

NEUTRINO PHYSICS

Oscillations and Majorana neutrino

31 may 2011

“*Neutrino Physics*”: <http://www.roma1.infn.it/people/rahatlou/FNS3/>

DIPARTIMENTO DI FISICA



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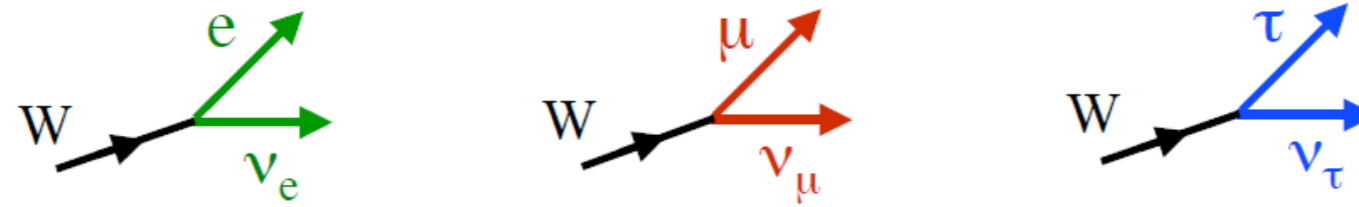
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Corso di Fisica Nucleare e Subnucleare II, A.A.2010-2011

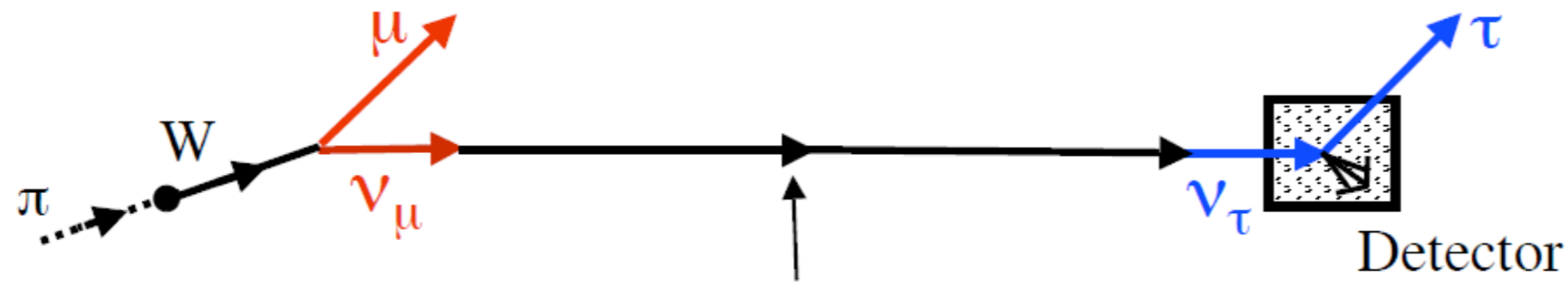
http://www.roma1.infn.it/people/luci/corso_fnsII.html

NEUTRINO OSCILLATION

- Neutrino flavour:



- Experimental observation:



Neutrino flavour change

- Implications:
 - Leptons mix: **lepton flavour not conserved**
 - Neutrinos have non zero mass: **there must be some ν mass spectrum**
- **Mixing angles? Neutrino masses? Dirac or Majorana ?**

NEUTRINOS IN THE STANDARD MODEL

- Fermions described by a Dirac field Ψ
- Standard Model(MS): chiral theory $SU(2)_L \times U(1)_Y$
 - Chirality projector $P_L^{(R)} = (1 \pm \gamma_5)/2$, $P_L^{(R)}\Psi = \Psi_L^{(R)}$
 - Ψ_L and Ψ_R have different properties under $SU(2)_L$
 - ▶ Ψ_R $SU(2)$ singlet \Rightarrow doesn't couple with W,Z bosons
 - ▶ Ψ_L $SU(2)$ doublet
 - ▶ Mass term (after EW symmetry breaking): $m\bar{\Psi}_L\Psi_R + \text{h.c.} \Rightarrow$ mix Ψ_L and Ψ_R
- Minimal Standard Model(MMS):
 - neutrinos are massless!
 - there are only 3 neutrinos lighter than $M_Z/2$
- Neutrino interaction:

– Charged current:
$$\mathcal{L}_W = -\frac{g}{\sqrt{2}} \sum_{\alpha=e,\mu,\tau} (\bar{\ell}_{L\alpha} \gamma^\lambda \nu_{L\alpha} W_\lambda^- + \bar{\nu}_{L\alpha} \gamma^\lambda \ell_{L\alpha} W_\lambda^+)$$

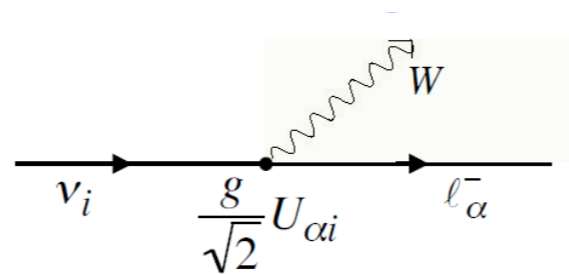
– Neutral current:
$$\mathcal{L}_Z = -\frac{g}{\cos\theta_W} \sum_{\alpha=e,\mu,\tau} \bar{\nu}_{L\alpha} \gamma^\lambda \nu_{L\alpha} Z_\lambda$$

INCORPORATE MASS AND MIXING

- **Higgs mechanism** (like in the quark sector):
 - Introduce **Dirac Mass Term** and diagonalize the mass matrix
 - **Unitary matrix** appears in Interaction Lagrangian
 - Neutral current not affected: **GIM mechanism**

$$\mathcal{L}_W = -\frac{g}{\sqrt{2}} \sum_{\alpha=e,\mu,\tau} \sum_{i=1,2,3} (\bar{\ell}_{L\alpha} \gamma^\lambda U_{\alpha i} \nu_{Li} W_\lambda^- + \bar{\nu}_{Li} \gamma^\lambda U_{\alpha i}^* \ell_{L\alpha} W_\lambda^+)$$

- **Amp($W^+ \rightarrow l_\alpha + \nu_i$) = $g/\sqrt{2} U_{\alpha i}^*$**



- **Orthogonality: 3 flavours \Rightarrow at least 3 mass eigenstates**

$$|\nu_\alpha\rangle = \sum_{i=1,2,3} U_{\alpha i}^* |\nu_i\rangle$$

$$|\nu_i\rangle = \sum_{\alpha=e,\mu,\tau} U_{\alpha i} |\nu_\alpha\rangle$$

- **Flavour fraction of $|\nu_i\rangle = |U_{\alpha i}|^2$**

ν field: creates $\bar{\nu}$ and destroys ν
This is why U^* appear when ket $|\nu\rangle$ used

CHIRALITY AND HELICITY

Chirality (X)

- Acts on Dirac Spinor Space
- Projector: $P_L^{(R)} = (1 \pm \gamma_5)/2$
- **Lorentz invariant!** Interactions don't depend on reference frame!!
- **Not conserved:** mass term mixes right and left component

Helicity (H)

- Acts on physical space: spin projection on momentum direction $H = \sigma \cdot p / |p|$
- Projector: $\Pi_L^{(R)} = (1 \pm \sigma \cdot p / |p|) / 2$
- **Not Lorentz invariant for massive particle,** momentum reversed if boost with $\beta > \beta_m = p/E$
- **Conserved**

If $m=0$ Helicity and Chirality coincide (not the case for neutrinos!): $X = H + O(m/E)$

Nature has related the Weak Force to chirality eigenstates

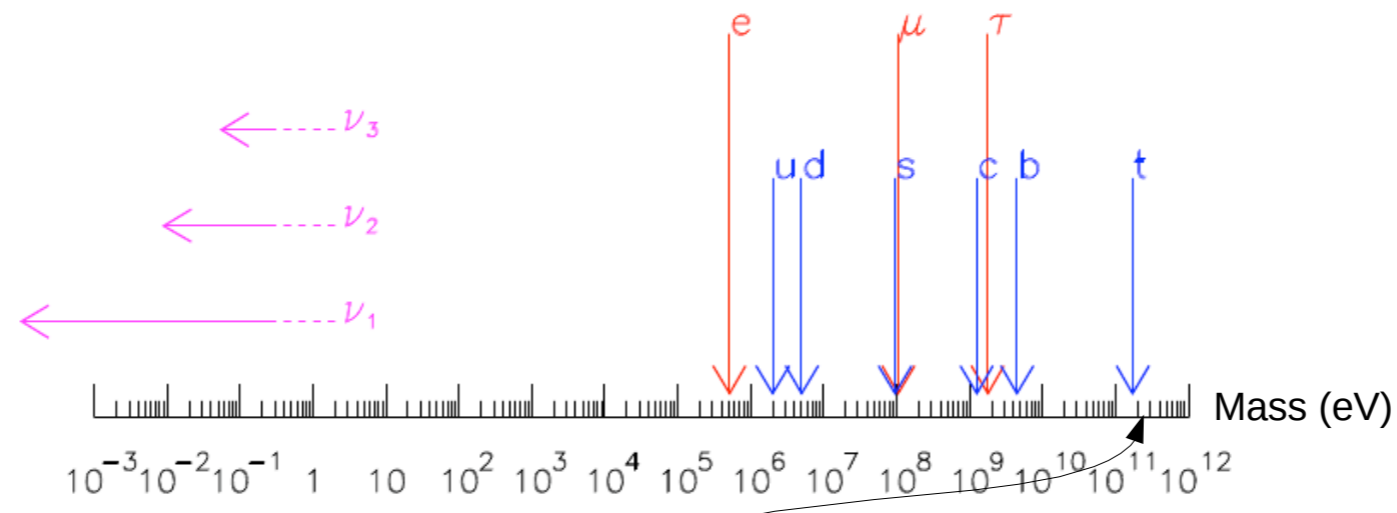
WHAT WE KNOW FROM EXPERIMENTS

- **Neutrino mixing matrix:**

$$U_{PMNS} = \begin{bmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{bmatrix} = \begin{bmatrix} 0.84 & 0.54 & 0.14 \\ 0.38 & 0.60 & 0.70 \\ 0.38 & 0.60 & 0.70 \end{bmatrix}$$

CKM		
0.97	0.22	0.003
0.22	0.97	0.04
0.009	0.04	0.99

- **Neutrino mass spectrum**

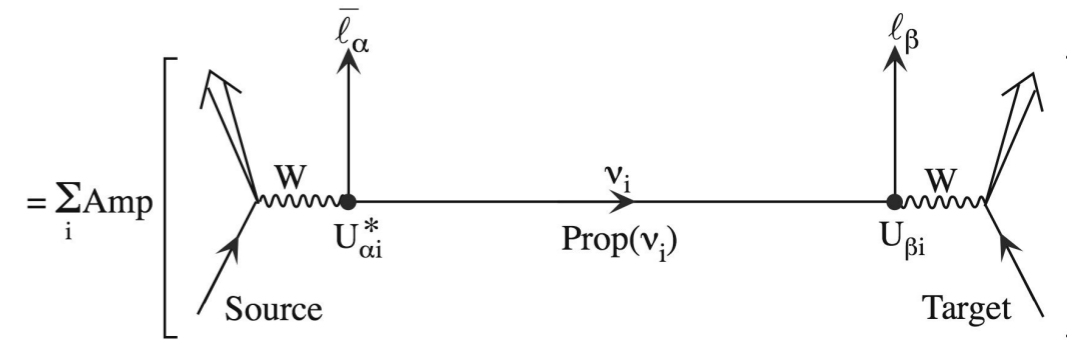
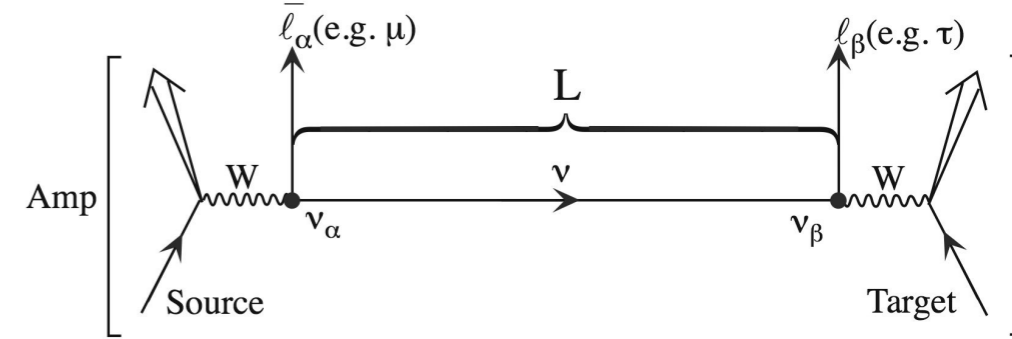


- Quarks and **charged leptons** produced as mass eigenstates
- **Neutrinos** as flavour eigenstates
- **Unitary triangles**, useful when measure sides and angles, **have no practical use in lepton flavour mixing**
 - ▶ **neutrino oscillation theory**

SPECIAL CASE: 2 NEUTRINOS

- Similar to $K^0-\bar{K}^0$ mixing: **weak eigenstates \neq strong eigenstates**
 - but **neutrinos don't decay** (no exponential term)
 - always relativistic and tiny mass difference**
 - **Flavour change in vacuum oscillates with L/E :**
(macroscopic quantum coherence interference)

- Why quarks and charged leptons don't oscillate?

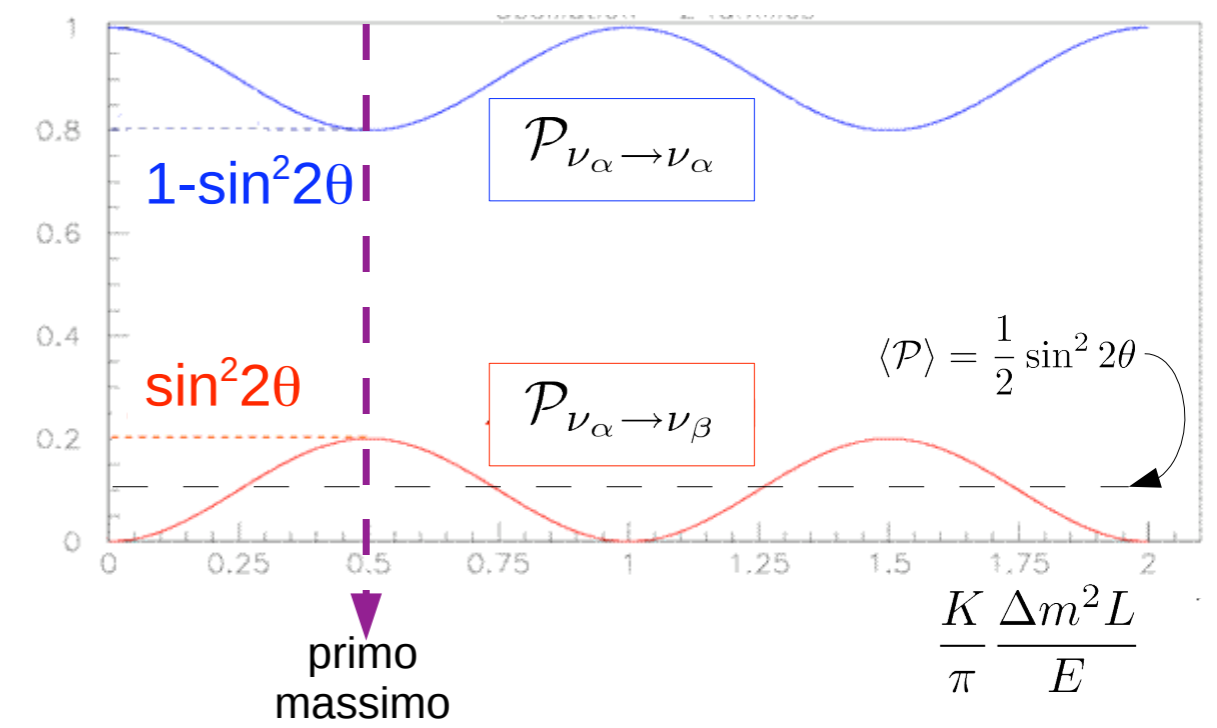


$$U = \begin{matrix} \nu_e \\ \nu_\mu \end{matrix} \begin{bmatrix} \nu_1 & \nu_2 \\ \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{bmatrix}$$

$$P[\nu_\alpha \rightarrow \nu_\beta] = \sin^2(2\theta) \sin^2(\Delta m^2 L / 4E)$$

no distinction
 $\theta \Leftrightarrow \pi/2 - \theta$, $\Delta m^2 \Leftrightarrow -\Delta m^2$

if Δm or $\theta = 0$ $P(\nu_\alpha \Rightarrow \nu_\beta) = \delta_{\alpha\beta}$



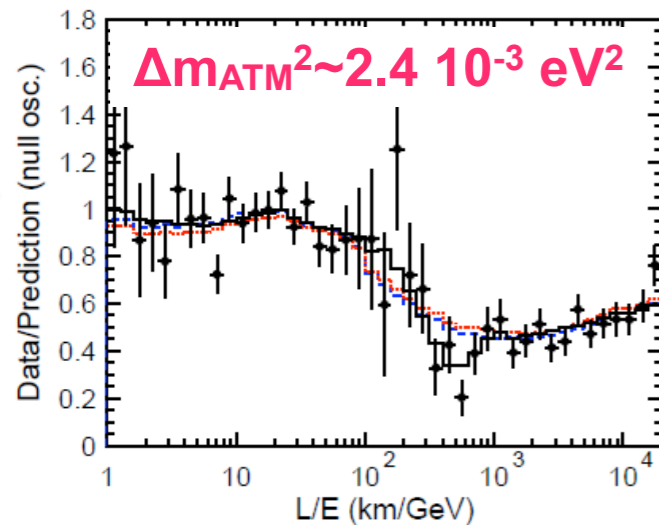
3 NEUTRINOS CASE

$$P[\nu_\alpha \rightarrow \nu_\beta] = \delta_{\alpha\beta} - 4 \sum_{i>j} \text{Re}(U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin^2(\Delta m_{ij}^2 L/4E) + 2 \sum_{i>j} \text{Im}(U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin^2(\Delta m_{ij}^2 L/2E)$$

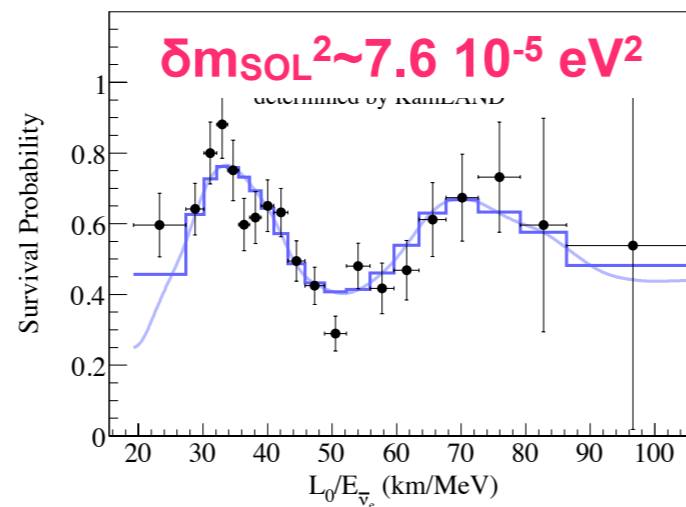
- Phenomenology simplified by two experimental results:

2 different mass scale: $\Delta m_{\text{ATM}}^2 \sim 30 * \delta m_{\text{SOL}}^2$

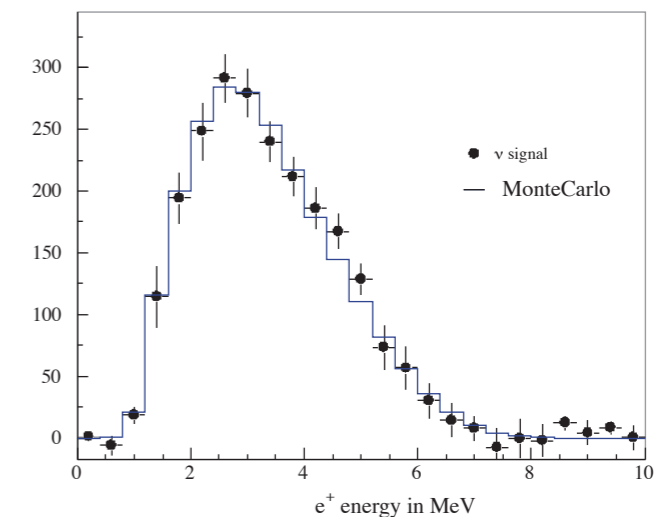
one small angle: $\theta_{13} < 10^\circ$



