An alternative measurement of CLQED

(at e+e-colliders in small angle Bhabha scattering)

A.Arbuzov D.Haidt C.Matteuzzi M.Paganoni L.T.

CERN-PH-TH/2004-016 - hep-ph/0402211 European Physics Journal C35, 267 (2004)

Roma "la Sapienza" 10/3/2006

We propose a method to determine the running of COED from the measurement of small-angle Bhabha scattering

The method is suited to high statistics experiments at e+e– colliders, which are equipped with luminometers in the appropriate angular region

We present a new simulation code predicting smallangle Bhabha scattering The electroweak Standard Model SU(2) \otimes U(1) contains Quantum Electrodynamics QED as a constitutive part.

The running of the electromagnetic coupling

 $\alpha_{\text{QED}}(q^2)$ is determined by the theory as $\alpha_{\text{QED}}(q^2) = \alpha_{\text{QED}}(0) / 1 - \Delta \alpha(q^2)$

 $\alpha_{OED}(0) = \alpha_0$

 $\alpha_0 = \frac{e^2}{2\pi\varepsilon_0 hc}$

is the Sommerfeld *"fine structure constant"*





$\Delta \alpha(q^2)$ Vacuum polarization $\Delta \alpha = \Delta \alpha_{lept} + \Delta \alpha_{had}$

arises from quantum loop contribution to the photon propagator receiving contributions from quarks (hadrons), leptons and gauge bosons

The hadronic contribution is estimated in the s channel with a dispersion integral

from the cross-section e+e- to hadrons cross-section

S. Eidelman and F. Jegerlehner: Z. Phys. C67 (1995) 602 F. Jegerlehner: hep-ph/0308117 M. Davier and A. Höcker: Phys. Lett. **B435** (1998) 427 M. Davier, S. Eidelman, A. Höcker and Z. Zhang: Eur. Phys. J. C27 (2003) 497

$$\begin{aligned} \Delta \alpha &= \sum_{f} \gamma \int_{f} \gamma \int_{f} \gamma \\ &= \frac{\alpha}{3\pi} \sum_{f} Q_{f}^{2} N_{cf} \left(\ln \frac{M_{Z}^{2}}{m_{f}^{2}} - \frac{5}{3} \right) \\ &= \Delta \alpha_{\text{leptons}} + \Delta \alpha_{\text{quarks}}^{(5)} \,. \end{aligned}$$

$$\begin{aligned} \alpha(s) &= \frac{\alpha}{1 - \Delta \alpha(s)} \\ \Delta \alpha(s) &= -4\pi \alpha \text{Re} \left[\Pi_{\gamma}'(s) - \Pi_{\gamma}'(0) \right] \;. \end{aligned}$$

$$Re\Pi_{\gamma}'(s) - \Pi_{\gamma}'(0) = \frac{s}{\pi} Re \int_{s_0}^{\infty} ds' \frac{Im\Pi_{\gamma}'(s')}{s'(s' - s - i\varepsilon)}$$

and using the optical theorem (unitarity) one has

$$Im\Pi'_{\gamma}(s) = \frac{s}{e^2} \sigma_{tot}(e^+e^- \to \gamma^* \to \text{hadrons})(s) \ .$$

In terms of the cross-section ratio

$$R(s) = \frac{\sigma_{tot}(e^+e^- \to \gamma^* \to \text{hadrons})}{\sigma(e^+e^- \to \gamma^* \to \mu^+\mu^-)}$$

2

where $\sigma(e^+e^-\to\gamma^*\to\mu^+\mu^-)=\frac{4\pi\alpha^2}{3s}$ at tree level, we finally obtain

$$\Delta \alpha^{(5)}_{\rm hadrons}(M_Z^2) = -\frac{\alpha M_Z^2}{3\pi} Re \int_{4m_\pi^2}^{\infty} ds \frac{R(s)}{s(s-M_Z^2-i\varepsilon)}$$

