Particle Physics - Chapter 10 LEP — e⁺e⁻ physics



Paolo Bagnaia SAPIENZA UNIVERSITÀ DI ROMA

AA 1**3-19**

last mod. 16-May-19

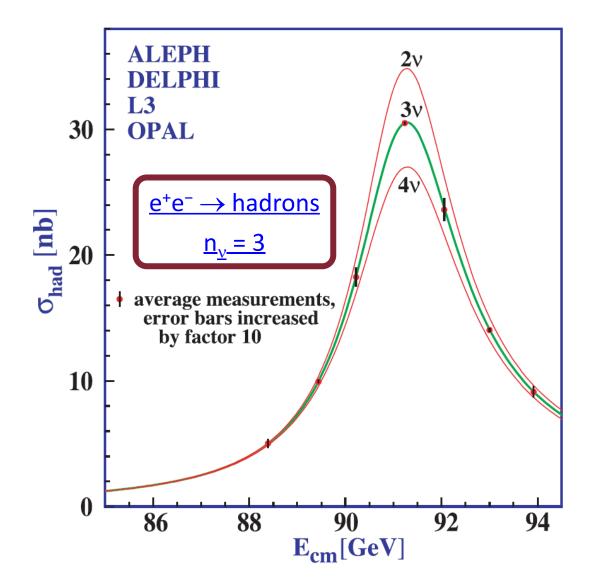
10 – LEP – e⁺e⁻ physics

i. Machine & detectors

- 1. The LEP Collider
- 2. Detectors
- 3. The L3 detector
- 4. LEP events
- ii. Exp. metods
 - 5. Data analysis
 - 6. Secondary verteces
 - 7. Efficiency and purity
 - 8. The luminosity

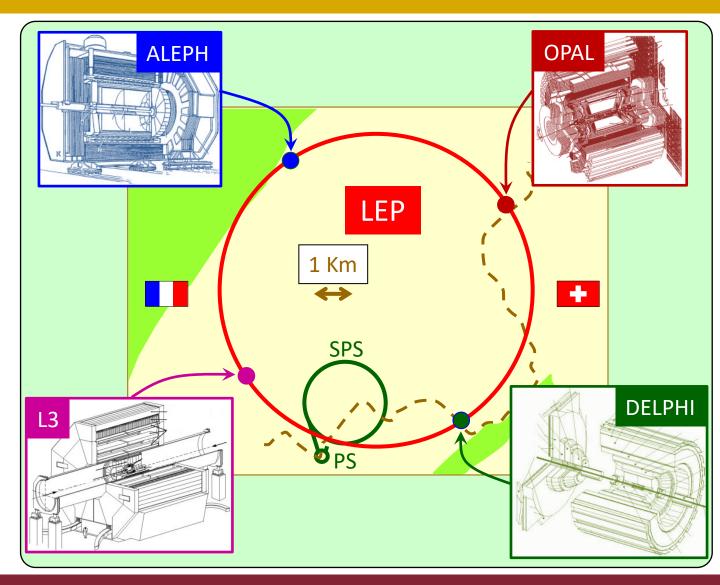
iii. Physics 1: Z & W

- 9. $e^+e^- \rightarrow Z \rightarrow f\bar{f}$
- 10. $d\sigma(e^+e^- \rightarrow f\bar{f}) / d\Omega$
- 11. $e^+e^- \rightarrow Z \rightarrow e^+e^-$
- 12. Radiative corrections
- 13. LEP1 SM fit
- 14. $e^+e^- \rightarrow W^+W^-$ @ LEP2
- 15. Global LEP(1+2) fit
- iv. Physics 2 : Higgs searches at LEP
 - 16. Search at LEP1
 - 17. Search at LEP2