SuperKamiokande



Kamland



Chooz

- Experiments with $\Delta m^2 L/E = O(1)$ can't distinguish δm_{SOL} eigenstates (m_1 and m_2)

- sensitive to 3rd column

- At solar energies (MeV) μ, τ under production threshold:

- sensitive to 1st row

- $|U_{e3}| = \sin(\theta_{13})$ θ_{13} only link between oscillations: $\theta_{13} < 10^\circ$

- oscillations decoupled

Solar

U_{e1}	U_{e2}	U_{e3}
$U_{\mu 1}$	$U_{\mu 2}$	$U_{\mu 3}$
$U_{\tau 1}$	$U_{\tau 2}$	$U_{\tau 3}$

Atmospheric

THE ATMOSPHERIC ANOMALY

- Primary cosmic produce π in the upper atmosphere:

- $\pi \Rightarrow \mu \nu_\mu, \mu \Rightarrow e \nu_\mu \nu_e \quad \phi(\nu_\mu) = 2 \cdot \phi(\nu_e)$

- Isotropy of the $>2\text{GeV}$ cosmic rays flux + Gauss' law :

- ν rate up/down symmetric (no need knowledge flux)

- Measured Flux: $[\phi(\nu_\mu)/\phi(\nu_e)]/[\phi(\nu_\mu)/\phi(\nu_e)]_{MC} \sim 0.65$

- Anomaly even without relying on knowledge of neutrino fluxes

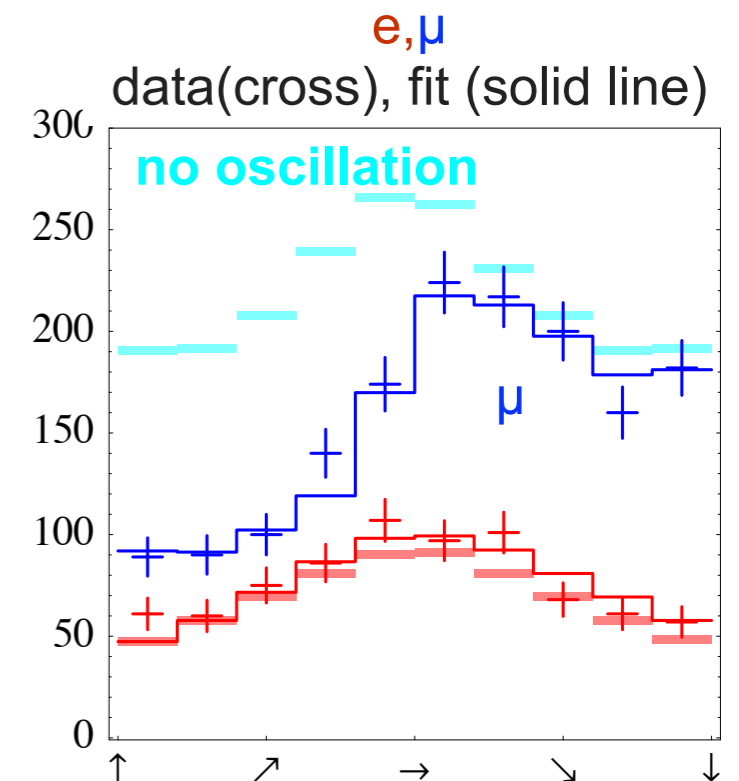
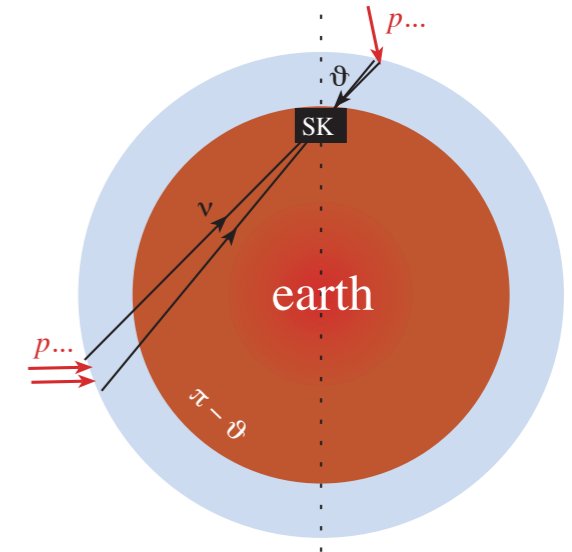
- $P_{ee}=1, P_{e\mu}=0, P_{\mu\mu}=1 - \sin^2(2\vartheta_{Atm})\sin^2(\Delta m^2_{Atm}L/4E_\nu)$

- Zenith no oscillation, Nadir average oscillation

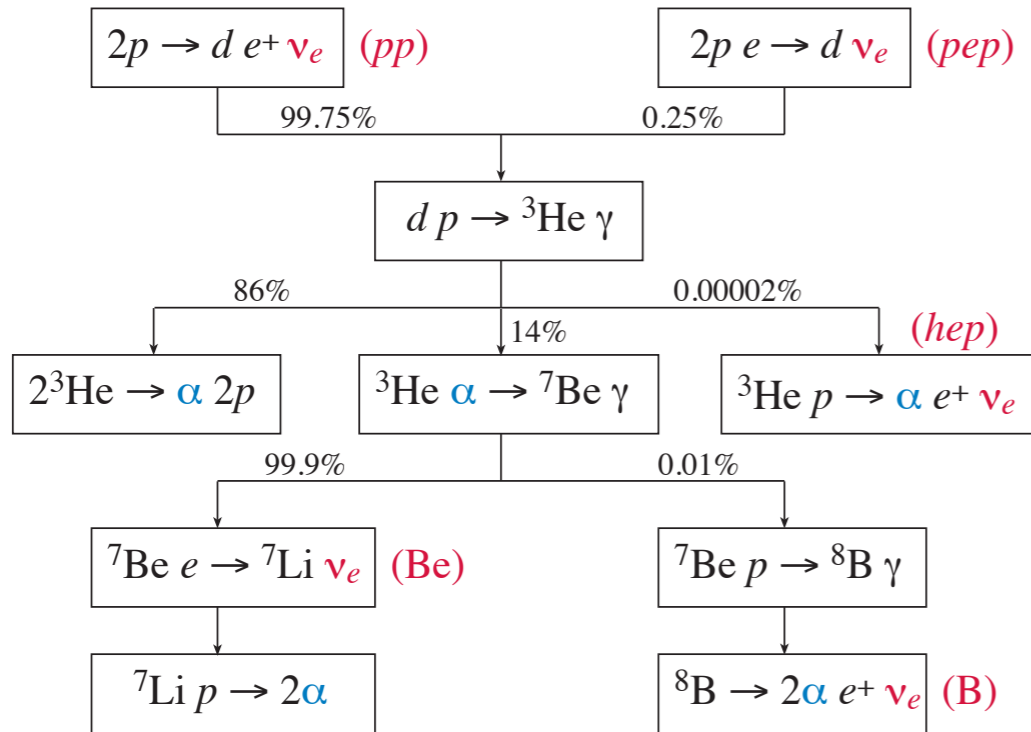
- ▶ $P_{\mu\mu} = 1 - 0.5 \cdot \sin^2(2\vartheta_{Atm}) = 1 - 0.5 N^\uparrow/N^\downarrow \Rightarrow \vartheta = 45^\circ$

- Oscillations start horizontal: $E_\nu \sim \text{GeV}, L \sim 1000\text{km},$

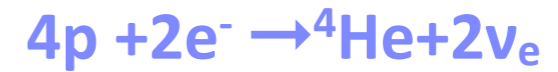
- ▶ $\Delta m^2_{Atm} \sim E_\nu/L \sim 3 \cdot 10^{-3} \text{ eV}$



NEUTRINOS FROM THE SUN



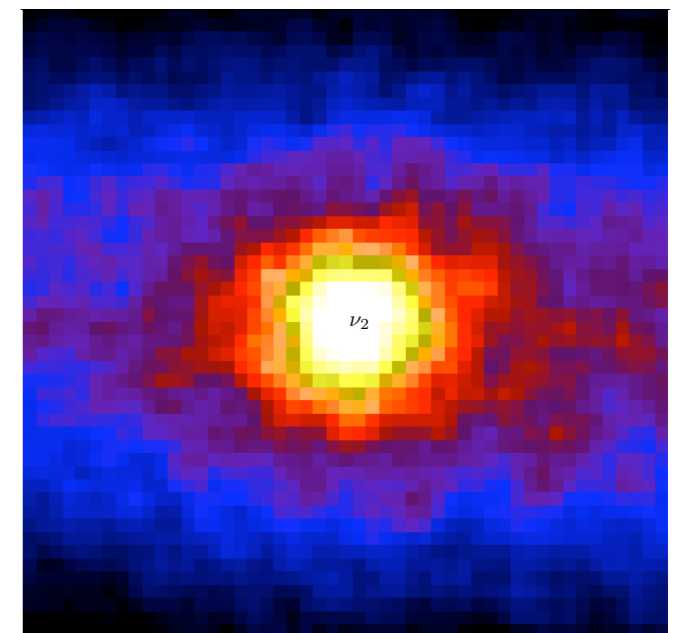
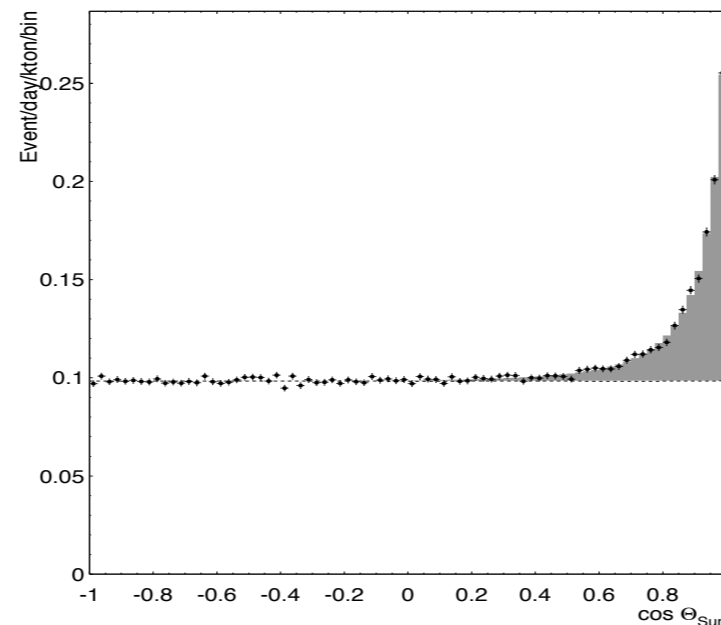
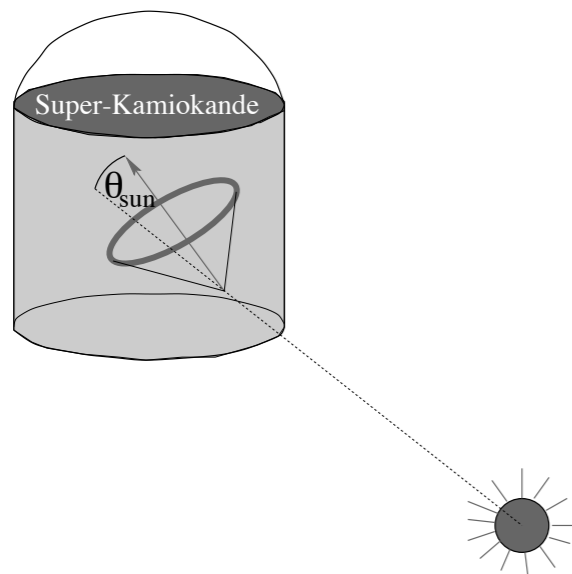
In the center of the sun



$$Q = 26.73 \text{ MeV}$$

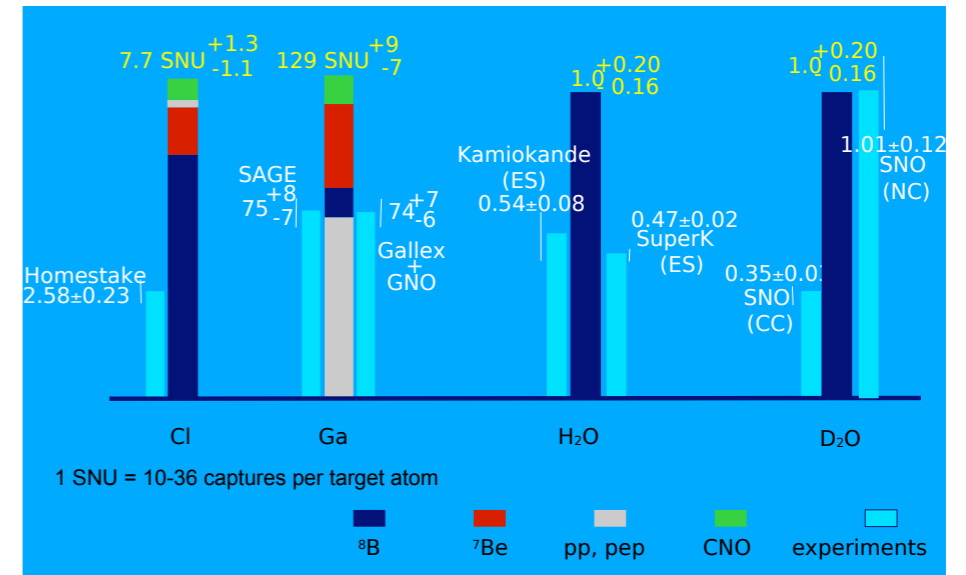
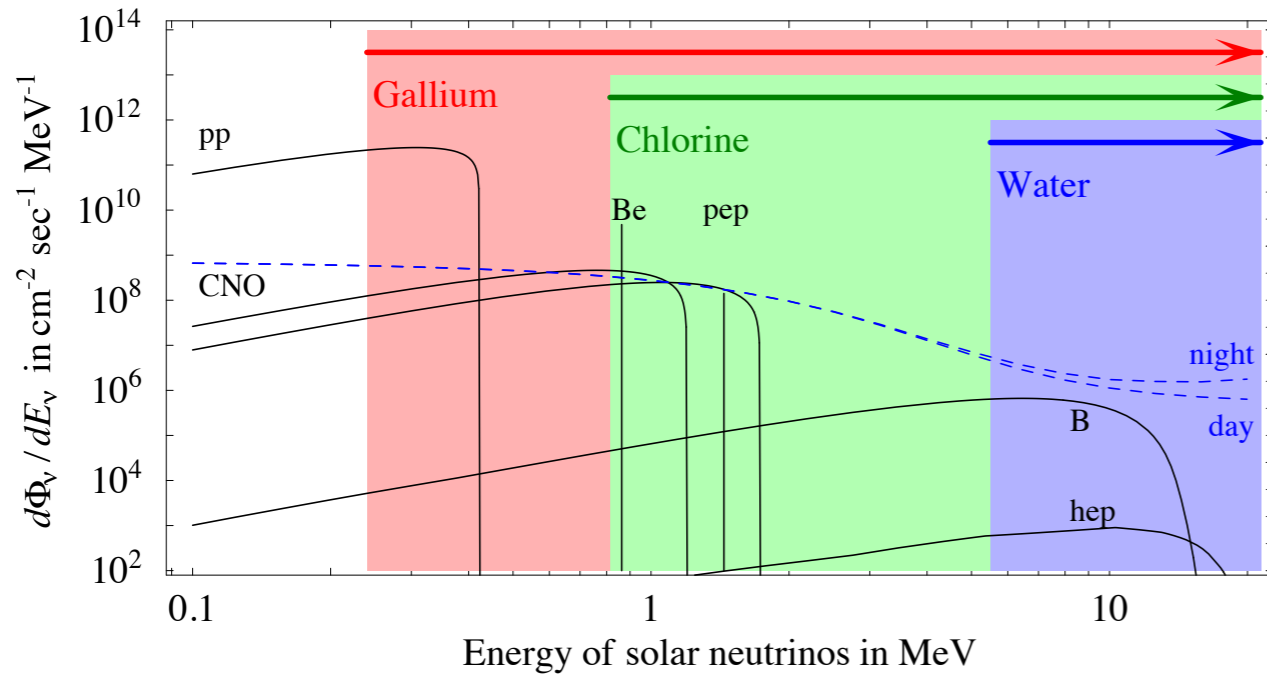
$$\langle E_\nu \rangle \approx 0.3 \text{ MeV}$$

$$\text{Solar } \Phi(\nu) \approx 6 \cdot 10^{10} \nu/\text{cm}^2\text{s}$$



SOLAR ANOMALY

- Several experiments sensitive to different solar ν 's measure a ν flux deficit: problem with solar model?



- SNO(D₂O Cerenkov detector) measure **both charged and total ν flux:**

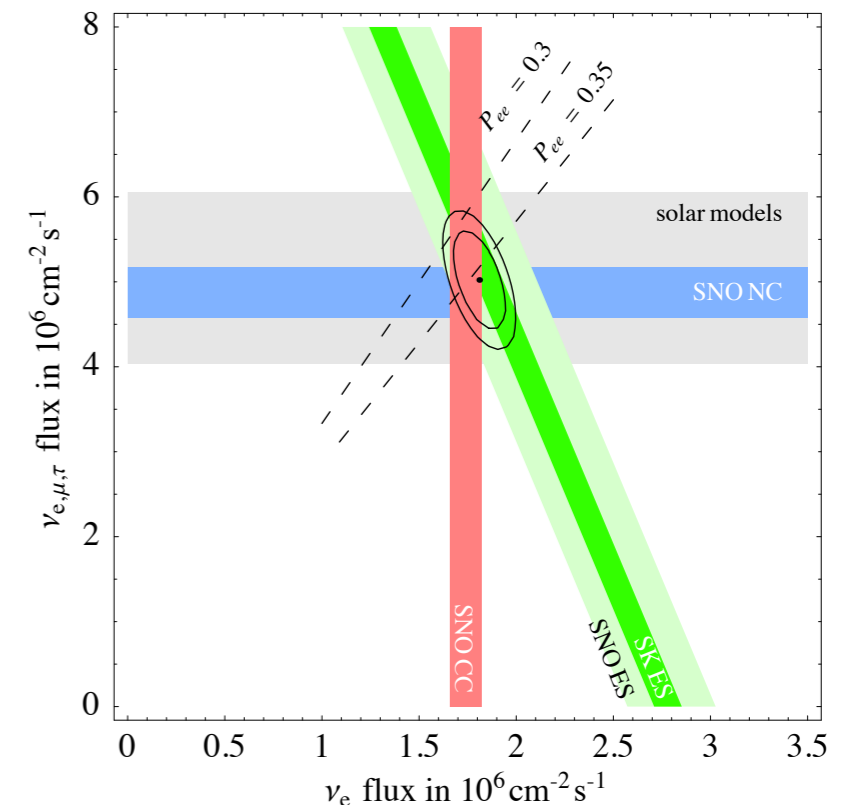
– ES: $\nu_{e,\mu,\tau} e \rightarrow \nu_{e,\mu,\tau} e \Rightarrow \Phi(\nu_e) + 0.155 \Phi(\nu_{\mu,\tau})$