 $R(s) = \frac{\sigma_{tot}(e^+e^- \to \gamma^* \to hadrons)}{\sigma(e^+e^- \to \gamma^* \to \mu^+\mu^-)}$



Here we follow an alternative approach: $e^{t} = \prod_{e} \Pi(t) = \Delta \alpha(t)$

- the running of α is evaluated by using small-angle Bhabha scattering
- This process provides unique information on the QED coupling constant α at low space-like momentum transfer $t = -|q^2|$ in the t channel, with $t = -(1/2)s(1 - \cos \theta)$ for example for

$$\begin{aligned} & \overline{s} = 91.1 GeV \\ & \theta = 30 \ mrad \\ & \theta = 150 \ mrad \\ & t = 30 \ GeV^2 \end{aligned}$$



by using alphaQED F. Jegerlehner



by using alphaQED F. Jegerlehner

The method to measure α_{OED}

exploits the fact that the cross section for the process $e+e- \rightarrow e+e-$ can be conveniently decomposed into three factors:

$$\frac{\mathrm{d}\sigma}{\mathrm{d}t} = \frac{\mathrm{d}\sigma^0}{\mathrm{d}t} \left(\frac{\alpha(t)}{\alpha(0)}\right)^2 \left(1 + \Delta r(t)\right)$$

- The Bhabha Born cross section, including soft and virtue photons is precisely known and accounts for the strongest dependence on t
- The vacuum-polarization effect in the leading photon t- hannel exchange is incorporated in the running of α and gives rise to the quared factor
- $\Delta r(t)$ collects all the remaining real (in particular collinear) and virtual radiative effects not incorporated in the running of α
- The experimental data (after correction for detector effects) have to be compared with this distribution

The evaluation of the luminosity

The precise determination of the luminosity at e+e- colliders is a crucial ingredient to obtain an accurate evaluation of all the physically relevant cross sections.

They necessarily have to rely on some reference process, which is usually taken to be the small-angle Bhabha scattering.

Given the high statistical precision provided by the LEP collider, an equally precise knowledge of the theoretical small-angle Bhabha cross section is mandatory. In the 1990's the substantial progress in measuring the luminosity reached by the LEP machine has prompted several groups to make a theoretical effort aiming

at a **0.1%** accuracy.

At even better accuracy can be reached once the complete two-loop Bhabha (including α constants) cross-section will be computed

This goal has indeed been achieved by developing a dedicated strategy. For the first time small-angle Bhabha scattering was evaluated analytically, following a new calculation technique that yields the required precision

> Arbuzov,Fadin,Lipatov,Merenkov,Kuraev,T.(1995) Nucl.Phys.B485(1997)457

Analytical calculations have been combined with Monte Carlo programs in order to simulate realistically the conditions of the LEP experiments

LABSMC

NLLBHA

SAMBHA

BHLUMI

Two-Loop Corrections to Bhabha Scattering

Alexander A. Penin 1,2

¹Institut für Theoretische Teilchenphysik, Universität Karlsruhe, 76128 Karlsruhe, Germany ²Institute for Nuclear Research, Russian Academy of Sciences, 117312 Moscow, Russia

The two-loop radiative photonic corrections to Bhabha scattering are computed in the leading order of the small electron mass expansion up to the nonlogarithmic term. After including the soft photon bremsstrahlung we obtain the infrared-finite result for the differential cross section, which can directly be applied to a precise luminosity determination of the present and future $e^+e^$ colliders.

hep-ph/0501120

PHYSICAL REVIEW D 71, 073009 (2005)

Master integrals for massive two-loop Bhabha scattering in QED

M. Czakon*

Institut für Theoretische Physik und Astrophysik, Universität Würzburg, Am Hubland, D-97074 Würzburg, Germany Institute of Physics, University of Silesia, Uniwersytecka 4, PL-40-007 Katowice, Poland

I. Gluza[†] DESY, Platanenallee 6, 15738 Zeuthen, Germany Institute of Physics, University of Silesia, Uniwersytecka 4, PL-40-007 Katowice, Polanek in Drogregos T. Riemann[‡]