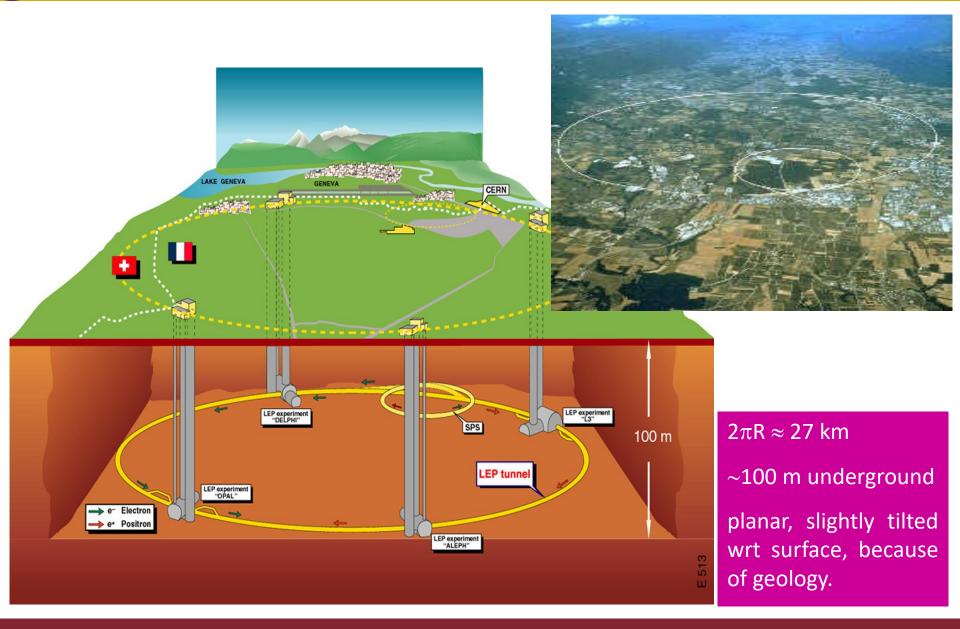


i. Machine & Detectors

- 1. The LEP Collider
- 2. Detectors
- 3. The L3 detector
- 4. LEP events
- 5. 16. [...]