– CC: $\nu_e D \rightarrow e^- pp \Rightarrow \Phi(\nu_e)$

– NC: $\nu D \rightarrow \nu pn \Rightarrow \Phi(\nu_{e,\mu,\tau})$

- NC rate as expected from Solar Model**

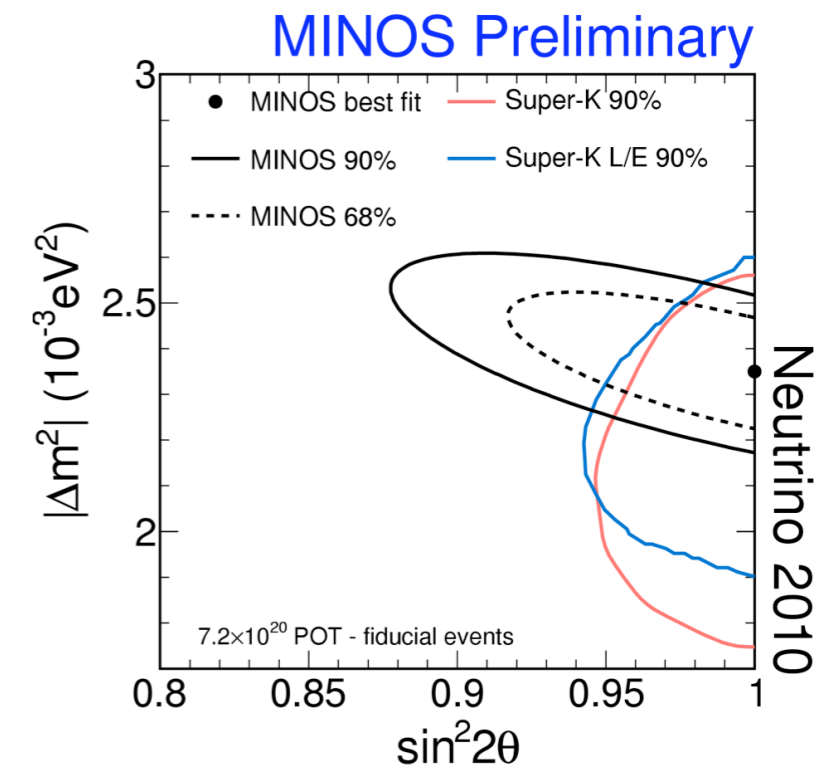
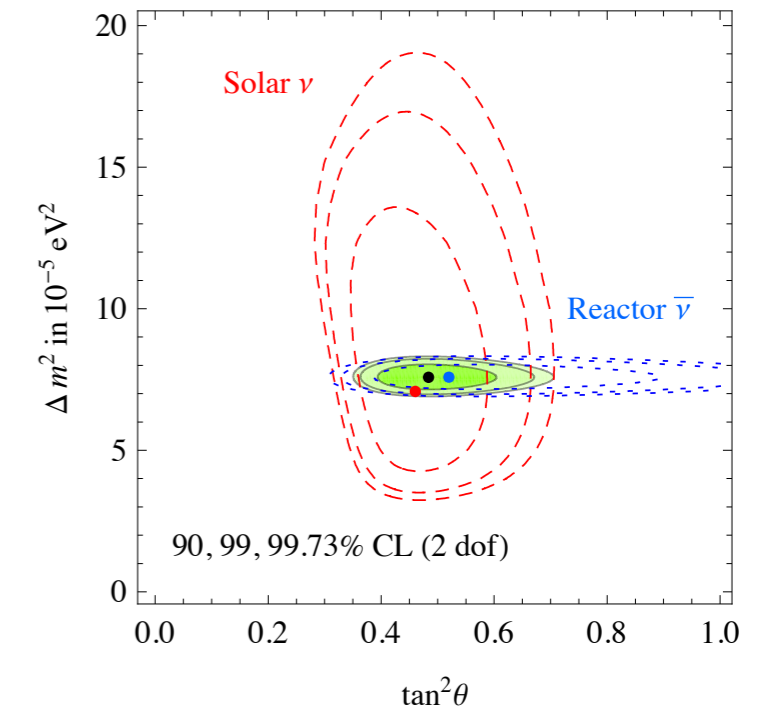
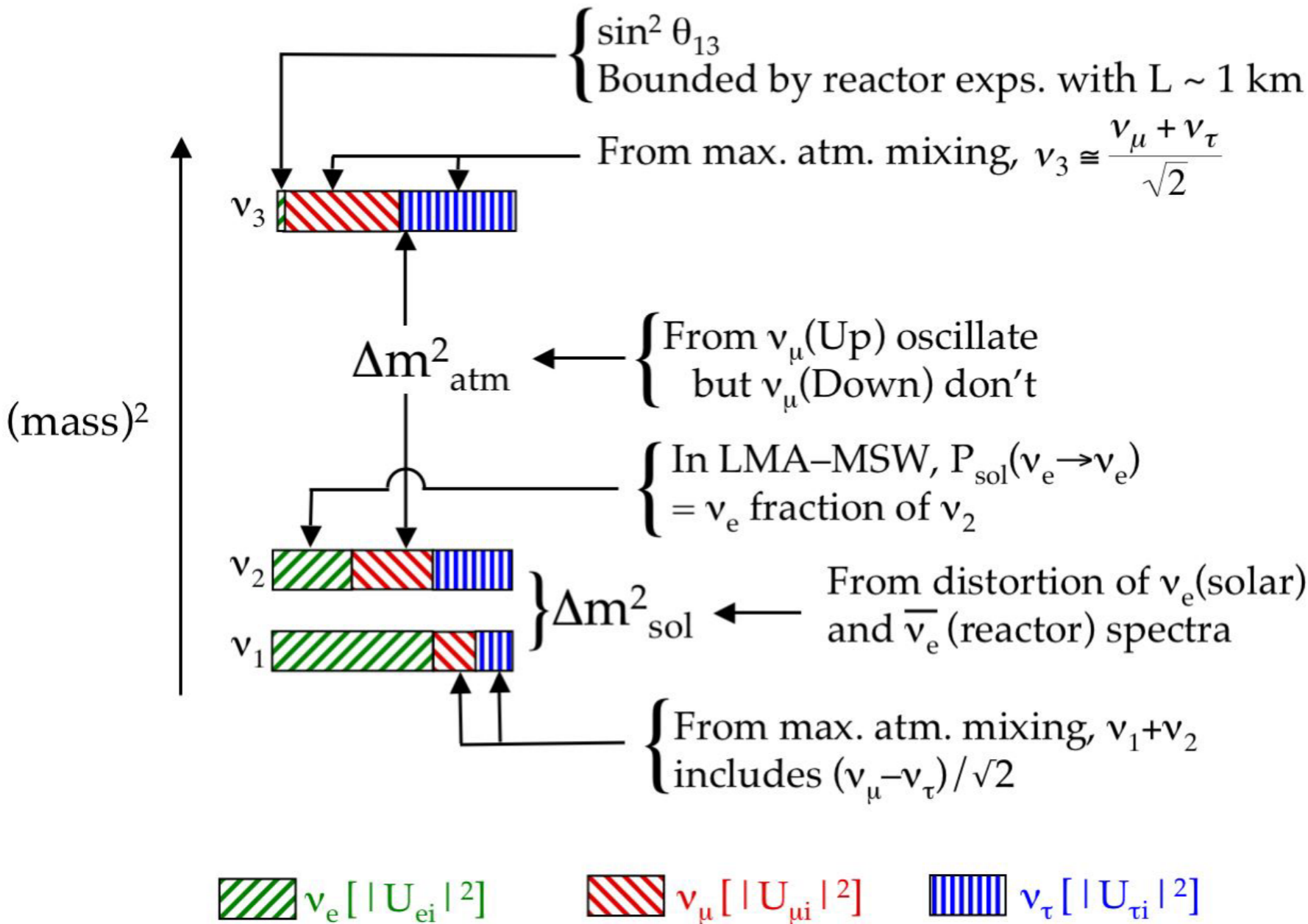
- CC/NC ratio:**
$$\frac{\phi(\nu_e)}{\phi(\nu_e) + \phi(\nu_{\mu,\tau})} = 0.357 \pm 0.030$$



THE WHOLE PICTURE

$$\theta_{\text{atm}} \approx \theta_{13} \approx 45^\circ, \theta_{\text{sun}} \approx \theta_{12} \approx 30^\circ, \theta_{13} \leq 10^\circ$$

$$|\Delta m_{13}^2| \approx |\Delta m_{23}^2| \approx |\Delta m_{\text{atm}}^2| \approx (2.40 \pm 0.15) \cdot 10^{-3} \text{ eV}^2 \quad \Delta m_{12}^2 \approx \Delta m_{\text{sol}}^2 \approx (7.58 \pm 0.21) \cdot 10^{-5} \text{ eV}^2$$



MASS SPECTRUM

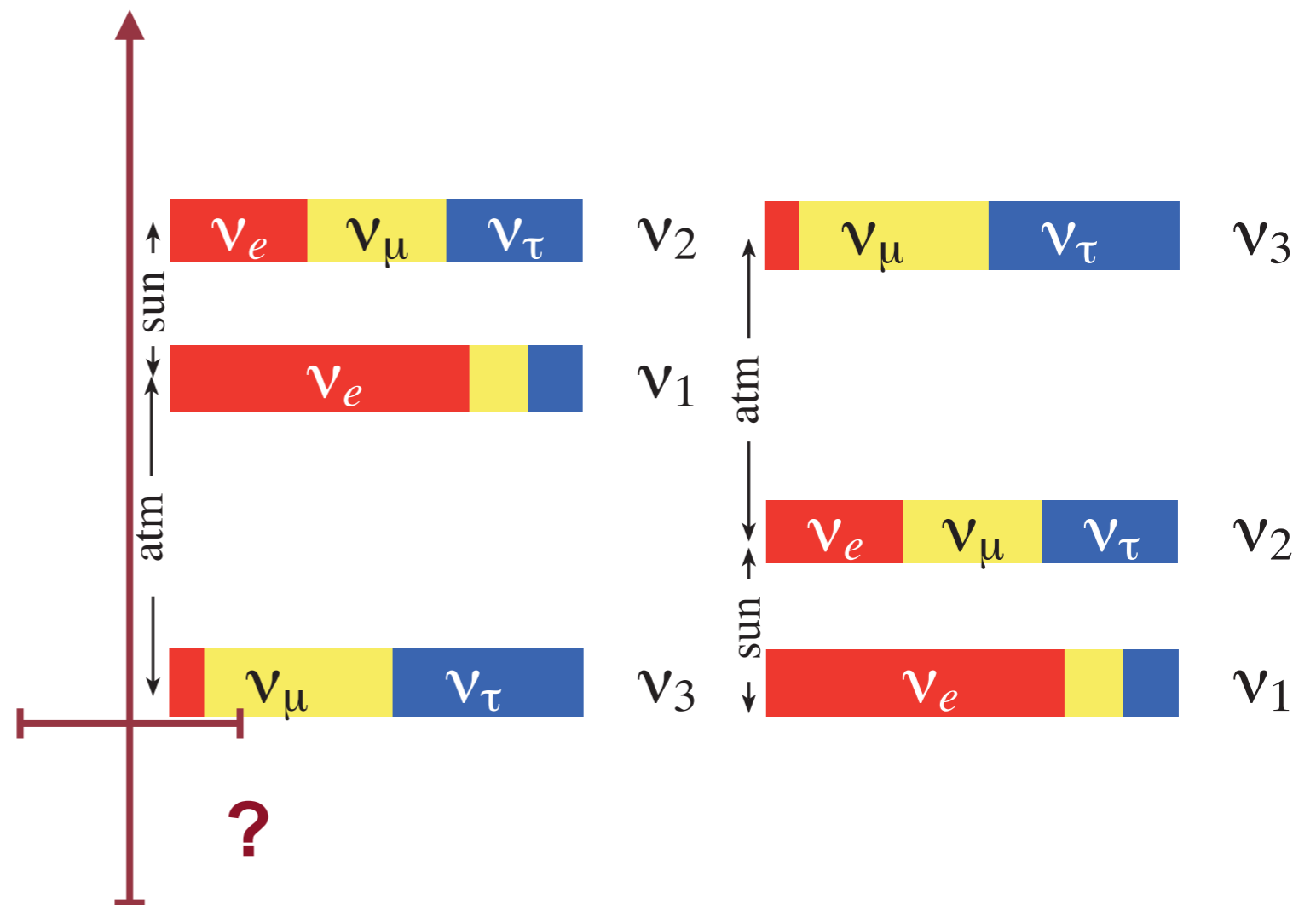
- From oscillation experiments we know that neutrinos are massive:

$$|\Delta m^2_{13}| \approx |\Delta m^2_{23}| \approx |\Delta m^2_{\text{atm}}| \approx (2.40 \pm 0.15) \cdot 10^{-3} \text{ eV}^2 \quad \Delta m^2_{12} \approx \Delta m^2_{\text{sol}} \approx (7.58 \pm 0.21) \cdot 10^{-5} \text{ eV}^2$$

- Oscillation experiments are not sensitive to the absolute neutrino mass

- Which is the absolute mass scale?

- Cosmology
- Beta Decay
- Neutrinoless Double Beta Decay



DIRECT MEASUREMENT

- **Based purely on kinematics without further assumptions**

- Kinematically constrained measurement: $\pi \rightarrow \mu\nu, \tau \rightarrow 5\pi\nu$

- ▶ Not competitive $m_\nu \leq O(100 \text{ keV})$ for π decay (MeV for τ decay)

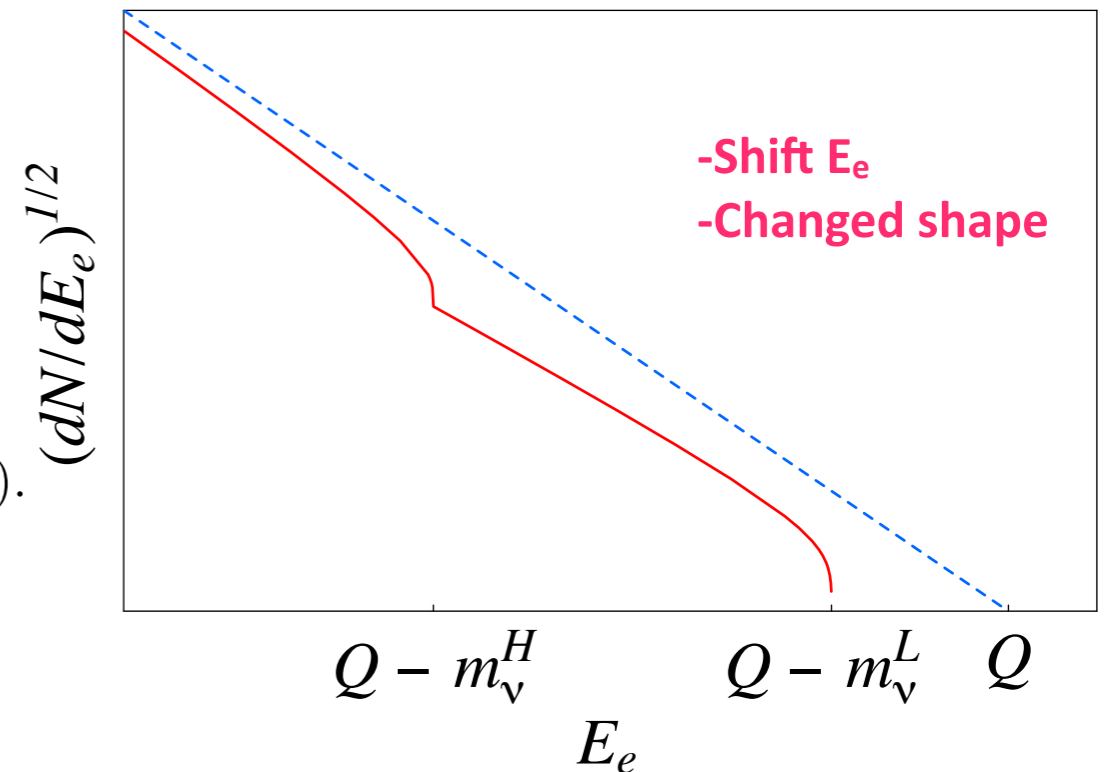
- Time of flight

- ▶ long baseline \Rightarrow neutrino from supernovae explosion (emitted in 10 s) $m_\nu \leq O(10 \text{ eV})$

- **Beta Decay**

$$\frac{d\Gamma}{dE} = \sum_i |U_{ei}|^2 \frac{d\Gamma_i}{dE},$$

$$\frac{d\Gamma_i}{dE} = Cp(E + m_e)(E_0 - E) \sqrt{(E_0 - E)^2 - m_i^2} F(E) \theta(E_0 - E - m_i).$$



- If different masses could not be resolved

$$\frac{d\Gamma}{dE} = Cp(E + m_e)(E_0 - E) \sqrt{(E_0 - E)^2 - m_\beta^2} F(E),$$

$$m_\beta^2 = \sum_i |U_{ei}|^2 m_i^2$$

- Events fraction near end-point $\approx (m_\nu/Q)^3$: 10^{-13} for ${}^3\text{H}$ \Rightarrow low Q, high count rate & energy resolution

KATRIN

- **The MAC-E filter:**

- Adiabatic guiding of electrons along magnetic field:

- ▶ $\mu = E_{K\perp}/B = \text{const}$

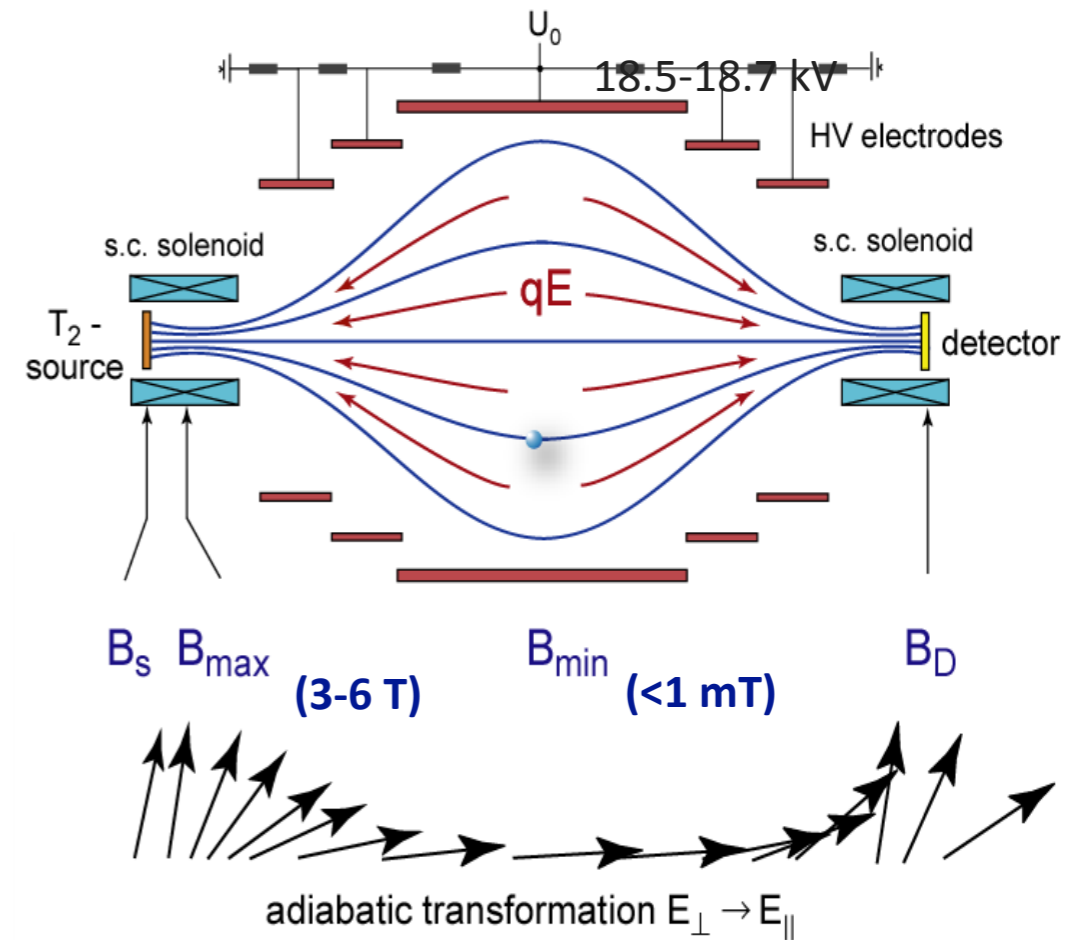
- ▶ $E_e = E_{K\perp} + E_{K\parallel} = \text{const}$

- ▶ $E_{K\perp} \Rightarrow E_{K\parallel}$

- ▶ High energy pass filter to due potential $E_{K\parallel} > U_0$

- High resolution $\Delta E/E = B_{\min}/B_{\max} \approx 10^{-4}$

- Large solid angle: 2π



Actual limits $m_\nu \leq 2.3 \text{ eV}$ 90% CL
(Mainz, Troitsk)

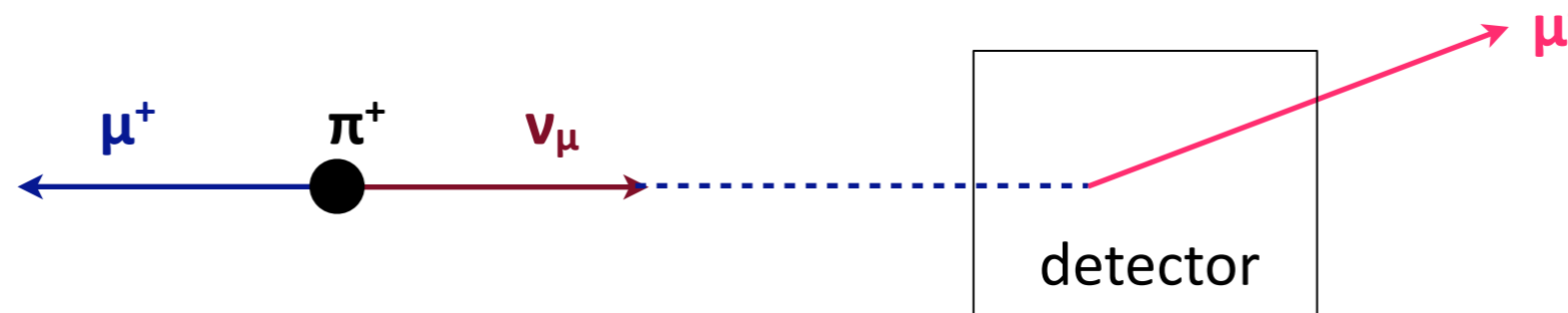
Katrin points to $m_\nu \approx 0.2 \text{ eV}$