Two-Loop Photonic Corrections to Massive Bhabha Scattering

hep-ph/0508127

A.A. Penin ^{a,b}

The cross section $d\sigma^0/dt$

$$\frac{\mathrm{d}\sigma^{0}}{\mathrm{d}t} = \frac{\mathrm{d}\sigma^{B}}{\mathrm{d}t} \left(\frac{\alpha(0)}{\alpha(t)}\right)^{2}$$

$$\frac{\mathrm{d}\sigma^B}{\mathrm{d}t} = \frac{\pi\alpha_0^2}{2s^2} \mathrm{Re}\{B_t + B_s + B_i\},\,$$

$$\begin{split} B_t &= \left(\frac{s}{t}\right)^2 \left\{ \frac{5+2c+c^2}{(1-\Pi(t))^2} + \xi \frac{2(g_v^2+g_a^2)(5+2c+c^2)}{(1-\Pi(t))} \\ &+ \xi^2 \left(4(g_v^2+g_a^2)^2 + (1+c)^2(g_v^4+g_a^4+6g_v^2g_a^2) \right) \right\} \\ B_s &= \frac{2(1+c^2)}{|1-\Pi(s)|^2} + 2\chi \frac{(1-c)^2(g_v^2-g_a^2) + (1+c)^2(g_v^2+g_a^2)}{1-\Pi(s)} \\ &+ \chi^2 \left[(1-c)^2(g_v^2-g_a^2)^2 + (1+c)^2(g_v^4+g_a^4+6g_v^2g_a^2) \right] \\ B_i &= 2\frac{s}{t}(1+c)^2 \left\{ \frac{1}{(1-\Pi(t))(1-\Pi(s))} \\ &+ (g_v^2+g_a^2) \left(\frac{\xi}{1-\Pi(s)} + \frac{\chi}{1-\Pi(t)} \right) \\ &+ (g_v^4+6g_v^2g_a^2+g_a^4)\xi\chi \right\} \end{split}$$

$$\Pi(t) = \Delta \alpha(t)$$

$$\chi = \frac{s}{s - m_z^2 + im_Z \Gamma_Z} \cdot \frac{1}{\sin 2\theta_w}$$

$$\xi = \frac{t}{t - m_Z^2} \cdot \frac{1}{\sin 2\theta_w},$$

$$g_a = -\frac{1}{2}, \quad g_v = -\frac{1}{2} + 2\sin^2 \theta_w),$$

$$t = (p_1 - q_1)^2 = -\frac{1}{2}s (1 - c),$$

$$c = \cos \theta, \qquad \theta = \widehat{p_1 q_1}.$$

The running of α

$$\Pi(t) = \Delta \alpha(t)$$

$$\Pi(t) = \frac{\alpha_0}{\pi} \left(\delta_t + \frac{1}{3}L - \frac{5}{9} \right) + \left(\frac{\alpha_0}{\pi} \right)^2 \left(\frac{1}{4}L + \zeta(3) - \frac{5}{24} \right) + \left(\frac{\alpha_0}{\pi} \right)^3 \Pi^{(3)}(t) + \mathcal{O}\left(\frac{m_e^2}{t} \right),$$

$$L = \ln \frac{Q^2}{m_e^2}, \qquad Q^2 = -t, \qquad \zeta(3) = 1.202$$

The radiative factor $1 + \Delta r(t)$ and neglected terms

For the present investigation of the small-angle Bhabha cross section only the correction consistently needed to maintain the required accuracy are kept

All these corrections are included in the new code SAMBHA

All the following contributions have been proved to be negligible and are dropped:

• Any electroweak effect beyond the tree level, for instance appearing in boxes or vertices with Z^O and W bosons, running weak coupling, etc.

- Box diagrams at order α^2 and larger

• Contributions of order α^2 without large logarithms, leading from order α^4 (i.e. $\alpha^4 L^4$) and subleading higher order ($\alpha^3 L^2$, $\alpha^4 L^3$, ...)

