

---

# CPT symmetry and quantum coherence tests in the neutral kaon system at KLOE



Antonio Di Domenico  
Dipartimento di Fisica, Università di Roma “La Sapienza”  
and INFN sezione di Roma, Italy



**Seminar at Physics Department, Warsaw University and  
A. Soltan Institute for Nuclear Studies,  
April 3<sup>rd</sup>, 2009, Warsaw, Poland**

---

# CPT: introduction

The three discrete symmetries of QM, C (charge conjugation), P (parity), and T (time reversal) are known to be violated in nature both singly and in pairs. Only CPT appears to be an exact symmetry of nature.

CPT theorem (Luders, Jost, Pauli, Bell 1955 -1957):

Exact CPT invariance holds for any quantum field theory (flat space-time) which assumes:

(1) Lorentz invariance (2) Locality (3) Unitarity (i.e. conservation of probability).

Testing the validity of the CPT symmetry probes the most fundamental assumptions of our present understanding of particles and their interactions.

Extension of CPT theorem to a theory of quantum gravity far from obvious (e.g. CPT violation appears in some models with space-time foam backgrounds).

No predictive theory incorporating CPT violation => only phenomenological models to be constrained by experiments.

The neutral kaon system offers unique possibilities to test CPT invariance e.g. :

$$\left| m_{K^0} - m_{\bar{K}^0} \right| / m_K < 10^{-18}, \quad \left| m_{B^0} - m_{\bar{B}^0} \right| / m_B < 10^{-14}, \quad \left| m_p - m_{\bar{p}} \right| / m_p < 10^{-8}$$

---

---

# 1) “Standard” tests of CPT symmetry in the neutral kaon system

# The neutral kaon system

The time evolution of a two-component state vector  $\Psi$  in the  $\{K^0, \bar{K}^0\}$  space is given by (Wigner-Weisskopf approximation):

$$i \frac{\partial}{\partial t} \Psi(t) = \mathbf{H} \Psi(t)$$

$\mathbf{H}$  is the effective hamiltonian (non-hermitian), decomposed into a Hermitian Part (mass matrix  $\mathbf{M}$ ) and an anti-Hermitian part ( $i/2$  decay matrix  $\mathbf{\Gamma}$ ):

$$\mathbf{H} = \mathbf{M} - \frac{i}{2} \mathbf{\Gamma} = \begin{pmatrix} m_{11} & m_{12} \\ m_{21} & m_{22} \end{pmatrix} - \frac{i}{2} \begin{pmatrix} \Gamma_{11} & \Gamma_{12} \\ \Gamma_{21} & \Gamma_{22} \end{pmatrix}$$

Diagonalizing the effective Hamiltonian:

eigenvalues

$$\lambda_{S,L} = m_{S,L} - \frac{i}{2} \Gamma_{S,L}$$

$$|K_{S,L}(t)\rangle = e^{-i\lambda_{S,L}t} |K_{S,L}(0)\rangle$$

$$\tau_S \sim 90 \text{ ps} \quad \tau_L \sim 51 \text{ ns}$$

$$m_L - m_S = 3.5 \times 10^{-15} \text{ GeV} \sim \Gamma_S / 2$$

eigenstates

$$|K_{S,L}\rangle = \frac{1}{\sqrt{2(1+|\varepsilon_{S,L}|)}} \left[ (1 + \varepsilon_{S,L}) |K^0\rangle \pm (1 - \varepsilon_{S,L}) |\bar{K}^0\rangle \right]$$

$$= \frac{1}{\sqrt{(1+|\varepsilon_{S,L}|)}} \left[ |K_{1,2}\rangle + \varepsilon_{S,L} |K_{2,1}\rangle \right]$$

$|K_{1,2}\rangle$  are  
CP =  $\pm 1$  states

small CP impurity  $\sim 2 \times 10^{-3}$

# CPT violation in the neutral kaon system: “standard” picture

CPT violation in the mixing:

$$\varepsilon_{S,L} = \varepsilon \pm \delta$$

$$\varepsilon = \frac{H_{12} - H_{21}}{2(\lambda_S - \lambda_L)} = \frac{-i\Im m_{12} - \Im \Gamma_{12}/2}{\Delta m + i\Delta\Gamma/2}$$

$$\delta = \frac{H_{11} - H_{22}}{2(\lambda_S - \lambda_L)} = \frac{1}{2} \frac{(m_{22} - m_{11}) - (i/2)(\Gamma_{22} - \Gamma_{11})}{\Delta m + i\Delta\Gamma/2}$$

- $\delta \neq 0$  implies CPT violation
- $\varepsilon \neq 0$  implies T violation
- $\varepsilon \neq 0$  or  $\delta \neq 0$  implies CP violation

$$m_{11} \equiv m_{K^0} \quad , \quad m_{22} \equiv m_{\bar{K}^0}$$

$$\Gamma_{11} \equiv \Gamma_{K^0} \quad , \quad \Gamma_{22} \equiv \Gamma_{\bar{K}^0}$$

$$\Delta m = m_L - m_S \quad , \quad \Delta\Gamma = \Gamma_S - \Gamma_L$$

(with a phase convention  $\Im \Gamma_{12} = 0$  )

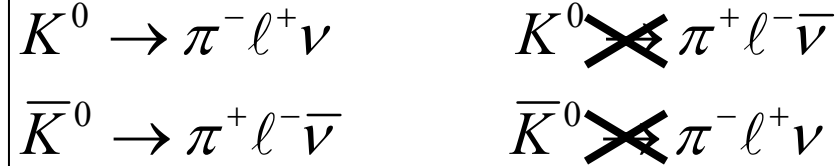
# CPT violation in the neutral kaon system: “standard” picture

## CPT violation in semileptonic decays

$$\langle \pi^- \ell^+ \nu | T | K^0 \rangle = a + b \quad \langle \pi^+ \ell^- \bar{\nu} | T | K^0 \rangle = c + d$$

$$\langle \pi^+ \ell^- \bar{\nu} | T | \bar{K}^0 \rangle = a^* - b^* \quad \langle \pi^- \ell^+ \nu | T | \bar{K}^0 \rangle = c^* - d^*$$

$\Delta S = \Delta Q$  rule



	CP	T	CPT	$\Delta S = \Delta Q$
$a$	$\Im = 0$	$\Im = 0$		
$b$	$\Re = 0$	$\Im = 0$	$= 0$	
$c$	$\Im = 0$	$\Im = 0$		$= 0$
$d$	$\Re = 0$	$\Im = 0$	$= 0$	$= 0$

Standard Model prediction of  $\Delta S = \Delta Q$  rule violation is  $x = c/a \sim O(10^{-7})$

Semileptonic charge asymmetry:

$$A_{S,L} = \frac{\Gamma(K_{S,L} \rightarrow \pi^- e^+ \nu) - \Gamma(K_{S,L} \rightarrow \pi^+ e^- \bar{\nu})}{\Gamma(K_{S,L} \rightarrow \pi^- e^+ \nu) + \Gamma(K_{S,L} \rightarrow \pi^+ e^- \bar{\nu})} = 2\Re \varepsilon \pm 2\Re \delta - 2\Re y \pm 2\Re x_{\pm}$$

$$A_S - A_L = 4(\Re \delta + \Re x_{-})$$

# CPT violation in the neutral kaon system: “standard” picture

## CPT violation in semileptonic decays

$$\begin{aligned} \langle \pi^- \ell^+ \nu | T | K^0 \rangle &= a + b & \langle \pi^+ \ell^- \bar{\nu} | T | K^0 \rangle &= c + d \\ \langle \pi^+ \ell^- \bar{\nu} | T | \bar{K}^0 \rangle &= a^* - b^* & \langle \pi^- \ell^+ \nu | T | \bar{K}^0 \rangle &= c^* - d^* \end{aligned}$$

$\Delta S = \Delta Q$  rule



CPT viol.	CPT & $\Delta S = \Delta Q$ viol.	$\Delta S = \Delta Q$ Viol.
$y = -\frac{b}{a}$	$x_- = -\frac{d^*}{a}$	$x_+ = \frac{c^*}{a}$

Standard Model prediction of  $\Delta S = \Delta Q$  rule violation is  $x = c/a \sim O(10^{-7})$

Semileptonic charge asymmetry:

$$A_{S,L} = \frac{\Gamma(K_{S,L} \rightarrow \pi^- e^+ \nu) - \Gamma(K_{S,L} \rightarrow \pi^+ e^- \bar{\nu})}{\Gamma(K_{S,L} \rightarrow \pi^- e^+ \nu) + \Gamma(K_{S,L} \rightarrow \pi^+ e^- \bar{\nu})} = 2\Re \varepsilon \pm 2\Re \delta - 2\Re y \pm 2\Re x_{\pm}$$

$$A_S - A_L = 4(\Re \delta + \Re x_-)$$

# CPT violation in the neutral kaon system: “standard” picture

## CPT violation in $\pi\pi$ decays

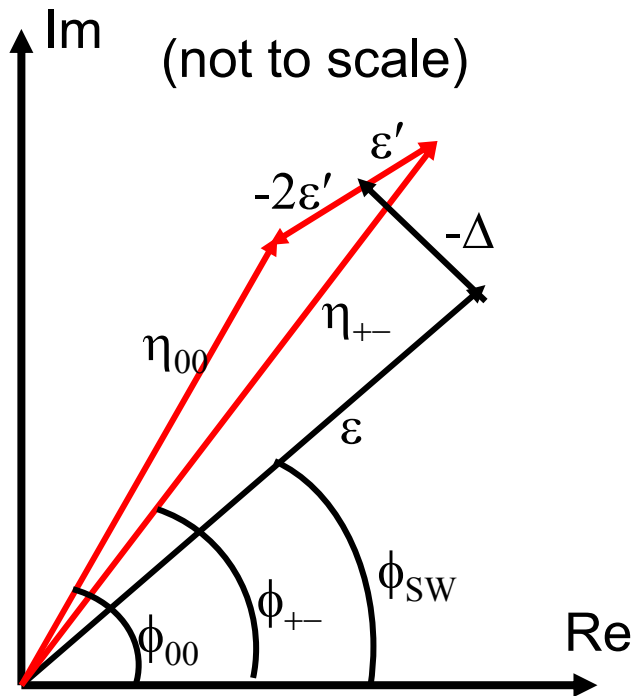
$$\langle \pi\pi; I | T | K^0 \rangle = (A_I + B_I) e^{i\delta_I}$$

$$\langle \pi\pi; I | T | \bar{K}^0 \rangle = (A_I^* - B_I^*) e^{i\delta_I}$$

$A_I(B_I)$  CPT conserving (violating)

$K \rightarrow \pi\pi$  amplitudes for  $I=0,2$

( $\delta_I$  strong phase shift for  $I=0,2$ )



$$\eta_{+-} = |\eta_{+-}| e^{i\phi_{+-}} = \frac{\langle \pi^+ \pi^- | T | K_L \rangle}{\langle \pi^+ \pi^- | T | K_S \rangle} = \varepsilon - \Delta + \varepsilon'$$

$$\eta_{00} = |\eta_{00}| e^{i\phi_{00}} = \frac{\langle \pi^0 \pi^0 | T | K_L \rangle}{\langle \pi^0 \pi^0 | T | K_S \rangle} = \varepsilon - \Delta - 2\varepsilon'$$

$$\Delta = \delta - \frac{\Re B_0}{\Re A_0} \quad \phi_{SW} = \arctan(2\Delta m / \Delta\Gamma)$$

$$\phi_{00} - \phi_{+-} \approx \frac{3}{\sqrt{2}} \frac{1}{|\eta_{+-}|} \frac{\Re A_2}{\Re A_0} \left( \frac{\Re B_2}{\Re A_2} - \frac{\Re B_0}{\Re A_0} \right) \approx -3 \Im \left( \frac{\varepsilon'}{\varepsilon} \right)$$

$$\phi_{+-} - \phi_{SW} \approx \frac{-1}{\sqrt{2} |\eta_{+-}|} \left[ \frac{m_{11} - m_{22}}{2\Delta m} + \frac{\Re B_0}{\Re A_0} \right]$$



# Neutral kaons at CPLEAR (CERN)

Pure initial  $K^0, \bar{K}^0$  are produced from antiproton annihilation at rest with a hydrogen target

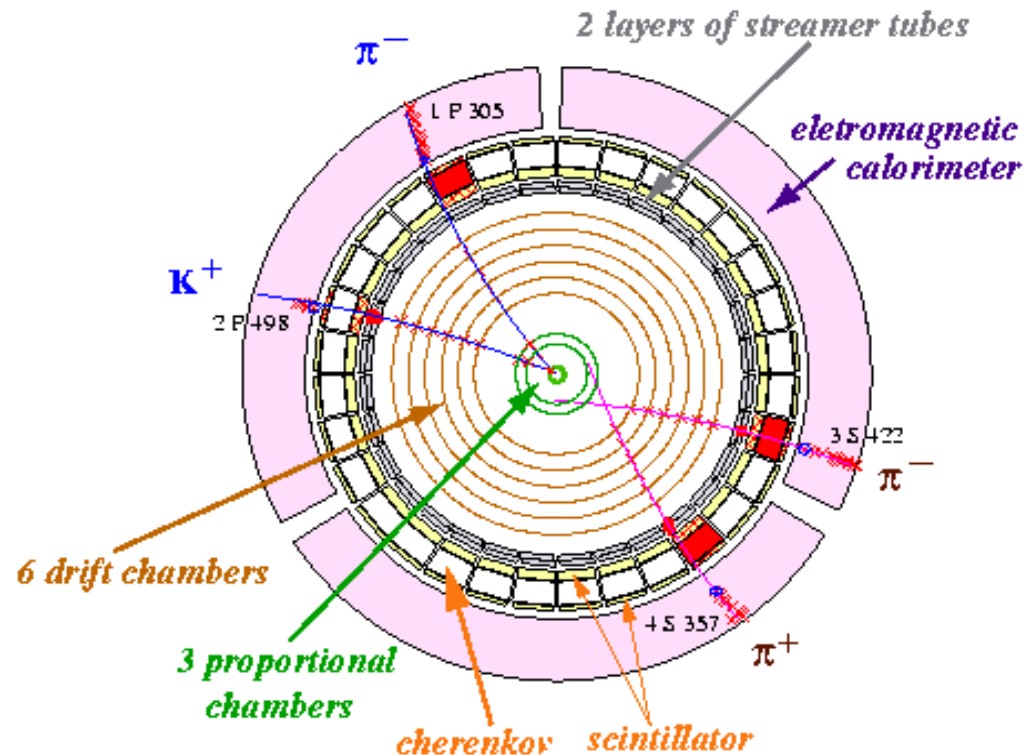
$$(p + \bar{p})_{REST} \rightarrow K^0 + K^- + \pi^+$$

$$(p + \bar{p})_{REST} \rightarrow \bar{K}^0 + K^+ + \pi^-$$

$$(p + \bar{p})_{REST} \rightarrow K^0 + \bar{K}^0$$

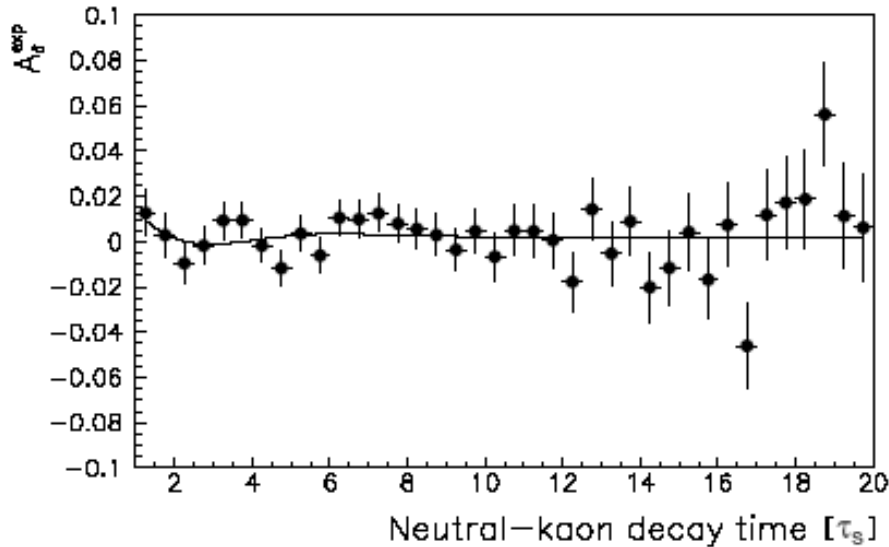
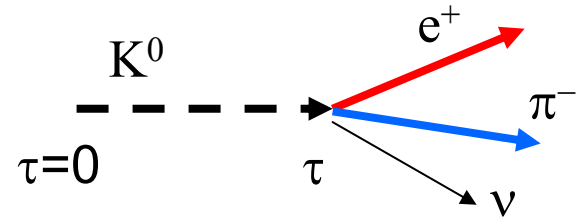
$P_K \sim 500$  MeV

The detection of a charged kaon tags the strangeness of the accompanying neutral kaon



# CPLEAR results

Test of **CPT** in the time evolution of neutral kaons using the semileptonic asymmetry



$$A_{\delta}(\tau) = \frac{\overline{R}_{+}(\tau) - \alpha R_{-}(\tau)}{\overline{R}_{+}(\tau) + \alpha R_{-}(\tau)} + \frac{\overline{R}_{-}(\tau) - \alpha R_{+}(\tau)}{\overline{R}_{-}(\tau) + \alpha R_{+}(\tau)}$$

$$R_{+(-)}(\tau) = R \left( K^0_{t=0} \rightarrow (e^{+(-)} \pi^{-(+)} \nu)_{t=\tau} \right)$$

$$\overline{R}_{-(+)}(\tau) = R \left( \overline{K}^0_{t=0} \rightarrow (e^{-(+)} \pi^{+(-)} \nu)_{t=\tau} \right)$$

$$\alpha = 1 + 4\Re \varepsilon_L$$

$$A_{\delta}(\tau \gg \tau_S) = 8\Re \delta$$

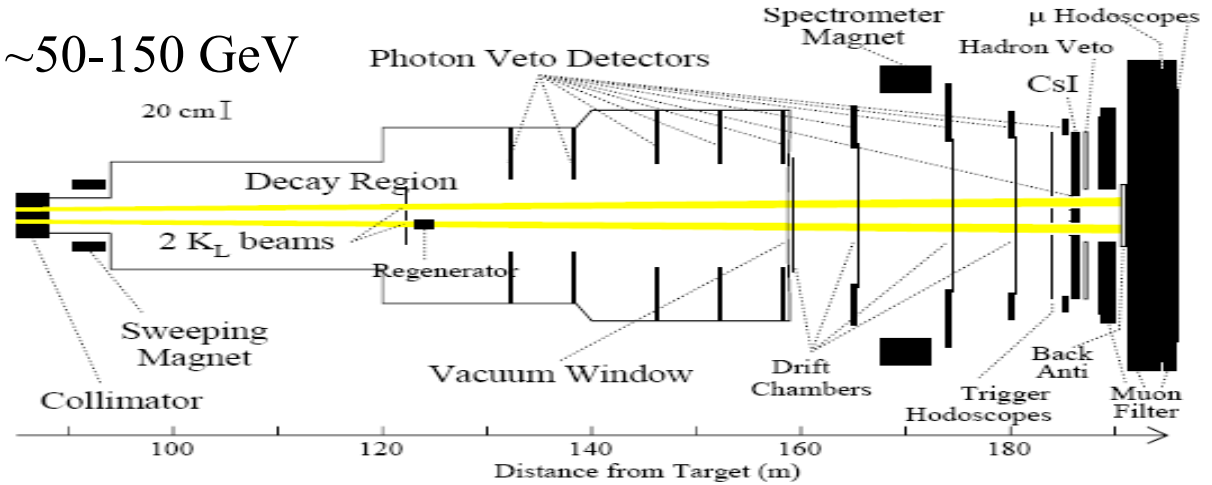
$$\Re \delta = (0.30 \pm 0.33 \pm 0.06) \times 10^{-3}$$

PLB444 (1998) 52

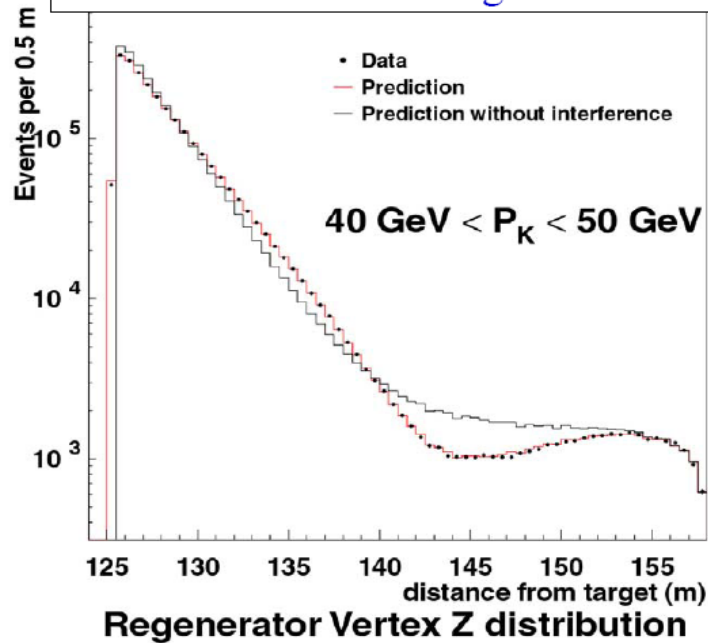
# KTeV (Fermilab) results

Regenerator beam  
decay distribution allows  
CPT tests based on  $\phi_{+-}$ ,  $\phi_{00}-\phi_{+-}$

