

G-APD Photon detection efficiency

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- ✦ Motivation
 - ✦ Measurements Setup
 - ✦ Samples
 - ✦ Fitting Procedures
 - ✦ Results
 - ✦ Conclusions
- ✦ **The results presented are preliminary.**

Motivation

★ Multi-pixel Geiger-mode photodiodes (G-APDs) used in calorimetric detectors. The crucial point is:

★ The Photon Detection Efficiency

Every detector can only convert a certain percentage of incident photons to signals. This overall efficiency is dependent on factors such as the surface reflection, fill factor, quantum efficiency and amplification probability. It is depending from λ .

$$\text{PDE} = \text{QE} \times \epsilon_{\text{geom}} \times \epsilon_{\text{Geiger}}$$

QE is the quantum efficiency of G-APD function of the wavelength

ϵ_{geom} is geometrical factor

ϵ_{Geiger} is the probability to trigger a Geiger

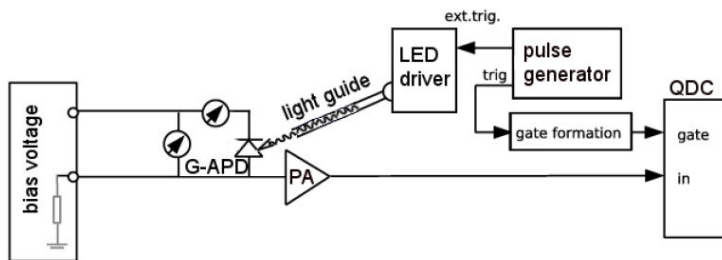
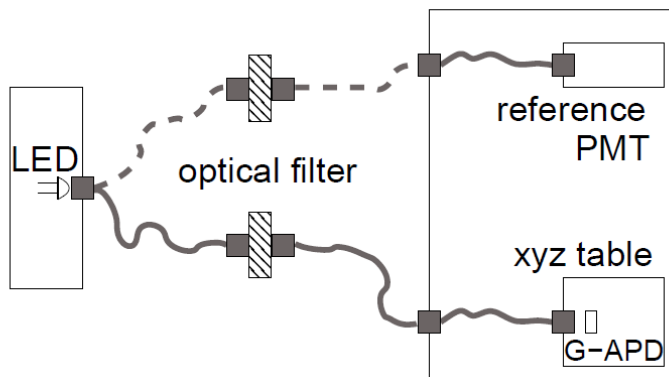
★ Comparison in same experimental conditions of various samples from different manufactures

Terms

- ★ **Fill factor.** The percentage of detector's surface area which is sensitive to photons
- ★ **Crosstalk.** With multiple avalanche regions on a single device one avalanche process may create photons that trigger another cell. The result is a pulse with doubled amplitude
- ★ **After-pulsing.** When the quenching does not completely drain all the charges in the sensitive area the cell will fire again a short time after the original pulse. This is caused by so-called charge-traps in the avalanche region, which capture single charges and release them again after a while.

Measurement Set up

Thermalized box
($\Delta T \sim 0.1^\circ\text{C}$)



★ Reference PMT

HAMAMTSU H5783P calibrated efficiency for
 $\lambda = 380\text{-}650\text{nm}$

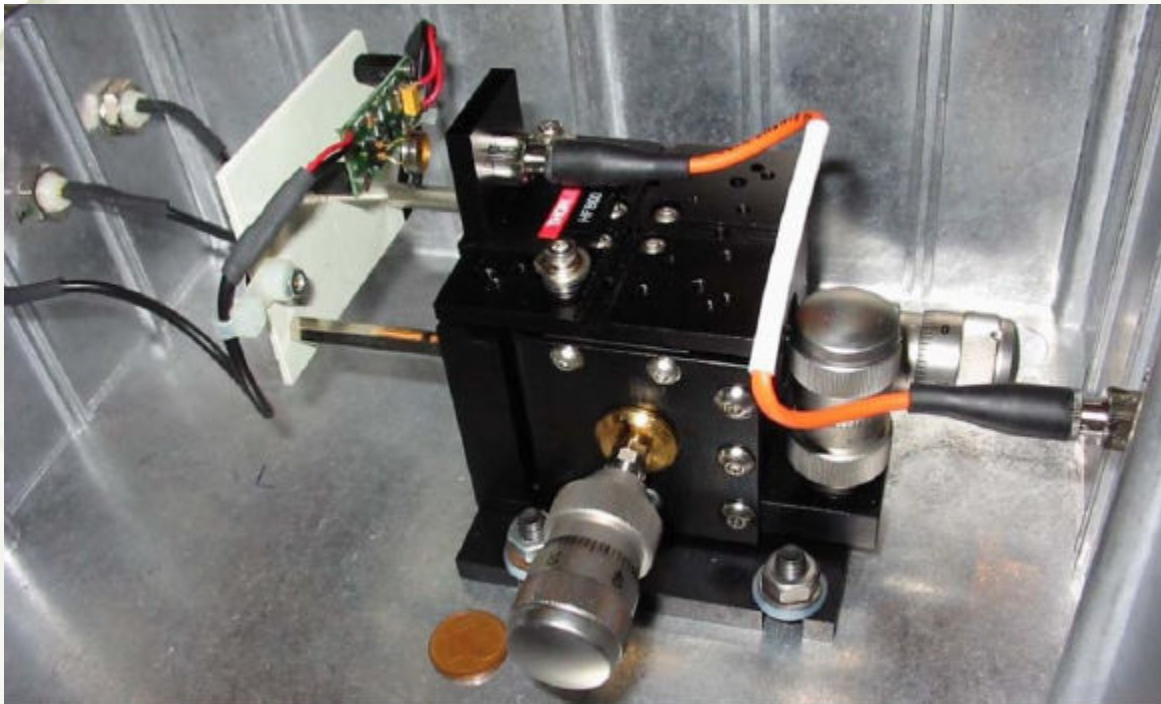
★ Filters FWHM $\pm 3\text{nm}$.

★ Optical Fibers: 50 μm core

★ Optical Connectors: superFC/PC

★ To estimate and correct for different optic coupling and **reconnection systematic error** other measurements with crossed fibers are also done

Measurement Setup

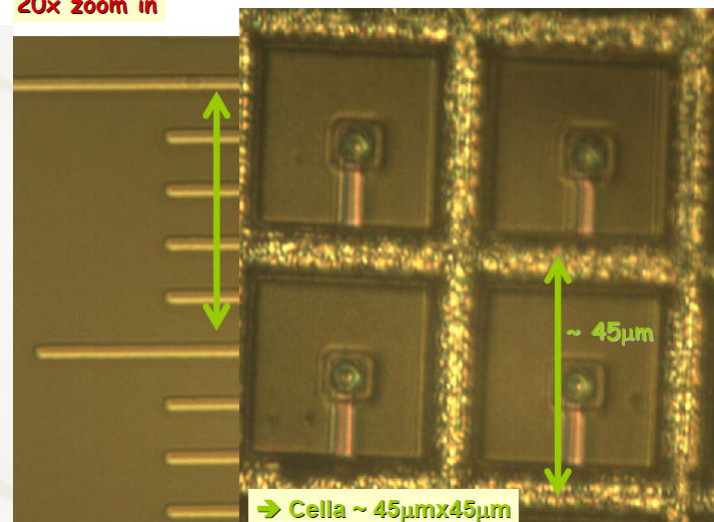


Samples

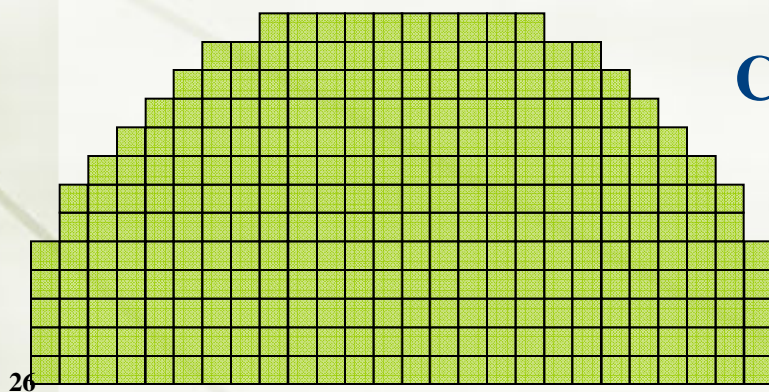
TABLE II. – [1] Sample kindly proved from Prof.M.Danilov,[2]Sentistive area octaganal shape, [3]Sample kindly provided from Dott.C. Piemonte(Fondazione Bruno Keller)