• Contributions from pair-produced hadrons, muons, taus and the corresponding virtual pair corrections to the vertices (estimated to be of the order of 0.5×10^{-4})

$\sqrt{s} \; (\text{GeV})$	91.187	91.2	189	206	500	1000	3000
	$45 \text{ mrad} < \theta < 110 \text{ mrad}$						
$\sqrt{\langle -t \rangle}$ (GeV)	3.4	3.4	7.1	7.7	18.8	37.5	112.6
QED	51.428	51.413	11.971	10.077	1.7105	0.42763	0.047514
QED_t	51.484	51.469	11.984	10.088	1.7124	0.42809	0.047566
EW	51.436	51.413	11.965	10.072	1.7105	0.42871	0.049507
$EW+VP_t$	54.041	54.018	12.743	10.745	1.8590	0.47303	0.055748
EW+VP	54.036	54.013	12.742	10.744	1.8588	0.47296	0.055742
	$5 \text{ mrad} < \theta < 50 \text{ mrad}$						
$\sqrt{\langle -t \rangle}$ (GeV)	1.1	1.1	2.2	2.4	5.8	11.6	34.8
QED	4963.4	4962.0	1155.4	972.54	165.08	41.271	4.5857
QED_t	4963.5	4962.1	1155.4	972.57	165.09	41.272	4.5858
EW	4963.4	4962.0	1155.4	972.53	165.08	41.272	4.5885
$EW+VP_t$	5075.0	5073.5	1190.6	1003.3	172.51	43.647	4.9603
EW+VP	5075.0	5073.5	1190.6	1003.3	172.51	43.646	4.9605

Table 1: Various cross sections in nb as a function of the centre-of- mass energy in GeV integrated over the two angular ranges 45-110 mrad and 5-50 mrad. The index t denotes the contraction of the corresponding t channel Feynman diagrams alone. The last columns are of interest for the timear Colliders.

Future Linear Collider

Linear Collider

Let us consider the case of a e+e- collider with E_{c.m.} from 500 to 1000 GeV

The acceptance angles for the Luminosity determination are:

$$1.8^{\circ} < \Theta < 7.2^{\circ}$$

The min and Max values for $t=-Q^2$ can be readily estimated





Monte Carlo codes and comparison

The program LABSMC, which was intended to describe large-angle Bhabha scattering at high energies, has been complemented with a set of routines from NLLBHA so as to be applicable to small-angle Bhabha scattering. This implied the insertion of the relevant second-order next-to-leading radiative corrections ($\mathcal{O}(\alpha^2 L)$) in the Monte Carlo code¹, which are crucial to achieve the per mille accuracy. The extension to cover small angles resulted in the new code SAMBHA containing the previously existing features together with the following new characteristics :

- the complete electroweak matrix element at the Born level;
- the complete set of O(α) QED radiative corrections (including radiation from amplitudes with Z-boson exchange);
- vacuum-polarization corrections by leptons, hadrons [19], and W-bosons;
- 1-loop electroweak radiative corrections and effective EW couplings by means of the DIZET
 v.6.30 [24] package; [24] D.Y. Bardin, M.S. Bilenkii, T. Riemann, M. Sachwitz and H. Vogt: Comput. Phys. Commun. 59 (1990) 303
- higher-order leading-logarithm photonic corrections by means of the electron structure functions [25, 26, 27, 28];
- light pair corrections in the O(α²L²) leading-logarithm approximation including (optionally) the two-photon and singlet mechanisms.

The code is applicable with the following restrictions:

- a) $E_{\text{beam}} \gg m_e$: the energy has to be much larger than the electron mass;
- b) $m_e/E_{\text{beam}} \ll \theta$: extemely small angles are not described well, but the condition is fulfilled in practice for both small- and large-angle Bhabha measurements in the experiments at LEP, SLC and NLC;
- c) starting from the second order in α , real photon emission is integrated over, i.e. events with two photons separated from electrons are not generated.