MAJORANA OR DIRAC

LEPTON NUMBER CONSERVATION

- **Experimental evidence:**

- Particle produced together with μ^+ in π^+ decay produce a μ^- and never a μ^+
- Opposite for π^- decay



- **Conventional explanation**

- ν_μ and $\bar{\nu}_\mu$ are **distinct** from each other
- There exists a quantum number conserved during interactions: the lepton number
 - ▶ **Dirac fermion**

- **Alternative explanation**

- Weak interactions couple to chirality eigenstates
- Left-handed chirality particle interacts giving a μ^- (μ^+ opposite for right-handed chirality)
- There exists **only one** particle with **two chirality states**
- We don't see μ^+ because chirality flip is suppressed $\propto (m_\nu/E_\nu)^2$
 - ▶ **Majorana fermion**

MAJORANA NEUTRINO

- Dirac equation: $i(\gamma^\mu \partial_\mu - m)\Psi = 0$
 - Ψ_L, Ψ_R irreducible representations of Lorentz group (Chirality $P_L^{(R)} = (1 \pm \gamma_5)/2$, $P_L^{(R)}\Psi = \Psi_L^{(R)}$)
 - ▶ $\Psi = \Psi_L + \Psi_R$, $i\gamma^\mu \partial_\mu \Psi_L = m\Psi_R$, $i\gamma^\mu \partial_\mu \Psi_R = m\Psi_L$
 - ▶ Massless fermions described by two degrees of freedom: decoupled equations
- Minimal description of a massive neutral fermion with 2 degrees of freedom (**Majorana 1937**):
 - $\Psi \equiv \Psi^c$ particle and anti-particle coincide
- C charge conjugation operator: $\Psi^c = C\bar{\Psi}^T$, $C = i\gamma^2\gamma^0$
 - Using γ properties: Ψ_R^c is left-handed
 - $\Psi \equiv \Psi^c \Rightarrow \Psi_L + \Psi_R = \Psi_L^c + \Psi_R^c \Rightarrow \underline{\Psi_R = \Psi_L^c}, \underline{\Psi_L = \Psi_R^c}$
 - ▶ Only two independent components: $\underline{\Psi^M = \Psi_L + \Psi_L^c}$
 - ➔ Majorana theory simpler and more economical than Dirac theory
- If $\Psi \equiv \Psi^c$
 - No longer free to phase-redefine ν_i without consequences
 - Mixing matrix U can contain additional CP-violating phases
 - Affect only processes with lepton number violation

$$U_{PMNS} \cdot \begin{bmatrix} e^{i\alpha_1/2} & 0 & 0 \\ 0 & e^{i\alpha_2/2} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

MASS TERM

- MS: chiral theory $SU(2)_L \times U(1)_Y$
 - Ψ_L and Ψ_R have different properties under $SU(2)_L$: Ψ_L doublet, Ψ_R singlet
- Ψ_L, Ψ_R irreducible representations of Lorentz group
- General Lorentz invariant mass term includes:
 - Dirac mass term: $L^D = -m_D \bar{\Psi}^D \Psi^D = -m_D (\bar{\Psi}_L \Psi_R + \bar{\Psi}_R \Psi_L)$
 - ▶ Need a Ψ_R^{ν} sterile component
 - ▶ L^D creates/absorbs ν_L and absorbs/creates $\bar{\nu}_R$
 - ▶ L^D mixes chirality, **does not** mix particle/antiparticle component
 - Majorana Mass term: $L^M = -1/2 m_M \bar{\Psi}^M \Psi^M = -1/2 m_M (\bar{\Psi}_L^c \Psi_L + \bar{\Psi}_L \Psi_L^c)$
 - ▶ L^M create/absorbs **one** particle with left and right chirality
 - ▶ L^M mixes chirality, mixes charge conjugated components
 - ➔ Violation of any additive quantum number (Lepton number, etc...)
 - ➔ Only possible for totally (under all MS gauge groups) neutral particles
 - ➔ Only neutrinos could have this mass term, they are very peculiar

MASS MATRIX

- Most general mass term for 1 v compatible with Lorentz invariance: $L^{D+M} = L^D + L^M_L + L^M_R$
- $L^{D+M} = -m_D \bar{\Psi}_L \Psi_R - 1/2 m_M \bar{\Psi}_L^C \Psi_L - 1/2 m_M \bar{\Psi}_R \Psi_R^C + h.c.$

$$L^{D+M} = -\frac{1}{2} \begin{bmatrix} \bar{\nu}_L^C & \bar{\nu}_R \end{bmatrix} \begin{bmatrix} m_L & m_D \\ m_D & m_R \end{bmatrix} \begin{bmatrix} \nu_L \\ \nu_R^C \end{bmatrix} + h.c.$$

Right components, sterile

Left components, active

field notation change $\Psi \rightarrow \nu$

$$\mathcal{L}^{D+M} = \frac{1}{2} \bar{N}_L^c M N_L + H.c., \quad M = \begin{pmatrix} m_L & m_D \\ m_D & m_R \end{pmatrix}, \quad N_L = \begin{pmatrix} \nu_L \\ \nu_R^c \end{pmatrix}.$$

- ν_L, ν_R are not mass eigenstates, only neutrino fields in term of which the model is constructed
- Diagonalizing the Mass Matrix:

$$N_L = U n_L, \quad n_L = \begin{pmatrix} \nu_{1L} \\ \nu_{2L} \end{pmatrix}, \quad U^T M U = \begin{pmatrix} m_1 & 0 \\ 0 & m_2 \end{pmatrix},$$

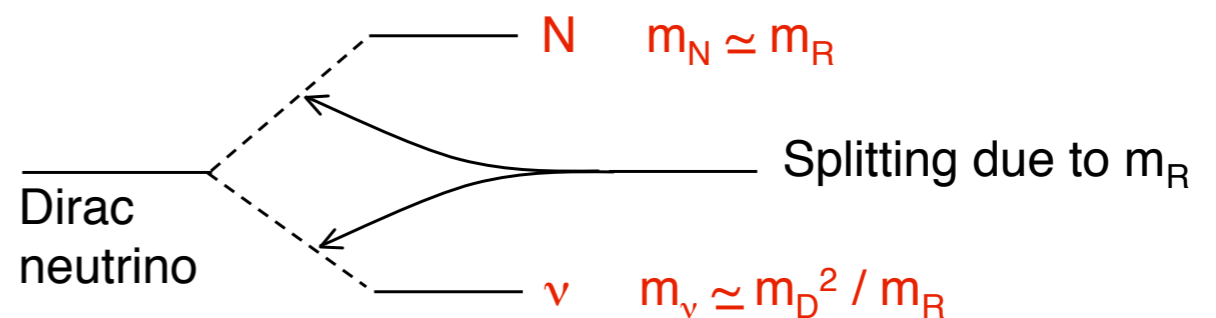
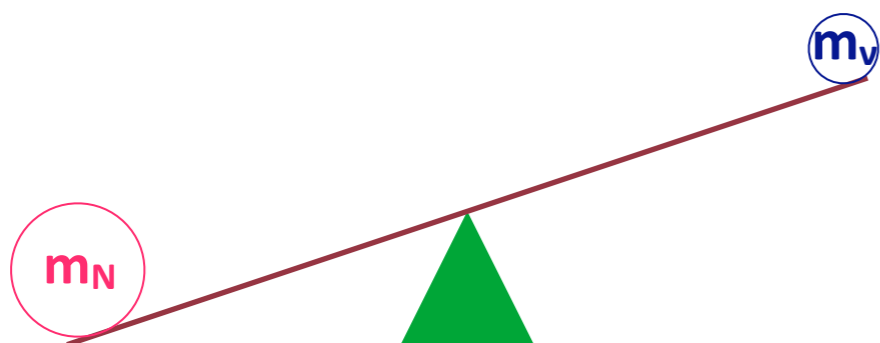
$$L^{D+M} = -\frac{1}{2} \sum_{k=1,2} m_k \bar{\nu}_{kL}^c \nu_{kL} + h.c.$$

$$\nu_k = \nu_{kL} + \nu_{kL}^c \quad (k = 1, 2).$$

- ▶ **Most general D+M mass term = Sum of 2 Majorana mass term for the fields $\nu_k = \nu_k^c$**
- ▶ As a result of $\bar{K}^0 K^0$ mixing, the neutral K mass eigenstates are $K_L, K_S = 0.5(\bar{K}^0 \pm K^0)$. As a result of neutrino mixing (induced by Majorana mass term) **v mass eigenstates are Majorana neutrino**
- ▶ $N_L = U n_L \Rightarrow \nu_L, \nu_R^c$ combination of ν_{1L}, ν_{2L} , possible oscillation between sterile and active states

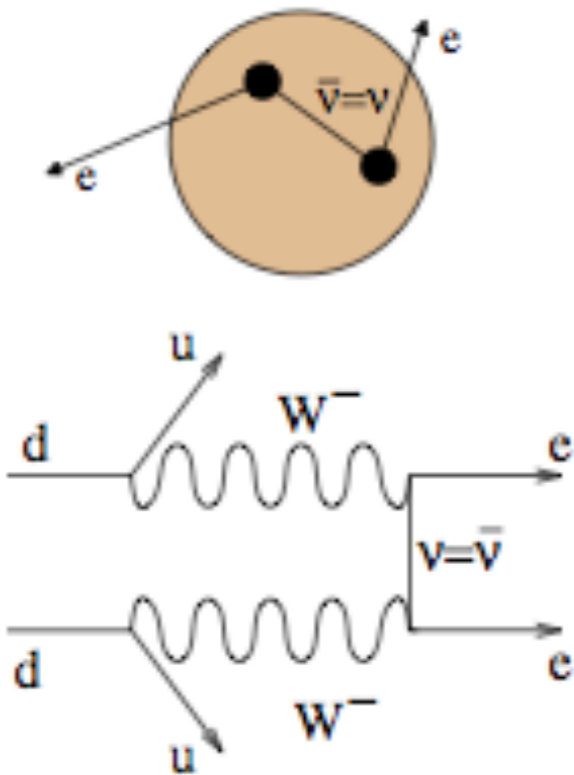
SEE-SAW

- Majorana masses **cannot** come from the progenitor of the Dirac Mass term: $H_{SM} \bar{\nu}_R \nu_L$
- Possibles progenitors of Majorana mass term:
 - $H_{SM} H_{SM} \bar{\nu}_L^c \nu_L$: not renormalizable ($\nu_L^c \nu_L$ isospin triplet)
 - $H_{\text{Isospin}=1} \bar{\nu}_L^c \nu_L$: excluded by Standard Model measurements (Z,W couplings and widths)
 - $m_R \bar{\nu}_R^c \nu_R$: **ok** ($\bar{\nu}_R^c \nu_R$ Isospin singlet)
 - ▶ $m_L=0$
 - ▶ m_D : order of magnitude EW symmetry breaking scale $\approx 100 \text{ GeV}$
 - ▶ m_R : unprotected by any symmetry
 - ➔ If MS is a low energy effective theory of a more general gauge group, it's reasonable to expect m_R of the order of this new symmetry breaking scale
 - ➔ $m_R \approx m_D^2 / m_\nu \approx 10^{15} \text{ GeV} \approx \text{GUT scale!}$
 - 2 Majorana neutrinos, one big mass sterile neutrino ($m_N = m_R$), one light neutrino ($m_\nu = m_D^2 / m_R$)
 - ▶ Explanation of the smallness of neutrino mass
 - ▶ Sterile neutrinos are very heavy and therefore decoupled from the active ones



HOW TO TEST MAJORANA NATURE

- The most sensitive LNV process: **Neutrinoless Double Beta Decay ($0\nu\beta\beta$)**
- Second order weak nuclear process: $(A,Z) \rightarrow (A,Z+2) + 2 e^-$
 - $(A,Z) \rightarrow (A,Z+2) + 2 e^- + 2\bar{\nu}$ allowed by the MS



Only if:

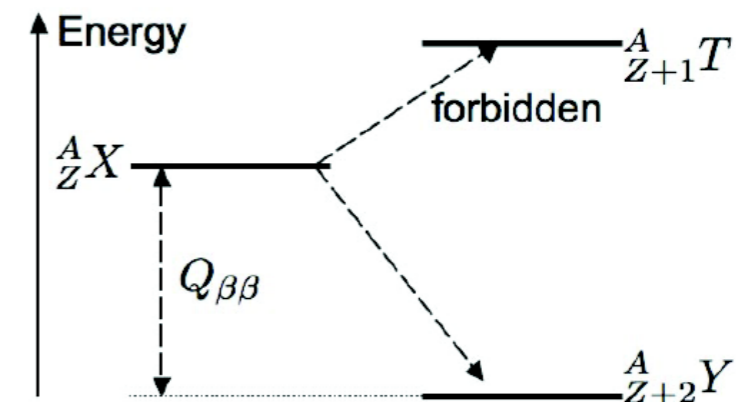
massive neutrinos \rightarrow chirality flip

Majorana neutrino

$\Delta L=2$

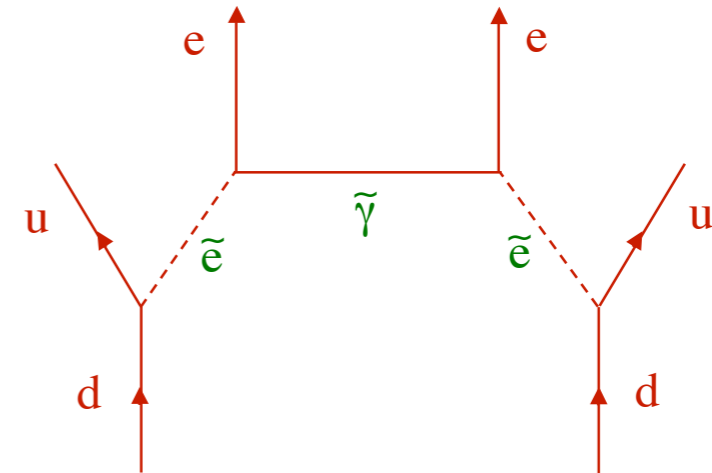
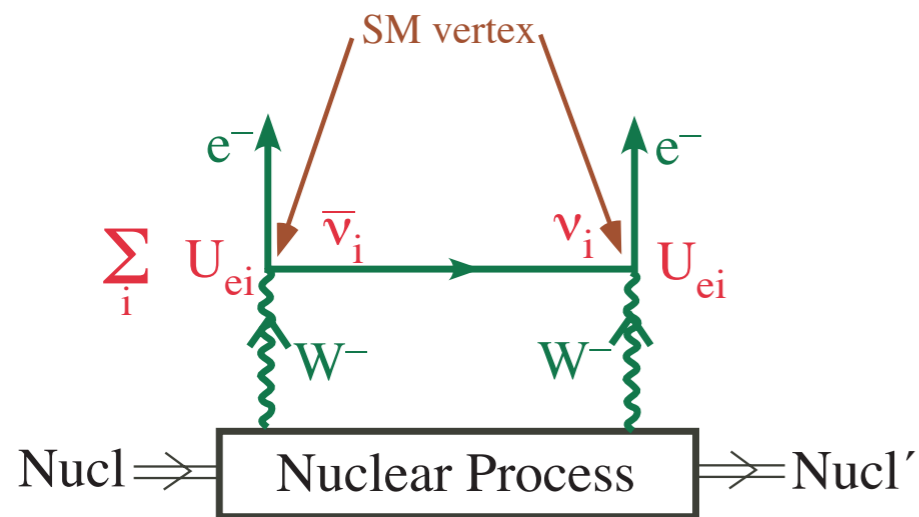
- **Possible only in few even-even nuclei:**

^{48}Ca , ^{76}Ge , ^{82}Se , ^{100}Mo , ^{116}Cd , ^{130}Te , ^{136}Xe , ^{150}Nd

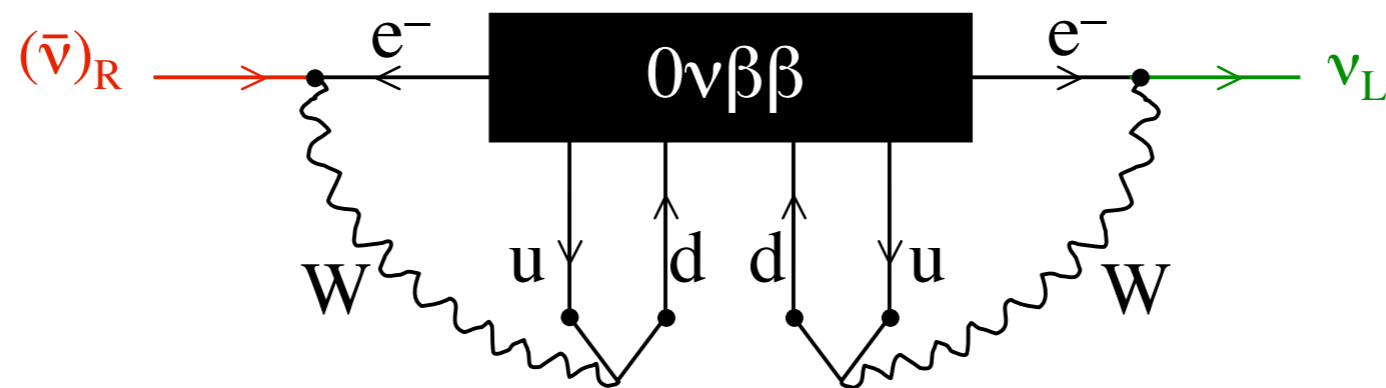


NEUTRINOLESS DOUBLE BETA DECAY: $0\nu\beta\beta$

- Many diagrams can contribute:



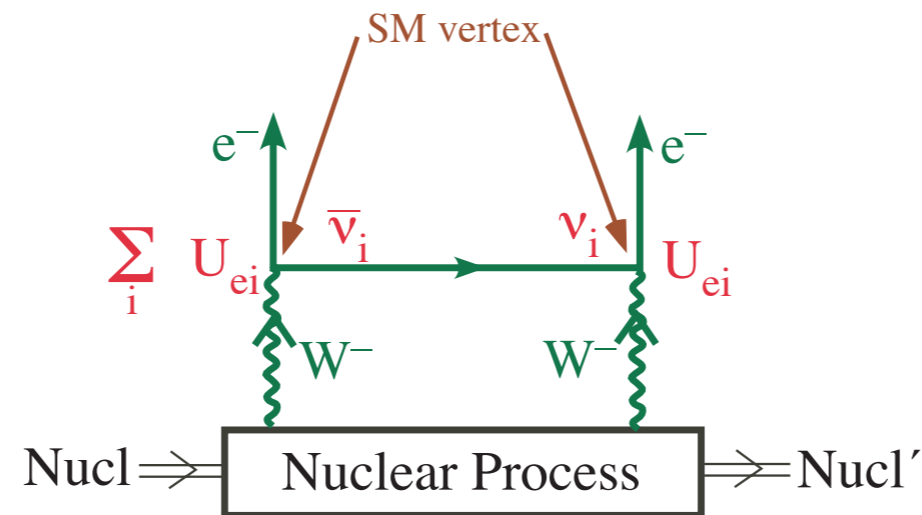
Whatever diagram causes $0\nu\beta\beta$, its observation would imply Majorana mass



Schetcher, Valle [Phys. Rev. D25 2951 1982](#)

NEUTRINOLESS DOUBLE BETA DECAY: $0\nu\beta\beta$

- Assuming the dominant mechanism is:



– Chirality flip $\Rightarrow \text{Amp}(0\nu\beta\beta) \propto |\sum m_i U_{ei}^2| \equiv m_{\beta\beta}$

- ▶ This is what you expect, the only term that violates L in the lagrangian is the ν mass term

$$m_{\beta\beta} = \cos^2 \theta_{13} (m_1 \cos^2 \theta_{12} + m_2 e^{2i\alpha} \sin^2 \theta_{12}) + m_3 e^{2i\beta} \sin^2 \theta_{13}$$

- ▶ Due to Majorana phases cancellations may occur

$0\nu\beta\beta \Leftrightarrow \nu$ MASS

- The measurable quantity is the half life:

Phase space factor $\sim Q^5$

Nuclear Matrix Element

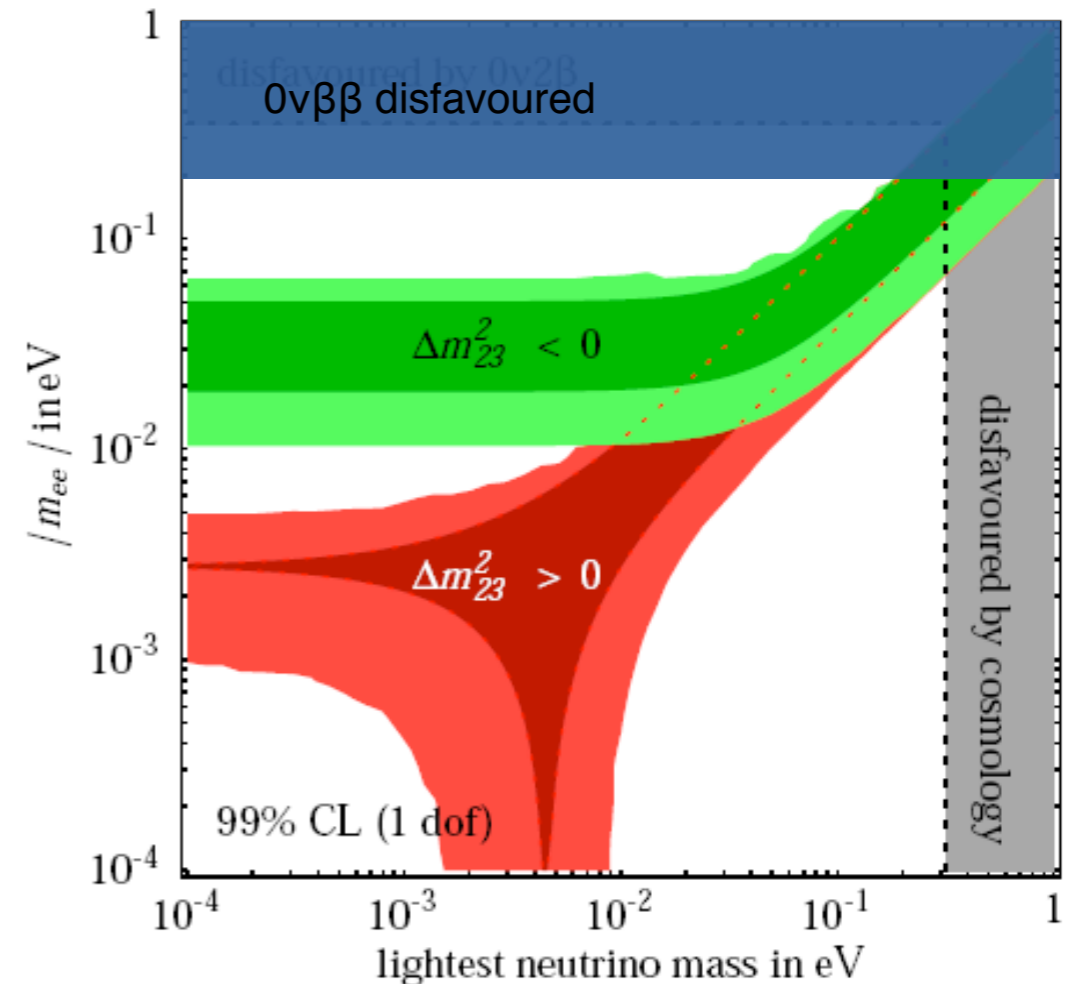
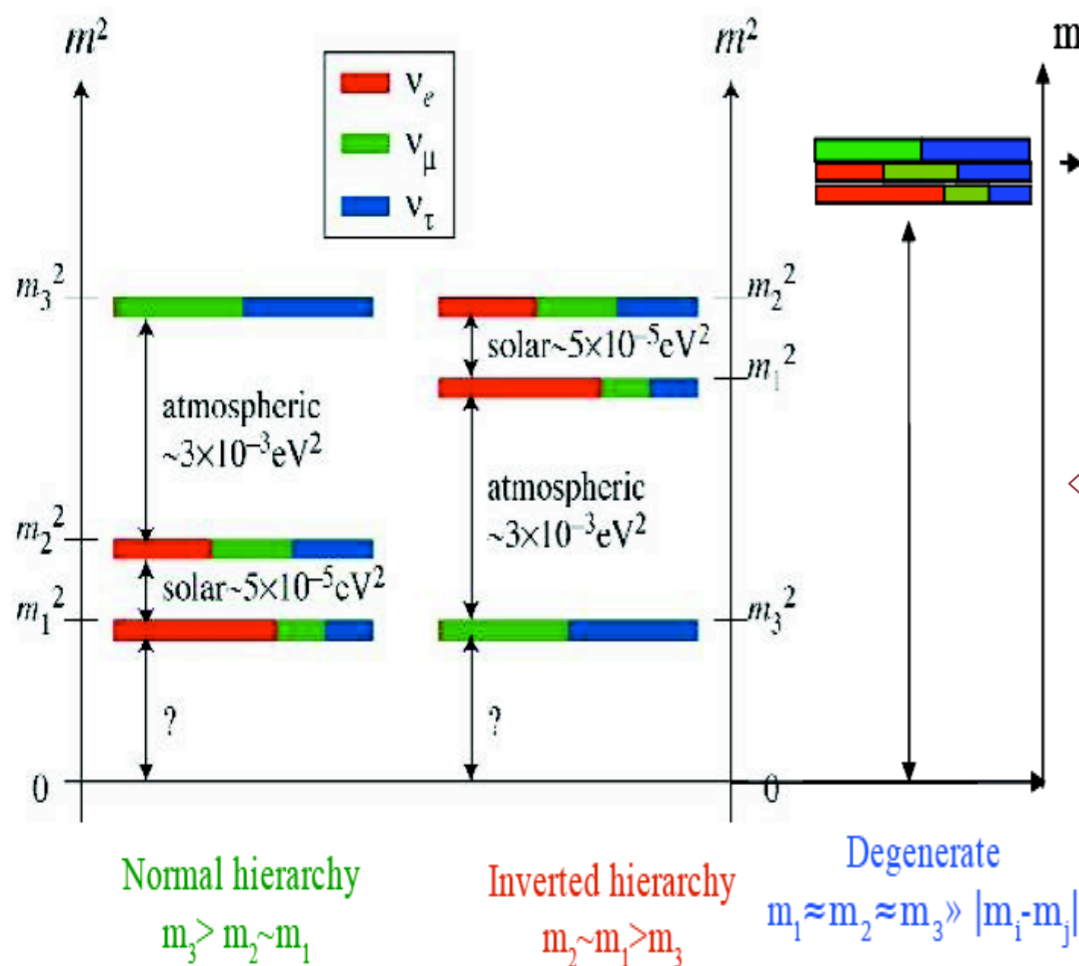
Effective neutrino mass

$$(\tau_{1/2}^{0\nu})^{-1} = G(Q, Z) |M_{nucl}|^2 |m_{\beta\beta}|^2$$

(light neutrino exchange mode)

$$m_{\beta\beta} = \left| \sum_i m_i \cdot U_{ie}^2 \right|$$

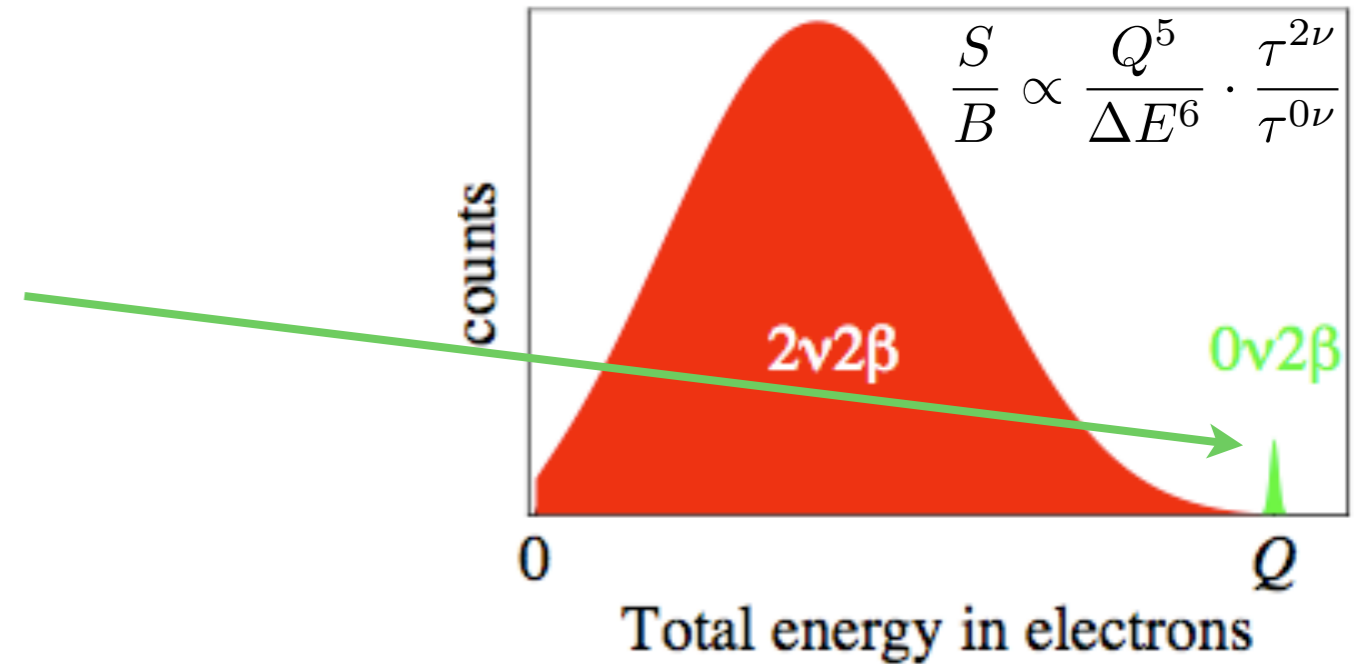
$$m_{\beta\beta} = \cos^2 \theta_{13} (m_1 \cos^2 \theta_{12} + m_2 e^{2i\alpha} \sin^2 \theta_{12}) + m_3 e^{2i\beta} \sin^2 \theta_{13}$$



Strumia, Vissani hep/ph 0606054

$0\nu\text{DBD}$ IN EXPERIMENTS

- Experiments measure the sum of the kinetic energies of the two emitted electrons
- Signature:** monochromatic line at the Q-value of the decay (2-3 MeV)



$$S^{0\nu\beta\beta} = \ln 2 N_A \cdot \frac{a}{A} \left(\frac{Mt}{B\Delta E} \right)^{1/2} \cdot \epsilon$$

Isotopic abundance → $\ln 2 N_A$
 Detector mass (kg) → M
 Measurement time (y) → t
 Atomic mass → A
 Background (counts/keV/kg/y) → B
 Energy Resolution (keV) → ΔE
 Efficiency → ϵ

- Remember: $m_{\beta\beta} \propto (\tau^{0\nu})^{-1/2}$

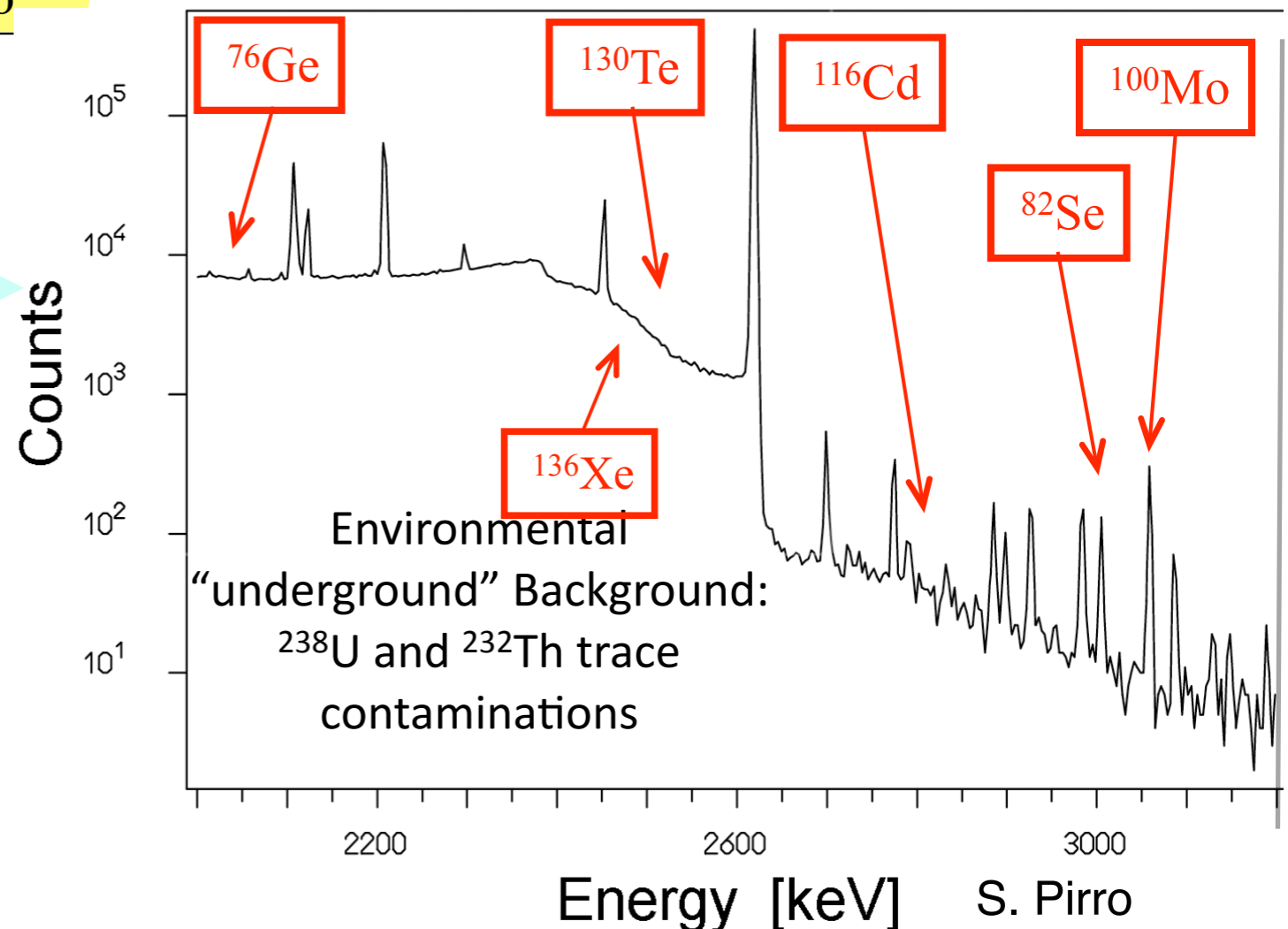
$\tau_{0\nu} \approx \geq 10^{24}$ y
 $\tau_{2\nu} \approx 10^{19/22}$ y
 τ primordial(Ur,Th) $\approx 10^{10}$ y

THE ISOTOPE CHOICE

Parent Isotope	$Q_{\beta\beta}$ (KeV)	Ab(%)
^{48}Ca	4271	0.187
^{76}Ge	2039	7.8
^{82}Se	2995	9
^{100}Mo	3034	9.6
^{116}Cd	2902	7.5
^{130}Te	2530	33.9
^{136}Xe	2479	8.9
^{150}Nd	3367	5.6

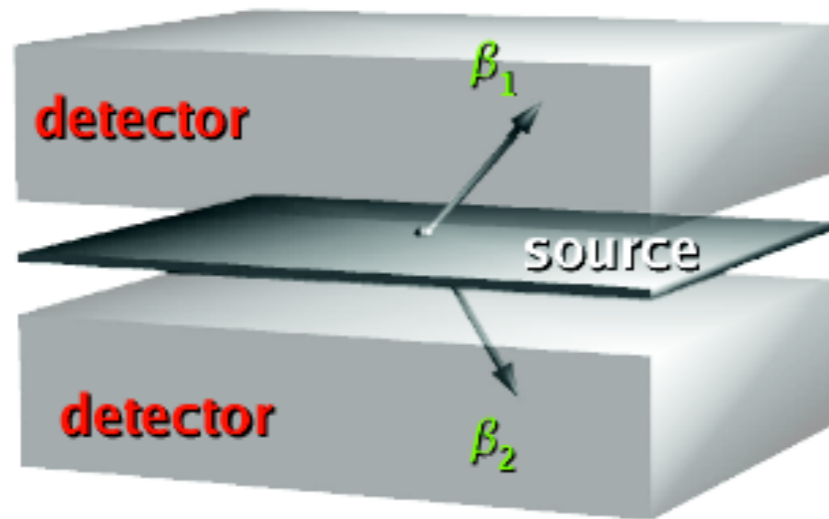
Isotopic abundance: **<10%**
(only exception ^{130}Te)

Gain ~ 100
if $Q_{\beta\beta} > 2615 \text{ keV}$
end of γ radioactivity (^{208}Tl)



EXPERIMENTAL STRATEGIES

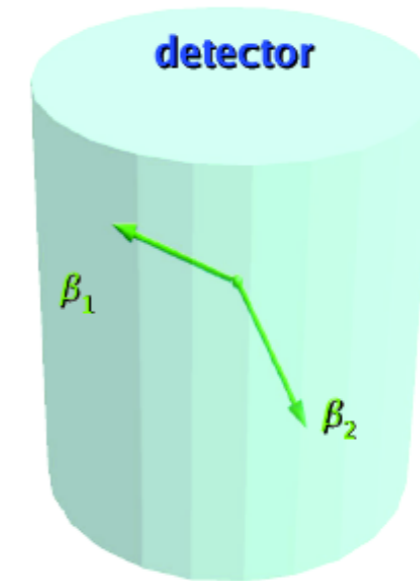
source \neq detector



+++ Topology, Bkgd(2 $\nu\beta\beta$ exception)
 --- M, ΔE , ϵ

Calo-tracko detectors
 (NEMO, MOON, DCBA)

source = detector



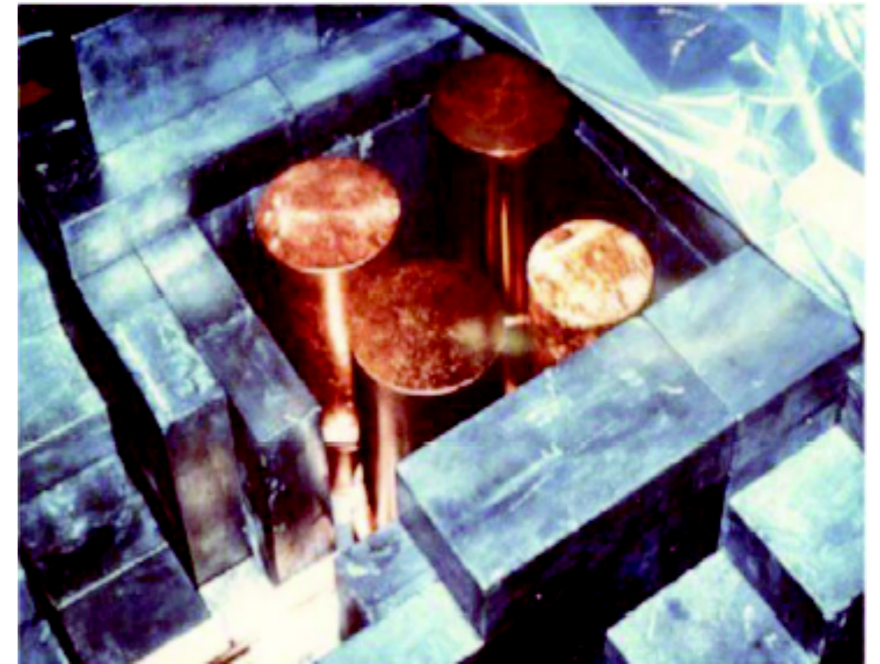
+++ M, ΔE , ϵ
 --- Topology, Bkgd(2 $\nu\beta\beta$ exce.)