Sample	Type	Photosensitive area [mm ²]	Number of pixel	Pixel pitch [μm]
HAMAMATSU	S10362-11-025U	1x1	1600	25x25
CPTA [1]	143	1.028[2]	556	43x43
IRST[3]	2007 prod	1x1	400	50x50

20x zoom in



CPTA



Eugeny Tarkosky

Simonetta Gentile, LCWS10, 26-30 March 2010, Beijing, China.



$\lambda=450\text{nm}$

pedestal

signal

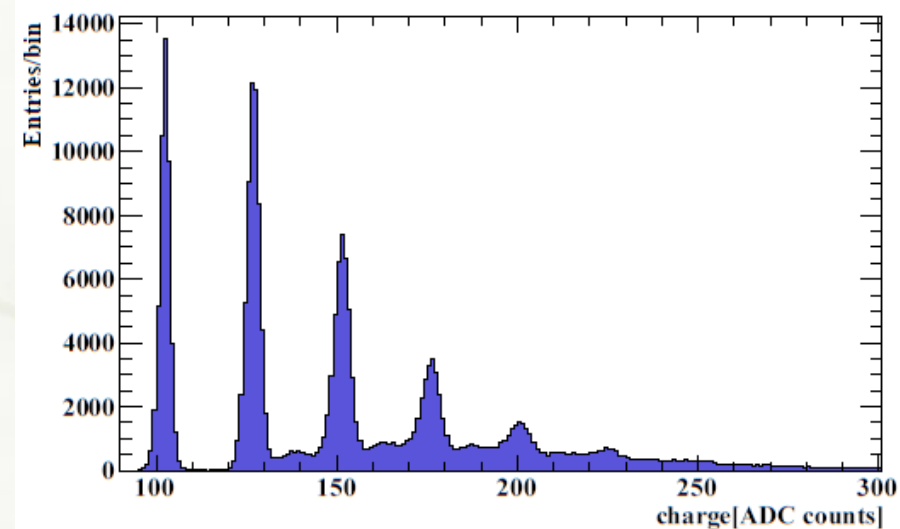
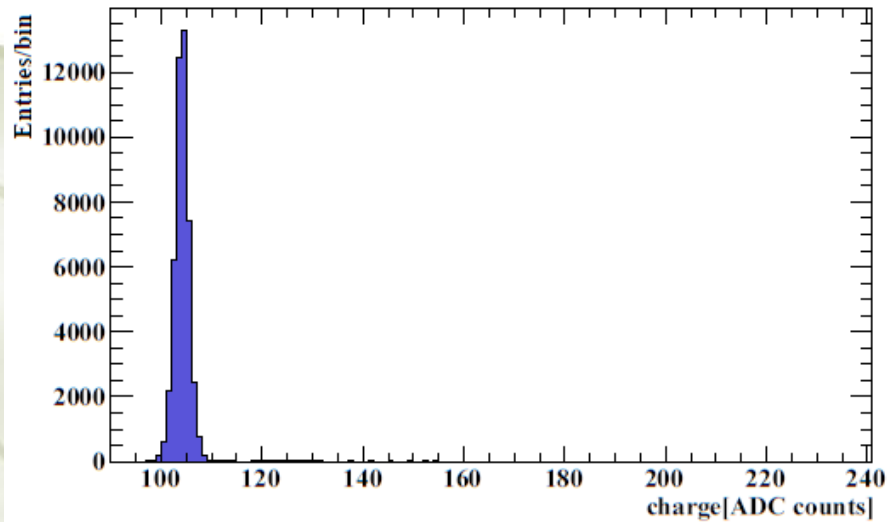


TABLE I. – Efficiency of reference detector PMT-based photosensor H5783P. Values provided on the used device as provided from the manufacture Hamamatsu[1]. Efficiency values used[2].

λ (nm)	$\epsilon_{\text{peak}}^{\text{ref}}$ [1] [%]	FWHM _{filter} (nm)	FWHM _{source} (nm)	$\epsilon_{\text{evaluated}}^{\text{ref}}$ [%]
380	23.46		± 8	22.98 -0.21 -0.05
400	22.69		± 13	22.75 $+0.46$ -0.10
450	20.33	± 3		20.33 $+0.27$ -0.28
500	15.45	± 3		15.45 $+0.32$ -0.68
565			± 30	5.30 $+2.37$ -2.63
600	2.30	± 3		2.30 $+0.19$ -0.19
650	0.28	± 3		0.28 $+0.05$ -0.04

Fit Procedure: Reference



Direct measurement, no amplification

wavelength 450nm

$$N(x) = N \times \sum_n (\text{Gauss}(x, \mu_n, \sigma_n) \times \text{Poisson}(n, \lambda))$$

$$\text{const} \times e^{-\lambda} \sum_n (\lambda^n / n! \cdot 1/\sigma_n \exp\{-(x-\mu_n)^2 / (2\sigma_n)^2\})$$

$$\mu_n = \mu_0 + n \times g$$

x is the charge in ADC counts.

n is the number of photons detected

λ is the mean number of the detected photons

gain g in units of ADC counts

$$\sigma_n^2 = \sigma_0^2 + n \times \sigma_1^2$$

n detected photons

electronic noise (σ_0)

signal fluctuation (σ_1)