$P_K \sim 50-150$  GeV



## $K_L - K_S$ Interference Downstream of Regenerator



$$|K_L\rangle \rightarrow |K_L\rangle + \rho |K_S\rangle$$

$$R(\pi^+\pi^-;t) \propto |\rho|^2 e^{-\Gamma_S t} + |\eta_{+-}|^2 e^{-\Gamma_L t} + 2|\rho||\eta_{+-}| e^{-(\Gamma_S+\Gamma_L)t} \cos(\Delta mt + \phi_\rho - \phi_{+-})$$

$$\phi_{+-} - \phi_{SW} = 0.61^\circ \pm 0.62^\circ \pm 1.01^\circ$$

$$\phi_{00}-\phi_{+-} = 0.39^\circ \pm 0.22^\circ \pm 0.45^\circ$$

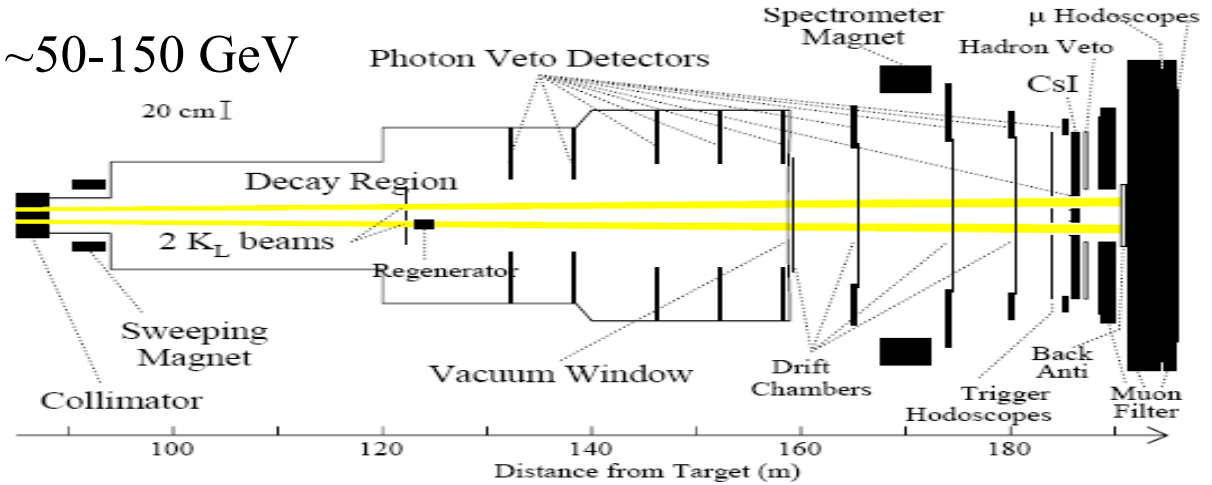
PRD67,012005 (2003)

# KTeV (Fermilab) results

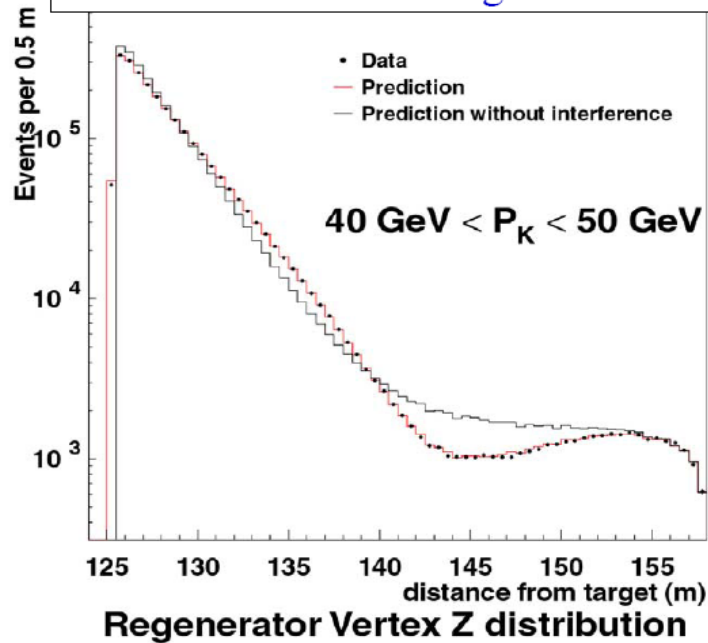
Regenerator beam  
decay distribution allows

CPT tests based on  $\phi_{+-}$ ,  $\phi_{00}-\phi_{+-}$

$P_K \sim 50-150$  GeV



$K_L - K_S$  Interference  
Downstream of Regenerator



$$|K_L\rangle \rightarrow |K_L\rangle + \rho |K_S\rangle$$

$$R(\pi^+\pi^-;t) \propto |\rho|^2 e^{-\Gamma_S t} + |\eta_{+-}|^2 e^{-\Gamma_L t} + 2|\rho||\eta_{+-}| e^{-(\Gamma_S+\Gamma_L)t} \cos(\Delta m t + \phi_\rho - \phi_{+-})$$

$$\begin{aligned} \phi_\varepsilon - \phi_{SW} &= 0.40^\circ \pm 0.56^\circ \\ \phi_{00}-\phi_{+-} &= 0.30^\circ \pm 0.35^\circ \end{aligned}$$

Presented at  
Moriond08, HQL08

# KTeV (Fermilab) results

$K_L$  semileptonic charge asymmetry:

$$A_L = (3322 \pm 58 \pm 47) \times 10^{-6}$$

PRL88,181601(2002)

Constraints on CPT violation in  $\pi\pi$  and semileptonic decays obtained combining KTeV and PDG results:

$$\Re\left(\frac{2}{3}\eta_{+-} + \frac{1}{3}\eta_{00}\right) - \frac{A_L}{2} = \Re\left(y + x_- + \frac{\Re B_0}{\Re A_0}\right) = (-3 \pm 35) \times 10^{-6}$$

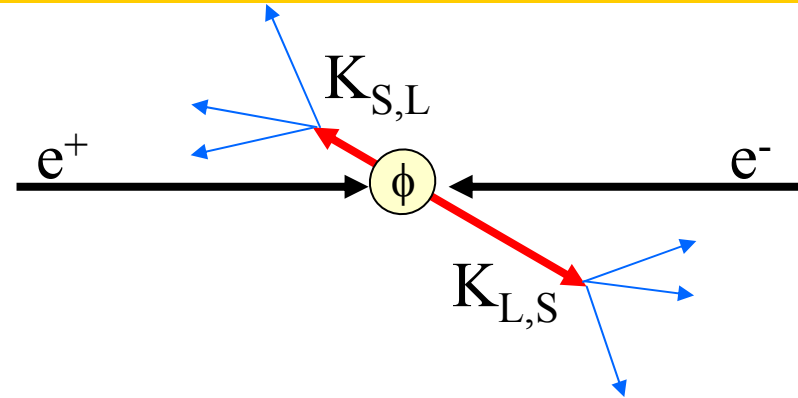
# Neutral kaons at a $\phi$ -factory

Production of the vector meson  $\phi$  in  $e^+e^-$  annihilations:

- $e^+e^- \rightarrow \phi$      $\sigma_\phi \sim 3 \mu\text{b}$   
 $W = m_\phi = 1019.4 \text{ MeV}$
- $\text{BR}(\phi \rightarrow K^0\bar{K}^0) \sim 34\%$
- $\sim 10^6$  neutral kaon pairs per  $\text{pb}^{-1}$  produced in an antisymmetric quantum state with  $J^{PC} = 1^{--}$  :

$$\mathbf{p}_K = 110 \text{ MeV}/c$$

$$\lambda_S = 6 \text{ mm} \quad \lambda_L = 3.5 \text{ m}$$



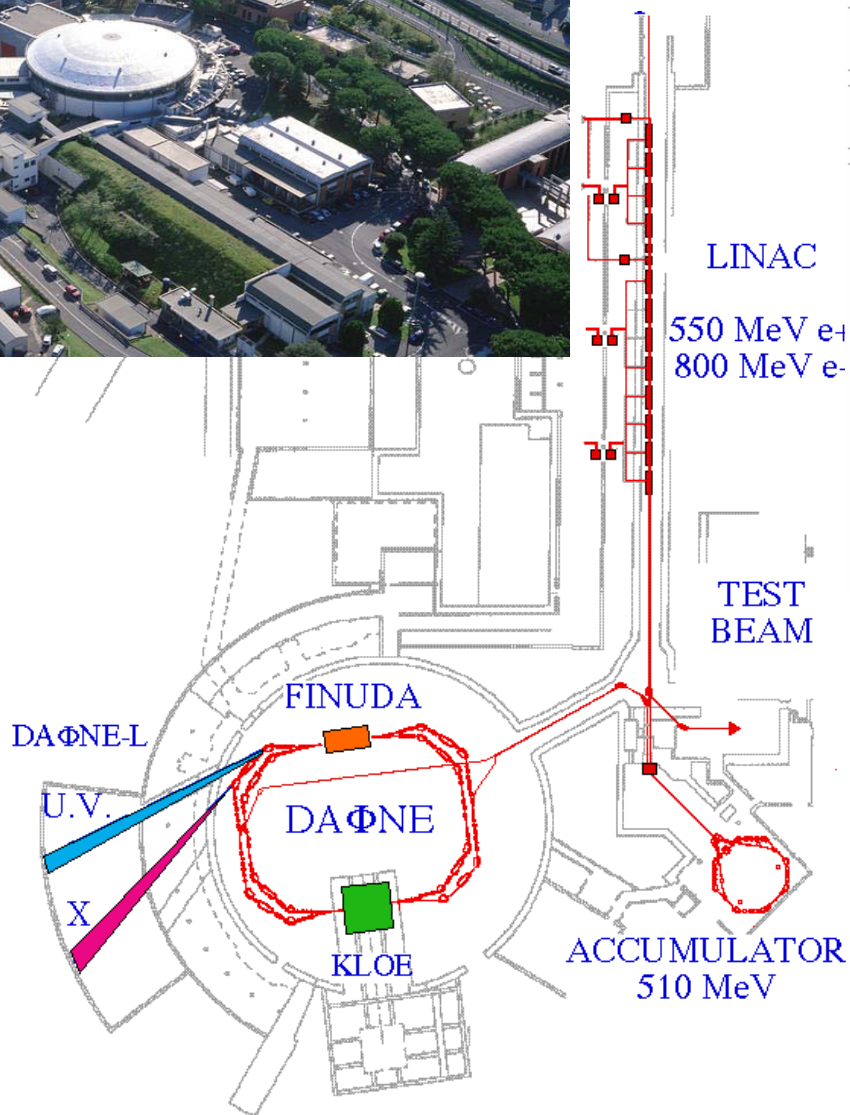
$$|i\rangle = \frac{1}{\sqrt{2}} \left[ |K^0(\vec{p})\rangle |\bar{K}^0(-\vec{p})\rangle - |\bar{K}^0(\vec{p})\rangle |K^0(-\vec{p})\rangle \right]$$

$$= \frac{N}{\sqrt{2}} \left[ |K_S(\vec{p})\rangle |K_L(-\vec{p})\rangle - |K_L(\vec{p})\rangle |K_S(-\vec{p})\rangle \right]$$

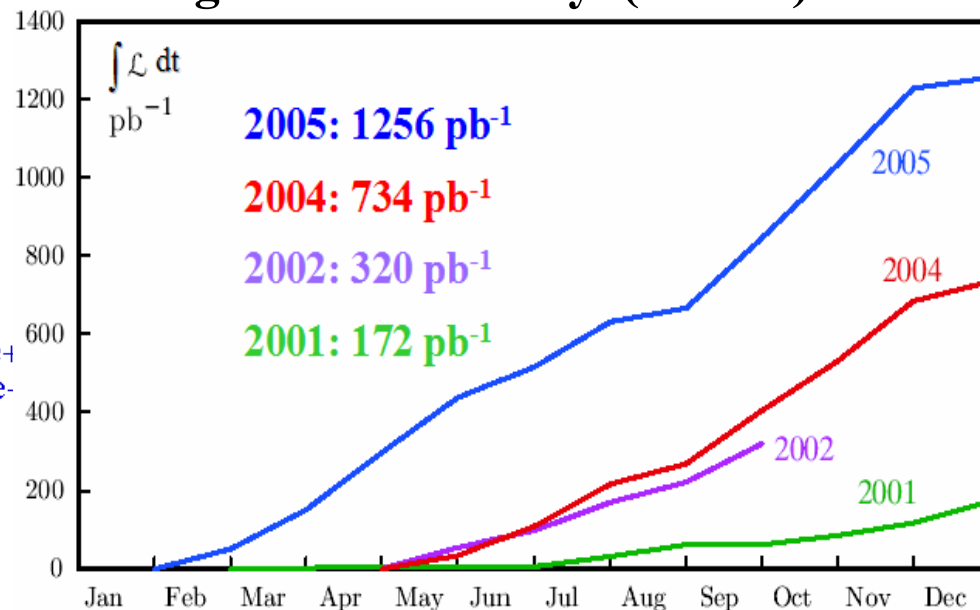
$$N = \sqrt{(1+|\varepsilon_S|^2)(1+|\varepsilon_L|^2)} / (1-\varepsilon_S\varepsilon_L) \cong 1$$

The detection of a kaon at large (small) times tags a  $K_S$  ( $K_L$ )  
 $\Rightarrow$  possibility to select a pure  $K_S$  beam (**unique** at a  $\phi$ -factory, not possible at fixed target experiments)

# DAΦNE: the Frascati $\phi$ -factory



## Integrated luminosity (KLOE)



Max  $\mathcal{L} \sim 1.4 \text{ cm}^{-2}\text{s}^{-1}$

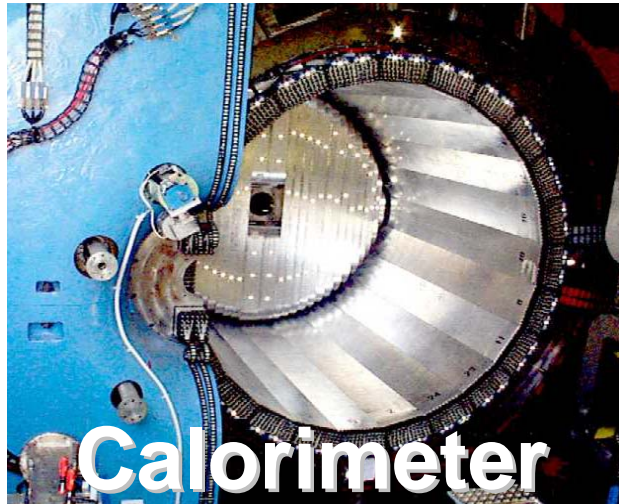
Day performance: 7-8 pb<sup>-1</sup>

Best month  $\int \mathcal{L} dt \sim 200 \text{ pb}^{-1}$

Total KLOE  $\int \mathcal{L} dt \sim 2.5 \text{ fb}^{-1}$   
(2001 - 05)

→  $\sim 2.5 \times 10^9$   $K_S K_L$  pairs

# The KLOE detector at DAΦNE



Lead/scintillating fiber  
4880 PMTs  
98% coverage of solid angle

$$\sigma_E/E \cong 5.7\% / \sqrt{E(\text{GeV})}$$

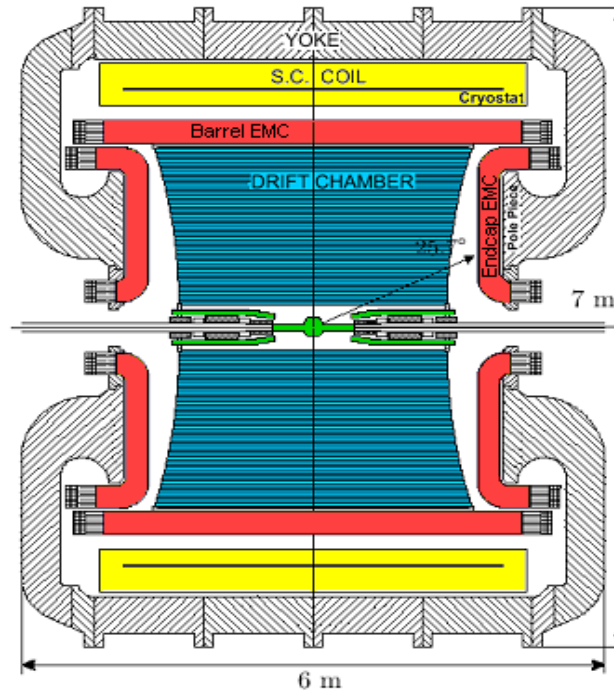
$$\sigma_t \cong 54 \text{ ps} / \sqrt{E(\text{GeV})} \oplus 50 \text{ ps}$$

(relative time between clusters)

$$\sigma_{\gamma\gamma} \sim 2 \text{ cm} (\pi^0 \text{ from } K_L \rightarrow \pi^+\pi^-\pi^0)$$

Superconducting coil

$$B = 0.52 \text{ T}$$



4 m diameter  $\times$  3.3 m length  
90% helium, 10% isobutane  
12582/52140 sense/total wires  
All-stereo geometry

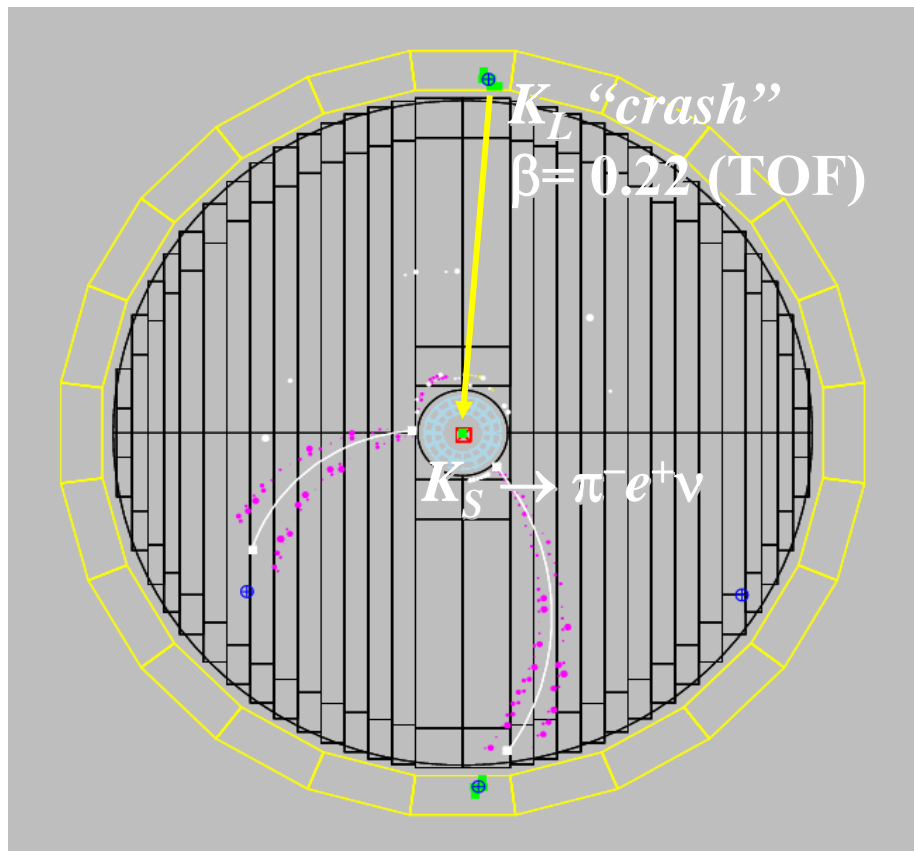
$$\sigma_p/p \cong 0.4\% \text{ (tracks with } \theta > 45^\circ)$$

$$\sigma_x^{\text{hit}} \cong 150 \mu\text{m (xy), 2 mm (z)}$$

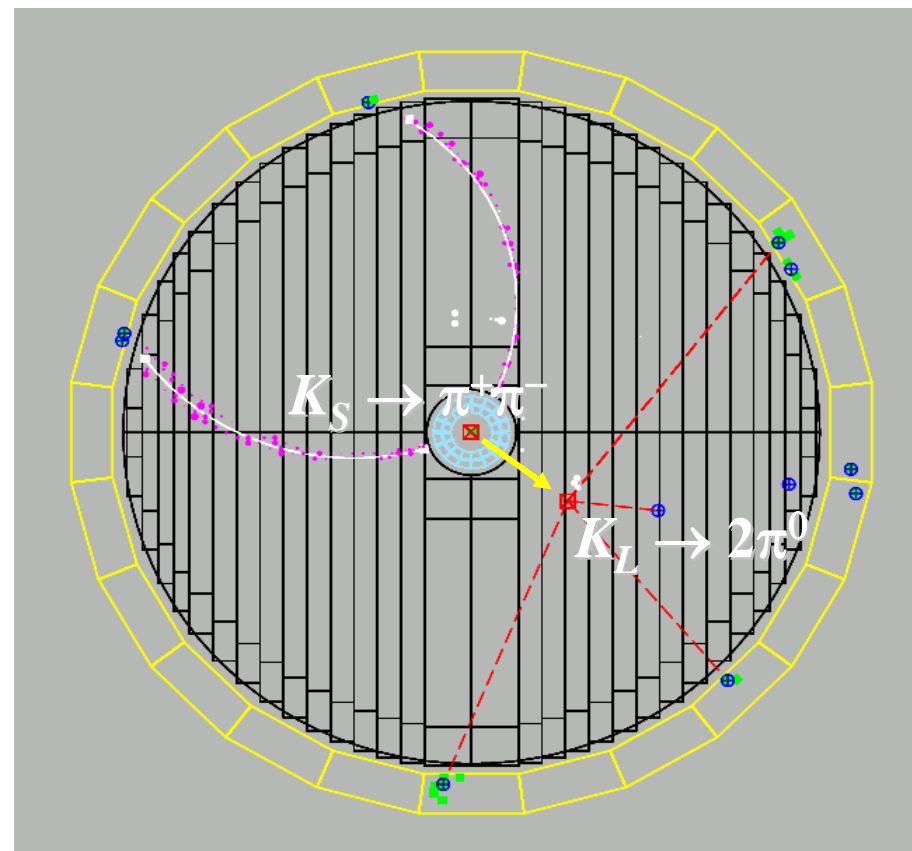
$$\sigma_x^{\text{vertex}} \sim 1 \text{ mm}$$