Comparison of SAMBHA with BHLUMI

BHLUMI is compared with SAMBHA for integral and, for the first time also

differential distributions

The actual measurements are of calorimetric type Therefore, event samples are generated with both programs, subjecting each event to a common set of calorimeter-like criteria (CALO)

 $\rho(t) = \left(\frac{d\sigma_{\text{sambha}}}{dt} - \frac{d\sigma_{\text{bhlumi}}}{dt}\right) / \frac{d\sigma_{\text{bhlumi}}}{dt}$



Calorimetric type measurement



Comparison and evaluation

Table 3: Numbers of events generated with $\tt BHLUMI$

$\sqrt{s}(\text{GeV})$	91.2	189	200
$\int \mathcal{L} dt \ (pb^{-1})$	75	150	200
Ring 2	1844850	863571	1028210
Ring 3	907754	425586	506131
Ring 4	513696	240550	286994
Ring 5	313218	146731	174740
Ring 6	201893	94033	112168



$$\sigma_i = \sigma_i^0 \left(\frac{\alpha(t_i)}{\alpha(0)}\right)^2 (1 + \Delta r_i),$$

$$\sigma_{i} = \int^{R_{i}} dt \frac{d\sigma}{dt}$$

$$\sigma_{i}^{0} = \int^{R_{i}} dt \frac{d\sigma^{0}}{dt}$$

$$\left(\frac{\alpha(t_{i})}{\alpha(0)}\right)^{2} = \int^{R_{i}} \frac{dt}{t_{\max} - t_{\min}} \left(\frac{\alpha(t)}{\alpha(0)}\right)^{2},$$

$$1 + \Delta r_{i} = \left(\frac{\alpha(0)}{\alpha(t_{i})}\right)^{2} \frac{\sigma_{i}}{\sigma_{i}^{0}}$$

$$^{2} = \frac{N_{i}}{\sigma_{i}^{0} \int \mathcal{L} \mathrm{d}t} \frac{1}{1 + \Delta r_{i}}, \qquad \left(\frac{\alpha}{\alpha}\right)$$

$$\left(\frac{\alpha(t)}{\alpha(0)}\right)^2 = (u_0 \pm \delta u_0) + (u_1 \pm \delta u_1) \cdot \log \frac{-t}{\langle -t \rangle}$$

Table 4: Theoretical predictions for each ring of the three factors of eq. 7. For the conditions defined in sect. 5.1 the angular boundary of ring i is $\theta_i = \arctan(7+3(i-1))/220)$.

No. of ring	1	2	3	4	5	6	7
	$\sqrt{s} = 91.2 \text{ GeV}$						
σ_i^0	63.077	24.728	12.170	6.8694	4.2517	2.8120	1.9552
$\left(\left(\left(\right) \right) \right)^{2}$	1.0.405	1.0475	1.0510	1.0551	1.0500	1.0000	1.0004
$\left(\frac{\alpha(t_i)/\alpha(0)}{\alpha(0)} \right)$	1.0425	1.0475	1.0516	1.0551	1.0582	1.0609	1.0634
$1 + \Delta r_i$	0.9426	0.9440	0.9412	0.9395	0.9240	0.8915	0.7982
	$\sqrt{s} = 189 \text{ GeV}$						
σ_i^0	14.685	5.7563	2.8324	1.5984	0.9889	0.6537	0.4542
$\left(\alpha(t_i) / \alpha(0) \right)^2$	1.0554	1.0613	1.0661	1.0702	1.0736	1.0767	1.0794
$1 + \Delta r_i$	0.9377	0.9390	0.9360	0.9329	0.9165	0.8858	0.7898
	$\sqrt{s} = 200 \text{ GeV}$						
σ_i^0	13.115	5.1406	2.5295	1.4274	0.8831	0.5838	0.4057
$\left(\alpha(t_i) / \alpha(0) \right)^2$	1.0565	1.0625	1.0673	1.0714	1.0749	1.0780	1.0807
$1 + \Delta r_i$	0.9376	0.9387	0.9352	0.9330	0.9158	0.8847	0.7896
	$\sqrt{s} = 1000 \text{ GeV}$						
σ_i^0	0.5248	0.2059	0.1014	0.0573	0.0356	0.0236	0.0165
$\left(\alpha(t_i) / \alpha(0) \right)^2$	1.0921	1.0994	1.1050	1.1096	1.1135	1.1169	1.1199
$1 + \Delta r_i$	0.8622	0.8620	0.8590	0.8545	0.8398	0.8084	0.7205
	$\sqrt{s} = 3000 \text{ GeV}$						
σ_i^0	0.0590	0.0234	0.0117	0.0067	0.0042	0.0028	0.0020
$\left(\alpha(t_i) / \alpha(0) \right)^2$	1.1192	1.1267	1.1325	1.1373	1.1414	1.1448	1.1479
$1 + \Delta r_i$	0.8467	0.8457	0.8422	0.8381	0.8253	0.7956	0.6975