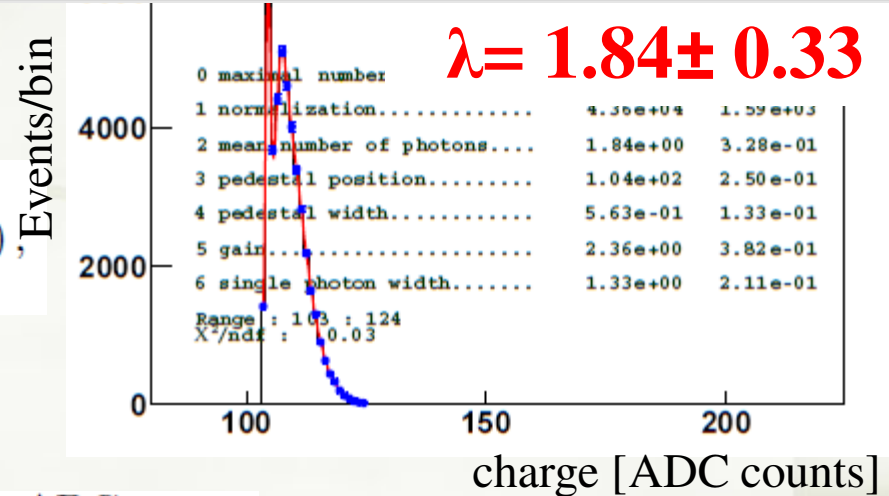
Single photon width

Due to ADC resolution



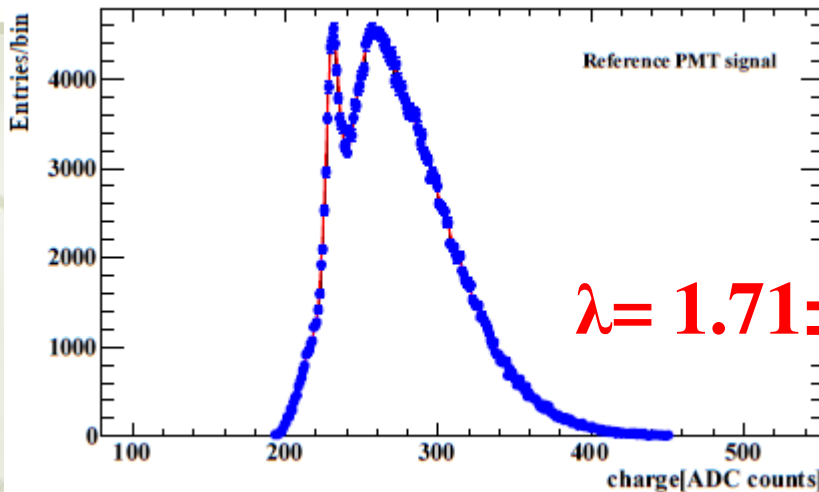
signal amplification

Simonetta Gentile, LCWS10, 26-30 March 2010, Beijing, China.

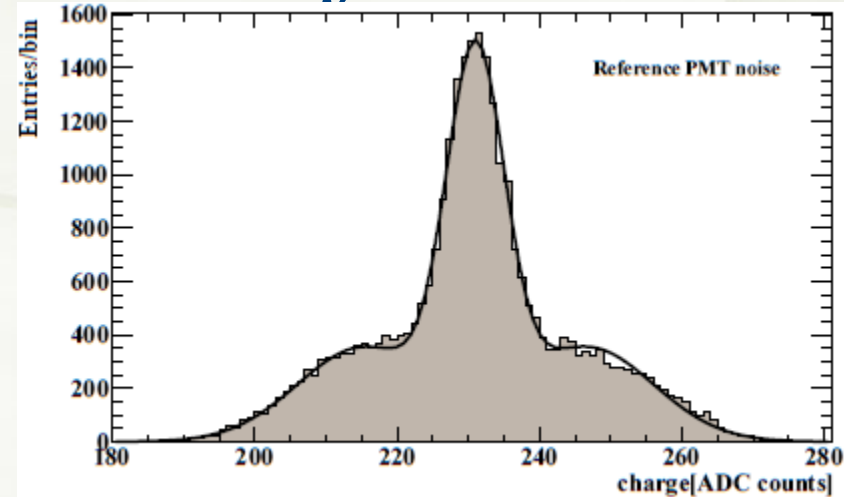


Fit Procedure : Reference

★ Reference PMT



$$\lambda = 1.71 \pm 0.02$$



$$\text{Noise}(x) = G_1(x-\delta/2) + G_0(x) + G_1(x+\delta/2)$$

ORTEC NIM amplifier

$$N(x) = N \times \text{Noise} \times \text{Poisson}(n, \lambda)$$

wavelength 450nm

$$\text{PMT } \varepsilon^{\text{ref}}_{\text{evaluated}} = 20.33^{+0.27}_{-0.28} \%$$

Fit Procedure: Silicon PhotoMultipliers

★ Ideal case

$$N(x) = N \times \sum_n (\text{Gauss}(x, \mu_n, \sigma_n) \times \text{Poisson}(n, \lambda)),$$

★ Real situation

★ Termogeneration

★ After-Pulse

★ Cross-talk

G-APD reponse:

$$A = G \times N_\gamma \times \text{PDE} \times (1 + \varepsilon) \times (1 + AP)$$

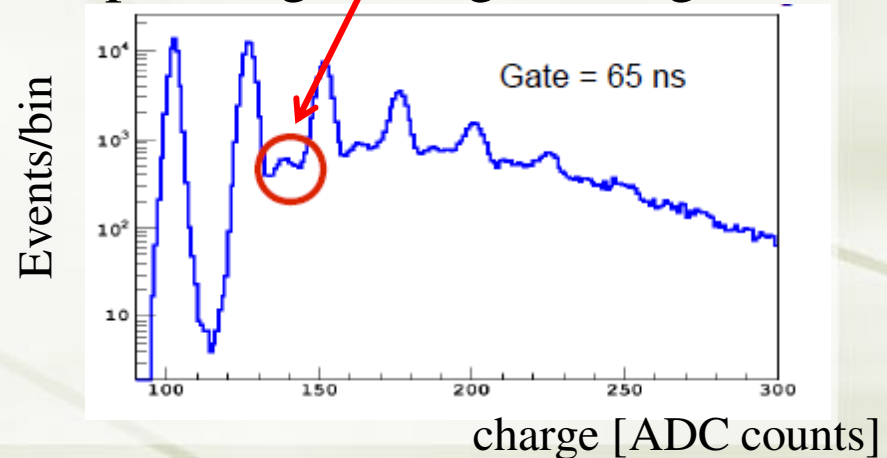
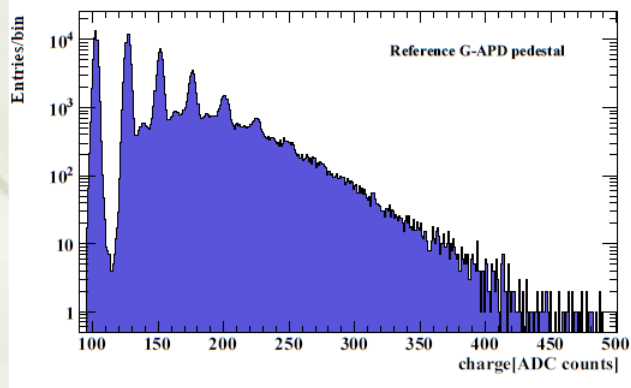
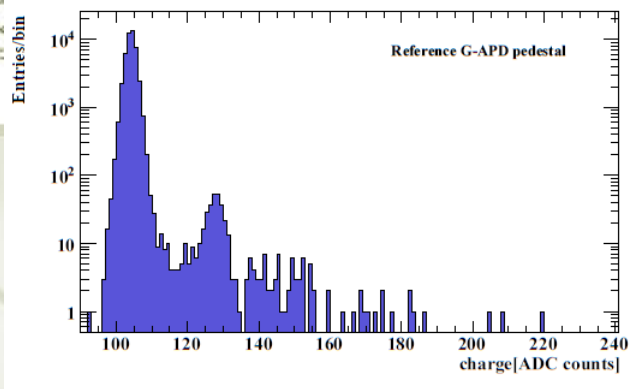
gain

Fit Procedure: Silicon PhotoMultipliers

◆ Hamamatsu MPPC:
S10362-11-025U $G \sim 3.4 \cdot 10^5$

◆ **AfterPulse**

depending from gate length



After Pulses

Residual distribution after a subtraction of best-fitted ideal gaussians from the signal spectrum