# $K_S$ and $K_L$ Tagging at KLOE



$K_S$  tagged by  $K_L$  interaction in EmC  
Efficiency  $\sim 30\%$  (largely geometrical)  
 $K_S$  angular resolution:  $\sim 1^\circ$  ( $0.3^\circ$  in  $\phi$ )  
 $K_S$  momentum resolution:  $\sim 2$  MeV

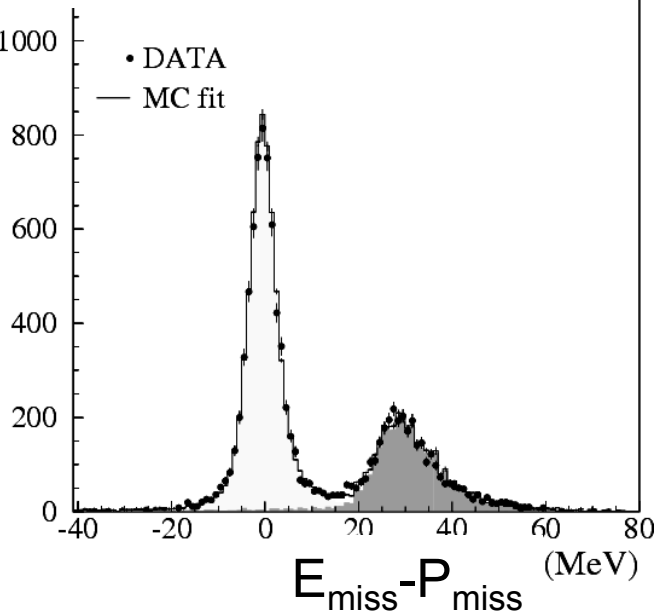


$K_L$  tagged by  $K_S \rightarrow \pi^+ \pi^-$  vertex at IP  
Efficiency  $\sim 70\%$  (mainly geometrical)  
 $K_L$  angular resolution:  $\sim 1^\circ$   
 $K_L$  momentum resolution:  $\sim 2$  MeV

# $K_S \rightarrow \pi e \nu$ : KLOE results

PLB 636(2006) 173

Data sample: 410 pb<sup>-1</sup>



$$\text{BR}(K_S \rightarrow \pi^- e^+ \nu) = (3.528 \pm 0.057 \pm 0.027) \times 10^{-4}$$

$$\text{BR}(K_S \rightarrow \pi^+ e^- \bar{\nu}) = (3.517 \pm 0.051 \pm 0.029) \times 10^{-4}$$

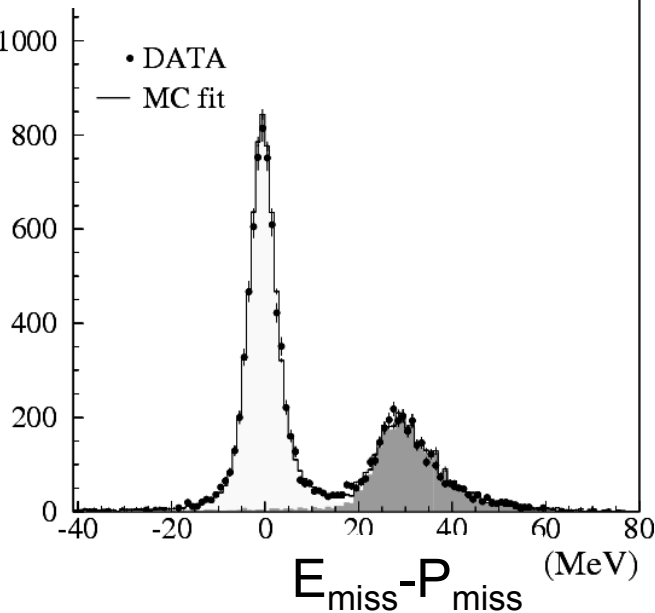
$$\text{BR}(K_S \rightarrow \pi e \nu) = (7.046 \pm 0.076 \pm 0.050) \times 10^{-4}$$

$$\text{BR}(\pi e \nu) [\text{KLOE '02}, 17 \text{ pb}^{-1}]: (6.91 \pm 0.34 \pm 0.15) \times 10^{-4}$$

# $K_S \rightarrow \pi e \nu$ : KLOE results

PLB 636(2006) 173

Data sample: 410 pb<sup>-1</sup>



$$\text{BR}(K_S \rightarrow \pi^- e^+ \nu) = (3.528 \pm 0.057 \pm 0.027) \times 10^{-4}$$

$$\text{BR}(K_S \rightarrow \pi^+ e^- \bar{\nu}) = (3.517 \pm 0.051 \pm 0.029) \times 10^{-4}$$

$$\text{BR}(K_S \rightarrow \pi e \nu) = (7.046 \pm 0.076 \pm 0.050) \times 10^{-4}$$

$$\text{BR}(\pi e \nu) [\text{KLOE '02, } 17 \text{ pb}^{-1}]: (6.91 \pm 0.34 \pm 0.15) \times 10^{-4}$$

$$A_S = \frac{\Gamma(K_S \rightarrow \pi^- e^+ \nu) - \Gamma(K_S \rightarrow \pi^+ e^- \bar{\nu})}{\Gamma(K_S \rightarrow \pi^- e^+ \nu) + \Gamma(K_S \rightarrow \pi^+ e^- \bar{\nu})}$$

$$A_S = (1.5 \pm 9.6 \pm 2.9) \times 10^{-3}$$

with 2.5 fb<sup>-1</sup>:

$$\delta A_S \sim 3 \times 10^{-3} \sim 2 \text{Re } \varepsilon$$

$$A_S - A_L = 4(\Re \delta + \Re x_-)$$



$$\Re x_- = (-0.8 \pm 2.4 \pm 0.7) \times 10^{-3}$$

CPT &  $\Delta S = \Delta Q$  viol.

$$A_S + A_L = 4(\Re \varepsilon - \Re y)$$



$$\Re y = (0.4 \pm 2.4 \pm 0.7) \times 10^{-3}$$

CPT viol.

input from other experiments

# CPT test: the Bell-Steinberger relation

Unitarity constraint:

$$|K\rangle = a_S |K_S\rangle + a_L |K_L\rangle$$

$$\left( -\frac{d}{dt} \| |K(t)\rangle \|^2 \right)_{t=0} = \sum_f |a_S \langle f|T|K_S\rangle + a_L \langle f|T|K_L\rangle|^2$$

$$\left( \frac{\Gamma_S + \Gamma_L}{\Gamma_S - \Gamma_L} + i \tan \phi_{SW} \right) \left( \frac{\Re \varepsilon}{1 + |\varepsilon|^2} - i \Im \delta \right) = \frac{1}{\Gamma_S - \Gamma_L} \sum_f \langle f|T|K_S\rangle^* \langle f|T|K_L\rangle$$

$$\left( \begin{array}{c} \underline{\Re \varepsilon} \\ 1 + |\varepsilon|^2 \\ \underline{\Im \delta} \end{array} \right) = \frac{1}{N} \left( \begin{array}{cc} 1 + k(1 - 2b) & (1 - k) \tan \phi_{SW} \\ (1 - k) \tan \phi_{SW} & -(1 + k) \end{array} \right) \left( \begin{array}{c} \sum_i \Re \alpha_i \\ \sum_i \Im \alpha_i \end{array} \right) \rightarrow \begin{array}{l} K_S \ K_L \\ \text{observables} \end{array}$$

$$\alpha_{+-} = \eta_{+-} \text{BR}(K_S \rightarrow \pi^+ \pi^-)$$

$$\alpha_{+-0} = \tau_S / \tau_L \eta_{+-0}^* \text{BR}(K_L \rightarrow \pi^+ \pi^- \pi^0)$$

$$\alpha_{00} = \eta_{00} \text{BR}(K_S \rightarrow \pi^0 \pi^0)$$

$$\alpha_{000} = \tau_S / \tau_L \eta_{000}^* \text{BR}(K_L \rightarrow \pi^0 \pi^0 \pi^0)$$

$$\alpha_{kl3} = 2\tau_S / \tau_L \text{BR}(K_L 13) [(A_S + A_L) / 4 - i \text{Im } x_+]$$

$$k = \tau_S / \tau_L, \quad b = \text{BR}(K_L \rightarrow \pi \ell \nu)$$

$$\eta_i = \langle f_i | T | K_L \rangle / \langle f_i | T | K_S \rangle$$

$$N = (1 + k)^2 + (1 - k)^2 \tan^2 \phi_{SW} - 2bk(1 + k)$$

# Experimental inputs to the Bell-Steinberger relation

	Value	Source
$\tau_{K_S}$	$0.08958 \pm 0.00005$ ns	PDG [14]
$\tau_{K_L}$	$50.84 \pm 0.23$ ns	KLOE average
$m_L - m_S$	$(5.290 \pm 0.016) \times 10^9$ s <sup>-1</sup>	PDG [14]
$\text{BR}(K_S \rightarrow \pi^+ \pi^-)$	$0.69186 \pm 0.00051$	KLOE average
$\text{BR}(K_S \rightarrow \pi^0 \pi^0)$	$0.30687 \pm 0.00051$	KLOE average
$\text{BR}(K_S \rightarrow \pi \ell \nu)$	$(11.77 \pm 0.15) \times 10^{-4}$	KLOE [6]
$\text{BR}(K_L \rightarrow \pi^+ \pi^-)$	$(1.933 \pm 0.021) \times 10^{-3}$	KLOE average
$\text{BR}(K_L \rightarrow \pi^0 \pi^0)$	$(0.848 \pm 0.010) \times 10^{-3}$	KLOE average
$\phi_{+-}$	$(43.4 \pm 0.7)^\circ$	PDG [14]
$\phi_{00}$	$(43.7 \pm 0.8)^\circ$	PDG [14]
$R_{S,\gamma} (E_\gamma > 20\text{MeV})$	$(0.710 \pm 0.016) \times 10^{-2}$	E731 [18]
$R_{S,\gamma}^{\text{th-IB}} (E_\gamma > 20\text{MeV})$	$(0.700 \pm 0.001) \times 10^{-2}$	KLOE MC [19]
$ \eta_{+-\gamma} $	$(2.359 \pm 0.074) \times 10^{-3}$	E773 [17]
$\phi_{+-\gamma}$	$(43.8 \pm 4.0)^\circ$	E773 [17]
$\text{BR}(K_L \rightarrow \pi^+ \pi^- \pi^0)$	$0.1262 \pm 0.0011$	KLOE average
$\eta_{+-0}$	$((-2 \pm 7) + i(-2 \pm 9)) \times 10^{-3}$	CPLEAR [10]
$\text{BR}(K_L \rightarrow 3\pi^0)$	$0.1996 \pm 0.0021$	KLOE average
$\text{BR}(K_S \rightarrow 3\pi^0)$	$< 1.5 \times 10^{-7}$ at 95% CL	KLOE [5]
$\phi_{000}$	uniform from 0 to $2\pi$	
$\text{BR}(K_L \rightarrow \pi \ell \nu)$	$0.6709 \pm 0.0017$	KLOE average
$A_L + A_S$	$(0.5 \pm 1.0) \times 10^{-2}$	$K_{\ell 3}$ average
$\text{Im}(x_+)$	$(0.8 \pm 0.7) \times 10^{-2}$	$K_{\ell 3}$ average

Main improvements done with KLOE measurements on  $K_S$  semileptonic and  $3\pi^0$  decays

# CPT test: the Bell-Steinberger relation

**KLOE result:** JHEP12(2006) 011

$$\text{Re } \varepsilon = (159.6 \pm 1.3) \times 10^{-5}$$

$$\text{Im } \delta = (0.4 \pm 2.1) \times 10^{-5}$$

CPLEAR: study of the time evolution of neutral kaons in semileptonic decays

$$\Re \delta = (0.30 \pm 0.33 \pm 0.06) \times 10^{-3}$$

PLB444 (1998) 52

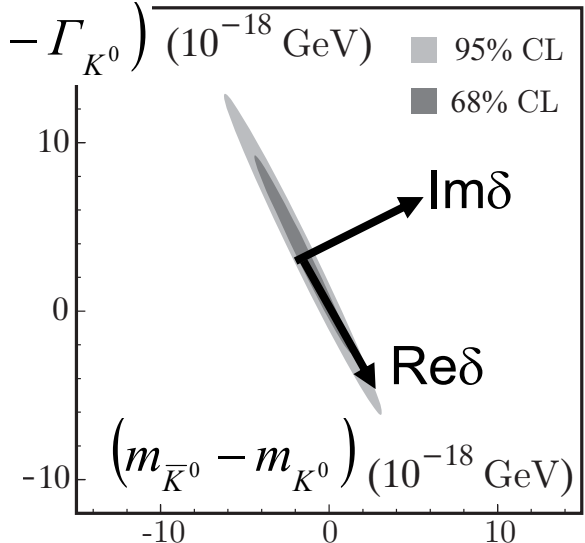
Combining  $\text{Re } \delta$  and  $\text{Im } \delta$  results:

$$\delta = \frac{1}{2} \frac{(m_{\bar{K}^0} - m_{K^0}) - (i/2)(\Gamma_{\bar{K}^0} - \Gamma_{K^0})}{\Delta m + i\Delta\Gamma/2} \quad (\Gamma_{\bar{K}^0} - \Gamma_{K^0}) (10^{-18} \text{ GeV})$$

Assuming  $(\Gamma_{\bar{K}^0} - \Gamma_{K^0}) = 0$ , i.e. no CPT viol. in decay:

$$-5.3 \times 10^{-19} < m_{\bar{K}^0} - m_{K^0} < 6.3 \times 10^{-19} \text{ GeV}$$

at 95% c.l.



# CPT test: the Bell-Steinberger relation

**M. Palutan**, presented at  
**FLAVIANET Kaon ws 08 (prelim.):**

$$\begin{aligned}\text{Re } \varepsilon &= (161.2 \pm 0.6) \times 10^{-5} \\ \text{Im } \delta &= (-0.1 \pm 1.4) \times 10^{-5}\end{aligned}$$

( using new KTeV results on  $\phi_{\pi\pi}$  :  
Moriond EW 08, HQL08)

Combining  $\text{Re}\delta$  and  $\text{Im}\delta$  results:

$$\delta = \frac{1}{2} \frac{(m_{\bar{K}^0} - m_{K^0}) - (i/2)(\Gamma_{\bar{K}^0} - \Gamma_{K^0})}{\Delta m + i\Delta\Gamma/2} \quad (\Gamma_{\bar{K}^0} - \Gamma_{K^0}) (10^{-18} \text{ GeV})$$

■ 95% CL  
■ 68% CL

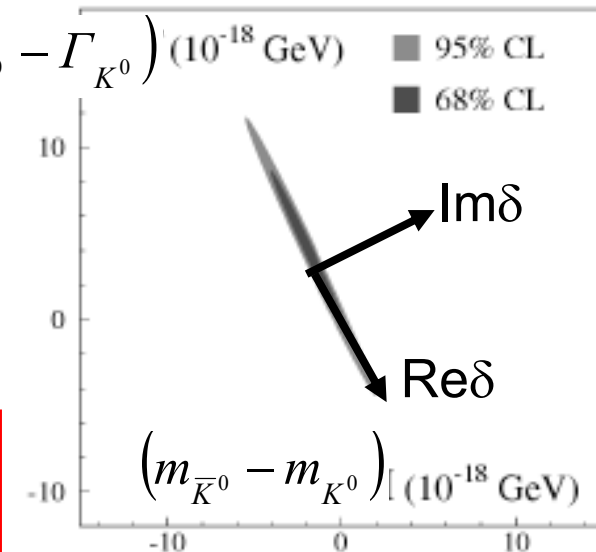
Assuming  $(\Gamma_{\bar{K}^0} - \Gamma_{K^0}) = 0$  , i.e. no CPT viol. in decay:

$$\left| m_{\bar{K}^0} - m_{K^0} \right| < 4.0 \times 10^{-19} \text{ GeV at 95\% C.L.}$$

CPLEAR: study of the time evolution of  
neutral kaons in semileptonic decays

$$\Re\delta = (0.30 \pm 0.33 \pm 0.06) \times 10^{-3}$$

**PLB444 (1998) 52**



---

---

## **2) Search for decoherence and CPT violation in the neutral kaon system**

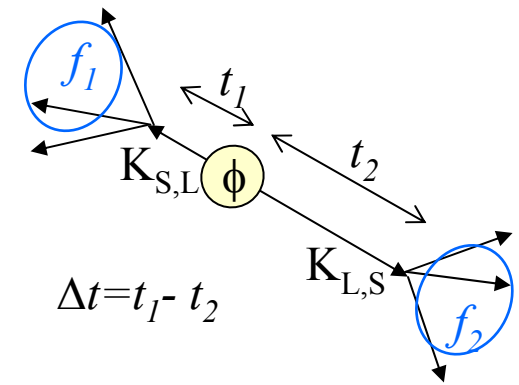


# Neutral kaon interferometry

$$|i\rangle = \frac{N}{\sqrt{2}} \left[ |K_S(\vec{p})\rangle |K_L(-\vec{p})\rangle - |K_L(\vec{p})\rangle |K_S(-\vec{p})\rangle \right]$$

Double differential time distribution:

$$I(f_1, t_1; f_2, t_2) = C_{12} \left\{ |\eta_1|^2 e^{-\Gamma_L t_1 - \Gamma_S t_2} + |\eta_2|^2 e^{-\Gamma_S t_1 - \Gamma_L t_2} - 2|\eta_1||\eta_2| e^{-(\Gamma_S + \Gamma_L)(t_1 + t_2)/2} \cos[\Delta m(t_2 - t_1) + \phi_1 - \phi_2] \right\}$$



where  $t_1(t_2)$  is the proper time of one (the other) kaon decay into  $f_1$  ( $f_2$ ) final state and:

$$\eta_i = |\eta_i| e^{i\phi_i} = \langle f_i | T | K_L \rangle / \langle f_i | T | K_S \rangle$$

$$C_{12} = \frac{|N|^2}{2} \left| \langle f_1 | T | K_S \rangle \langle f_2 | T | K_S \rangle \right|^2$$

**characteristic interference term at a  $\phi$ -factory  $\Rightarrow$  interferometry**

$$f_i = \pi^+\pi^-, \pi^0\pi^0, \pi l\nu, \pi^+\pi^-\pi^0, 3\pi^0, \pi^+\pi^-\gamma \text{ ..etc}$$

# Neutral kaon interferometry

Integrating in  $(t_1+t_2)$  we get the time difference ( $\Delta t=t_1-t_2$ ) distribution (1-dim plot simpler to manipulate than 2-dim plot):

$$I(f_1, f_2; \Delta t \geq 0) = \frac{C_{12}}{\Gamma_S + \Gamma_L} \left\{ |\eta_1|^2 e^{-\Gamma_L \Delta t} + |\eta_2|^2 e^{-\Gamma_S \Delta t} - 2 |\eta_1| |\eta_2| e^{-(\Gamma_S + \Gamma_L) \Delta t / 2} \cos(\Delta m \Delta t + \phi_2 - \phi_1) \right\}$$

for  $\Delta t < 0$      $\Delta t \rightarrow |\Delta t|$     and  $1 \leftrightarrow 2$

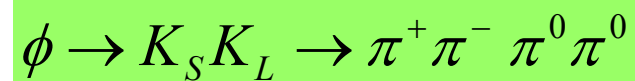
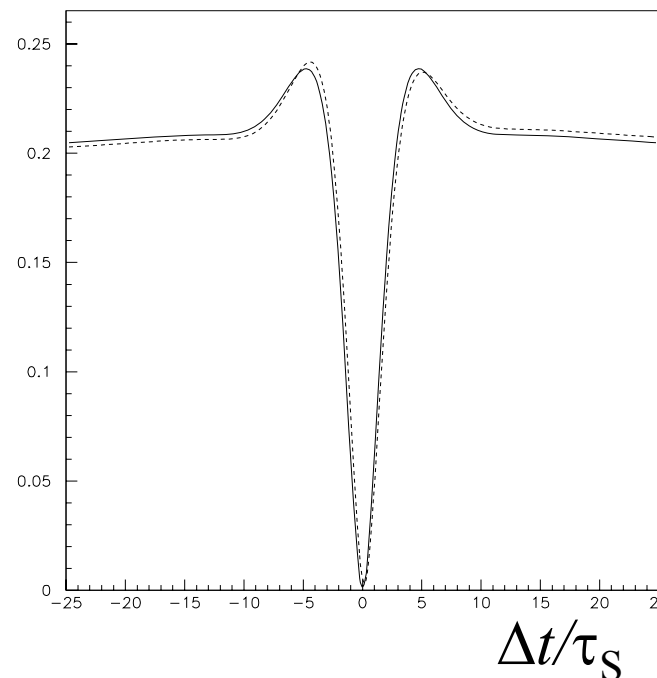
From these distributions for various final states  $f_i$  one can measure the following quantities:

$$\Gamma_S, \Gamma_L, \Delta m, |\eta_i|, \phi_i \equiv \arg(\eta_i)$$

Phases (difference of) from the interference term => **interferometry**

# Neutral kaon interferometry: main observables

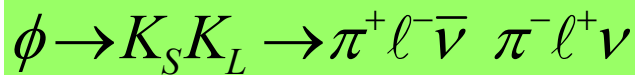
$I(\Delta t)$  (a.u)