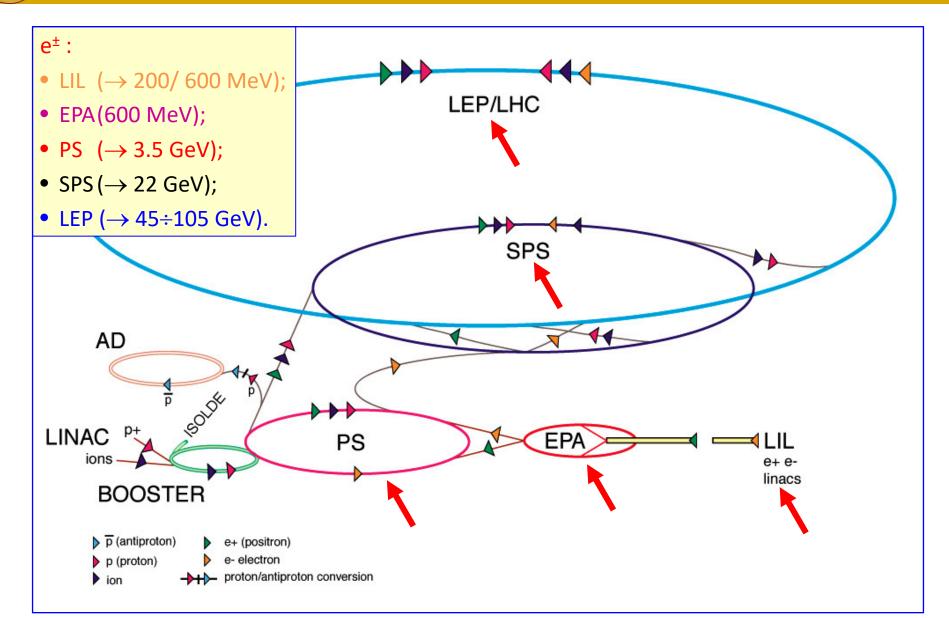


The LEP collider



2/9

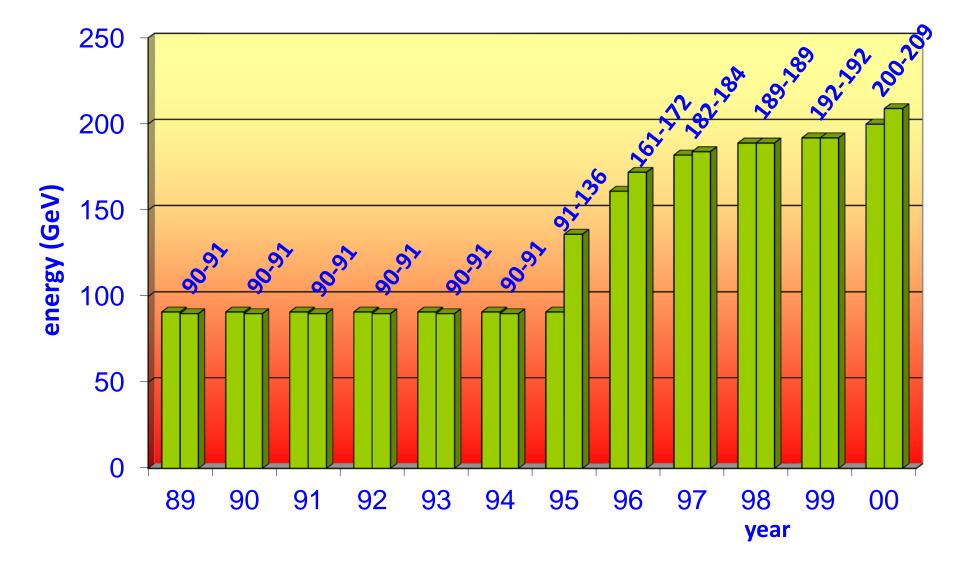
The LEP collider : e[±] acceleration



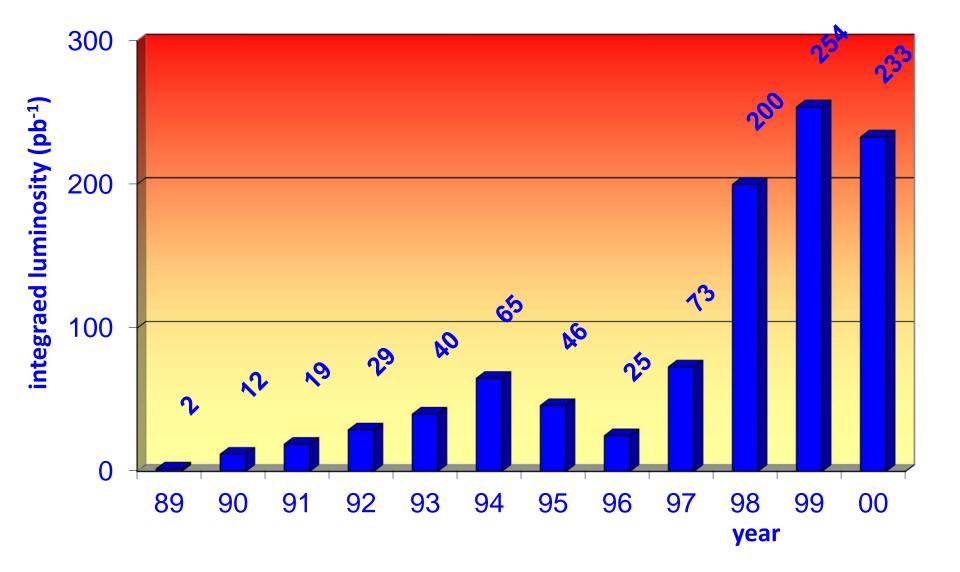
1	-		
Þ		1	
Þ		1	2

	LEP 1	LEP 2
Circumference (Km)	26.66	same
E _{max} / beam (GeV)	50	105
max lumi £ (10 ³⁰ cm ⁻² s ⁻¹)	~25	~100
time between collisions (µs)	22 (11)	22
packet length (cm)	1.8	
packet radius (hori.) (µm)	200÷300	
packet radius (vert.) (µm)	2.5÷8	
injection energy (GeV)	22	same
particles/packet (10 ¹¹)	4.5	same
packet number	4+4 (8+8)	4+4
years	1989-1995	1996-2000