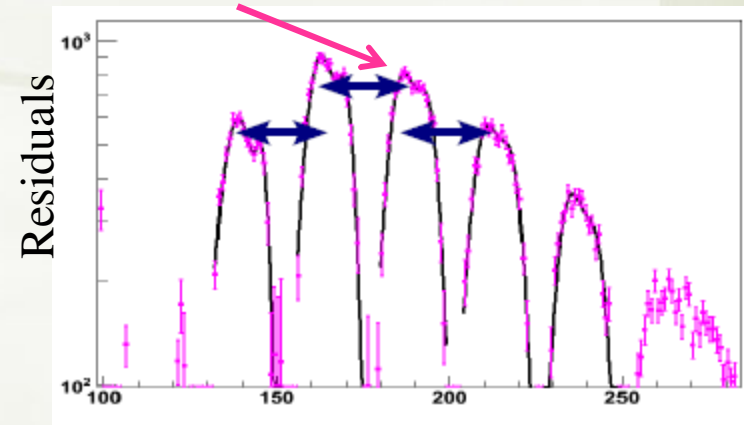
$$P_i^{\text{noAP}} = P_i^0 \times (1 - P_{\text{AP}})^i$$

P_i^0 is probability to get initially i cells fired

P_{AP} is a probability to get an AP

$$P_i^{\text{AP}} = 1 - P_i^{\text{noAP}} = P_i^0 \times (1 - (1 - P_{\text{AP}})^i)$$

$$P_i^{\text{AP}} = P_i^{\text{AP1}} + P_i^{\text{AP2}} = P_i^0 \times [1 - (1 - P_{\text{AP}})] \times [(1 - P_{\text{AP}})^j] + P_i^0 \times [1 - (1 - P_{\text{AP}})] \times [(1 - P_{\text{AP}})^j], j \geq 1$$



Double gaussian approximation for the after –pulse contribution
 $\delta_{1,2}$ distance from gaussian simulating AP from main peak

$$P(x) = P_i^{\text{noAP}} \times G(\mu_i, \sigma_i) + P_i^{\text{AP1}} \times G(\mu_i + \delta_1, \sigma_1) + P_i^{\text{AP2}} \times G(\mu_i + \delta_2, \sigma_2)$$

After Pulse fit

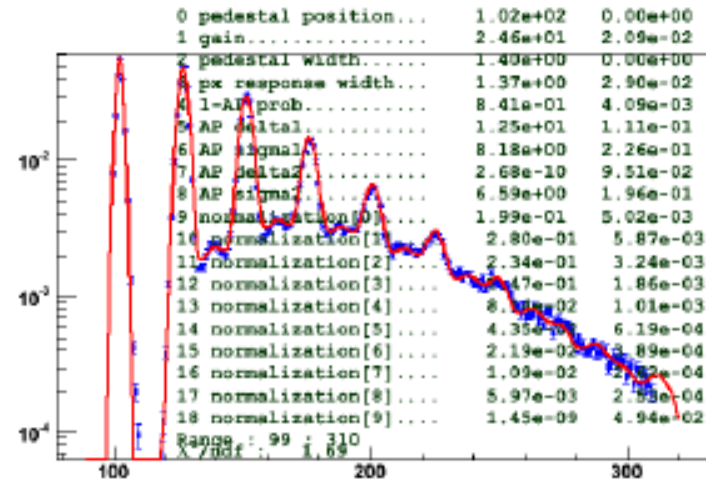
Fit Procedure yields:

✦ Probability to get i cells fired.

✦ After Pulse probability:

AP ~ 15% (65 ns gate)

Events/bin



charge [ADC counts]

Cross talk

★ In ideal case without cross-talk the value of P_i^0 are distributed according Poisson statistics

Peak 0 - from P(0)

Peak 1 - from P(1) without xtalk:

X

$P(1)x(1-\epsilon)$

Peak 2 - from P(2) without xtalk and P(1) with 1xtalk

X

X→X

X

$P(2)x(1-\epsilon)^2+P(1)x\epsilon x(1-\epsilon)$

Peak 3 – from P(3),

P(2)

and

P(1)

X

X→X

X

X→X→X

X

X

X→X

X

$P(3)x(1-\epsilon)^3+2xP(2)x(1-\epsilon)^2x\epsilon+P(1)x\epsilon^2x(1-\epsilon)$

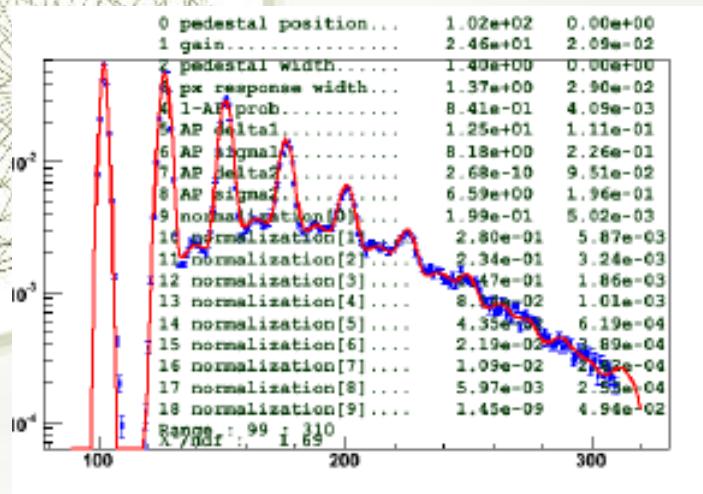
$$\sum_{j=0}^i P_j^0 (1-\epsilon)^j \epsilon^{i-j} B(i-1, j-1),$$

$B(i-1, j-1)$

Binomial coeff.

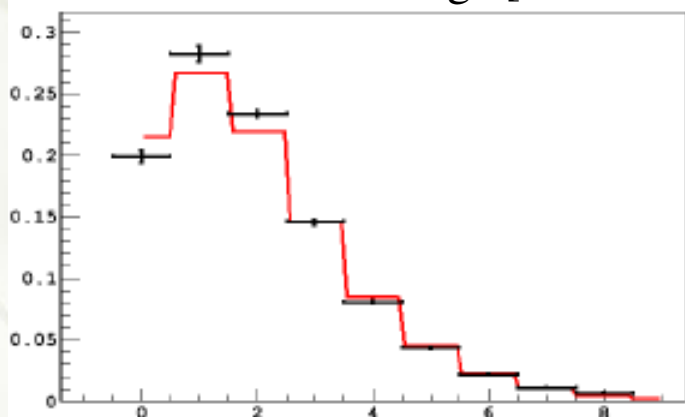
Cross talk fit

Events/bin



charge [ADC counts]

P



Peak number

$$\star N_{\gamma} = 1.55 \pm 0.02$$

$$\star X_{\text{talk}} = 0.20 \pm 0.01$$

$$\star 1\text{-AP} = 0.84 \pm 0.01$$

Probability to observe i fired cells obtained from signal fit

Exercise:

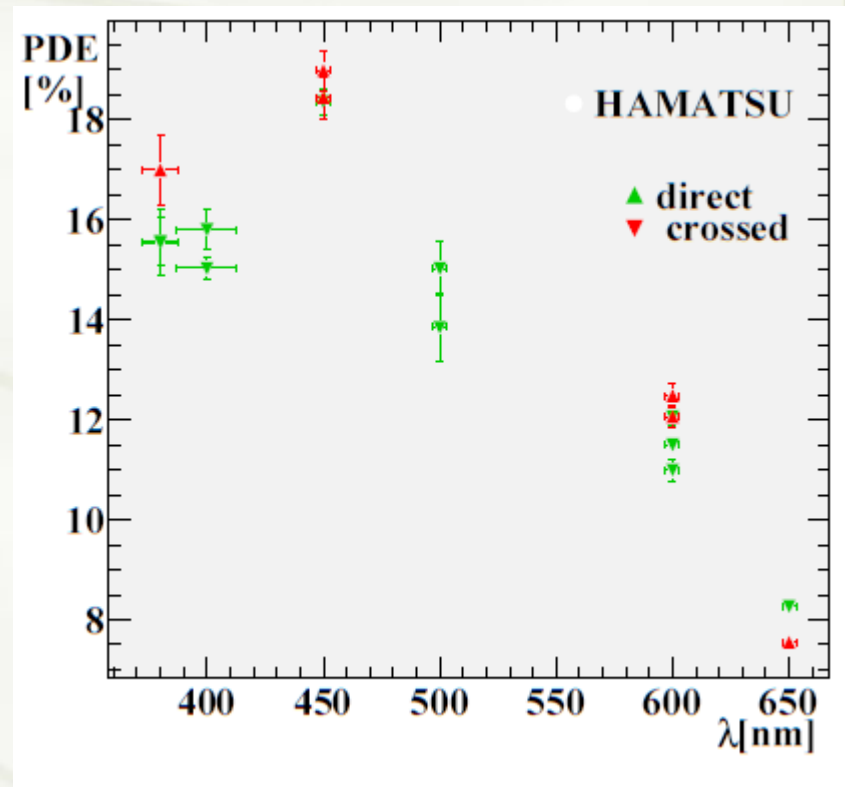
$$N_{\gamma}^{\text{PMT}} \approx 1.71 / 0.2033 = 8.4$$