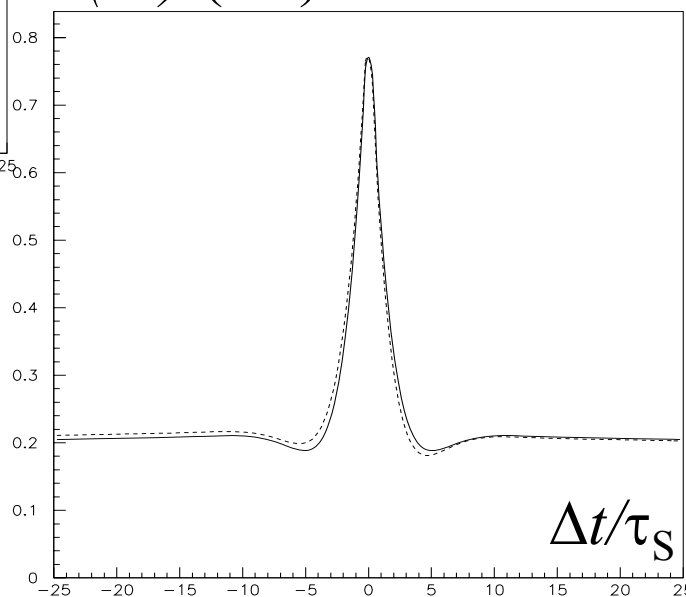
$$\Re\left(\frac{\varepsilon'}{\varepsilon}\right) \quad \Im\left(\frac{\varepsilon'}{\varepsilon}\right)$$

$$\Re\delta + \Re x_-$$

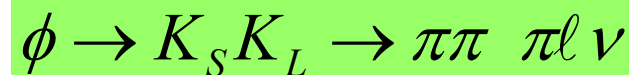
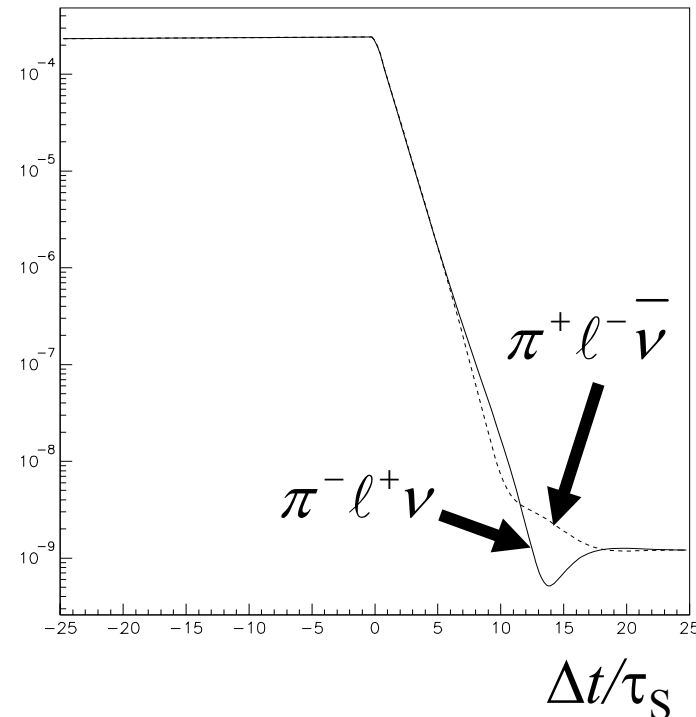
$$\Im\delta + \Im x_+$$



$I(\Delta t)$  (a.u)



$I(\Delta t)$  (a.u)



$$A_L = 2\Re\varepsilon - \Re\delta$$

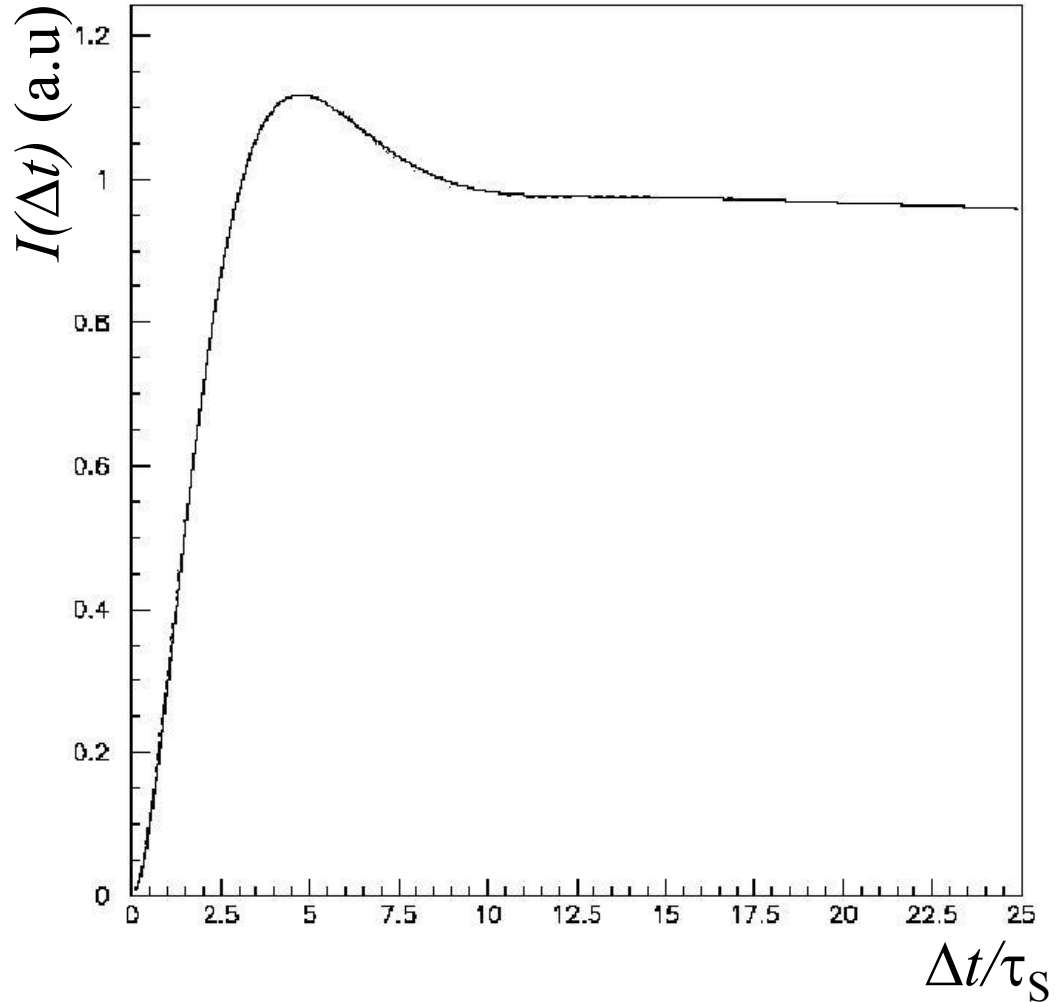
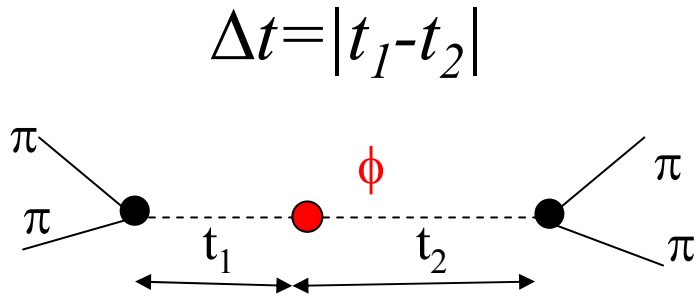
$$- \Re y - \Re x_-$$

$$\phi_{\pi\pi}$$

$$\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \quad \pi^+ \pi^-$$

$$|i\rangle = \frac{1}{\sqrt{2}} \left[ |K^0\rangle |\bar{K}^0\rangle - |\bar{K}^0\rangle |K^0\rangle \right]$$

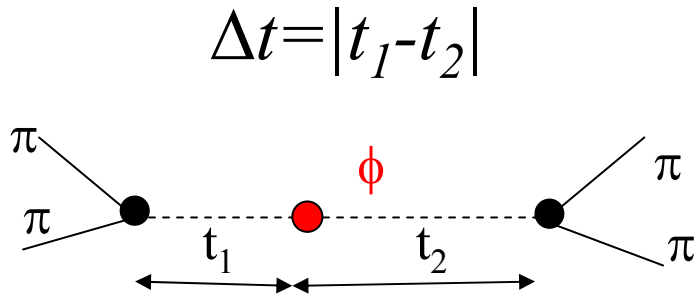
Same final state for both kaons:  $f_1 = f_2 = \pi^+ \pi^-$



$$\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \quad \pi^+ \pi^-$$

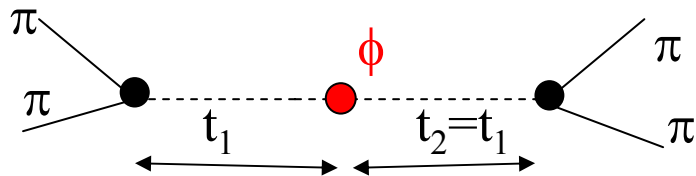
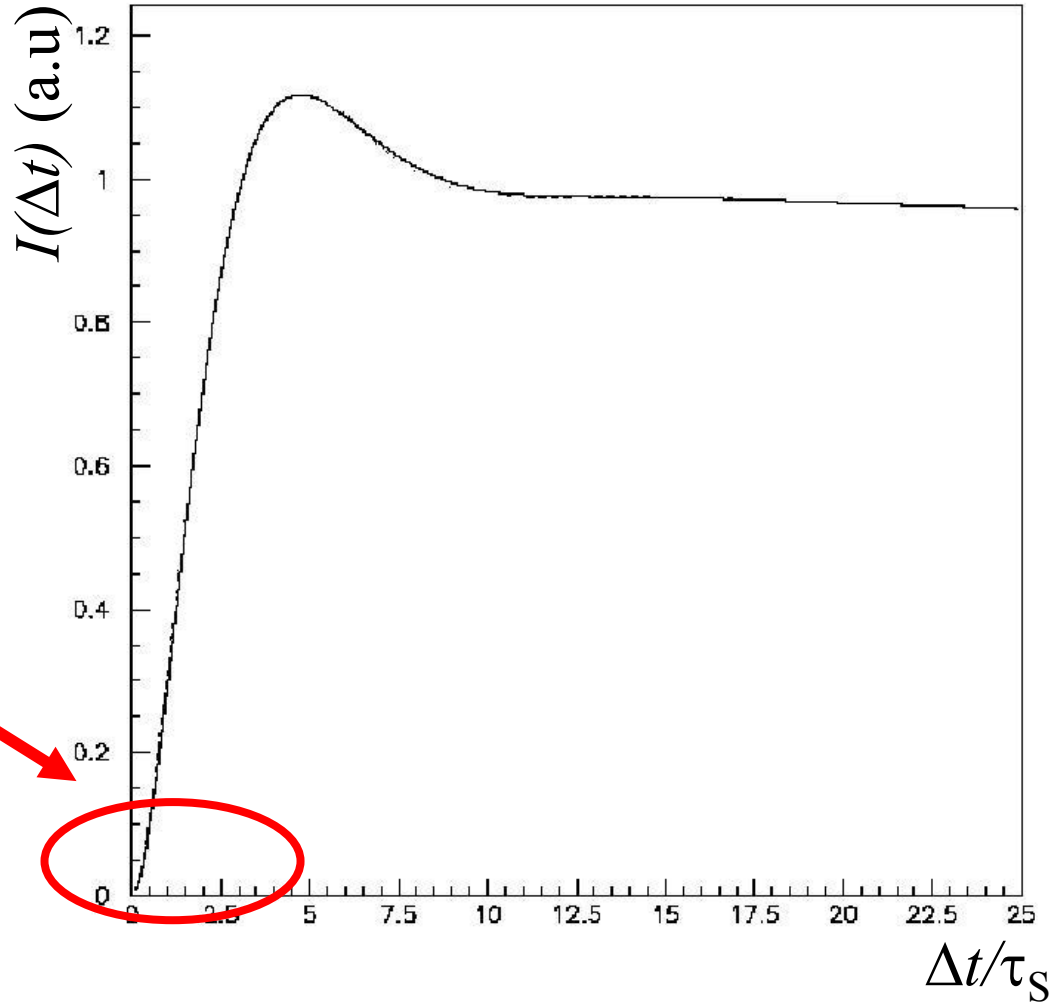
$$|i\rangle = \frac{1}{\sqrt{2}} \left[ |K^0\rangle |\bar{K}^0\rangle - |\bar{K}^0\rangle |K^0\rangle \right]$$

Same final state for both kaons:  $f_1 = f_2 = \pi^+ \pi^-$



EPR correlation:

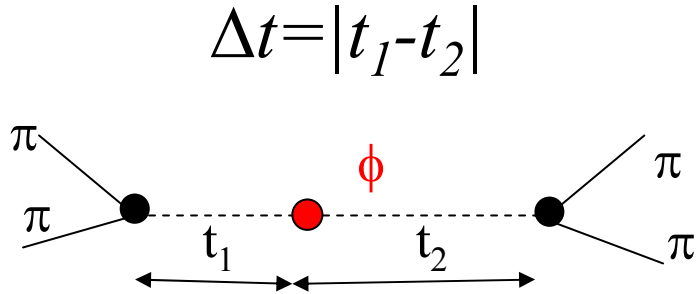
no simultaneous decays  
( $\Delta t=0$ ) in the same  
final state due to the  
destructive  
quantum interference



$$\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \quad \pi^+ \pi^-$$

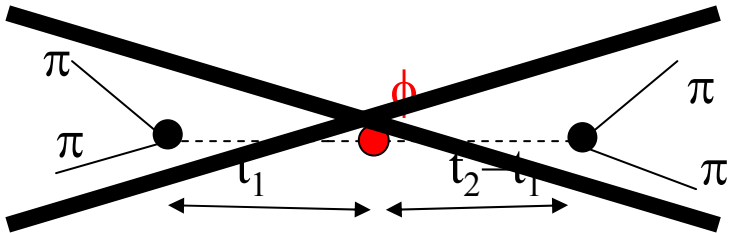
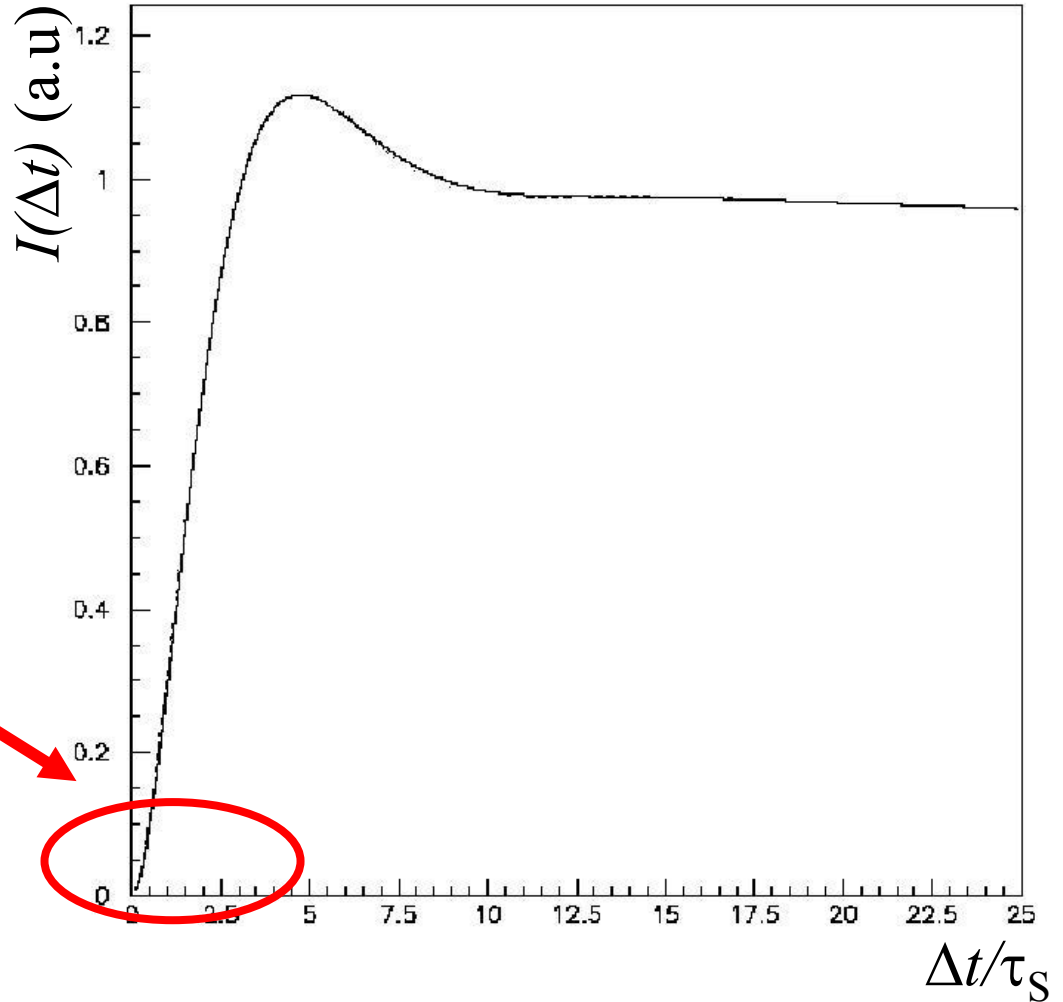
$$|i\rangle = \frac{1}{\sqrt{2}} \left[ |K^0\rangle |\bar{K}^0\rangle - |\bar{K}^0\rangle |K^0\rangle \right]$$

Same final state for both kaons:  $f_1 = f_2 = \pi^+ \pi^-$



EPR correlation:

no simultaneous decays  
( $\Delta t=0$ ) in the same  
final state due to the  
destructive  
quantum interference



# $\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ : test of quantum coherence

$$|i\rangle = \frac{1}{\sqrt{2}} \left[ |K^0\rangle |\bar{K}^0\rangle - |\bar{K}^0\rangle |K^0\rangle \right]$$

$$I(\pi^+ \pi^-, \pi^+ \pi^-; \Delta t) = \frac{N}{2} \left[ \left| \langle \pi^+ \pi^-, \pi^+ \pi^- | K^0 \bar{K}^0(\Delta t) \rangle \right|^2 + \left| \langle \pi^+ \pi^-, \pi^+ \pi^- | \bar{K}^0 K^0(\Delta t) \rangle \right|^2 - 2 \Re \left( \langle \pi^+ \pi^-, \pi^+ \pi^- | K^0 \bar{K}^0(\Delta t) \rangle \langle \pi^+ \pi^-, \pi^+ \pi^- | \bar{K}^0 K^0(\Delta t) \rangle^* \right) \right]$$

Feynman described the phenomenon of interference as containing “the only mystery” of quantum mechanics

# $\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ : test of quantum coherence

$$|i\rangle = \frac{1}{\sqrt{2}} \left[ |K^0\rangle |\bar{K}^0\rangle - |\bar{K}^0\rangle |K^0\rangle \right]$$

$$I(\pi^+ \pi^-, \pi^+ \pi^-; \Delta t) = \frac{N}{2} \left[ \left| \langle \pi^+ \pi^-, \pi^+ \pi^- | K^0 \bar{K}^0(\Delta t) \rangle \right|^2 + \left| \langle \pi^+ \pi^-, \pi^+ \pi^- | \bar{K}^0 K^0(\Delta t) \rangle \right|^2 \right. \\ \left. - (1 - \zeta_{00}) \cdot 2 \Re \left( \langle \pi^+ \pi^-, \pi^+ \pi^- | K^0 \bar{K}^0(\Delta t) \rangle \langle \pi^+ \pi^-, \pi^+ \pi^- | \bar{K}^0 K^0(\Delta t) \rangle^* \right) \right]$$

Feynman described the phenomenon of interference as containing “the only mystery” of quantum mechanics



# $\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ : test of quantum coherence

$$|i\rangle = \frac{1}{\sqrt{2}} \left[ |K^0\rangle |\bar{K}^0\rangle - |\bar{K}^0\rangle |K^0\rangle \right]$$

$$I(\pi^+ \pi^-, \pi^+ \pi^-; \Delta t) = \frac{N}{2} \left[ \left| \langle \pi^+ \pi^-, \pi^+ \pi^- | K^0 \bar{K}^0(\Delta t) \rangle \right|^2 + \left| \langle \pi^+ \pi^-, \pi^+ \pi^- | \bar{K}^0 K^0(\Delta t) \rangle \right|^2 \right. \\ \left. - (1 - \zeta_{0\bar{0}}) \cdot 2\Re \left( \langle \pi^+ \pi^-, \pi^+ \pi^- | K^0 \bar{K}^0(\Delta t) \rangle \langle \pi^+ \pi^-, \pi^+ \pi^- | \bar{K}^0 K^0(\Delta t) \rangle^* \right) \right]$$