Diodes (MAJORANA, GERDA)
 Bolometers (CUORE, LUCIFER)
 Solid-state devices scintillators (COBRA)
 Solid scintillators (CANDLES)
 Liquid loaded scintillator (SNO++, Kamland)
 Gaseous/Liquid TPC (EXO)

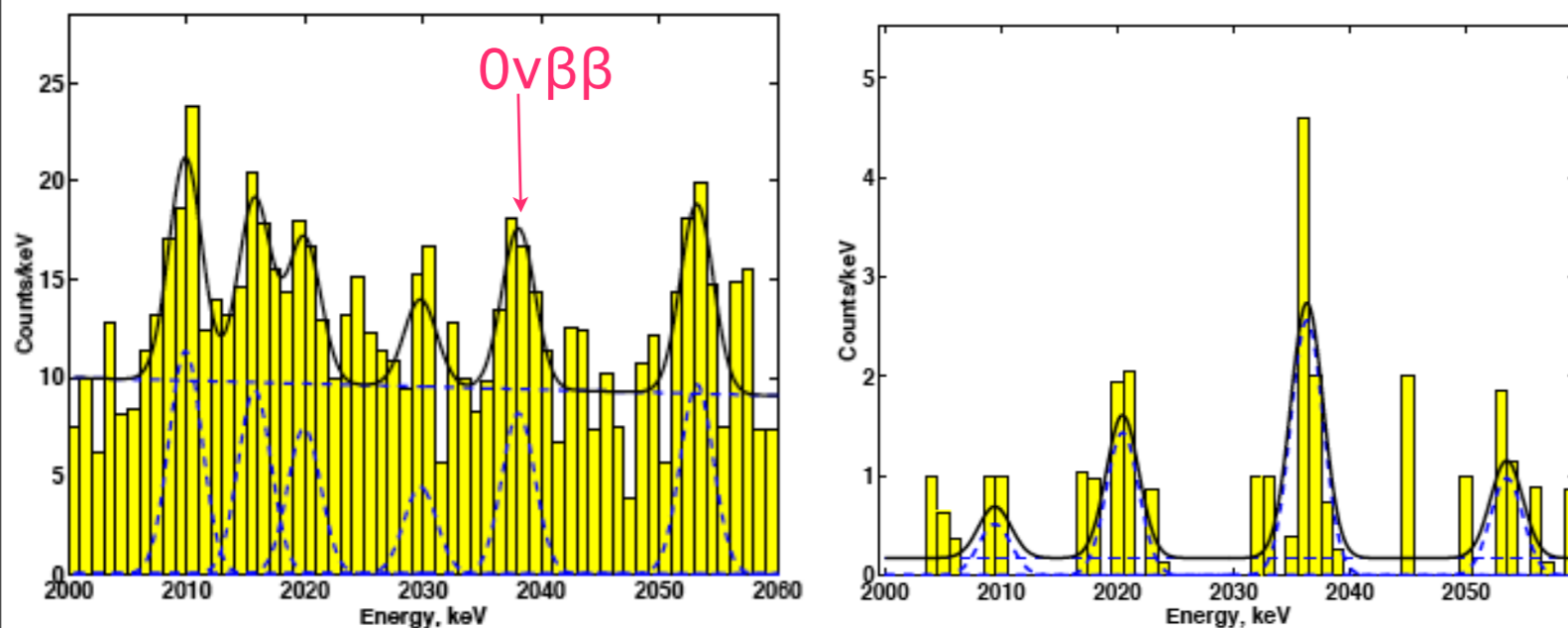
HEIDELBERG-MOSCOW: KLAPDOR CLAIM

source = detector

- 5 HP-Ge diodes: 10.9 kg (86% enriched ^{76}Ge)
- Exposure: 53.9 kg y (1990-2001)
- $\Delta E_{\text{FWHM}} \sim 4 \text{ keV}$ @ $Q_{\beta\beta} \approx 2039 \text{ keV}$
- $\tau^{0\nu}_{1/2} > 1.9 \cdot 10^{25} \text{ y} \Leftrightarrow \langle m_{\beta\beta} \rangle < 0.35 \text{ eV}$



Klapdor et al. Phys. Lett. B 586 (198) 2004



- Exposure: 71.7 kg y (1990-2003)
- Background $\sim 0.11 \text{ counts/keV/kg/y}$

$$\tau^{0\nu}_{1/2} = 1.2 \cdot 10^{25} \text{ y}$$

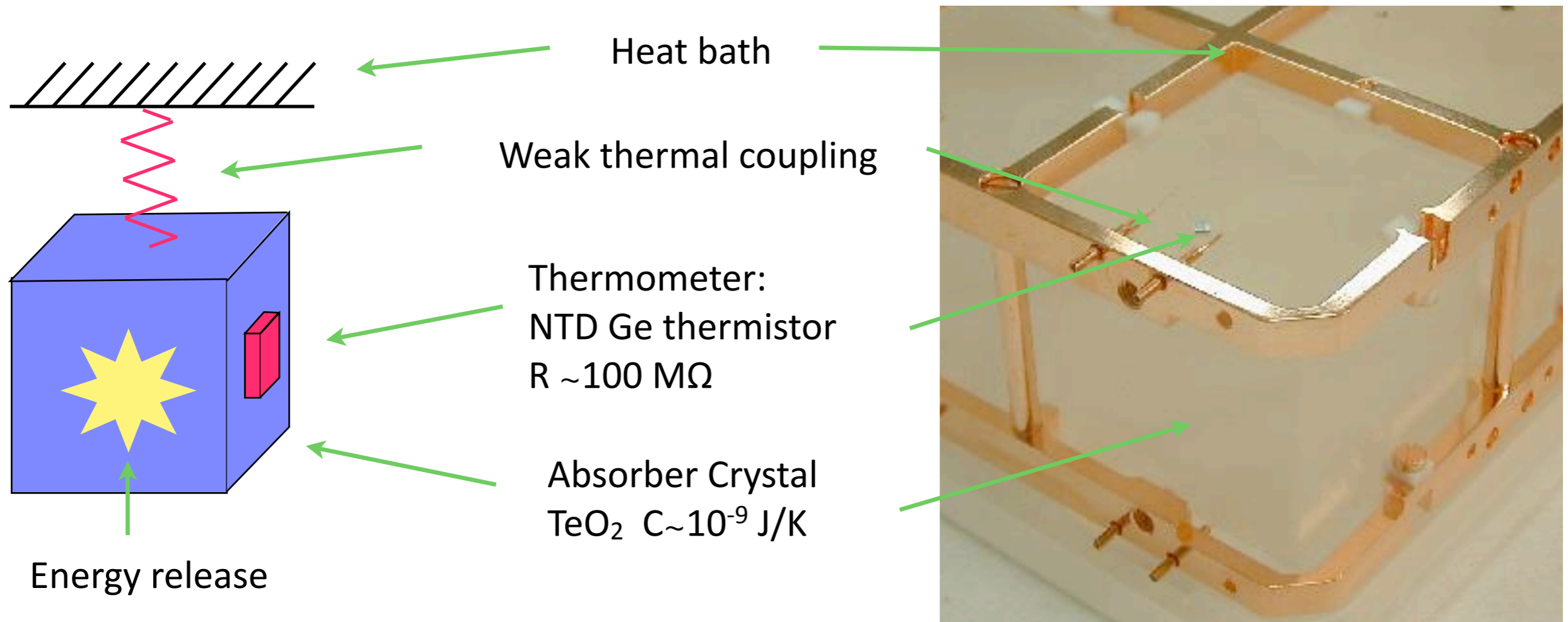
\Leftrightarrow

$$\langle m_{\beta\beta} \rangle = 0.44 \text{ eV}$$

CUORICINO

- Particle energy converted into phonons \rightarrow temperature variation $\Delta T = E/C$
- Need very low heat capacity: TeO_2 crystals (dielectric, diamagnetic) @ $\sim 8\text{mK}$

source = detector



- Detector response in this configuration: $\approx 0.1\text{ mK/MeV} \approx 0.3\text{ mV/MeV}$

CUORICINO RESULTS

- Exposure (2003-2008):

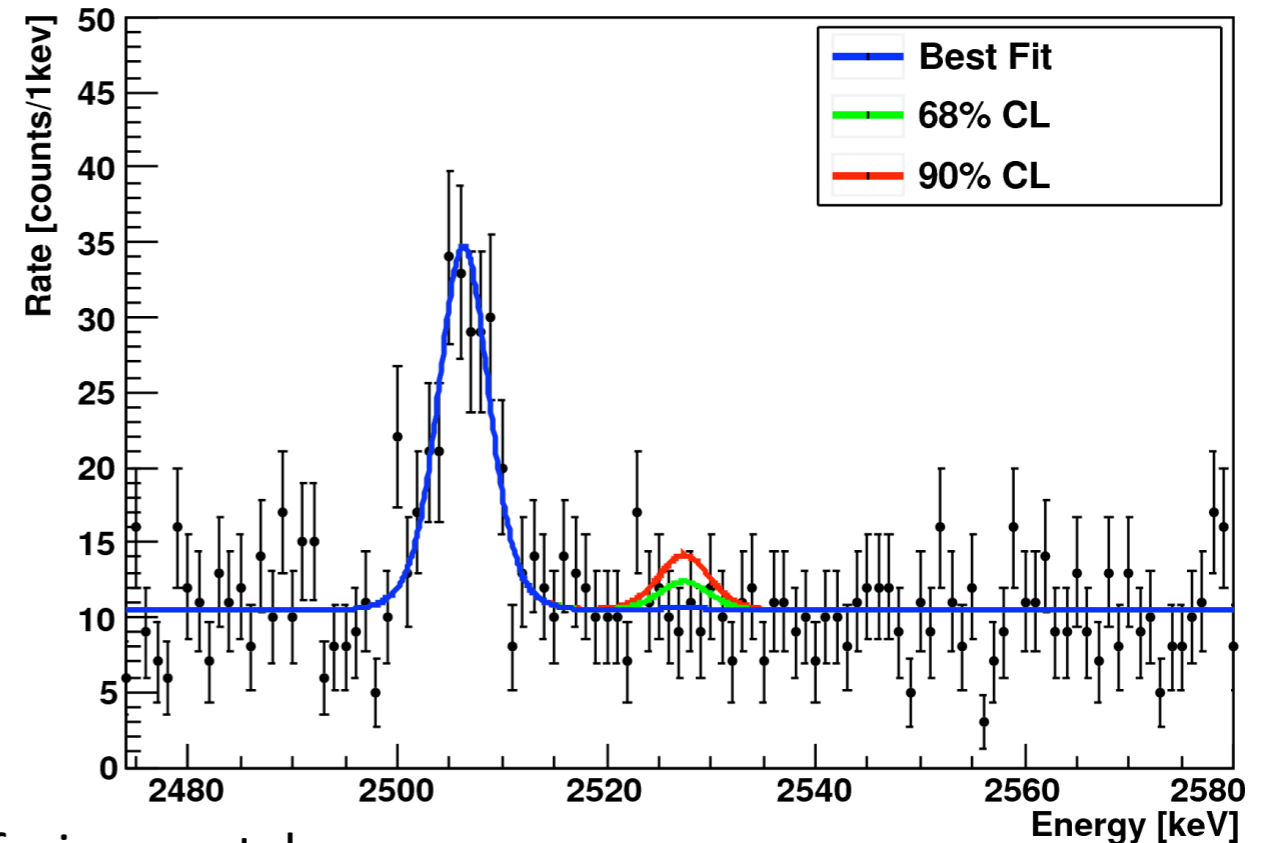
$$M \cdot t = 19.75 \text{ kg } ^{130}\text{Te} \cdot \text{y}$$

- Background level:

$$(0.16 \pm 0.01) \text{ counts/keV/kg/y}$$

- ~50% from degraded α from inert material (Cu) facing crystals
- ~40% from ^{208}Tl multi-Compton (cryostat contamination)

- $\Delta E_{\text{FWHM}} \sim 7.5 \text{ keV}$ @ $Q_{\beta\beta} \sim 2527 \text{ keV}$



$$\tau_{1/2}^{0\nu} > 2.8 \cdot 10^{24} \text{ y @90\%CL} \quad \Leftrightarrow \quad m_{\beta\beta} < 0.3 \div 0.7 \text{ eV}$$

NEMO 3

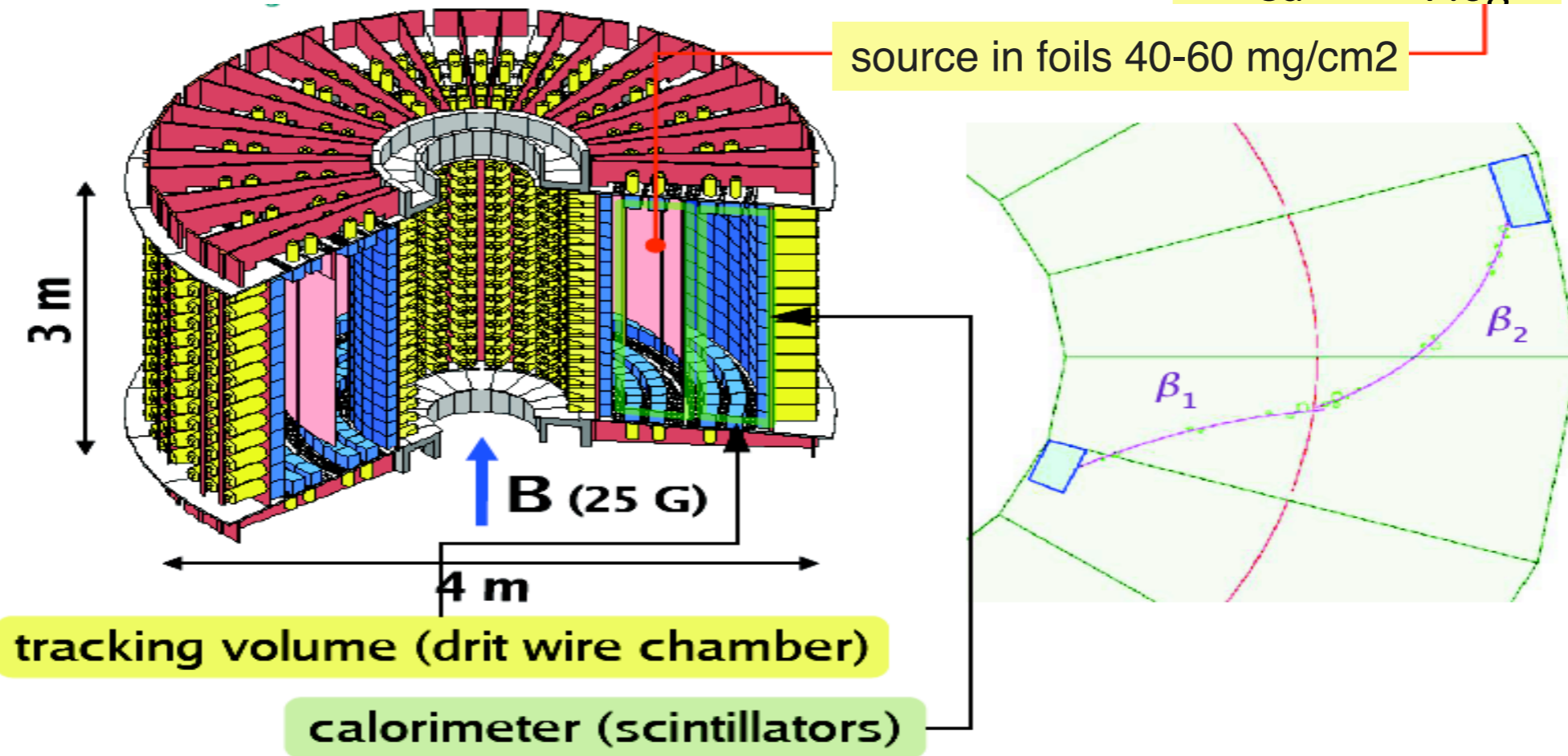
- **Tracking detector:** ~6000 Geiger mode drift chambers (95%He+4%alcohol+1%Ar)
- **Calorimeter:** ~2000 plastic scintillators + PMTs
 - $\Delta E_{FWHM}/E \sim 8\% @ 3\text{MeV}$ $\sigma_T \sim 300 \text{ ps} @ 1\text{MeV}$
 - 3-5% charge confusion

Source	Mass
^{100}Mo	6.9 kg
^{82}Se	0.9 kg
^{130}Te	0.45 kg
^{116}Cd	0.4 kg
^{150}Nd	37g
^{96}Zr	9.4g
^{48}Ca	7.0g

} $0\nu\beta\beta$

} $2\nu\beta\beta$

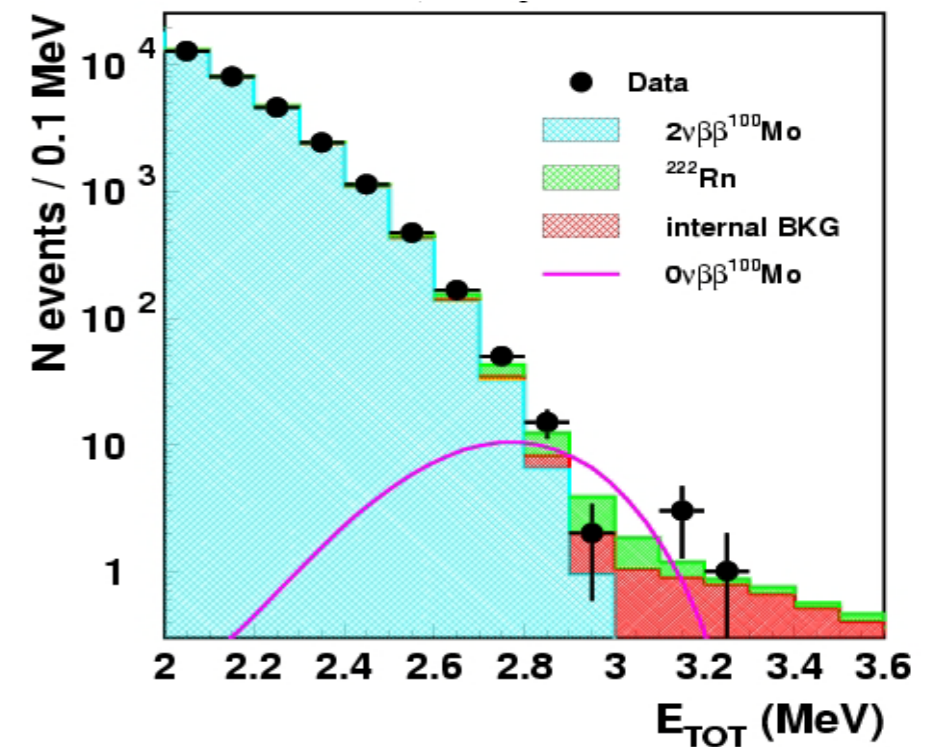
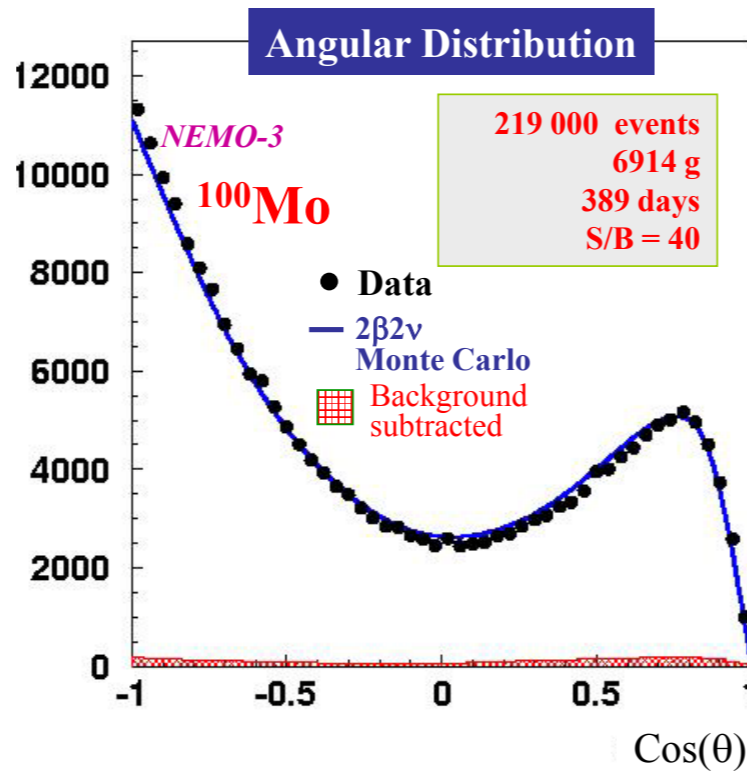
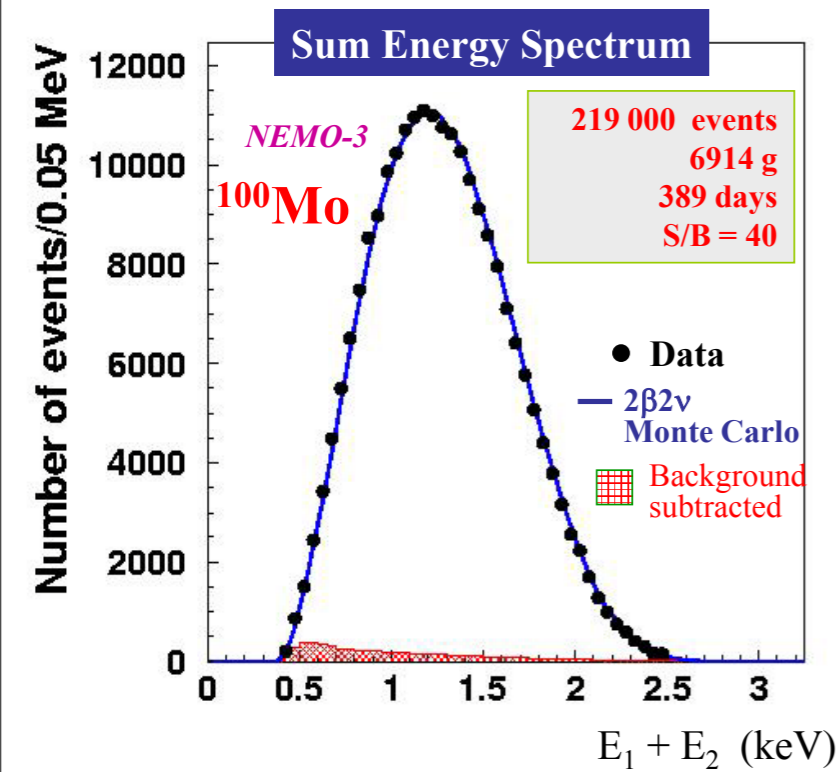
source \neq detector



