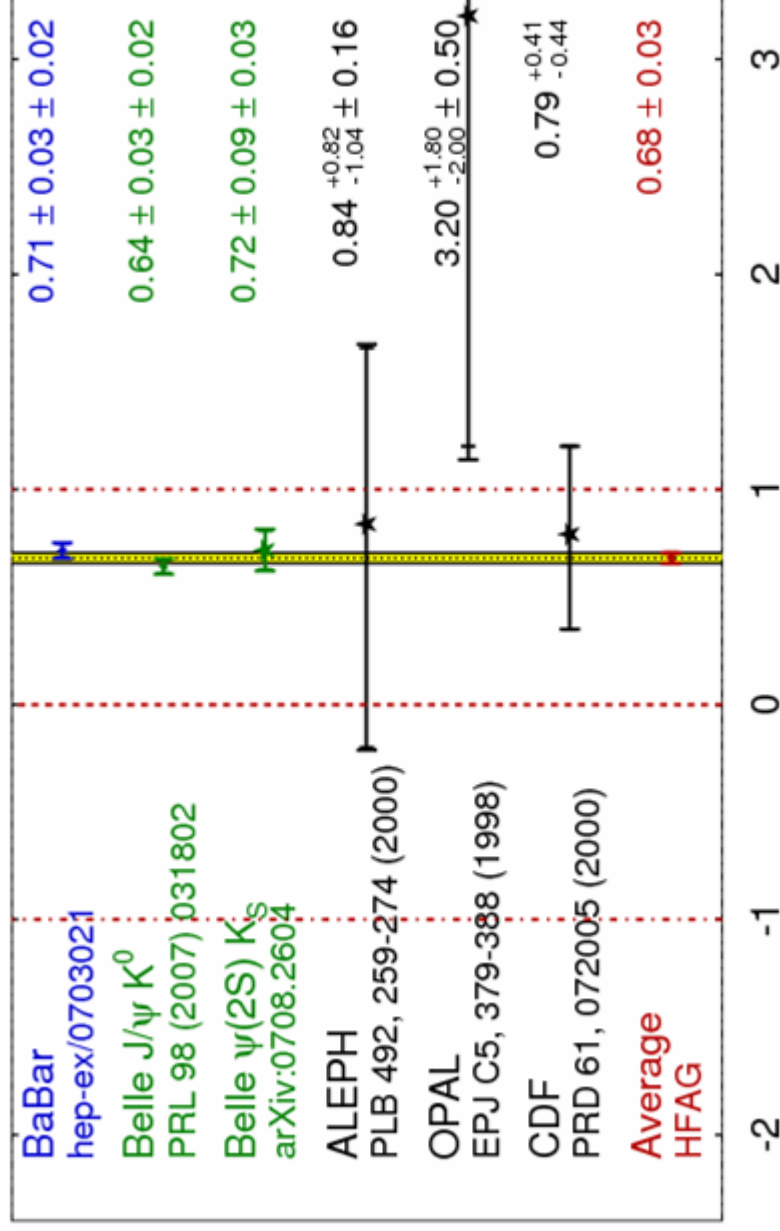
Effect of 20% b-bbar dilution asymmetry is very small

- The mean is of the sideband subtracted σ_{ct} resolution for a 4-track vertex is 25.05 μm
- This has to be multiplied by the ct resolution scale factor determined from the prompt peak: $s = 1.262 \pm 0.020$
- The most probable value is at 18.5 μm . This means 23.3 μm after sigma ct scaling or 77.8 fs.



$$\sin(2\beta) \equiv \sin(2\phi_1)$$

HFAG
LP 2007
PRELIMINARY



2000:

- **CDF Run I** measurement on $\sin(2\beta)$ on 110 pb^{-1}
- $B^0 \rightarrow J/\Psi K_S$: ~ 400 signal candidates
- $\sin(2\beta) = 0.79^{+0.41}_{-0.44}$ (stat + syst) PRD 61, 072005 (2000)

B Factories:

- **2005 Babar:** $\sin(2\beta) = 0.722 \pm 0.040$ (stat) ± 0.023 (syst) PRL 94, 161803 (2005)
- **2007 Belle:** $\sin(2\beta) = 0.642 \pm 0.031$ (stat) ± 0.017 (syst) PRL 98, 031802 (2007)
- **2007 PDG:** $\sin(2\beta) = 0.673 \pm 0.028$

2005:

- **CDF Run II** measurement on $\Delta\Gamma_s$ assuming $\beta_s = 0$ on 260 pb^{-1}
- $B_s \rightarrow J/\Psi \Phi$: ~ 200 signal candidates PRL 94, 101803 (2005)

2007:

- **DØ** measurement on $\Delta\Gamma_s$ and β_s on 1.1 fb^{-1}
- $B_s \rightarrow J/\Psi \Phi$: ~ 1040 signal candidates
- $2\beta_s = -0.79 \pm 0.56$ (stat) $^{+0.14}_{-0.01}$ (syst) rad PRL 98, 121801 (2007)