Feynman described the phenomenon of interference as containing “the only mystery” of quantum mechanics

Decoherence parameter:

$$\zeta_{0\bar{0}} = 0 \rightarrow \text{QM}$$

$$\zeta_{0\bar{0}} = 1 \rightarrow \text{total decoherence}$$

(also known as Furry's hypothesis or spontaneous factorization)  
[W.Furry, PR 49 (1936) 393]

# $\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ : test of quantum coherence

- Analysed data:  $L=380 \text{ pb}^{-1}$
- Fit including  $\Delta t$  resolution and efficiency effects + regeneration
- $\Gamma_S, \Gamma_L, \Delta m$  fixed from PDG

**KLOE result:** [PLB 642\(2006\) 315](#)

$$\zeta_{0\bar{0}} = (1.0 \pm 2.1_{\text{STAT}} \pm 0.4_{\text{SYST}}) \times 10^{-6}$$

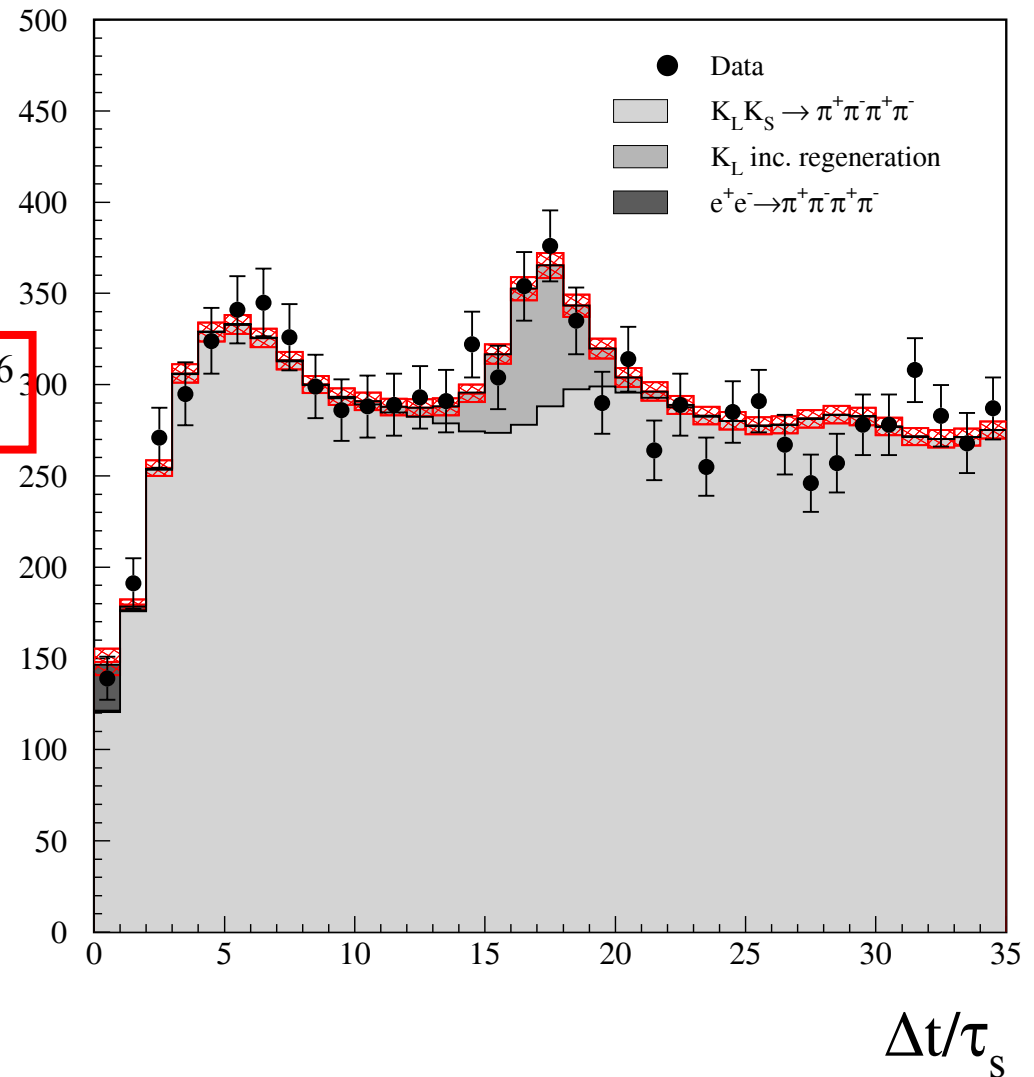
as CP viol.  $O(|\eta_{+-}|^2) \sim 10^{-6}$   
 $\Rightarrow$  high sensitivity to  $\zeta_{0\bar{0}}$

From CPLEAR data, Bertlmann et al.  
(PR D60 (1999) 114032) obtain:

$$\zeta_{0\bar{0}} = 0.4 \pm 0.7$$

In the B-meson system, BELLE coll.  
(PRL 99 (2007) 131802) obtains:

$$\zeta_{0\bar{0}}^B = 0.029 \pm 0.057$$



# $\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ : test of quantum coherence

- Analysed data:  $L=380 \text{ pb}^{-1}$
- Fit including  $\Delta t$  resolution and efficiency effects + regeneration
- $\Gamma_S, \Gamma_L, \Delta m$  fixed from PDG

**KLOE result:** PLB 642(2006) 315

$$\zeta_{0\bar{0}} = (1.0 \pm 2.1_{\text{STAT}} \pm 0.4_{\text{SYST}}) \times 10^{-6}$$

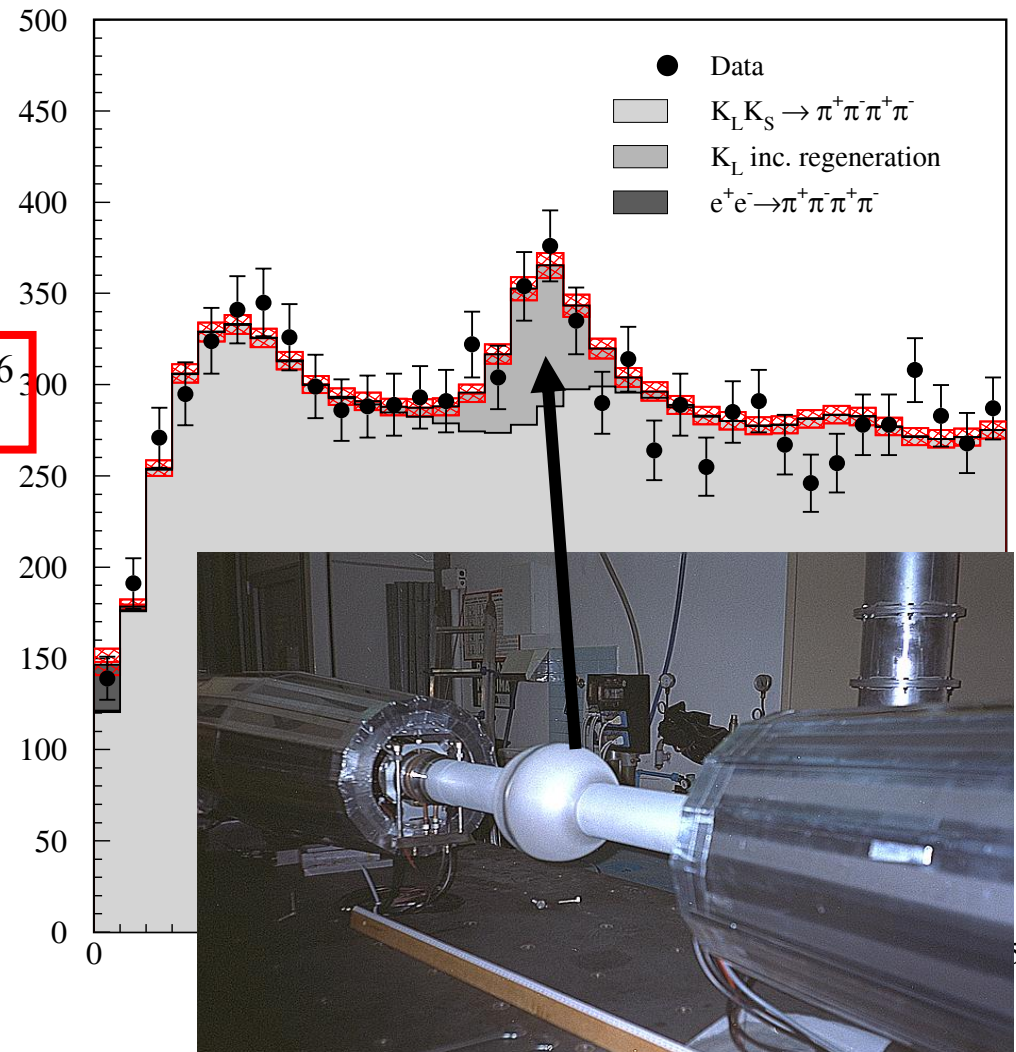
as CP viol.  $O(|\eta_{+-}|^2) \sim 10^{-6}$   
 $\Rightarrow$  high sensitivity to  $\zeta_{0\bar{0}}$

From CPLEAR data, Bertlmann et al.  
(PR D60 (1999) 114032) obtain:

$$\zeta_{0\bar{0}} = 0.4 \pm 0.7$$

In the B-meson system, BELLE coll.  
(PRL 99 (2007) 131802) obtains:

$$\zeta_{0\bar{0}}^B = 0.029 \pm 0.057$$



# $\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ : test of quantum coherence

- Analysed data:  $L=380 \text{ pb}^{-1}$
- Fit including  $\Delta t$  resolution and efficiency effects + regeneration
- $\Gamma_S, \Gamma_L, \Delta m$  fixed from PDG

**KLOE result:** [PLB 642\(2006\) 315](#)

$$\zeta_{0\bar{0}} = (1.0 \pm 2.1_{\text{STAT}} \pm 0.4_{\text{SYST}}) \times 10^{-6}$$

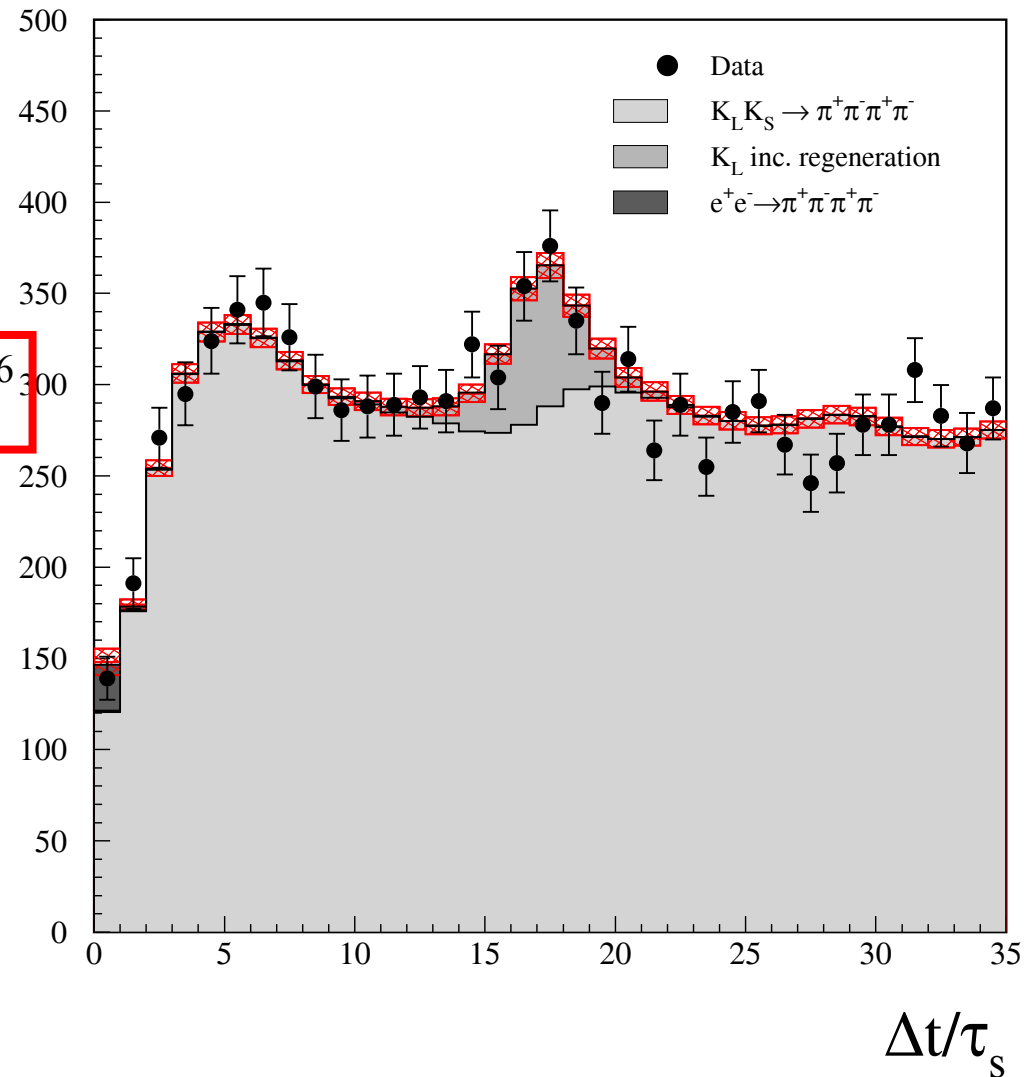
as CP viol.  $O(|\eta_{+-}|^2) \sim 10^{-6}$   
 $\Rightarrow$  high sensitivity to  $\zeta_{0\bar{0}}$

From CPLEAR data, Bertlmann et al.  
(PR D60 (1999) 114032) obtain:

$$\zeta_{0\bar{0}} = 0.4 \pm 0.7$$

In the B-meson system, BELLE coll.  
(PRL 99 (2007) 131802) obtains:

$$\zeta_{0\bar{0}}^B = 0.029 \pm 0.057$$



# $\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ : test of quantum coherence

- Analysed data:  $L=1.5 \text{ fb}^{-1}$  (2004-05 data)
- Fit including  $\Delta t$  resolution and efficiency effects + regeneration
- $\Gamma_S, \Gamma_L, \Delta m$  fixed from PDG

## KLOE FINAL:

$$\zeta_{0\bar{0}} = (1.4 \pm 9.5_{\text{STAT}} \pm 3.8_{\text{SYST}}) \times 10^{-7}$$

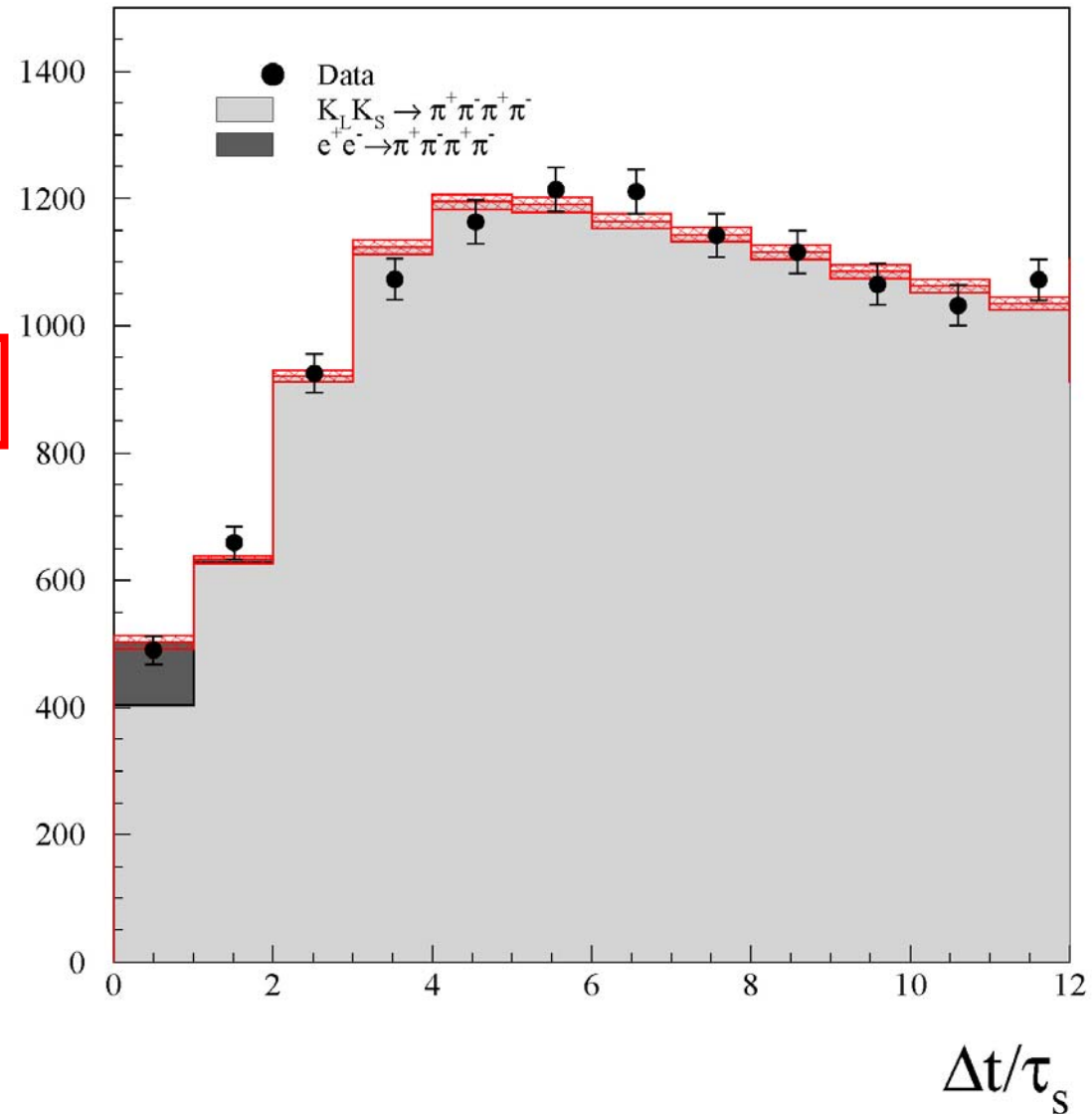
as CP viol.  $O(|\eta_{+-}|^2) \sim 10^{-6}$   
 $\Rightarrow$  high sensitivity to  $\zeta_{0\bar{0}}$

From CPLEAR data, Bertlmann et al.  
(PR D60 (1999) 114032) obtain:

$$\zeta_{0\bar{0}} = 0.4 \pm 0.7$$

In the B-meson system, BELLE coll.  
(PRL 99 (2007) 131802) obtains:

$$\zeta_{0\bar{0}}^B = 0.029 \pm 0.057$$



# $\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ : test of quantum coherence

- Analysed data:  $L=1.5 \text{ fb}^{-1}$  (2004-05 data)
- Fit including  $\Delta t$  resolution and efficiency effects + regeneration
- $\Gamma_S, \Gamma_L, \Delta m$  fixed from PDG

## KLOE FINAL:

$$\zeta_{0\bar{0}} = (1.4 \pm 9.5_{\text{STAT}} \pm 3.8_{\text{SYST}}) \times 10^{-7}$$

as CP viol.  $O(|\eta_{+-}|^2) \sim 10^{-6}$   
 $\Rightarrow$  high sensitivity to  $\zeta_{0\bar{0}}$

From CPLEAR data, Bertlmann et al.  
(PR D60 (1999) 114032) obtain:

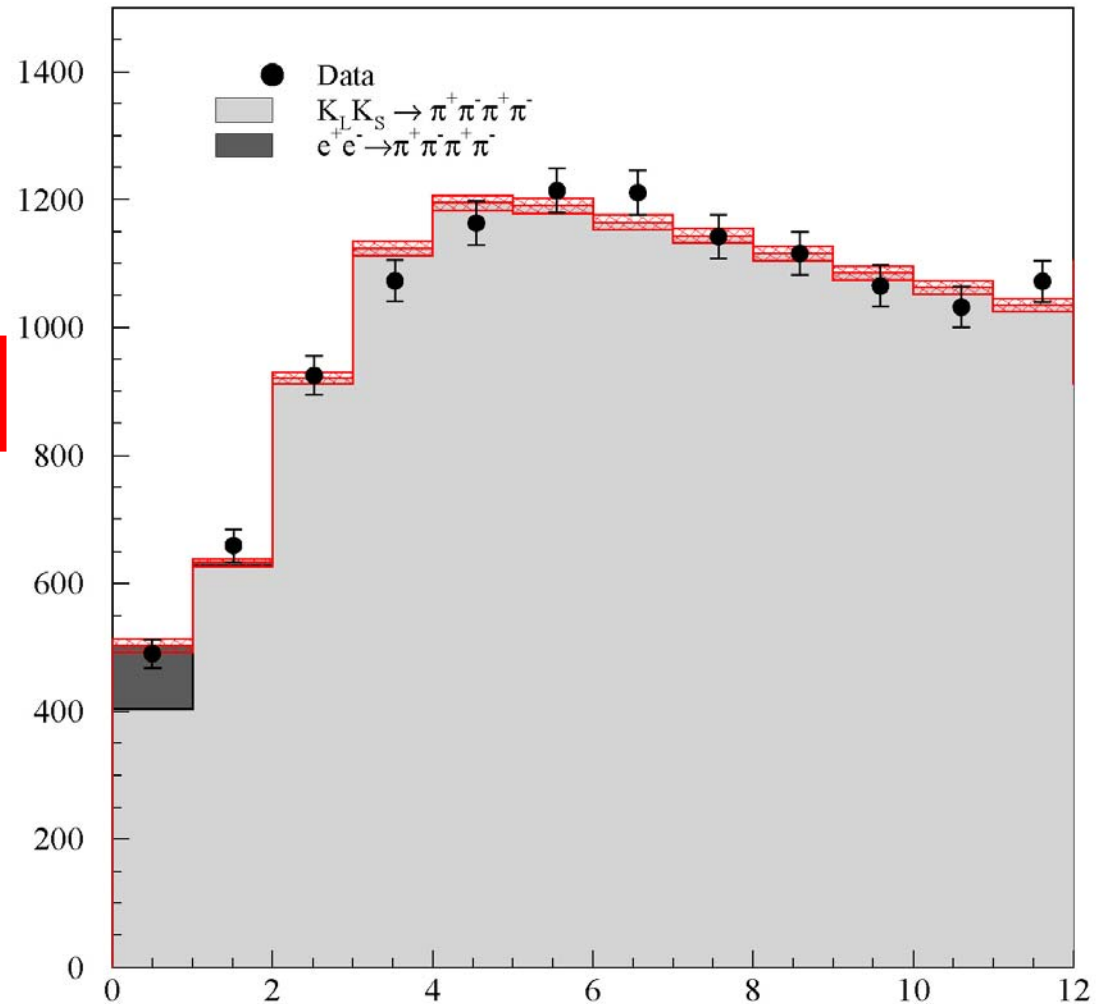
$$\zeta_{0\bar{0}} = 0.4 \pm 0.7$$

In the B-meson system, BELLE coll.  
(PRL 99 (2007) 131802) obtains:

$$\zeta_{0\bar{0}}^B = 0.029 \pm 0.057$$

Comparison with quantum optics test precisions

$\Delta t / \tau_S$



# Decoherence and CPT violation

Modified Liouville – von Neumann equation for the density matrix of the kaon system:

$$\dot{\rho}(t) = \underbrace{-iH\rho + i\rho H^\dagger}_{\text{QM}} + L(\rho)$$

← extra term inducing decoherence:  
pure state => mixed state

# Decoherence and CPT violation

Modified Liouville – von Neumann equation for the density matrix of the kaon system:

$$\dot{\rho}(t) = \underbrace{-iH\rho + i\rho H}_{\text{QM}} + L(\rho)$$

← extra term inducing decoherence:  
pure state => mixed state

## Possible decoherence due quantum gravity effects:

**Black hole information loss paradox** => Possible decoherence near a black hole.

Hawking [1] suggested that at a microscopic level, in a quantum gravity picture, non-trivial space-time fluctuations (generically space-time foam) could give rise to decoherence effects, which would necessarily entail a violation of CPT [2].