NEMO 3 RESULTS

$$^{100}\text{Mo}: \tau^{2\nu}_{1/2} = (7.11 \pm 0.02 \pm 0.54) \cdot 10^{18} \text{ y}$$

$$^{100}\text{Mo}: \tau^{0\nu}_{1/2} > 1.1 \cdot 10^{24} \text{ y}$$



Isotope	Exposure (kg·y)	$T_{1/2}(0\nu\beta\beta), \text{ y}$	$\langle m_\nu \rangle, \text{ eV [NME ref.]}$
^{100}Mo	26.6	$> 1.1 \cdot 10^{24}$	$< 0.45 - 0.93$ [1-3]
^{82}Se	3.6	$> 3.6 \cdot 10^{23}$	$< 0.9 - 1.6$ [1-3]; < 2.3 [7]
^{150}Nd	0.095	$> 1.8 \cdot 10^{22}$	$< 1.7 - 2.4$ [4,5]; $< 4.8 - 7.6$ [6]
^{130}Te	1.4	$> 9.8 \cdot 10^{22}$	$< 1.6 - 3.1$ [2,3]
^{96}Zr	0.031	$> 9.2 \cdot 10^{21}$	$< 7.2 - 19.5$ [2,3]
^{48}Ca	0.017	$> 1.3 \cdot 10^{22}$	< 29.6 [7]

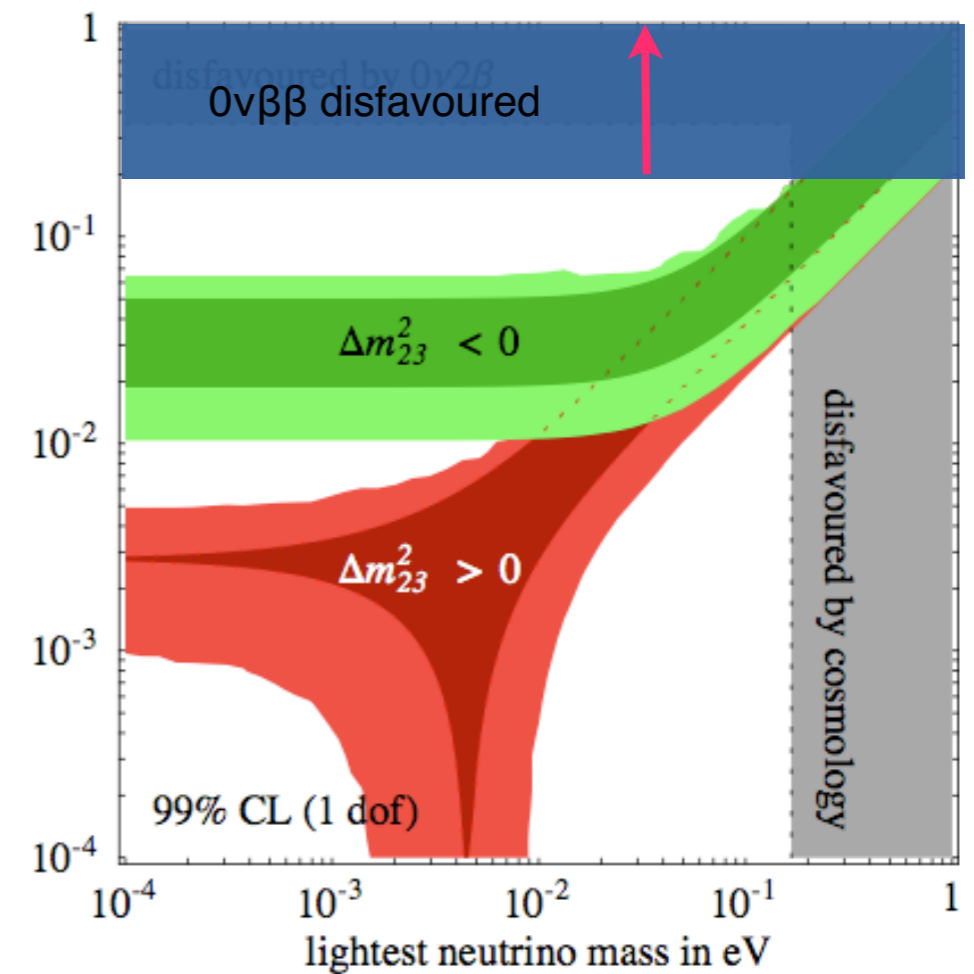
Isotope	S/B	$(2\nu\beta\beta), \text{ y (NEMO 3)}$
^{100}Mo	40	$(7.11 \pm 0.02(\text{stat}) \pm 0.54(\text{syst})) \cdot 10^{18}$ (SSD favoured) [1]
$^{100}\text{Mo}(0^+_1)$	3	$(5.7^{+1.3}_{-0.9}(\text{stat})) \pm 0.8(\text{syst}) \cdot 10^{20}$ [2]
^{82}Se	4	$(9.6 \pm 0.3(\text{stat}) \pm 1.0(\text{syst})) \cdot 10^{19}$ [1]
^{116}Cd	7.5	$(2.8 \pm 0.1(\text{stat}) \pm 0.3(\text{syst})) \cdot 10^{19}$ [3]
^{130}Te	0.35	$(6.9 \pm 0.9(\text{stat}) \pm 1.0(\text{syst})) \cdot 10^{20}$ [6]
^{150}Nd	2.8	$(9.11^{+0.25}_{-0.22}(\text{stat}) \pm 0.63(\text{syst})) \cdot 10^{18}$ [4]
^{96}Zr	1.0	$(2.35 \pm 0.14(\text{stat}) \pm 0.16(\text{syst})) \cdot 10^{19}$ [5]
^{48}Ca	6.8	$(4.4^{+0.5}_{-0.4}(\text{stat}) \pm 0.4(\text{syst})) \cdot 10^{19}$ [6]

Background: natural radioactivity, mainly ^{214}Bi and ^{208}Tl , Rn, neutrons (n,γ), muons

FUTURE STRATEGIES

$$S^{m_{\beta\beta}} = \left(\frac{A}{\ln 2 N_A a \epsilon G} \right)^{1/2} \frac{1}{|M_{nucl}|} \left(\frac{B \Delta E}{Mt} \right)^{1/4}$$

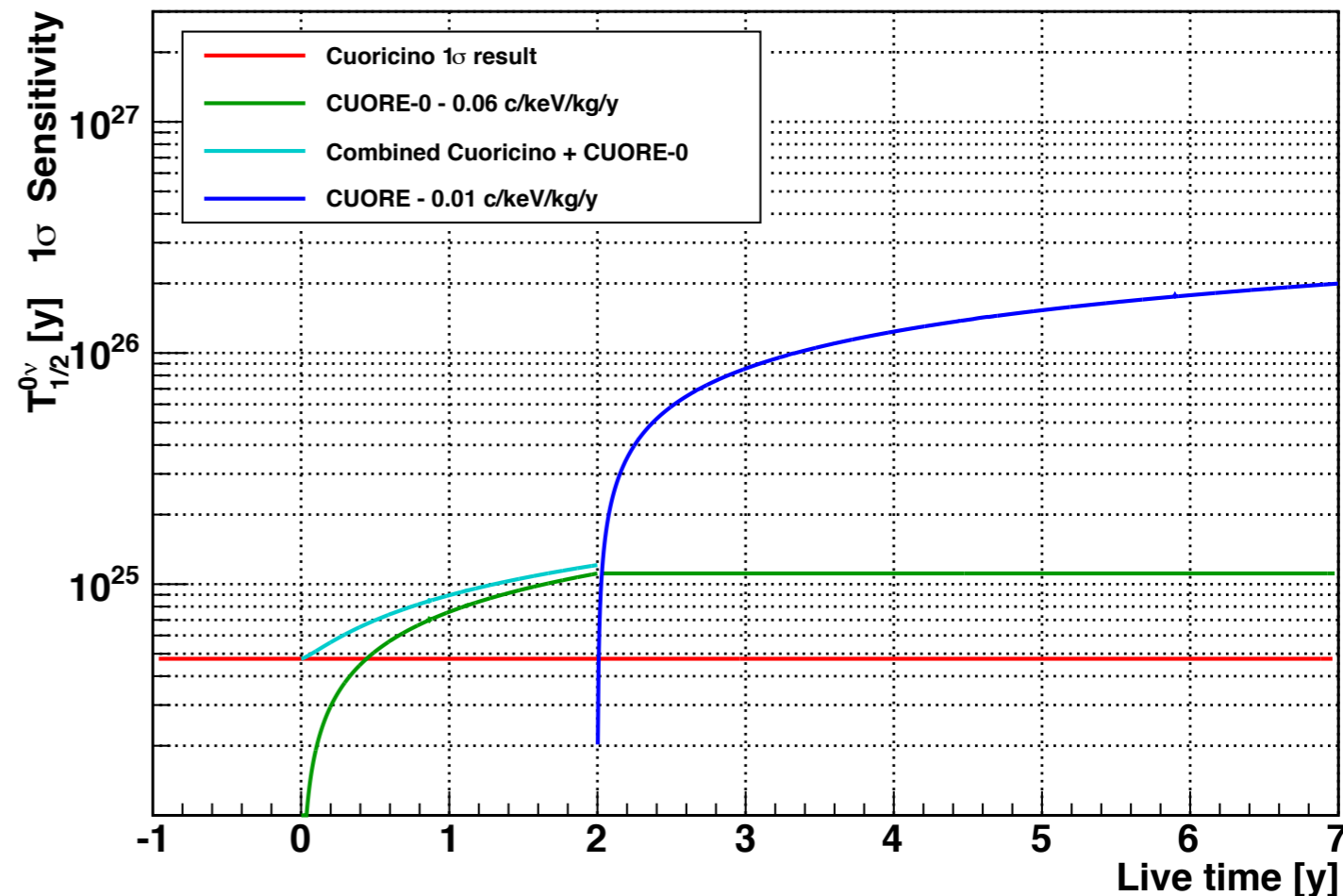
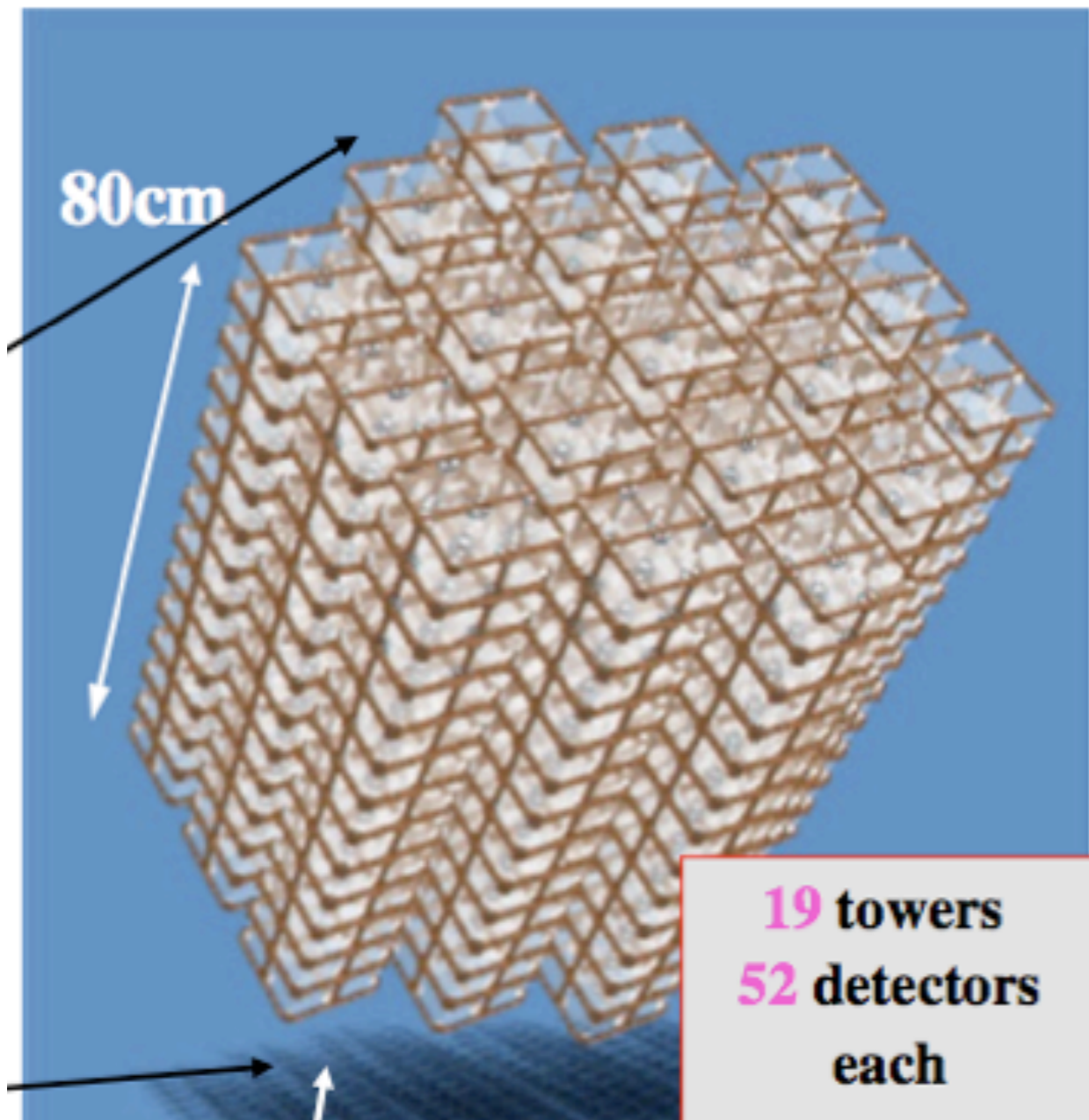
- Enrichment: difficult and expensive
- To start to explore(cover) inverted hierarchy:
 - $M \sim 0.1(1)$ Ton
 - $B \sim 10^{-2}(10^{-3})$ counts/keV/kg/y
- Background sources:
 - Natural radioactivity: U, Th ($\tau \sim 10^{10}$ y) in detector and surroundings
 - ➔ Contamination $\sim 10^{-13}$ g/g (close or below detectability of HPGE, NAA, ICPMS)
 - Neutrons: from radioactivity and muon-induced
 - Cosmic rays: (in)direct interaction and activation



CUORE

source = detector

Closed packed array of 988 TeO_2 crystals $\approx 200 \text{ Kg } ^{130}\text{Te} \sim 10^{27}$ nuclides



Background: 10^{-2} counts/keV/kg/y

$$T_{1/2}^{0\nu} = 2.0 \cdot 10^{26} \text{ y}$$

$$\langle m_{\beta\beta} \rangle = 44-87 \text{ meV}$$

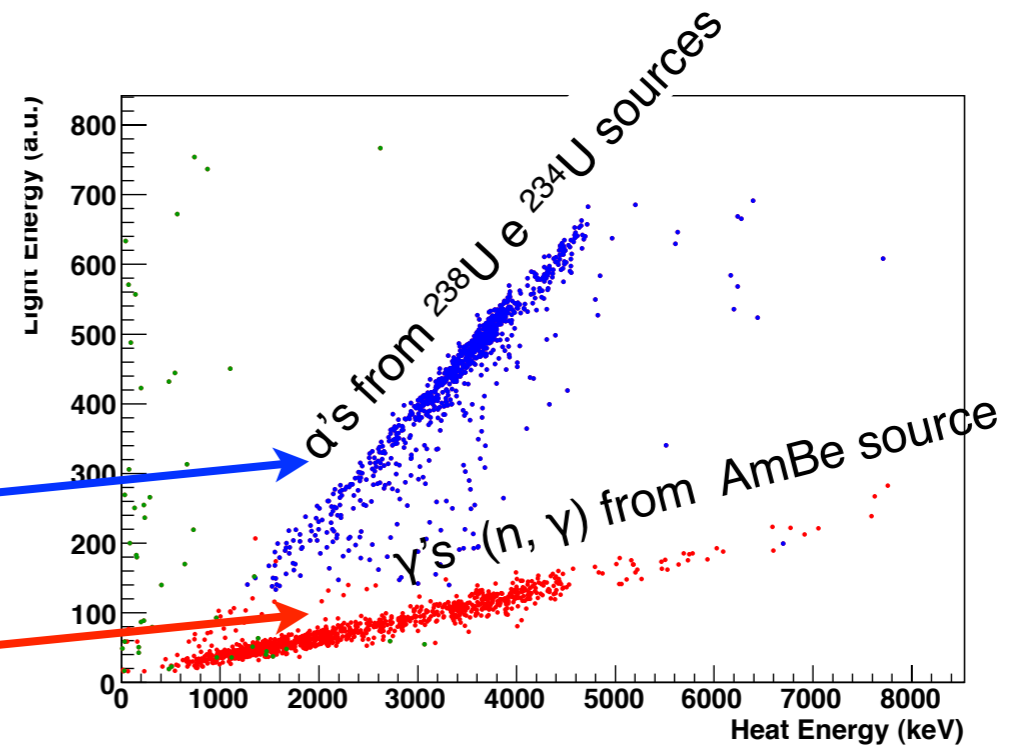
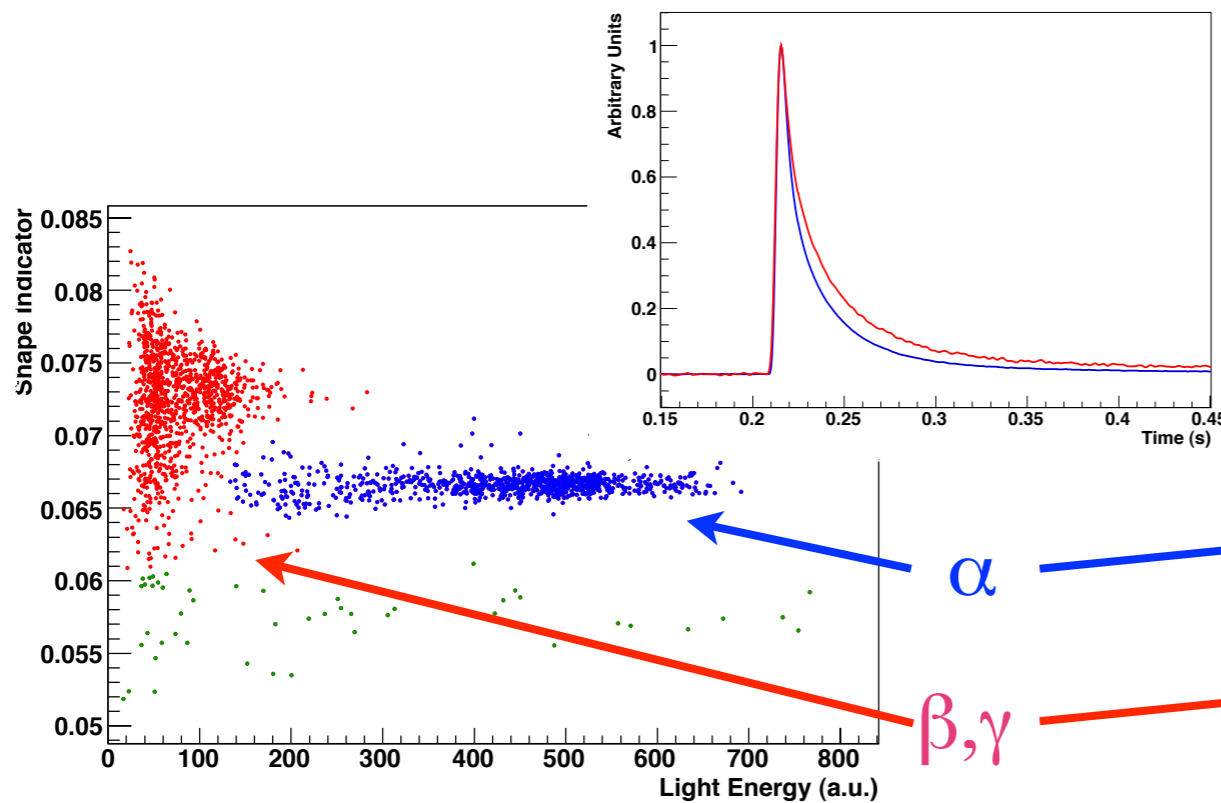
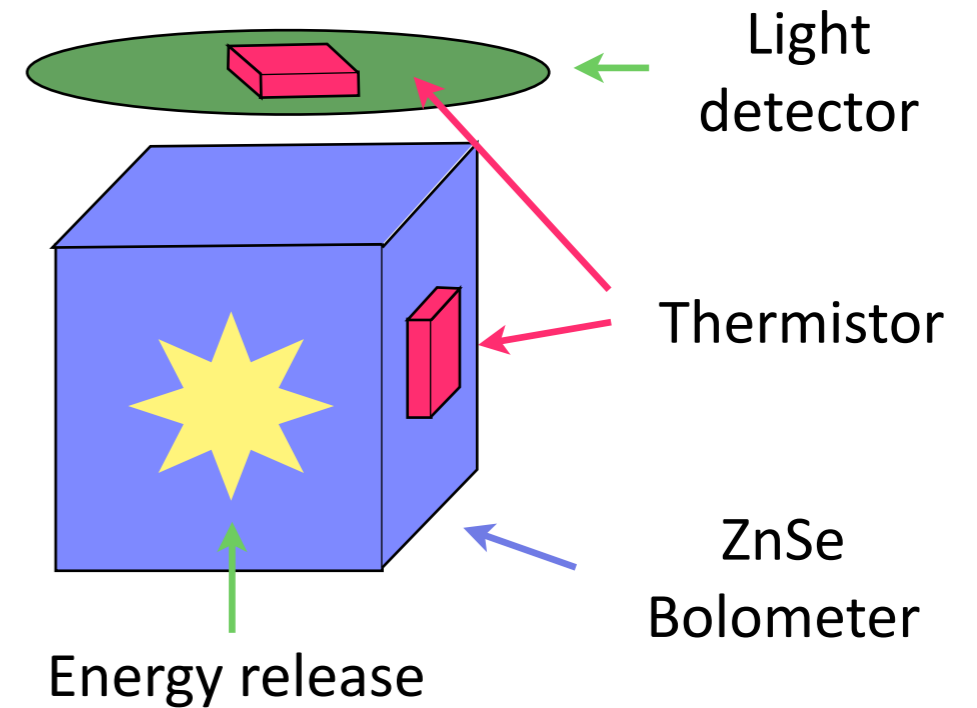
LUCIFER