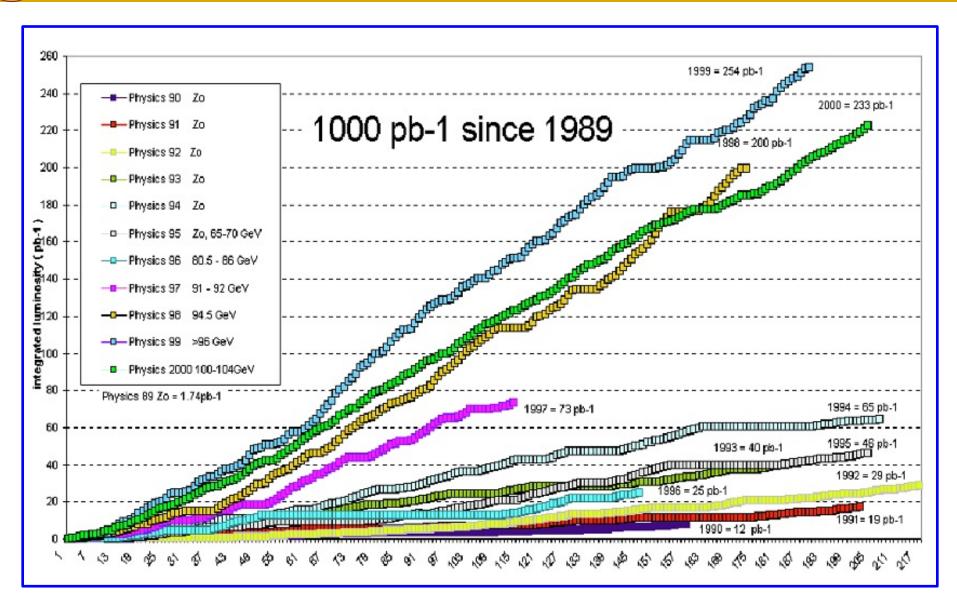




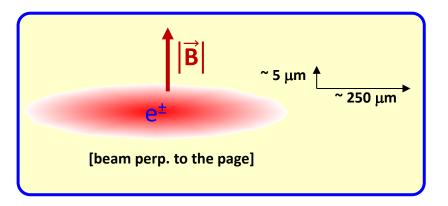




The LEP collider: \mathcal{L}_{int} vs day



- $\Delta E_{orbit} \propto e^2 E^4 / (M^4 R)$; [§ 8]
- $> \Delta E^{e_{orbit}}(MeV) = 8.85 \times 10^{-5} E^4 (GeV) / R (Km);$
- $\langle R_{LEP} \rangle = 4.25 \times 10^3 \text{ m} (\rightarrow \text{see table});$
- in QED, the bremsstrahlung is not deterministic; the formula gives the average; a further (annoying) effect is the increase of emittance, i.e. the increase of the packets both in space and momentum; this effect is greater in the horizontal plane, as an effect of the magnetic bending:
 - $\succ~\sigma_{hori}~$ = 200 \div 300 $\mu m;$
 - $\succ \sigma_{vert} = 2.5 \div 8 \,\mu m.$



E _{beam} (GeV)	√s (GeV)	∆E _{orbit} (GeV)
45	90	~0.1
90	180	~1.4
100	200	~2.1

The LEP collider: *Leftective*

- Assume $\mathcal{L}_{max} = 2 \times 10^{31} \text{ cm}^{-2} \text{ s}^{-1}$:
- $\sigma_{tot}(e^+e^- \rightarrow Z, \sqrt{s=m_Z}) \approx 40 \text{ nb}$:
 - ≻ $R_{max}(e^+e^- \rightarrow Z, \sqrt{s=m_Z}) = 𝔅 σ_{tot} = 0.8 Hz;$
 - > 6×10⁴ events / day → 10⁷ events/ year;
 - ▶ [??? no !!!];
- ... because ...
- the luminosity normally quoted corresponds to the "peak lumi.", i.e. the first minutes after acceleration and squeezing;
 - $\mathfrak{L}(t) = \mathfrak{L}_{max} \exp(-t/\tau)$ (stochastic effects + optics corrections)
 - \rightarrow < $\mathfrak{L} \approx \frac{1}{2} \mathfrak{L}_{max}$
 - + techn. stops, maintenance, mistakes, ...
- global efficiency ~ ¼

• also data @ $\sqrt{s} \neq m_z$ (e.g. to measure the lineshape), where σ much smaller.