J. Ellis et al.[3-6] => model of decoherence for neutral kaons => 3 new CPTV param.  $\alpha, \beta, \gamma$ :

$$L(\rho) = L(\rho; \alpha, \beta, \gamma)$$
$$\alpha, \gamma > 0, \quad \alpha\gamma > \beta^2$$

At most:  $\alpha, \beta, \gamma = O\left(\frac{M_K^2}{M_{\text{PLANCK}}}\right) \approx 2 \times 10^{-20} \text{ GeV}$

[1] Hawking, Comm.Math.Phys.87 (1982) 395; [2] Wald, PR D21 (1980) 2742; [3] Ellis et. al, NP B241 (1984) 381; PRD53 (1996)3846 [4] Huet, Peskin, NP B434 (1995) 3; [5] Benatti, Floreanini, NPB511 (1998) 550 [6] Bernabeu, Ellis, Mavromatos, Nanopoulos, Papavassiliou: Handbook on kaon interferometry [hep-ph/0607322]



# Decoherence and CPT violation

Modified Liouville – von Neumann equation for

$$\dot{\rho}(t) = -i[H, \rho] + \dots$$



J.A. Wheeler

**Possible decoherence due to**  
**Black hole information loss**

Hawking [1] suggested that trivial space-time fluctuations lead to decoherence effects, which would necessarily erode information. J. Ellis et al. [3-6] => model of decoherence for

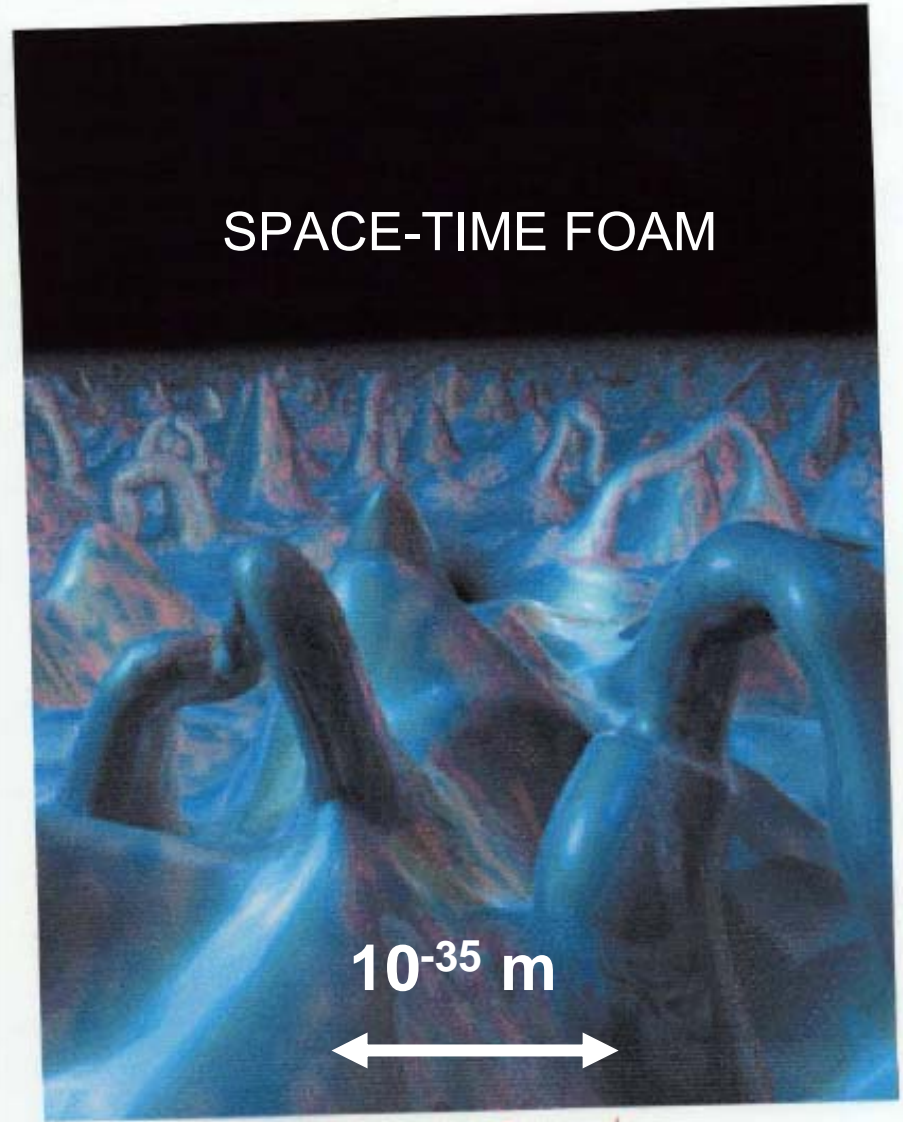
$$L(\rho) = L(\rho; \alpha, \beta, \gamma)$$

At most:  $\alpha, \beta, \gamma$

$$\alpha, \gamma > 0, \quad \alpha\gamma > \beta^2$$

- [1] Hawking, Comm.Math.Phys.87 (1982) 395; [2] Wald, P. PRD53 (1996)3846 [4] Huet, Peskin, NP B434 (1995) 3; [5] Bernabeu, Ellis, Mavromatos, Nanopoulos, Papavassiliou: F

AN ARTIST'S IMPRESSION OF SPACE-TIME FOAM



SPACE-TIME FOAM

$10^{-35}$  m

$10^{-35}$  m

(AFTER WEINBERG 99)

# Decoherence and CPT violation

Modified Liouville – von Neumann equation for the density matrix of the kaon system:

$$\dot{\rho}(t) = \underbrace{-iH\rho + i\rho H}_{\text{QM}} + L(\rho)$$

← extra term inducing decoherence:  
pure state => mixed state

## Possible decoherence due quantum gravity effects:

**Black hole information loss paradox** => Possible decoherence near a black hole.

Hawking [1] suggested that at a microscopic level, in a quantum gravity picture, non-trivial space-time fluctuations (generically space-time foam) could give rise to decoherence effects, which would necessarily entail a violation of CPT [2].

J. Ellis et al.[3-6] => model of decoherence for neutral kaons => 3 new CPTV param.  $\alpha, \beta, \gamma$ :

$$L(\rho) = L(\rho; \alpha, \beta, \gamma)$$
$$\alpha, \gamma > 0, \quad \alpha\gamma > \beta^2$$

At most:  $\alpha, \beta, \gamma = O\left(\frac{M_K^2}{M_{\text{PLANCK}}}\right) \approx 2 \times 10^{-20} \text{ GeV}$

[1] Hawking, Comm.Math.Phys.87 (1982) 395; [2] Wald, PR D21 (1980) 2742; [3] Ellis et. al, NP B241 (1984) 381; PRD53 (1996)3846 [4] Huet, Peskin, NP B434 (1995) 3; [5] Benatti, Floreanini, NPB511 (1998) 550 [6] Bernabeu, Ellis, Mavromatos, Nanopoulos, Papavassiliou: Handbook on kaon interferometry [hep-ph/0607322]

# $\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ : decoherence & CPTV by QG

Study of time evolution of **single kaons**  
decaying in  $\pi^+ \pi^-$  and semileptonic final state

CPLEAR **PLB 364, 239 (1999)**

$$\alpha = (-0.5 \pm 2.8) \times 10^{-17} \text{ GeV}$$

$$\beta = (2.5 \pm 2.3) \times 10^{-19} \text{ GeV}$$

$$\gamma = (1.1 \pm 2.5) \times 10^{-21} \text{ GeV}$$

In the complete positivity hypothesis

$$\alpha = \gamma \quad , \quad \beta = 0$$

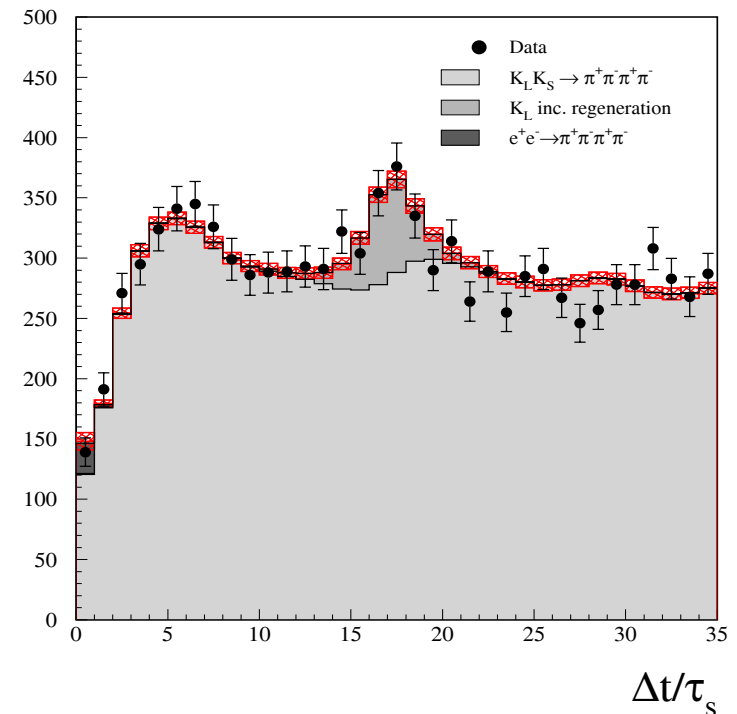
=> only one independent parameter:  $\gamma$

The fit with  $I(\pi^+ \pi^-, \pi^+ \pi^-; \Delta t, \gamma)$  gives:

**KLOE result**  $L=380 \text{ pb}^{-1}$  **PLB 642(2006) 315**

$$\gamma = \left( 1.1_{-2.4}^{+2.9} \text{STAT} \pm 0.4_{\text{SYST}} \right) \times 10^{-21} \text{ GeV}$$

Complete positivity guarantees the positivity of the eigenvalues of density matrices describing states of correlated kaons.



# $\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ : decoherence & CPTV by QG

Study of time evolution of **single kaons**  
decaying in  $\pi^+ \pi^-$  and semileptonic final state

CPLEAR **PLB 364, 239 (1999)**

$$\alpha = (-0.5 \pm 2.8) \times 10^{-17} \text{ GeV}$$

$$\beta = (2.5 \pm 2.3) \times 10^{-19} \text{ GeV}$$

$$\gamma = (1.1 \pm 2.5) \times 10^{-21} \text{ GeV}$$

In the complete positivity hypothesis

$$\alpha = \gamma \quad , \quad \beta = 0$$

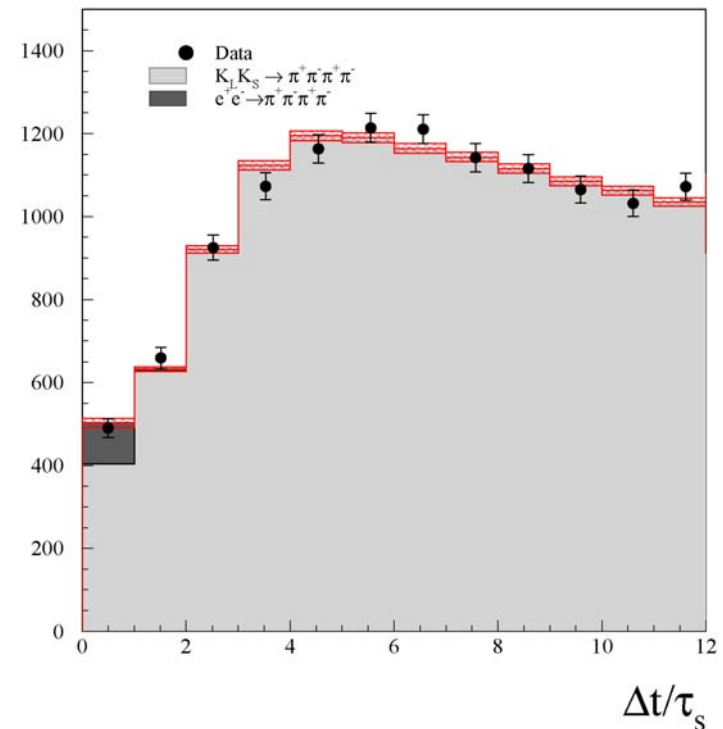
=> only one independent parameter:  $\gamma$

The fit with  $I(\pi^+ \pi^-, \pi^+ \pi^-; \Delta t, \gamma)$  gives:

**KLOE FINAL**  $L = 1.5 \text{ fb}^{-1}$

$$\gamma = (0.7 \pm 1.2_{\text{STAT}} \pm 0.3_{\text{SYST}}) \times 10^{-21} \text{ GeV}$$

Complete positivity guarantees the positivity of the eigenvalues of density matrices describing states of correlated kaons.



# $\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ : CPT violation in correlated K states

In presence of decoherence and CPT violation induced by quantum gravity (CPT operator “ill-defined”) the definition of the particle-antiparticle states could be modified. This in turn could induce a breakdown of the correlations imposed by Bose statistics (EPR correlations) to the kaon state:

[Bernabeu, et al. PRL 92 (2004) 131601, NPB744 (2006) 180].

$$\begin{aligned} |i\rangle &\propto (K^0 \bar{K}^0 - K^0 \bar{K}^0) + \omega (K^0 \bar{K}^0 + K^0 \bar{K}^0) \\ &\propto (K_S K_L - K_L K_S) + \omega (K_S K_S - K_L K_L) \end{aligned}$$

at most one expects:  $|\omega|^2 = O\left(\frac{E^2 / M_{PLANCK}}{\Delta\Gamma}\right) \approx 10^{-5} \Rightarrow |\omega| \sim 10^{-3}$

In some microscopic models of space-time foam arising from non-critical string theory:

[Bernabeu, Mavromatos, Sarkar PRD 74 (2006) 045014]

$$|\omega| \sim 10^{-4} \div 10^{-5}$$

The maximum sensitivity to  $\omega$  is expected for  $f_1=f_2=\pi^+\pi^-$

All CPTV effects induced by QG ( $\alpha, \beta, \gamma, \omega$ ) could be simultaneously disentangled.

# $\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ : CPT violation in correlated K states

Fit of  $I(\pi^+ \pi^-, \pi^+ \pi^-; \Delta t, \omega)$ :

- Analysed data:  $380 \text{ pb}^{-1}$

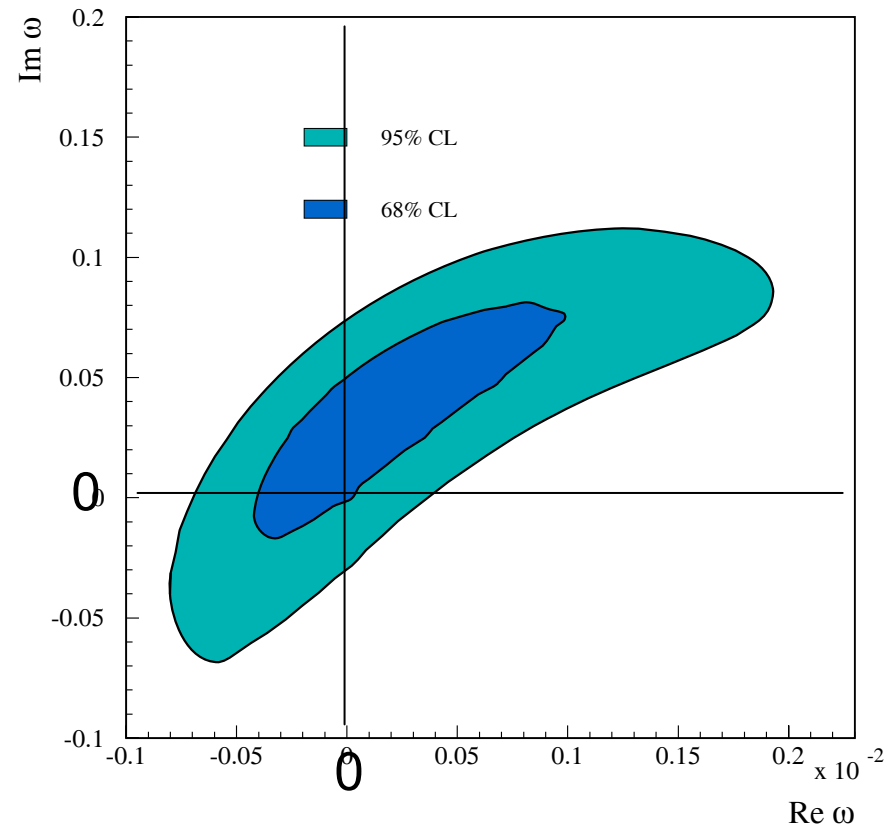
**KLOE result :** [PLB 642\(2006\) 315](#)

$$\Re \omega = \left( 1.1_{-5.3}^{+8.7} \text{STAT} \pm 0.9_{\text{SYST}} \right) \times 10^{-4}$$

$$\Im \omega = \left( 3.4_{-5.0}^{+4.8} \text{STAT} \pm 0.6_{\text{SYST}} \right) \times 10^{-4}$$

$$|\omega| < 2.1 \times 10^{-3} \quad \text{at } 95\% \text{ C.L.}$$

$\text{Im } \omega \times 10^{-2}$



In the B system [Alvarez, Bernabeu, Nebot JHEP 0611, 087]:

$\text{Re } \omega \times 10^{-2}$

$$-0.0084 \leq \Re \omega \leq 0.0100 \quad \text{at } 95\% \text{ C.L.}$$

# $\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$ : CPT violation in correlated K states

Fit of  $I(\pi^+ \pi^-, \pi^+ \pi^-; \Delta t, \omega)$ :

- Analysed data:  $1.5 \text{ fb}^{-1}$  (2004-05 data)