- **Scintillating bolometers:** use different α/γ light emission for background discrimination

- Quenching factor ≈ 4
- α discrimination $>99\%$
- ≈ 20 kg ^{82}Se + background 10^{-3} counts/kg/keV/y

$$\tau^{0\nu}_{1/2} = 2.3 \cdot 10^{26} \text{ y}$$

$$\langle m_{\beta\beta} \rangle = 49\text{-}61 \text{ meV}$$



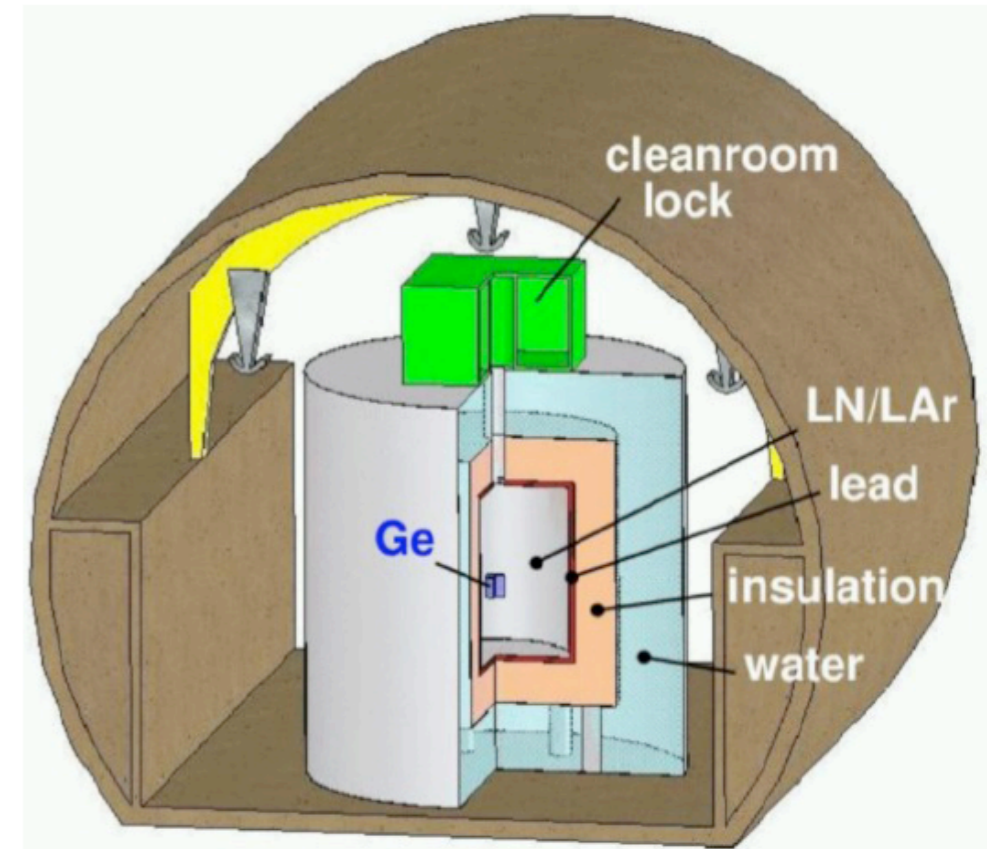
GERDA

- Background: detector surroundings & Ge cosmogenic activation

source = detector

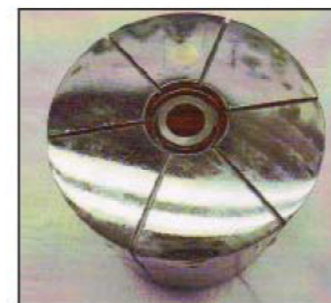
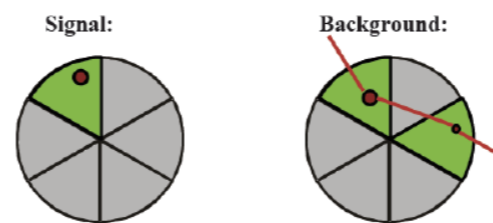
- Phase 1:

- 18 kg bare (HM+IGEX) ^{76}Ge diodes in LAr
- Background $\sim 10^{-2}$ counts/keV/kg/y
- Scrutinize KK-HM claim in 1 year
- Commissioning started Nov 2010



- Phase 2:

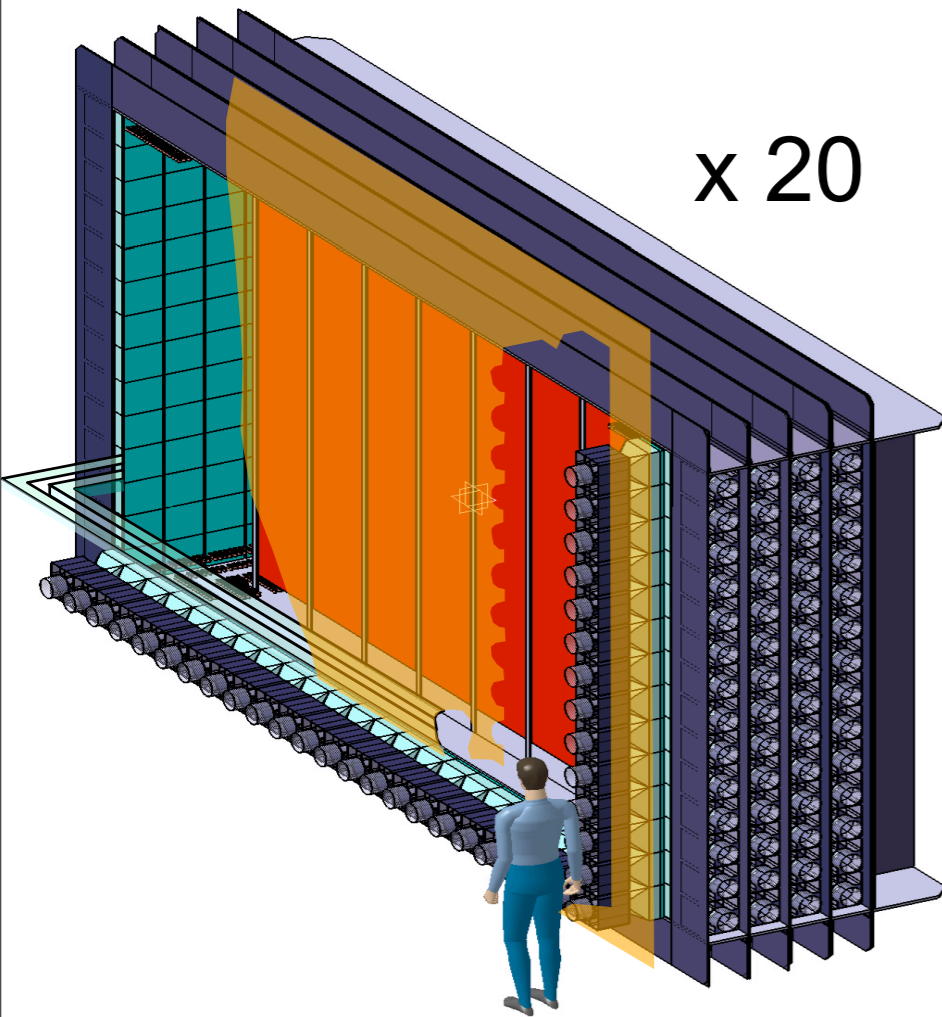
- 40 Kg enriched segmented diodes
- Background $\sim 10^{-3}$ counts/keV/kg/y
- Sensitivity: $\tau^{0\nu}_{1/2} \sim 2 \cdot 10^{26}$ y
 $\langle m_{\beta\beta} \rangle < 90-200$ meV



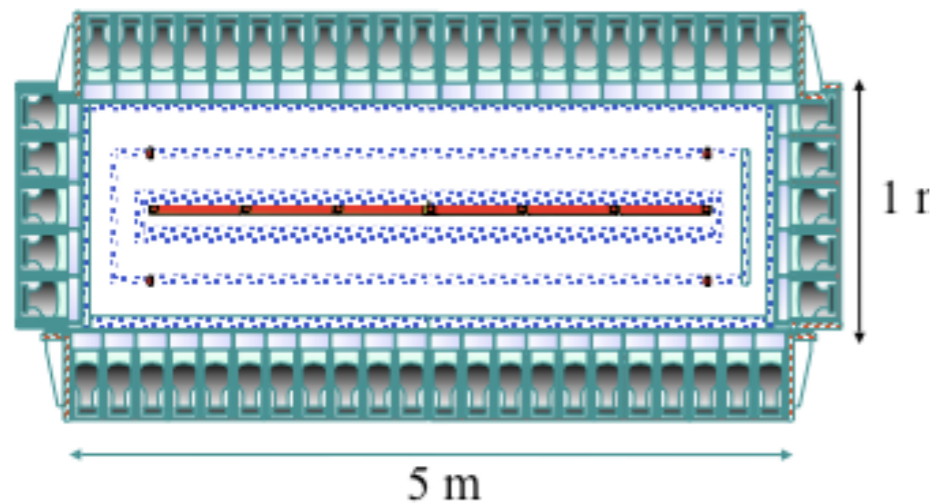
SUPERNEMO

source ≠ detector

First prototype module in 2011



x 20



NEMO-3

SuperNEMO

^{100}Mo
 $T_{1/2}(\beta\beta 2\nu) = 7 \cdot 10^{18} \text{ y}$

Choice of isotope

^{82}Se (and/or ^{150}Nd)
 $T_{1/2}(\beta\beta 2\nu) = 10^{20} \text{ y}$

7 kg

Isotope mass **M**

100 - 200 kg

$\epsilon(\beta\beta 0\nu) = 8 \%$

Efficiency **ϵ**

$\epsilon(\beta\beta 0\nu) \sim 30 \%$

$^{214}\text{Bi} < 300 \mu\text{Bq/kg}$
 $^{208}\text{Tl} < 20 \mu\text{Bq/kg}$
 $(^{208}\text{Tl}, ^{214}\text{Bi}) \sim 1 \text{ evt/ 7 kg /y}$

$N_{\text{exclu}} = f(\text{BKG})$
Internal contaminations
 ^{208}Tl and ^{214}Bi in the $\beta\beta$ foil

$^{214}\text{Bi} < 10 \mu\text{Bq/kg}$
 $^{208}\text{Tl} < 2 \mu\text{Bq/kg}$
 $(^{208}\text{Tl}, ^{214}\text{Bi}) \sim 1 \text{ evt/ 100 kg /y}$

FWHM(calor)=8% @3MeV

$2\nu\beta\beta$

FWHM(calor)=4% @3MeV

$T_{1/2}(\beta\beta 0\nu) > 2 \cdot 10^{24} \text{ y}$
 $\langle m_\nu \rangle < 0.3 - 0.7 \text{ eV}$

SENSITIVITY

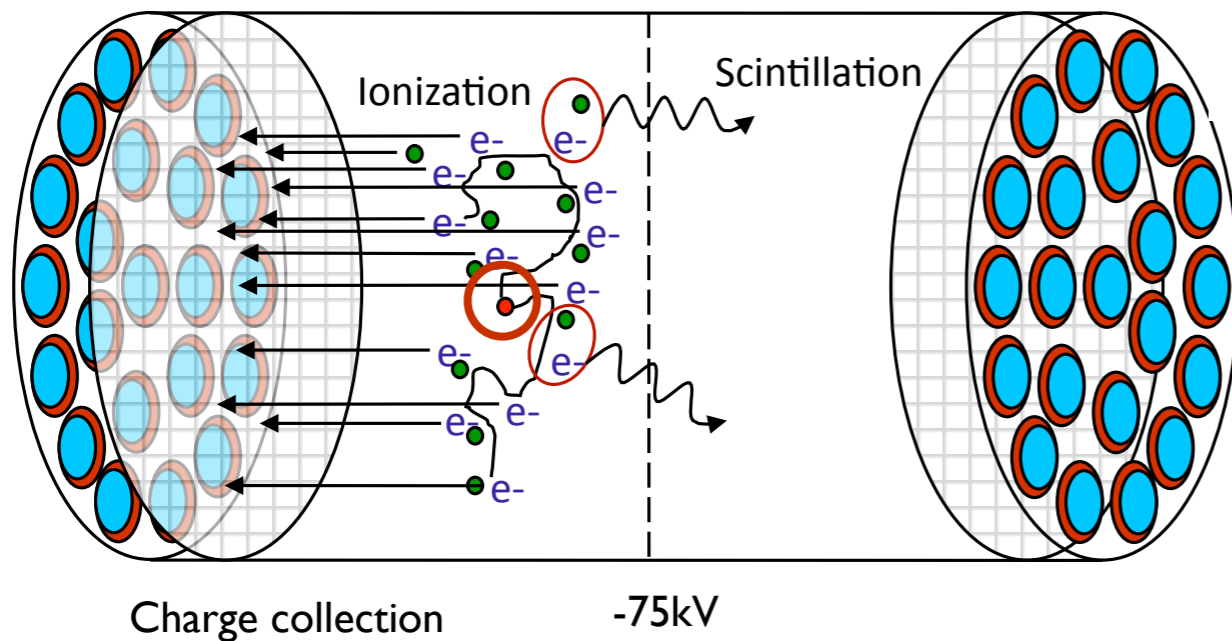
$T_{1/2}(\beta\beta 0\nu) > 2 \cdot 10^{26} \text{ y}$
 $\langle m_\nu \rangle < 50 \text{ meV}$

- 1) $\beta\beta$ source production
- 3) Radiopurity

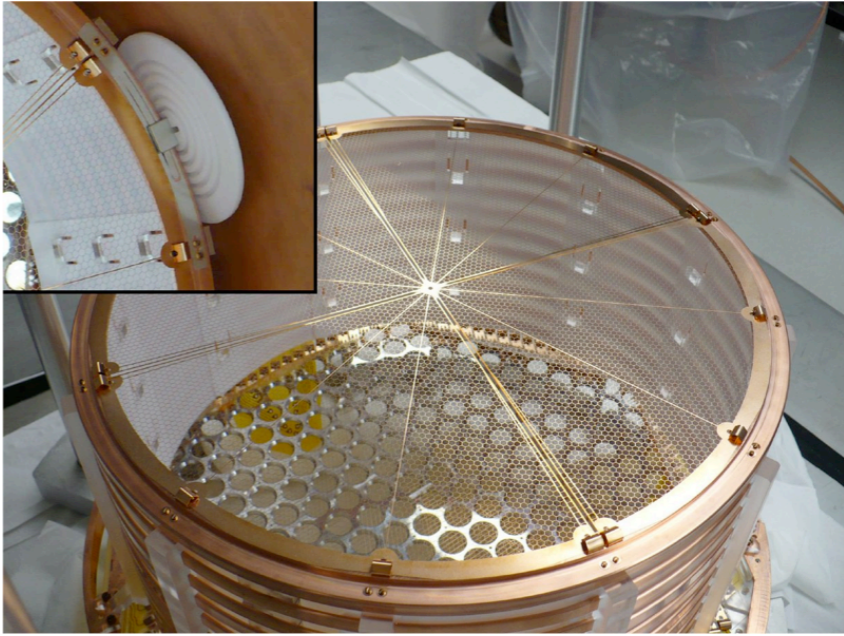
- 2) Energy resolution
- 4) Tracking

EXO-200

- 200 kg Liquid (80% ^{136}Xe) Xe TPC + scintillation: $^{136}\text{Xe} \rightarrow ^{136}\text{Ba}^{++} + 2e^- (+ 2\nu_e)$

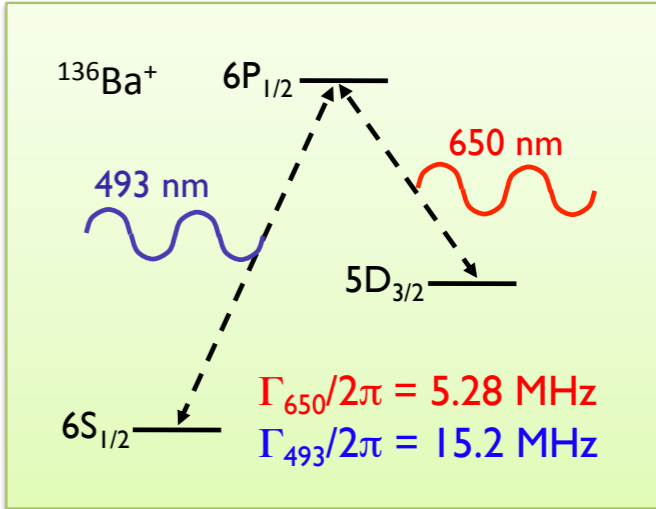


source = detector



Mass (ton)	Eff. (%)	Run Time (yr)	σ_E/E @ 2.5MeV (%)	Radioactive Background (events)	$T_{1/2}^{0\nu\beta\beta}$ (yr, 90%CL)	$m_{\beta\beta}$ (meV)
0.2	70	2	1.6	40	6.4×10^{25}	133-186

$^{136}\text{Ba}^+$ level structure



- Full EXO ~Ton scale gas or liquid TPC
- Single Ba^+ tagging in real time
 - Ion extraction from TPC and trapping
 - Ion identification with Laser Induced Fluorescence

LOADED LIQUID SCINTILLATORS

- Poor resolution but high mass and low background compensate

source = detector

Data taking foreseen in 2011

SNO++

^{150}Nd (i.a.=5.6%)

0.1% natural load Nd ~ 56 kg ^{150}Nd

$\Delta E_{\text{FWHM}} \sim 6.4\%$ @ 3367 keV

Sensitivity(3y): $\langle m_{\beta\beta} \rangle \sim 100$ meV

Kamland -Xe

^{136}Xe (i.a.=8.9%)

200-400 kg enriched ^{136}Xe

$\Delta E_{\text{FWHM}} \sim 5\%$ @ 2479 keV

Sensitivity(5y): $\langle m_{\beta\beta} \rangle < 150$ meV

Simulated SNO+ Energy Spectrum