$$\text{PDE} = N_{\gamma} / N_{\gamma}^{\text{PMT}} \approx 18\%$$

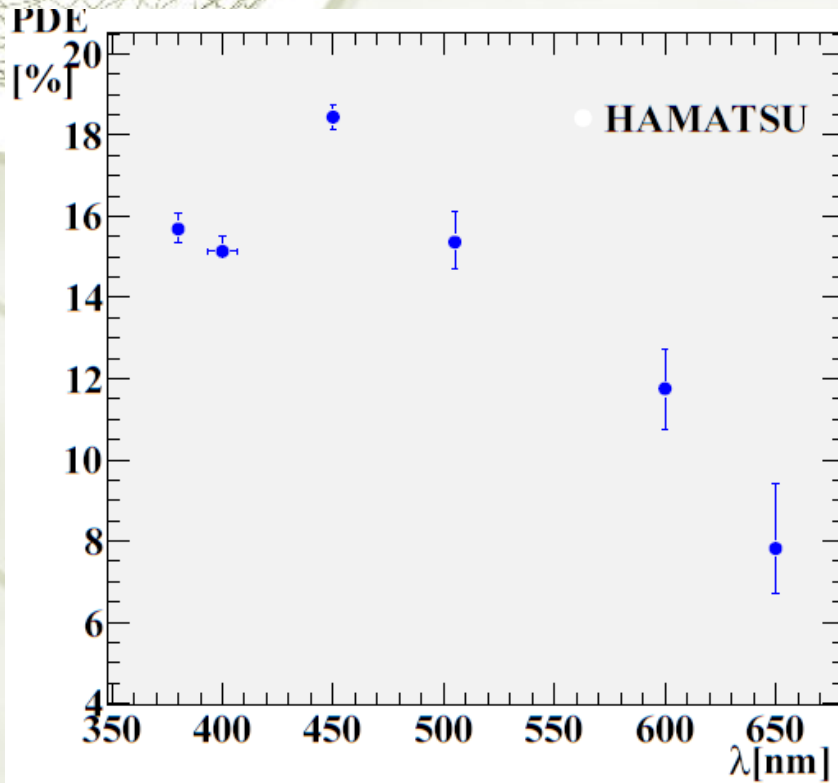
Optical contact

★ A source of systematics is the optical contact

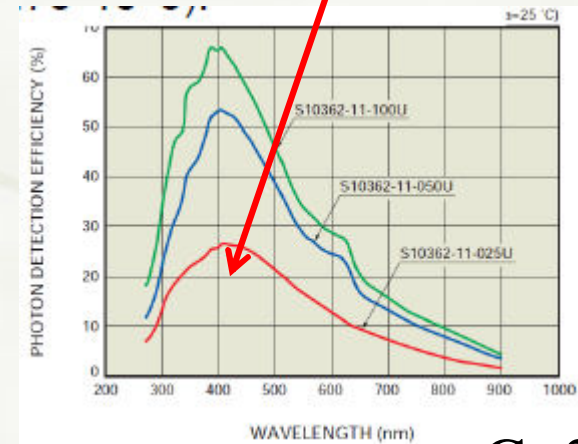
The absolute error is $\sim 1\%$



Photon detection results



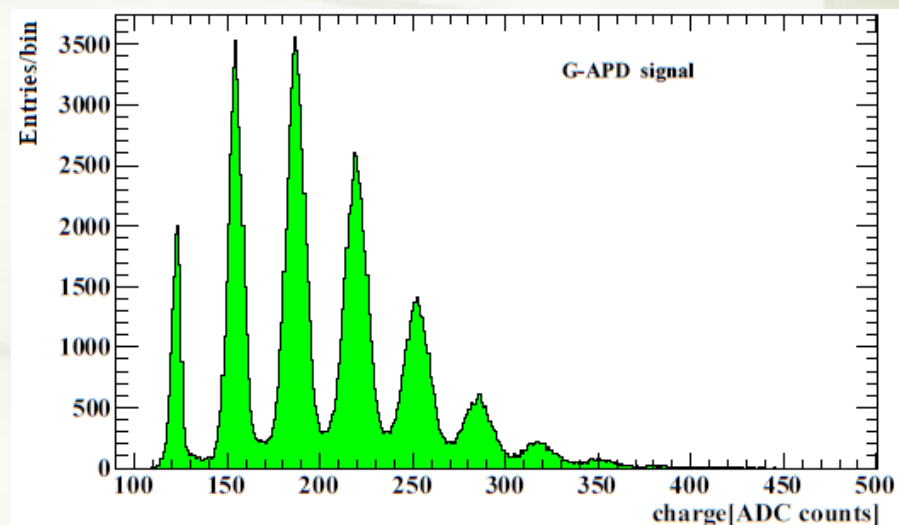
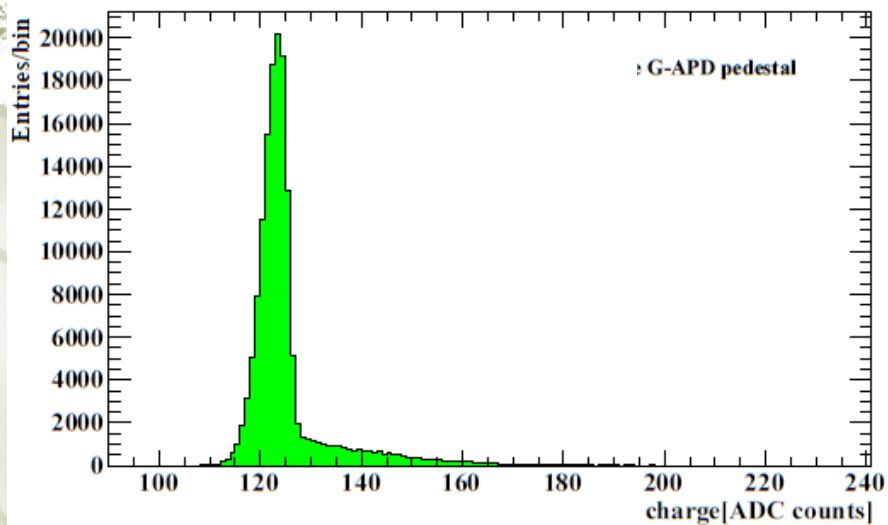
S10362-11-025U MPPC
Hamamatsu