 \Rightarrow @ LEP 1 :

 4×10^6 hadronic events $\times 4 \exp =$

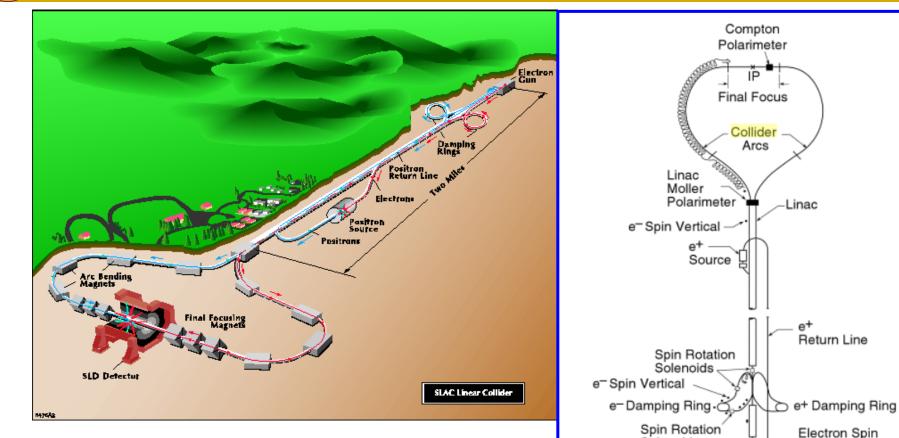
= 15.5 \times 10⁶ hadronic events

+ the corresponding leptons.

Problem: use the formulæ of § 8 and the LEP parameters to compute \mathscr{L}_{bc} and μ (= \mathscr{P}_{int}). Comment on TDAQ requirements. Is LEP trigger/DAQ "easy" or "difficult" ? [please think before answering]

The LEP collider : the competition - SLC





SLC : Stanford Linear Collider (1989-98):

- the first example of linear e⁺e⁻ collider;
- lower energy (only Z pole) and less intense;
- polarized beams;
- promising new technique ($\sqrt{s} > 500 \text{ GeV} \rightarrow a \text{ circular } e^+e^-$ requires a huge ring).