Final formula:

$$\left(\frac{\alpha(t_i)}{\alpha(0)}\right)^2 = \frac{N_i}{\sigma_i^0 \int \mathcal{L} dt} \frac{1}{1 + \Delta r_i},$$

Which can be transformed in a linear fit defining the t dependence of α :

$$\left(\frac{\alpha(t)}{\alpha(0)}\right)^2 = \left(u_0 \pm \delta u_0\right) + \left(u_1 \pm \delta u_1\right) \cdot \log \frac{-t}{\langle -t \rangle}$$

Table 5: Table of fit results; the uncertainties δu_0 and δu_1 are uncorrelated.

\sqrt{s}	$91.2 {\rm GeV}$	$189 {\rm GeV}$	$200 {\rm GeV}$
u_0	$1.0573 {\pm} 0.0005$	$1.0698 {\pm} 0.0008$	$1.0703{\pm}0.0007$
u_1	0.0242 ± 0.0028	$0.0284{\pm}0.0041$	$0.0318{\pm}0.0038$
$\langle -t \rangle$	$8.5 \ { m GeV^2}$	$36.6 \ { m GeV^2}$	$40.9 \ \mathrm{GeV^2}$

$$\int \mathcal{L} dt = \frac{n_0}{1 + 2\Delta\alpha(\langle t \rangle)} \qquad \qquad \frac{\delta n_0}{n_0} = 10^{-3} \qquad \text{statistical precision}$$

The Data

LEP

EUROPEAN ORGANISATION FOR NUCLEAR RESEARCH

CERN-PH-EP/2005-014 21 February 2005 Revised 28 June 2005

Measurement of the running of the QED coupling in small-angle Bhabha scattering at LEP

OPAL Collaboration

Abstract

Using the OPAL detector at LEP, the running of the effective QED coupling $\alpha(t)$ is measured for space-like momentum transfer from the angular distribution of small-angle Bhabha scattering. In an almost ideal QED framework, with very favourable experimental conditions, we obtain:

 $\Delta\alpha(-6.07\,{\rm GeV}^2) - \Delta\alpha(-1.81\,{\rm GeV}^2) = (440 \pm 58 \pm 43 \pm 30) \times 10^{-5}\,,$

where the first error is statistical, the second is the experimental systematic and the third is the theoretical uncertainty. This agrees with current evaluations of $\alpha(t)$. The null hypothesis that α remains constant within the above interval of -t is excluded with a significance above 5σ . Similarly, our results are inconsistent at the level of 3σ with the hypothesis that only leptonic loops contribute to the running. This is currently the most significant direct measurement where the running $\alpha(t)$ is probed differentially within the measured t range.