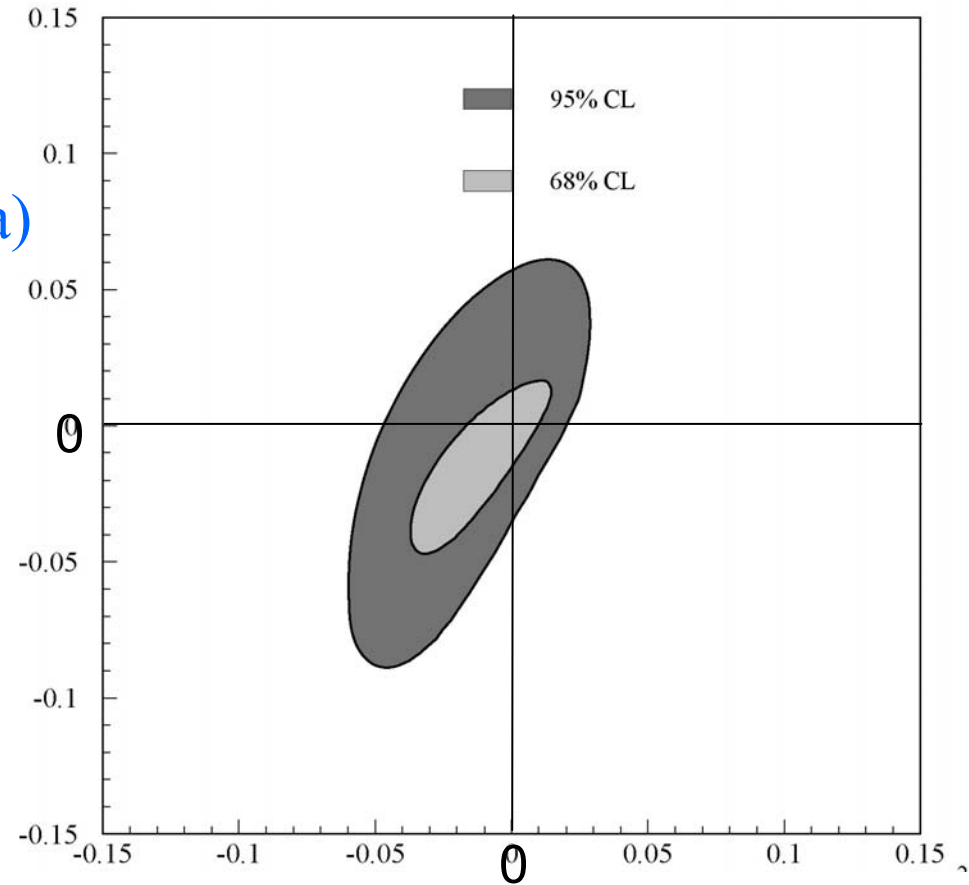
**KLOE FINAL :**

$$\Re \omega = \left( -1.6_{-2.1}^{+3.0}{}_{STAT} \pm 0.4_{SYST} \right) \times 10^{-4}$$

$$\Im \omega = \left( -1.7_{-3.0}^{+3.3}{}_{STAT} \pm 1.2_{SYST} \right) \times 10^{-4}$$

$$|\omega| < 1.0 \times 10^{-3} \quad \text{at } 95\% \text{ C.L.}$$

$\text{Im } \omega \times 10^{-2}$



In the B system [Alvarez, Bernabeu, Nebot JHEP 0611, 087]:

$$-0.0084 \leq \Re \omega \leq 0.0100 \quad \text{at } 95\% \text{ C.L.}$$

---

---

### **3) Tests of Lorentz invariance and CPT symmetry in the neutral kaon system**



# CPT and Lorentz invariance violation (SME)

Kostelecky et al. developed a phenomenological effective model providing a framework for CPT and Lorentz violations, based on spontaneous breaking of CPT and Lorentz symmetry, which might happen in quantum gravity (e.g. in some models of string theory)

**Standard Model Extension (SME)** [Kostelecky PRD61, 016002, PRD64, 076001]

## CPT violation in neutral kaons according to SME:

- CPTV only in mixing, not in decay, at first order (i.e.  $B_I = y = x_- = 0$ )
- $\delta$  cannot be a constant (momentum dependence)

$$\varepsilon_{S,L} = \varepsilon \pm \delta$$

$$\delta = i \sin \phi_{SW} e^{i\phi_{SW}} \gamma_K \left( \Delta a_0 - \vec{\beta}_K \cdot \Delta \vec{a} \right) / \Delta m$$

where  $\Delta a_\mu$  are four parameters associated to SME lagrangian terms and related to CPT and Lorentz violation.

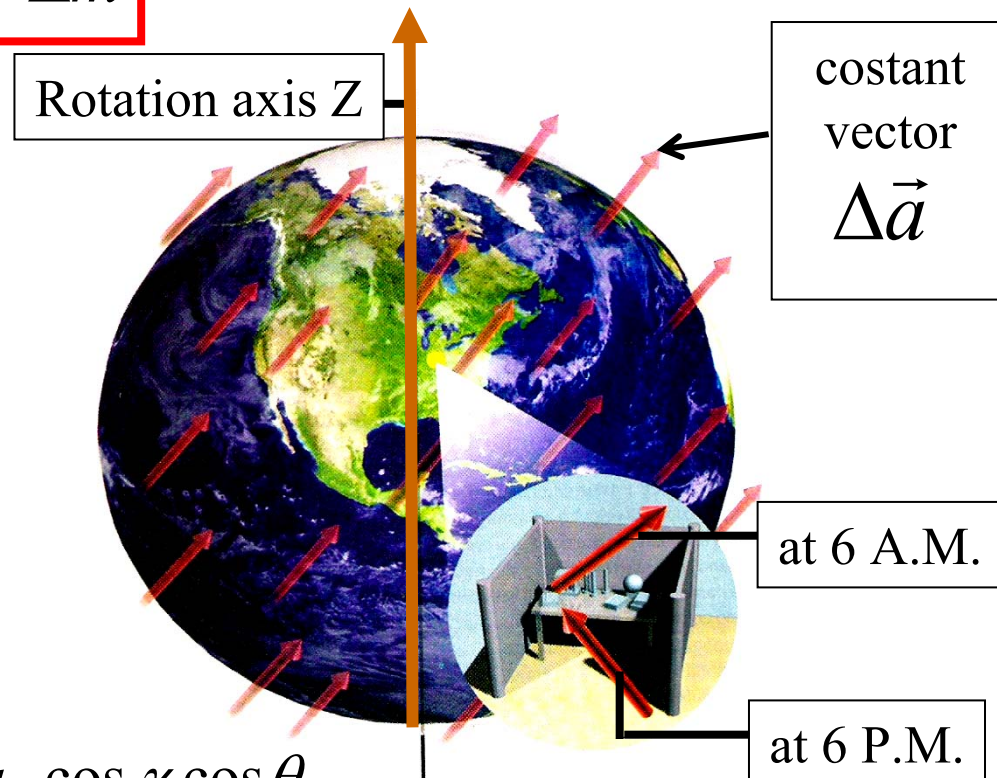
# CPT and Lorentz invariance violation (SME)

$$\delta = i \sin \phi_{SW} e^{i\phi_{SW}} \gamma_K (\Delta a_0 - \vec{\beta}_K \cdot \Delta \vec{a}) / \Delta m$$

$\delta$  depends on sidereal time  $t$  since laboratory frame rotates with Earth (fixed beam).

For a  $\phi$ -factory there is an additional dependence on the polar and azimuthal angle  $\theta, \phi$  of the kaon momentum in the laboratory frame:

$$\begin{aligned} \bar{\delta}(|\vec{p}|, \theta, t) &= \frac{1}{2\pi} \int_0^{2\pi} \delta(\vec{p}, t) d\phi \\ &= \frac{i \sin \phi_{SW} e^{i\phi_{SW}}}{\Delta m} \gamma_K \left[ \Delta a_0 + \beta_K \Delta a_Z \cos \chi \cos \theta \right. \\ &\quad \left. + \beta_K \Delta a_Y \sin \chi \cos \theta \sin \Omega t \right. \\ &\quad \left. + \beta_K \Delta a_X \sin \chi \cos \theta \cos \Omega t \right] \end{aligned}$$



$\Omega$ : Earth's sidereal frequency  
 $\chi$ : angle between the z lab. axis and the Earth's rotation axis

# CPT and Lorentz invariance violation (SME)

$$\delta = i \sin \phi_{SW} e^{i\phi_{SW}} \gamma_K (\Delta a_0 - \vec{\beta}_K \cdot \Delta \vec{a}) / \Delta m$$

$\delta$  depends on sidereal time  $t$  since laboratory frame rotates with Earth (fixed beam).

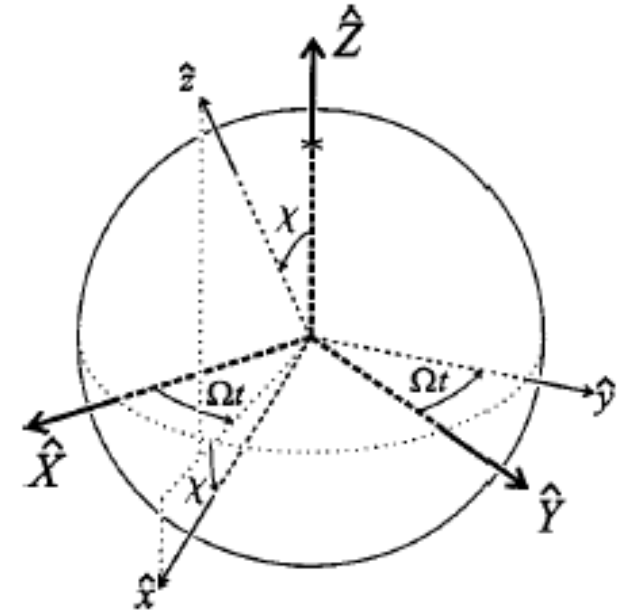
For a  $\phi$ -factory there is an additional dependence on the polar and azimuthal angle  $\theta, \phi$  of the kaon momentum in the laboratory frame:

$$\bar{\delta}(|\vec{p}|, \theta, t) = \frac{1}{2\pi} \int_0^{2\pi} \delta(\vec{p}, t) d\phi$$

$$= \frac{i \sin \phi_{SW} e^{i\phi_{SW}}}{\Delta m} \gamma_K \left[ \Delta a_0 + \beta_K \Delta a_Z \cos \chi \cos \theta \right.$$

$$+ \beta_K \Delta a_Y \sin \chi \cos \theta \sin \Omega t$$

$$\left. + \beta_K \Delta a_X \sin \chi \cos \theta \cos \Omega t \right]$$



(in general  $z$  lab. axis is non-normal to Earth's surface)

$\Omega$ : Earth's sidereal frequency  
 $\chi$ : angle between the  $z$  lab. axis and the Earth's rotation axis

# CPT and Lorentz invariance violation (SME)

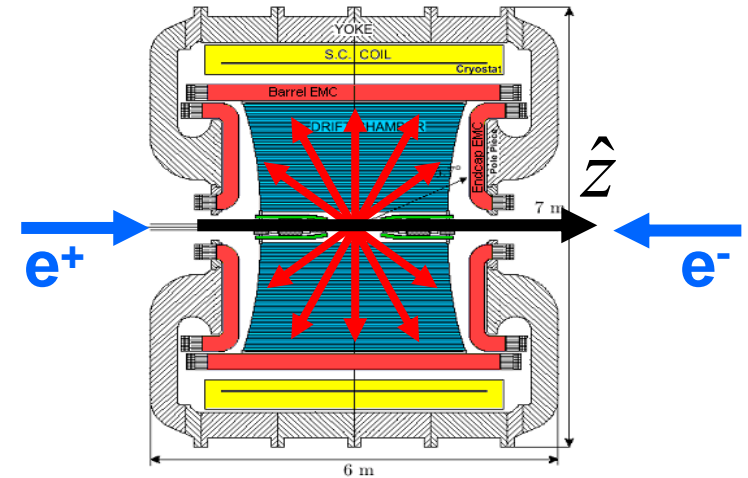
$$\delta = i \sin \phi_{SW} e^{i\phi_{SW}} \gamma_K \left( \Delta a_0 - \vec{\beta}_K \cdot \Delta \vec{a} \right) / \Delta m$$

$\delta$  depends on sidereal time  $t$  since laboratory frame rotates with Earth (fixed beam).

For a  $\phi$ -factory there is an additional dependence on the polar and azimuthal angle  $\theta, \phi$  of the kaon momentum in the laboratory frame:

$$\begin{aligned} \bar{\delta}(|\vec{p}|, \theta, t) &= \frac{1}{2\pi} \int_0^{2\pi} \delta(\vec{p}, t) d\phi \\ &= \frac{i \sin \phi_{SW} e^{i\phi_{SW}}}{\Delta m} \gamma_K \left[ \Delta a_0 + \beta_K \Delta a_Z \cos \chi \cos \theta \right. \\ &\quad \left. + \beta_K \Delta a_Y \sin \chi \cos \theta \sin \Omega t \right. \\ &\quad \left. + \beta_K \Delta a_X \sin \chi \cos \theta \cos \Omega t \right] \end{aligned}$$

At DAΦNE K mesons are produced with angular distribution  $dN/d\Omega \propto \sin^2\theta$



$\Omega$ : Earth's sidereal frequency  
 $\chi$ : angle between the  $z$  lab. axis and the Earth's rotation axis

# Measurement of $\Delta a_0$ at KLOE

## $\Delta a_0$ from $K_S$ and $K_L$ semileptonic charge asymmetries

$$\bar{\delta}(|\vec{p}|, \theta, t) = \frac{i \sin \phi_{SW} e^{i\phi_{SW}}}{\Delta m} \gamma_K [\Delta a_0 + \beta_K \Delta a_Z \cos \chi \cos \theta$$

tagged  $K_S$  and  $K_L$   
(symmetric polar angle  $\theta$  and  
sidereal time  $t$  integration)

$$+ \beta_K \Delta a_Y \sin \chi \cos \theta \sin \Omega t$$

$$+ \beta_K \Delta a_X \sin \chi \cos \theta \cos \Omega t]$$

$$A_{S,L} = \frac{\Gamma(K_{S,L} \rightarrow \pi^- e^+ \nu) - \Gamma(K_{S,L} \rightarrow \pi^+ e^- \bar{\nu})}{\Gamma(K_{S,L} \rightarrow \pi^- e^+ \nu) + \Gamma(K_{S,L} \rightarrow \pi^+ e^- \bar{\nu})}$$

$$= 2\Re \varepsilon \pm 2\Re \delta - 2\Re y \pm 2\Re x_{\pm}$$

$$A_S - A_L \cong \frac{4\Re(i \sin \phi_{SW} e^{i\phi_{SW}}) \gamma_K \Delta a_0}{\Delta m}$$

with  $L=400 \text{ pb}^{-1}$  (**preliminary**):

$$\Delta a_0 = (0.4 \pm 1.8) \times 10^{-17} \text{ GeV}$$

( $\Delta a_0$  evaluated for the first time)

with  $L=2.5 \text{ fb}^{-1}$ :  $\sigma(\Delta a_0) \sim 7 \times 10^{-18} \text{ GeV}$

# Measurement of $\Delta a_{X,Y,Z}$ at KLOE

$\Delta a_{X,Y,Z}$  from  $\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$   
 (analysis vs polar angle  $\theta$  and sidereal time  $t$ )

$$\eta_{+-} = \varepsilon - \delta(p, \theta, t)$$

$I[\pi^+ \pi^- (\cos \theta > 0), \pi^+ \pi^- (\cos \theta < 0); \Delta t]$

- at  $\Delta t \gg \tau_s$  sensitive to  $\text{Re}(\delta/\varepsilon) = 0$
- at  $\Delta t \sim \tau_s$  sensitive to  $\text{Im}(\delta/\varepsilon)$

With  $L = 1 \text{ fb}^{-1}$  (**preliminary**):

$$\Delta a_X = (-6.3 \pm 6.0) \times 10^{-18} \text{ GeV}$$

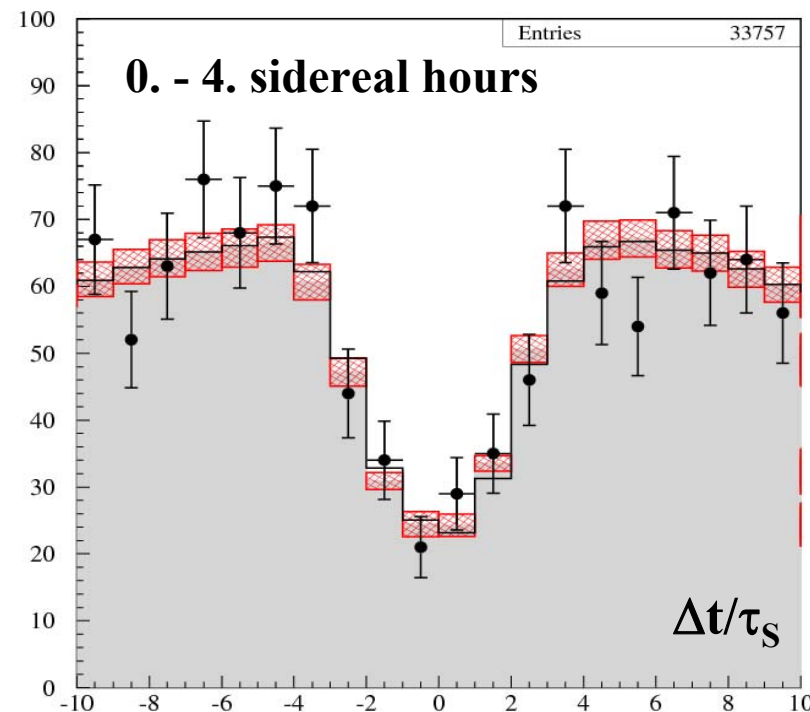
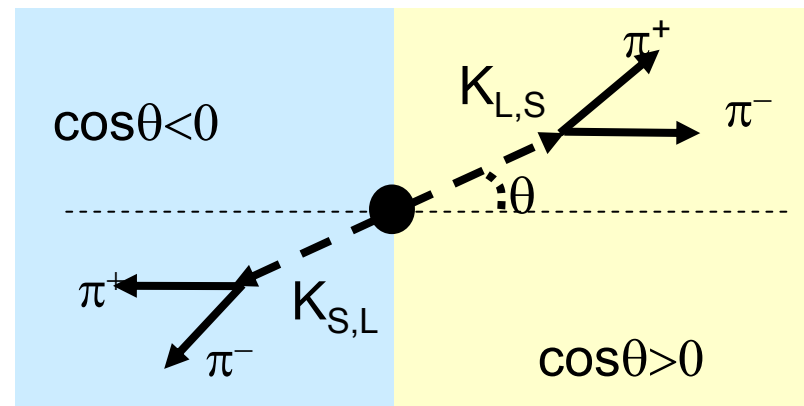
$$\Delta a_Y = (2.8 \pm 5.9) \times 10^{-18} \text{ GeV}$$

$$\Delta a_Z = (2.4 \pm 9.7) \times 10^{-18} \text{ GeV}$$

KTeV :  $\Delta a_X, \Delta a_Y < 9.2 \times 10^{-22} \text{ GeV}$  @ 90% CL

BABAR  $\Delta a_{X,Y}^B, (\Delta a_0^B - 0.30 \Delta a_Z^B) \sim O(10^{-13} \text{ GeV})$

[PRL 100 (2008) 131802]



---

## 4) Future plans

# KLOE-2 at upgraded DAΦNE

## Upgrade of DAΦNE in luminosity:

Crabbed waist scheme at DAΦNE (proposal by P. Raimondi)

- increase L by a factor  $O(5)$
- requires minor modifications
- relatively low cost
- Successful experimental test at DAΦNE

**KLOE-2 Plan:** {

- phase 0: KLOE restart taking data end 2009 with a minimal upgrade ( $L \sim 5 \text{ fb}^{-1}$ )
- phase 1: full KLOE upgrade (KLOE-2) > 2011 ( $L > 20 \text{ fb}^{-1}$ )

## Physics issues:

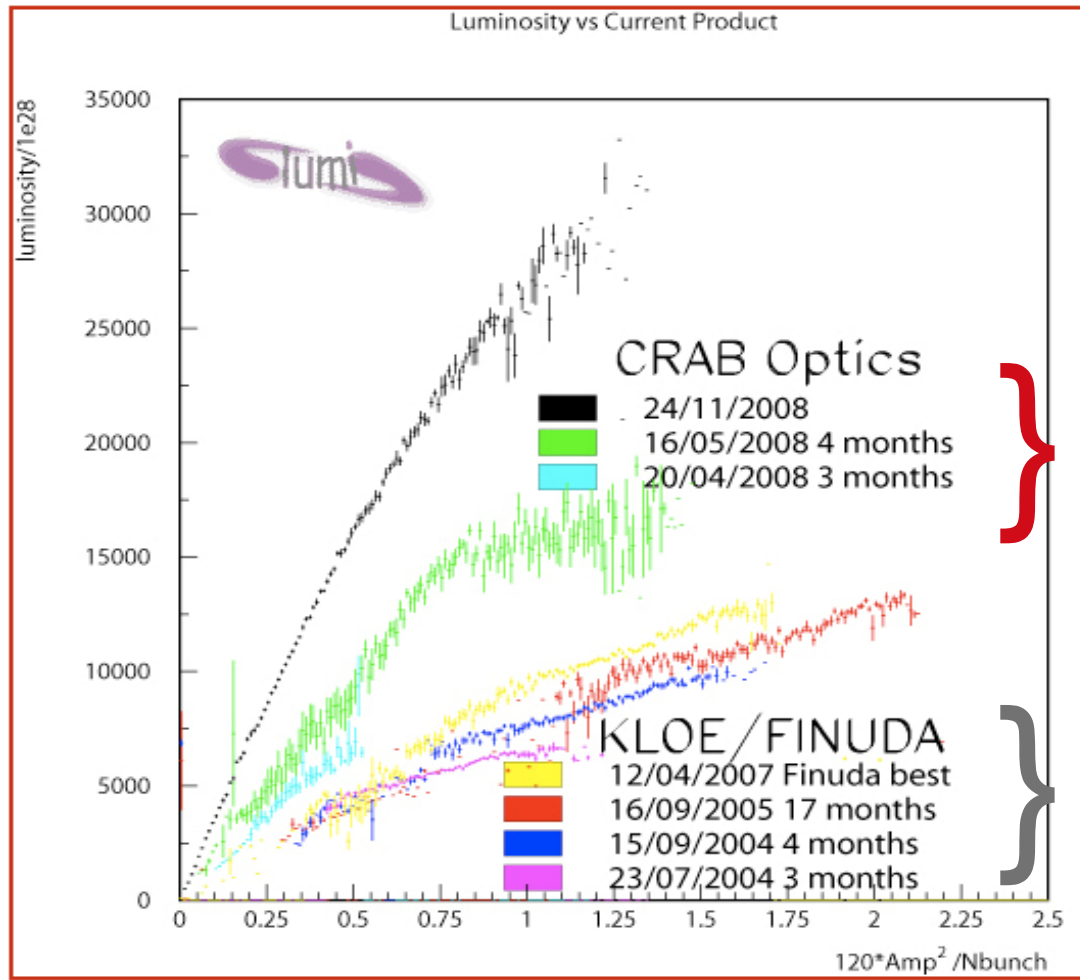
- Neutral kaon interferometry, CPT symmetry & QM tests
- Kaon physics, CKM, LFV, rare  $K_S$  decays
- $\eta, \eta'$  physics
- Light scalars,  $\gamma\gamma$  physics
- Hadron cross section at low energy, muon anomaly

## Detector upgrade issues:

- Inner tracker R&D
- $\gamma\gamma$  tagging system
- Calorimeter, increase of granularity
- FEE maintenance and upgrade
- Computing and networking update
- etc.. (Trigger, software, ...)