Solenoid

Thermionic

Source

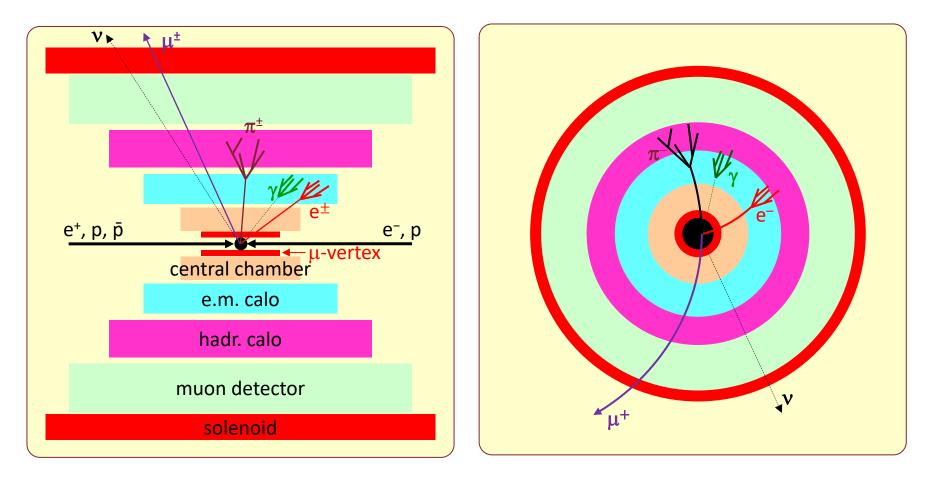


Direction

Polarized

e⁻ Source

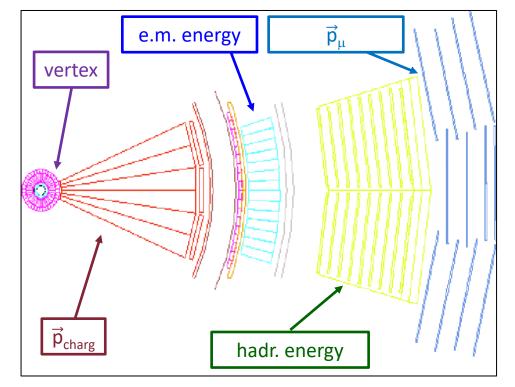
Detectors



A typical detector of LEP / TeVatron / LHC (ATLAS is the only remarkable exception).

Notice both the possible measurement of E, \vec{p} and the particle id. capability.

Detectors: principles



A detector fully operational allows for both the measurement of the 4-momenta of all the particles and their identification ("*part.id*"). The charge is measured by the sign of the bending.

	\vec{p}_{charg}	E _{em}	E _h	\vec{p}_{μ}	sec. vtx. ?
e [±]	yes	yes	~no	no	yes
γ	no	yes	~no	no	diff.
π [±] , K [±]	yes	small	yes	no	yes
n, K ⁰	no	small	yes	no	diff.
μ±	yes	mip	mip	yes	yes
ν	no (but <i>hermeticity</i>)				

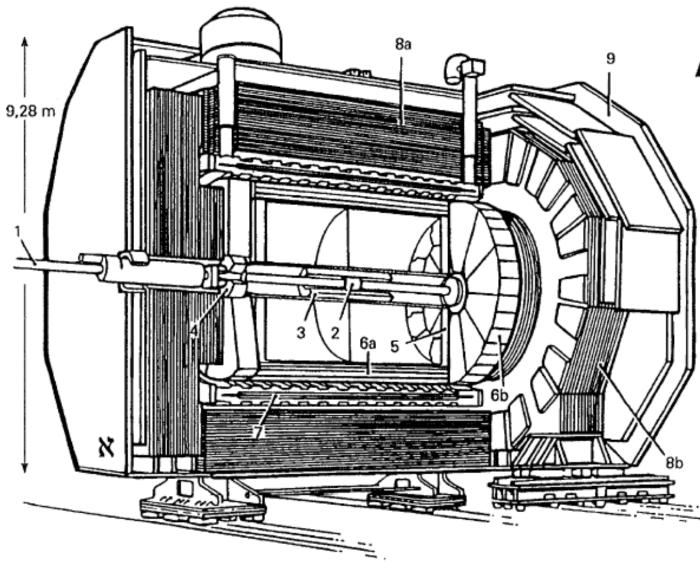
The ν 's are "detectable" from the conservation of the 4-momentum, i.e. :

$$\begin{cases} \vec{p}_{v} = -\sum_{all} \vec{p}_{j}; \\ E_{v} = \sqrt{s} - \sum_{all} E_{j}; \end{cases} \quad \left[\bigoplus m_{v}^{2} = E_{v}^{2} - |\vec{p}|_{v}^{2} = 0 \right]. \end{cases}$$

Problem : what happens if there are two v's in the final state ? An interesting question ... and not uncommon $[Z \rightarrow \tau\tau, ZH \rightarrow v\bar{v}b\bar{b}]$.