Small-angle Bhabha scattering

an almost pure QED process. Differential cross section can be written as:



experimentally: high data statistics, very high purity

This process and method advocated by Arbuzov et al., Eur.Phys.J.C 34(2004)267

G.Abbiendi

Small-angle Bhabha scattering in OPAL



2 cylindrical calorimeters encircling the beam pipe at \pm 2.5 m from the Interaction Point

19 Silicon layersTotal Depth 22 X_0 18 Tungsten layers(14 cm)

18 Tungsten layers

Each detector layer divided into 16 overlapping wedges

Sensitive radius: 6.2 – 14.2 cm, corresponding to scattering angle of 25 – 58 mrad from the beam line



4 March 2005

G.Abbiendi

Results

OPAL



19



EUROPEAN ORGANIZATION FOR NUCLEAR RESEARCH

CERN-EP/2000-005 January 06, 2000

Measurement of the Running of the Fine-Structure Constant

The L3 Collaboration

Abstract

Small-angle Bhabha scattering data recorded at the Z resonance and large-angle Bhabha scattering data recorded at $\sqrt{s} = 189$ GeV by the L3 detector at LEP are used to measure the running of the effective fine-structure constant for spacelike momentum transfers. The results are

$$\alpha^{-1}(-2.1 \text{ GeV}^2) - \alpha^{-1}(-6.25 \text{ GeV}^2) = 0.78 \pm 0.26$$

 $\alpha^{-1}(-12.25 \text{ GeV}^2) - \alpha^{-1}(-3434 \text{ GeV}^2) = 3.80 \pm 1.29$

in agreement with theoretical predictions.



Figure 3: Measurements of $\alpha^{-1}(Q^2)$ for $Q^2 < 0$. The results of the small-angle and large-angle Bhabha scattering measurements described in this article are shown as a solid circle and square, respectively. The corresponding reference Q^2 values at which the value of $\alpha^{-1}(Q^2)$ is fixed to its expectation are shown as open symbols. The error bar on the large-angle point indicates the experimental and the total uncertainty.

EUROPEAN ORGANIZATION FOR NUCLEAR RESEARCH

CERN-PH-EP/2005-021 May 12, 2005

Measurement of the Running of the Electromagnetic Coupling at Large Momentum-Transfer at LEP

The L3 Collaboration

Abstract

The evolution of the electromagnetic coupling, α , in the momentum-transfer range 1800 GeV² < $-Q^2$ < 21600 GeV² is studied with about 40000 Bhabha-scattering events collected with the L3 detector at LEP at centre-of-mass energies $\sqrt{s} = 189 - 209$ GeV. The running of α is parametrised as:

$$\alpha(Q^2) = \frac{\alpha_0}{1 - C\Delta\alpha(Q^2)}$$

where $\alpha_0 \equiv \alpha(Q^2 = 0)$ is the fine-structure constant and C = 1 corresponds to the evolution expected in QED. A fit to the differential cross section of the $e^+e^- \rightarrow e^+e^-$ process for scattering angles in the range $|\cos \theta| < 0.9$ excludes the hypothesis of a constant value of α , C = 0, and validates the QED prediction with the result:

$$C = 1.05 \pm 0.07 \pm 0.14$$
,

where the first uncertainty is statistical and the second systematic.





Conclusions

We propose a novel approach to access directly and to measure the running of α_{QED} in the space-like region .

- It consists in analysing small-angle Bhabha scattering. Depending on the particular angular detector coverage and on the energy of the beams, it allows a sizeable range of the t variable to be covered.
- The feasibility of the method has been put in evidence by the use of a new tool, **SAMBHA**, to calculate the small-angle Bhabha differential cross section with a theoretical accuracy of better than 0.1%.
- The information obtained in the t channel can be compared with the existing results of the s channel measurements. This represents a complementary approach, which is direct, transparent and based only on QED interactions and furthermore free of some of the drawbacks inherent in the s channel methods.
- The method outlined can be readily applied to the experiments at LEP and SLC. It can also be exploited by future e+e- colliders as well as by existing low energy machines.
- An extremely precise measurement of the QED running coupling Δα(t) for small values of t may be envisaged with a dedicated luminometer even at low machine energies.