# DAΦNE Luminosity versus colliding currents

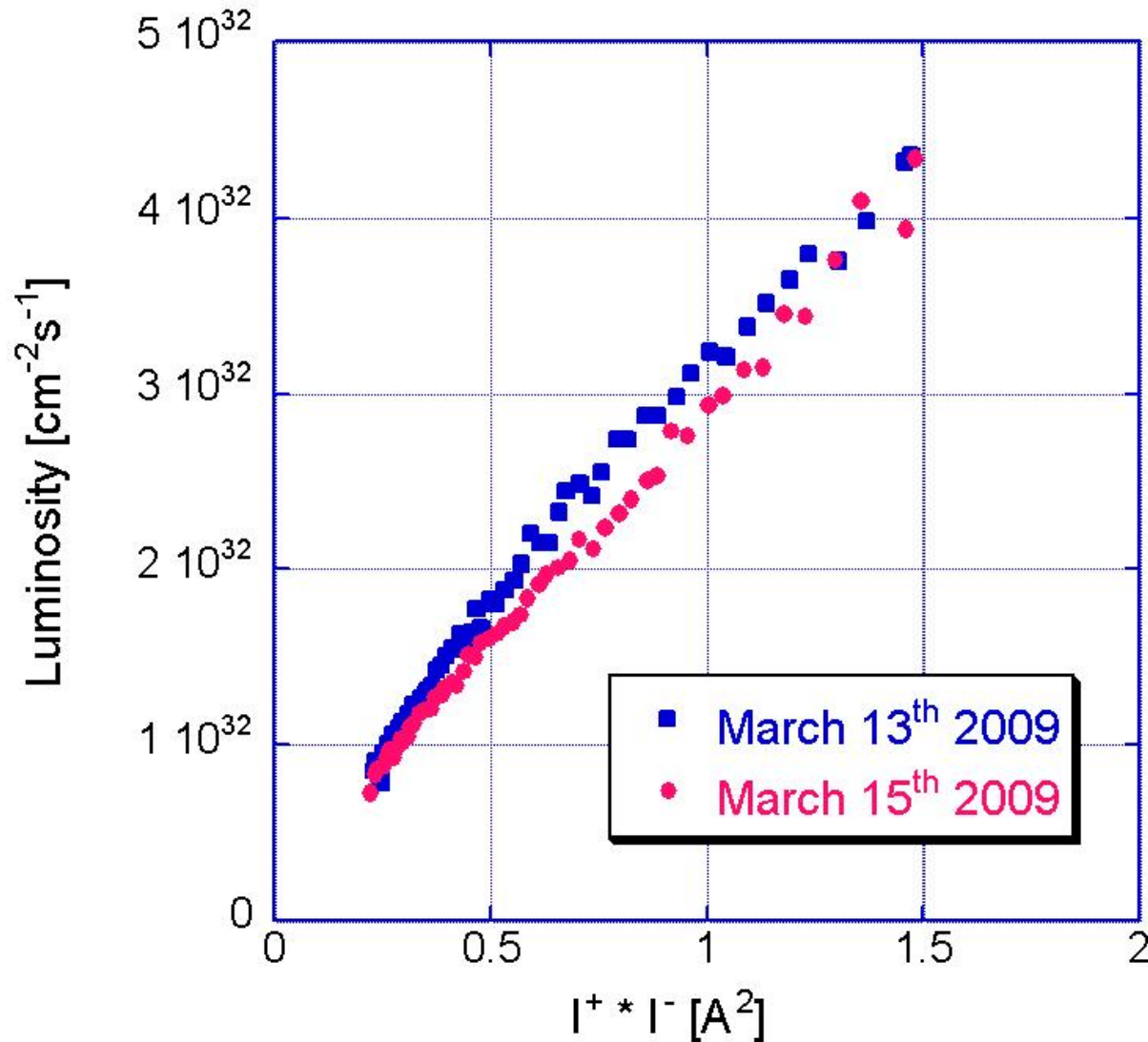


NEW COLLISION SCHEME:  
Large Piwinski angle  
Crab-Waist compensation SXTs

original collision scheme

from P. Raimondi's talk

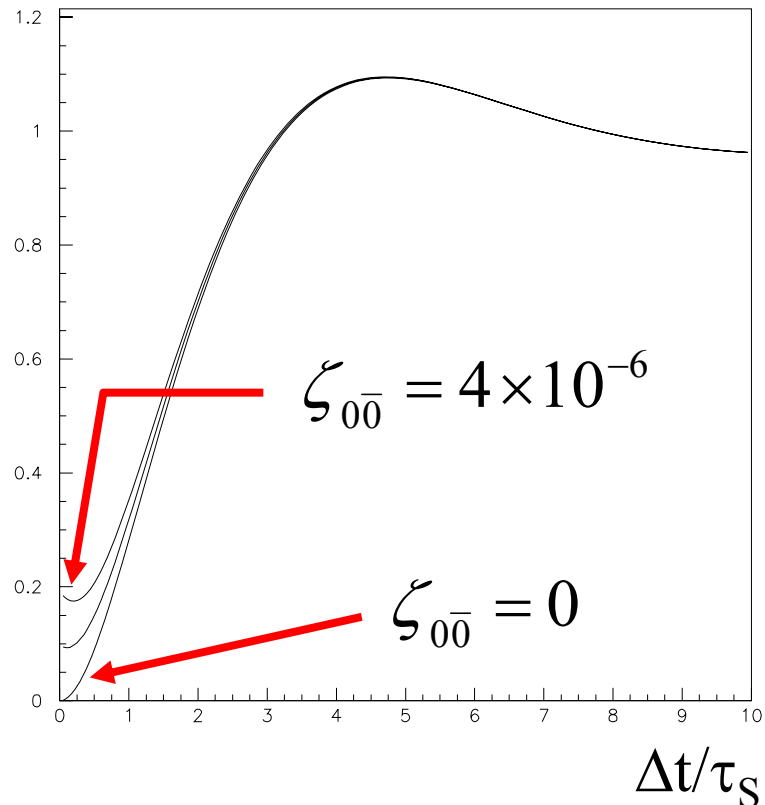
# DAΦNE Luminosity versus colliding currents



# Interferometry at KLOE-2: $\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$

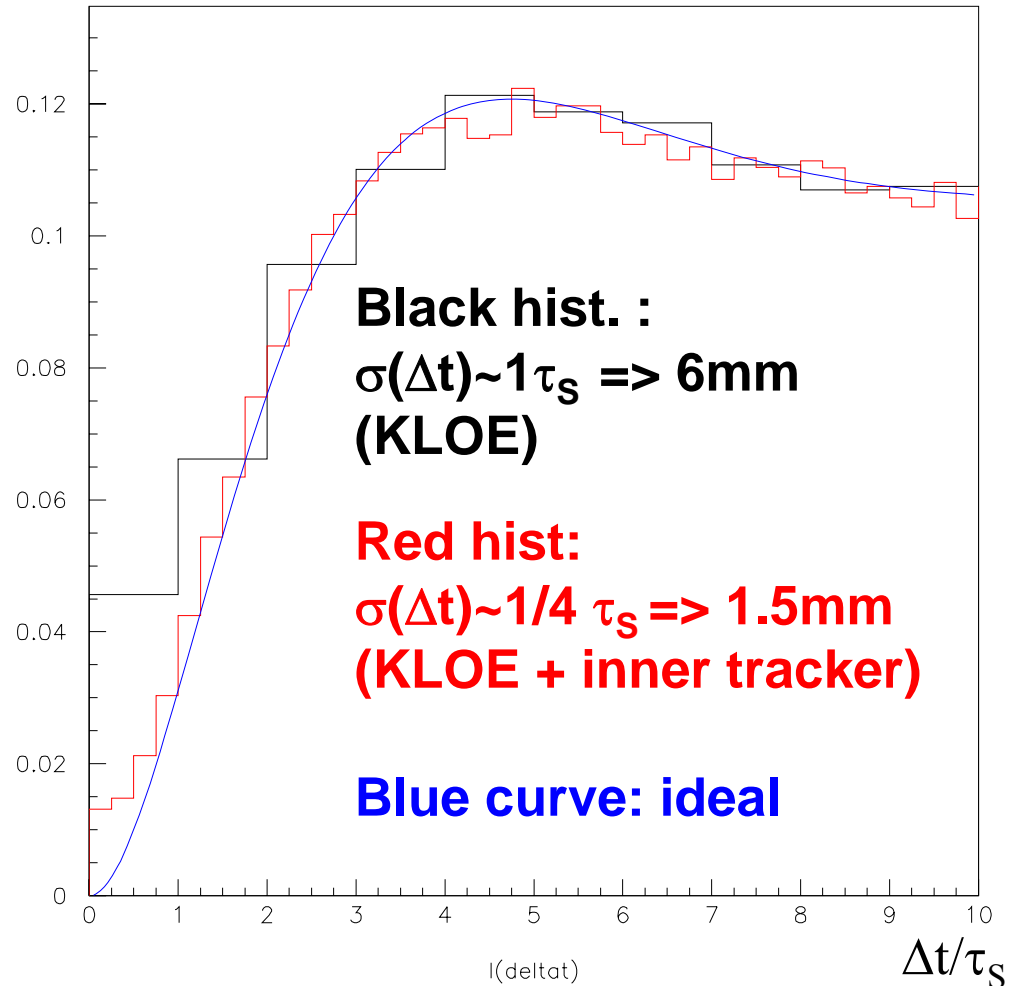
Possible signal of decoherence concentrated at very small  $\Delta t$

$I(\pi^+ \pi^-, \pi^+ \pi^-; \Delta t)$  (a.u.)



Theoretical distribution

$I(\pi^+ \pi^-, \pi^+ \pi^-; \Delta t)$  (a.u.)

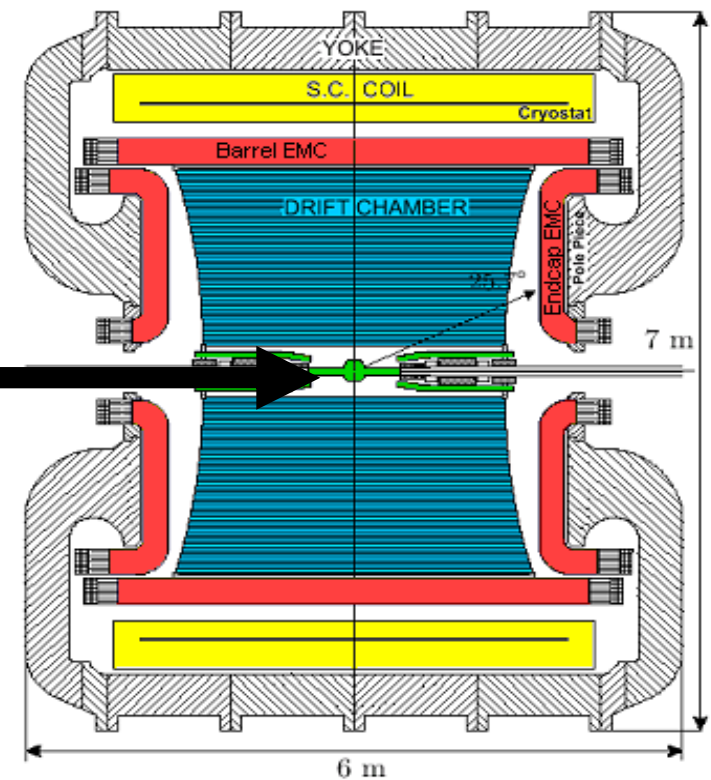
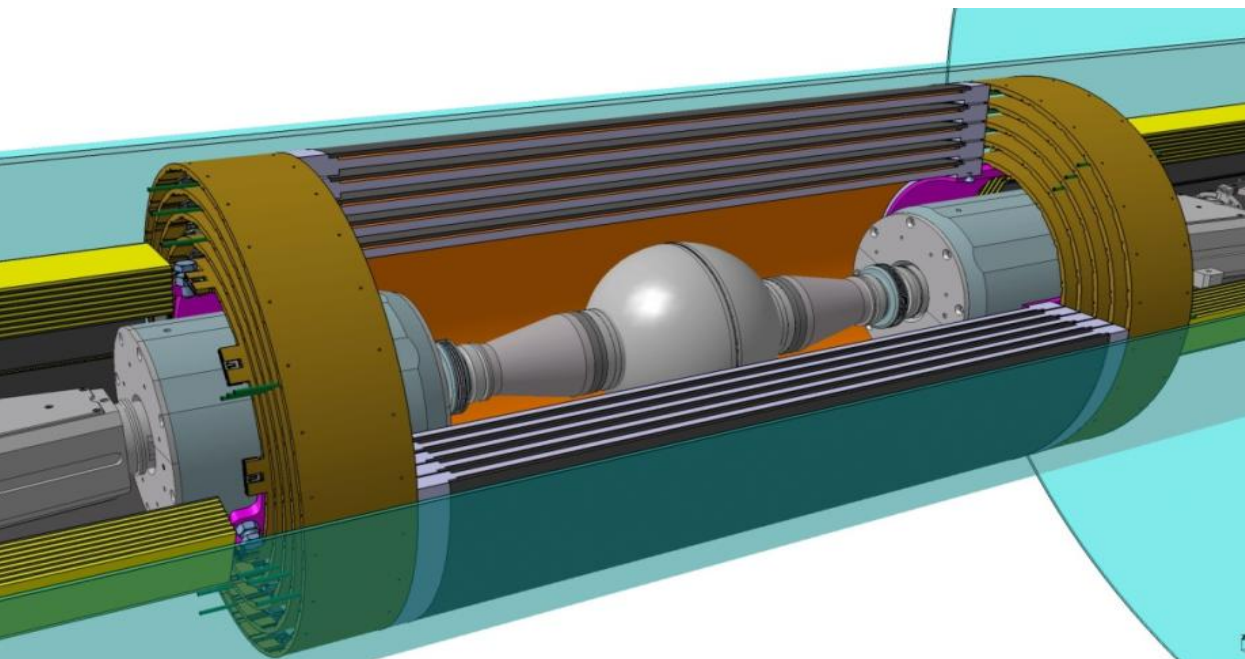


Reconstructed distribution (MC)

# Inner tracker at KLOE

- 5 independent tracking layers for a fine vertex reconstruction of  $K_S$  and  $\eta$
- $200 \mu\text{m}$   $\sigma_{r\phi}$  and  $500 \mu\text{m}$   $\sigma_z$  spatial resolutions with XV readout
- 700 mm active length
- from 150 to 250 mm radii
- 1.8%  $X_0$  total radiation length in the active region

\_Realized with **Cylindrical-GEM** detectors



# Perspectives with KLOE-2 at upgraded DAΦNE

Mode	Test of	Param.	Present best published measurement	KLOE-2 L=50 fb <sup>-1</sup>
$K_S \rightarrow \pi e \nu$	CP, CPT	$A_S$	$(1.5 \pm 11) \times 10^{-3}$	$\pm 1 \times 10^{-3}$
$\pi^+ \pi^- \pi e \nu$	CP, CPT	$A_L$	$(3322 \pm 58 \pm 47) \times 10^{-6}$	$\pm 25 \times 10^{-6}$
$\pi^+ \pi^- \pi^0 \pi^0$	CP	$\text{Re}(\varepsilon'/\varepsilon)$	$(1.65 \pm 0.26) \times 10^{-3}$ (*)	$\pm 0.2 \times 10^{-3}$
$\pi^+ \pi^- \pi^0 \pi^0$	CP, CPT	$\text{Im}(\varepsilon'/\varepsilon)$	$(-1.2 \pm 2.3) \times 10^{-3}$ (*)	$\pm 3 \times 10^{-3}$
$\pi e \nu \pi e \nu$	CPT	$\text{Re}(\delta) + \text{Re}(x_-)$	$\text{Re}(\delta) = (0.25 \pm 0.23) \times 10^{-3}$ (*) $\text{Re}(x_-) = (-4.2 \pm 1.7) \times 10^{-3}$ (*)	$\pm 0.2 \times 10^{-3}$
$\pi e \nu \pi e \nu$	CPT	$\text{Im}(\delta) + \text{Im}(x_+)$	$\text{Im}(\delta) = (-0.6 \pm 1.9) \times 10^{-5}$ (*) $\text{Im}(x_+) = (0.2 \pm 2.2) \times 10^{-3}$ (*)	$\pm 3 \times 10^{-3}$
$\pi^+ \pi^- \pi^+ \pi^-$		$\Delta m$	$(5.288 \pm 0.043) \times 10^9 \text{ s}^{-1}$	$\pm 0.03 \times 10^9 \text{ s}^{-1}$

(\*) = PDG 2008 fit

# Perspectives with KLOE-2 at upgraded DAΦNE

Mode	Test of	Param.	Present best published measurement	KLOE-2 L=50 fb <sup>-1</sup>
$\pi^+\pi^- \quad \pi^+\pi^-$	QM	$\zeta_{00}$	$(1.0 \pm 2.1) \times 10^{-6}$	$\pm 0.1 \times 10^{-6}$
$\pi^+\pi^- \quad \pi^+\pi^-$	QM	$\zeta_{SL}$	$(1.8 \pm 4.1) \times 10^{-2}$	$\pm 0.2 \times 10^{-2}$
$\pi^+\pi^- \quad \pi^+\pi^-$	CPT & QM	$\alpha$	$(-0.5 \pm 2.8) \times 10^{-17} \text{ GeV}$	$\pm 2 \times 10^{-17} \text{ GeV}$
$\pi^+\pi^- \quad \pi^+\pi^-$	CPT & QM	$\beta$	$(2.5 \pm 2.3) \times 10^{-19} \text{ GeV}$	$\pm 0.1 \times 10^{-19} \text{ GeV}$
$\pi^+\pi^- \quad \pi^+\pi^-$	CPT & QM	$\gamma$	$(1.1 \pm 2.5) \times 10^{-21} \text{ GeV}$	$\pm 0.2 \times 10^{-21} \text{ GeV}$ compl. pos. hyp. $\pm 0.1 \times 10^{-21} \text{ GeV}$
$\pi^+\pi^- \quad \pi^+\pi^-$	CPT & EPR corr.	Re( $\omega$ )	$(1.1 \pm 7.0) \times 10^{-4}$	$\pm 2 \times 10^{-5}$
$\pi^+\pi^- \quad \pi^+\pi^-$	CPT & EPR corr.	Im( $\omega$ )	$(3.4 \pm 4.9) \times 10^{-4}$	$\pm 2 \times 10^{-5}$
$K_{S,L} \rightarrow \pi e \nu$	CPT & Lorentz	$\Delta a_0$	$[(0.4 \pm 1.8) \times 10^{-17} \text{ GeV}]$	$\pm 2 \times 10^{-18} \text{ GeV}$
$\pi^+\pi^- \quad \pi^+\pi^-$	CPT & Lorentz	$\Delta a_Z$	$[(2.4 \pm 9.7) \times 10^{-18} \text{ GeV}]$	$\pm 7 \times 10^{-19} \text{ GeV}$
$\pi^+\pi^- \quad \pi e \nu$	CPT & Lorentz	$\Delta a_{X,Y}$	$[<10^{-21} \text{ GeV}]$	$\pm 4 \times 10^{-19} \text{ GeV}$

[...] = preliminary

# Conclusions

---

---

- The neutral kaon system is an excellent laboratory for the study of CPT symmetry and the basic principles of Quantum Mechanics;
- Several parameters related to possible
  - CPT violation (within QM)
  - CPT violation and decoherence
  - CPT violation and Lorentz symmetry breakinghave been recently measured at KLOE, in some cases with a precision reaching the interesting Planck's scale region;
- All results are consistent with no CPT violation
- The analysis of the full KLOE data sample is completed (apart the analysis of CPTV and LV);
- KLOE and DAΦNE are going to be upgraded
- KLOE (KLOE-2) will restart taking data at the end of this year
- Neutral kaon interferometry, CPT symmetry and QM tests are one of the main issues of the KLOE-2 physics program
- Other interesting QM tests possible, e.g. quantum eraser.