$G \sim 2.75 \cdot 10^5$
Including AP and xtalk

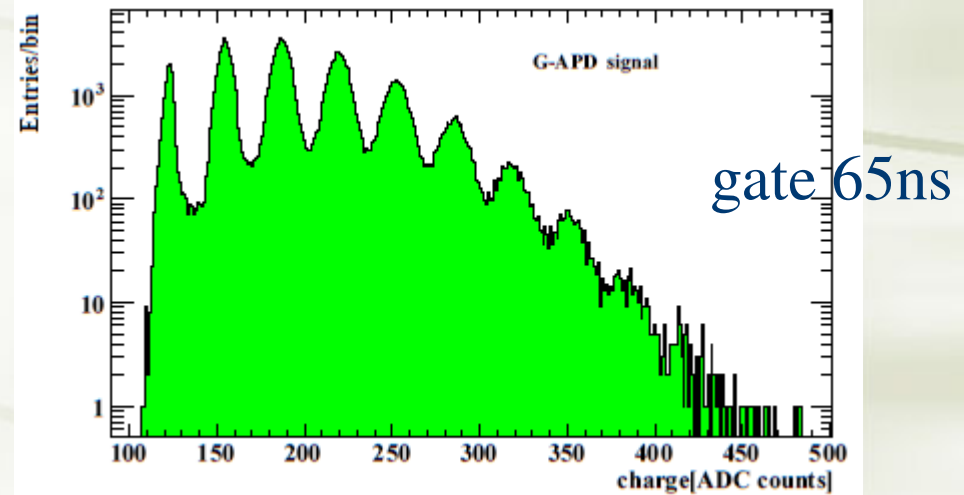
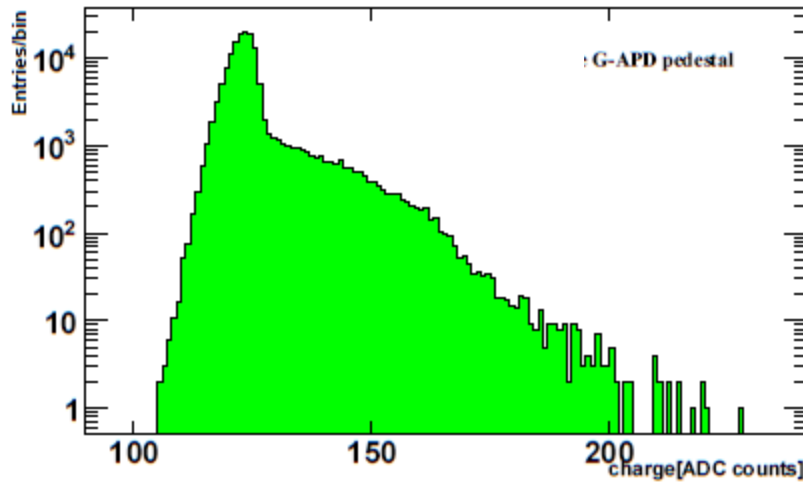
$\lambda=600\text{nm}$

CPTA



signal

$G \sim 4.7 \cdot 10^5$

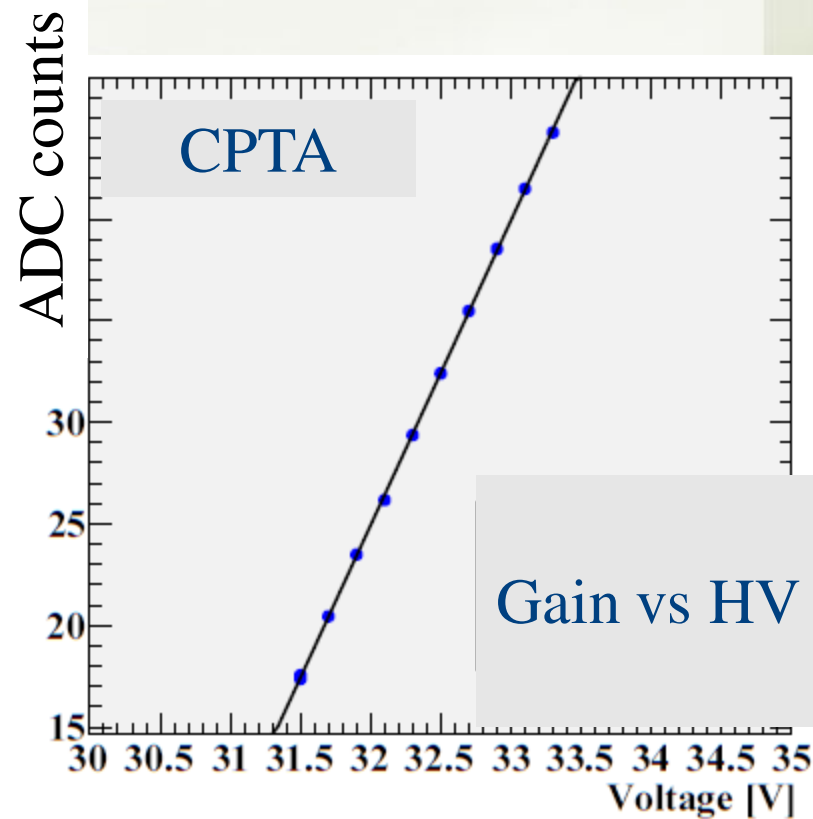
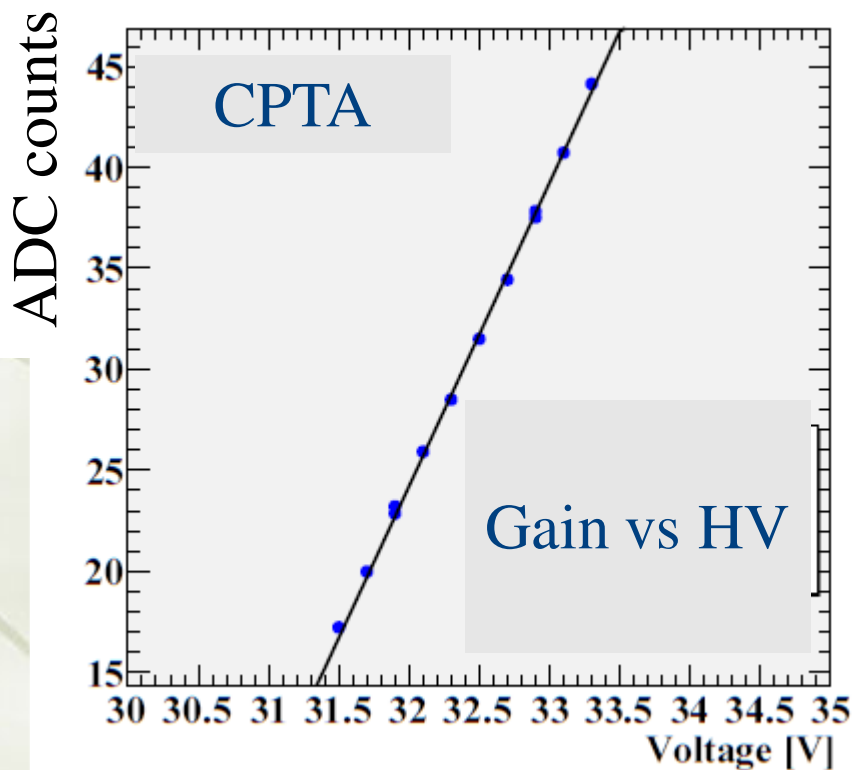


$$N(x) = N \times \sum_n (\text{Gauss}(x, \mu_n, \sigma_n) \times \text{Poisson}(n, \lambda)) \text{const} \times e^{-\lambda} \sum_n (\lambda^n / n! \cdot 1/\sigma_n \exp\{- (x - \mu_n)^2 / (2\sigma_n^2)\})$$

Real situation:

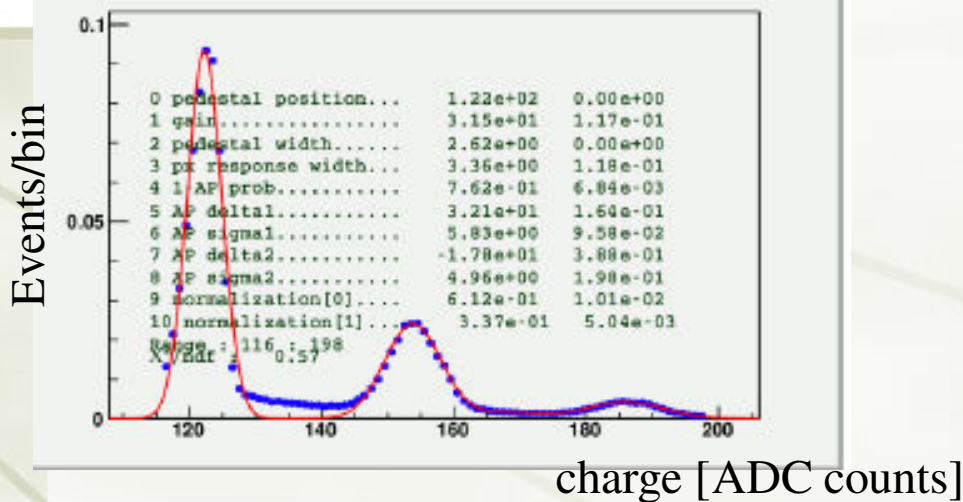
- ✦ Termogeneration $\rightarrow \sim 30\%$ our timing
- ✦ After-pulsing \rightarrow minor compared to Termogener.
- ✦ Cross-talk \rightarrow much lower than Hamamatsu

Gain vs HV



PDE CPTA

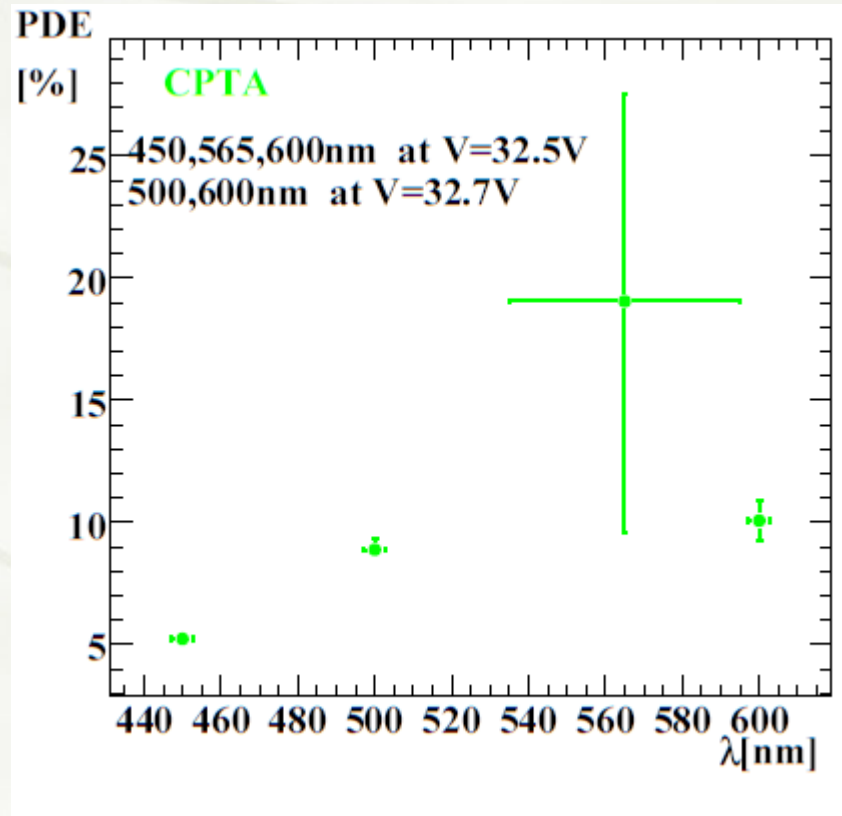
CPTA



Preliminary results

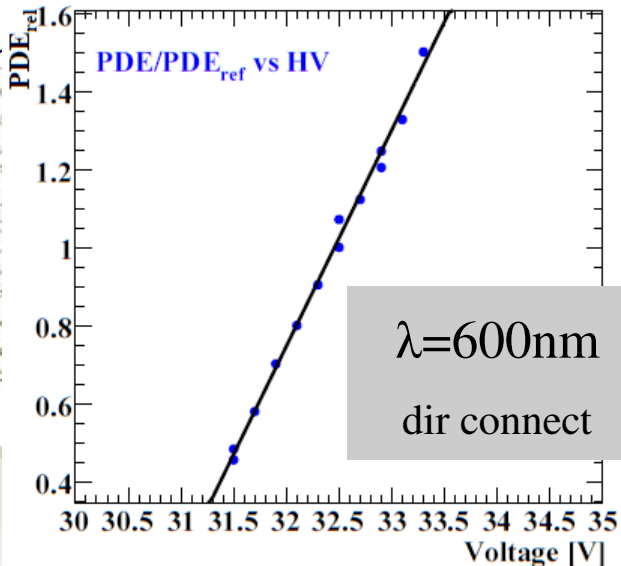
- ◆ Ignoring Thermogeneration contribution.
- ◆ AP considered as a correction term taking in account AP and TG
- ◆ **Low crosstalk value**
- ◆ No sensitivity to crosstalk in the fit

PDE CPTA



- Similar results extrapolating all point at 32.5V

$m=0.55\pm 0.01$



PDE vs HV



As test:

at **32.7V**

PDE extrap $\sim 10.14 \pm 0.08 \%$

PDE meas $= 10.07 \pm 0.09 \%$

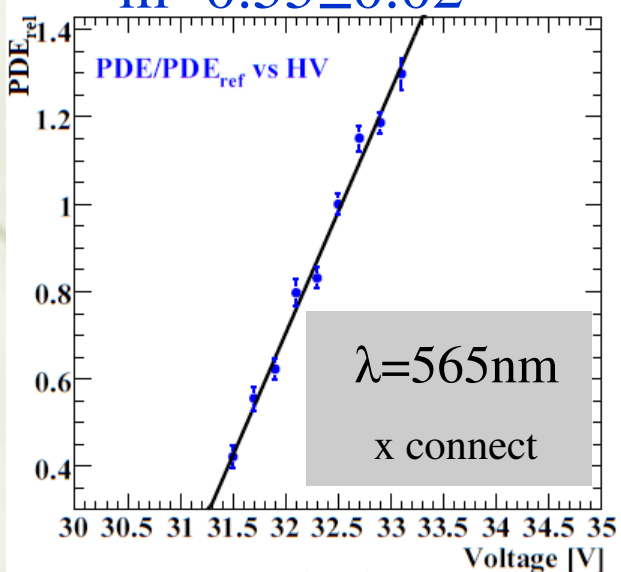
Not included
error on
wavelength

PDE extrap [%]

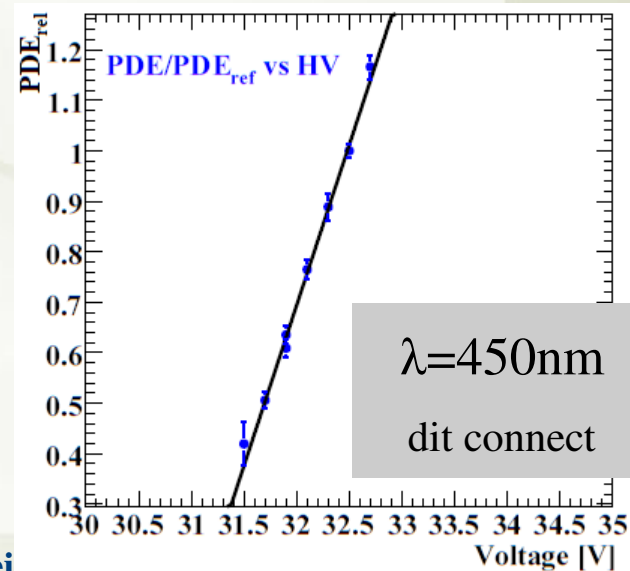
32.7V , 32.5 V

$m=0.64\pm 0.02$

$m=0.55\pm 0.02$

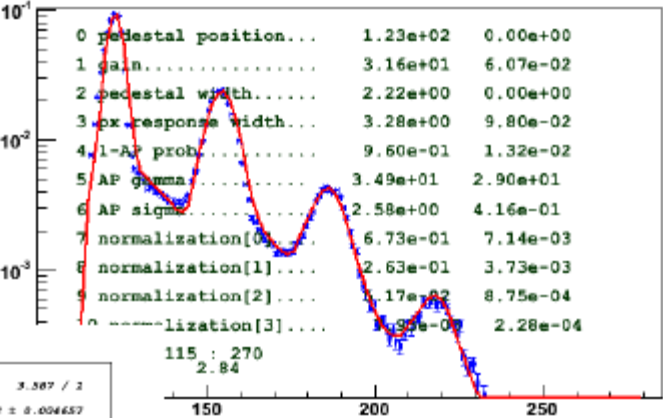
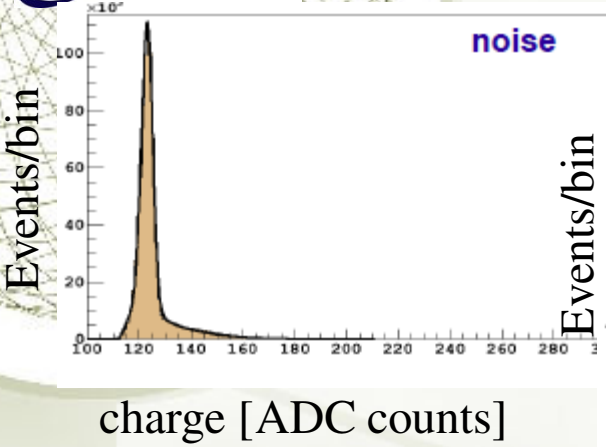


- **565nm**
- 21.15 ± 0.23**
- 19.05 ± 0.22**
- **450nm**
- 5.90 ± 0.05**
- 5.23 ± 0.05**

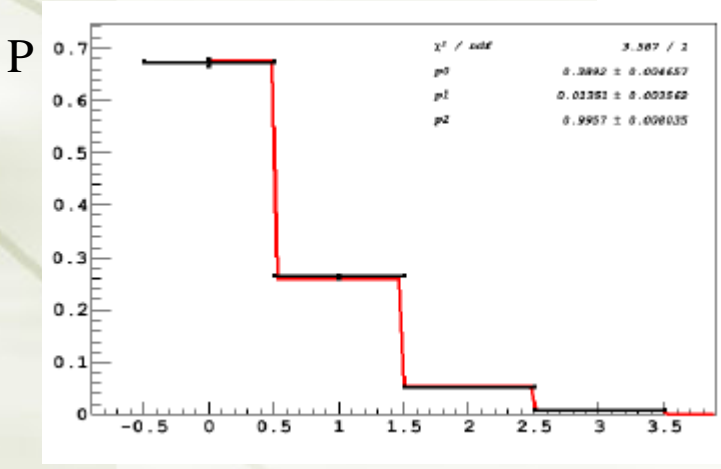


Only statistical error

CPTA Crosstalk



Average x-talk
~ 1.7%



charge [ADC counts]

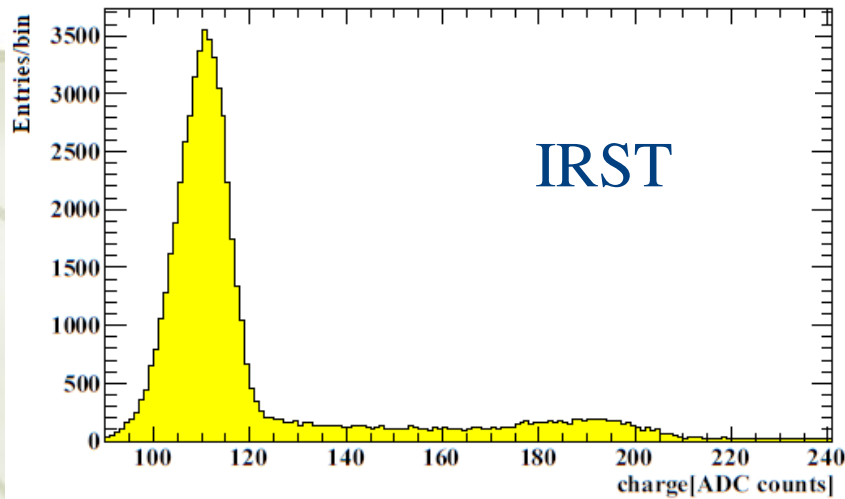
◆ Thermogeneration taken in account

◆ Asymmetric shape AP
 $(dP/dx \sim (G-x)^\gamma)$

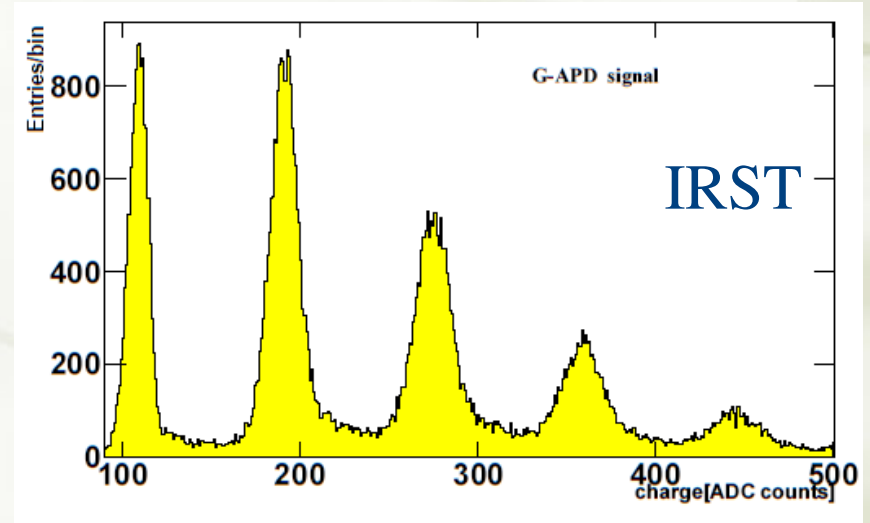
$\gamma = 1 / (\alpha \tau - 1)$
 τ trap life time
 α recovery time

$\lambda=600\text{nm}$

Pedestal



Signal



Different light intensity of CPTA sample
Peculiar specimen

Conclusion

- ★ Estimation of PDE based on LED response measurements on Hamatsu and CPTA G-APD.
- ★ Fit procedure including individual AP and cross talk
- ★ Systematic error:
 - ★ **Different fibers** for reference and test detector. Negligible
 - ★ **Reconnection of fibers.** Weighted mean over several measurements after reconnection
 - ★ **Fit procedure:** weighted mean over several measurements for different light intensities
- ★ Possible improvement of fit procedure