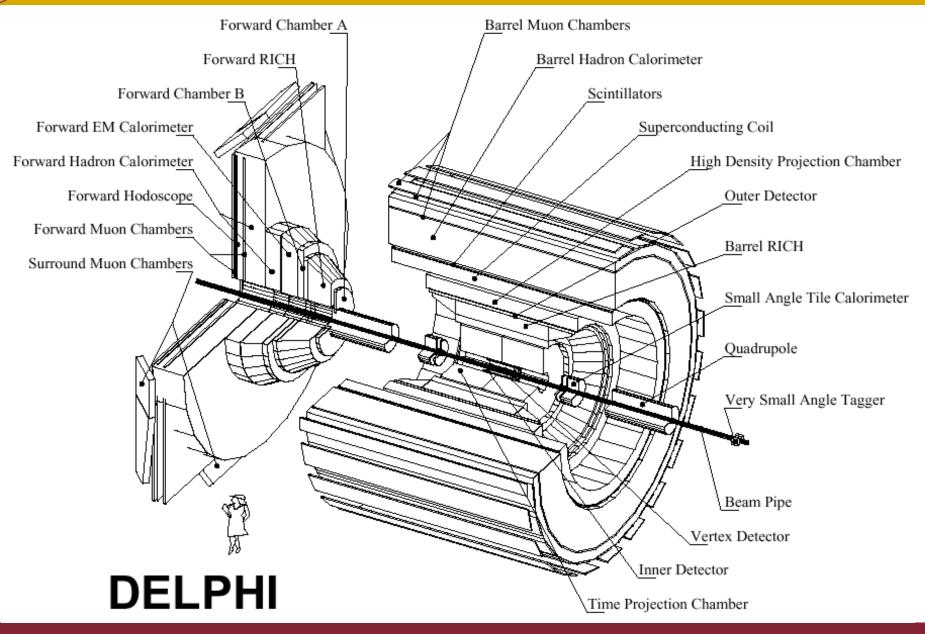
X : Detectors



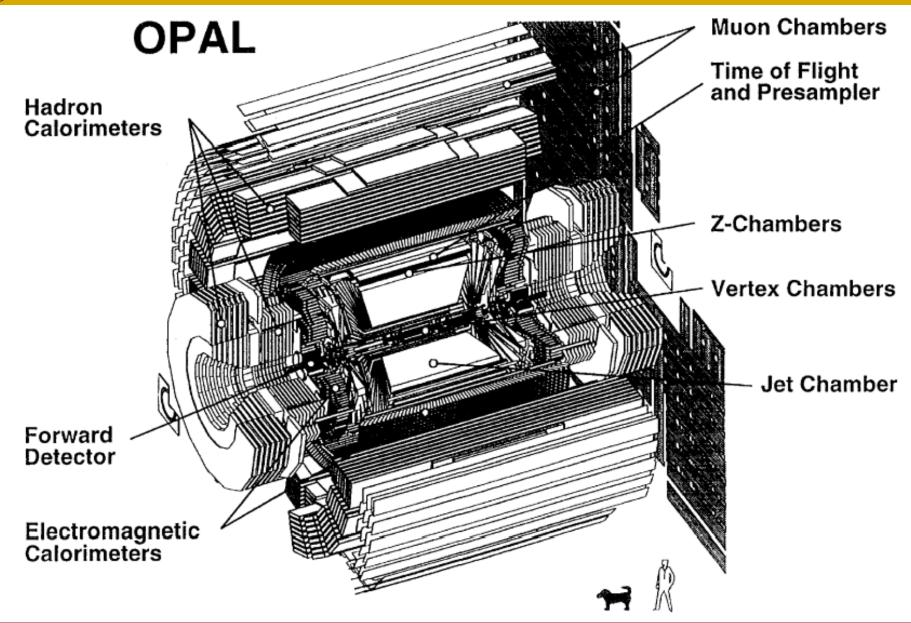
ALEPH

- 1 Beam Pipe
- 2 Silicon Vertex Detector
- 3 Inner Tracking Chamber
- 4 Luminosity Monitor
- 5 TPC Endplate
- 6 Electromagnetic Calorimeter 6a Barrel
 - 6b Endcap
- 7 Superconducting Coil
- 8 Hadron Calorimeter
 - 8a Barrel
 - 8b Endcap
- 9 Muon Chambers

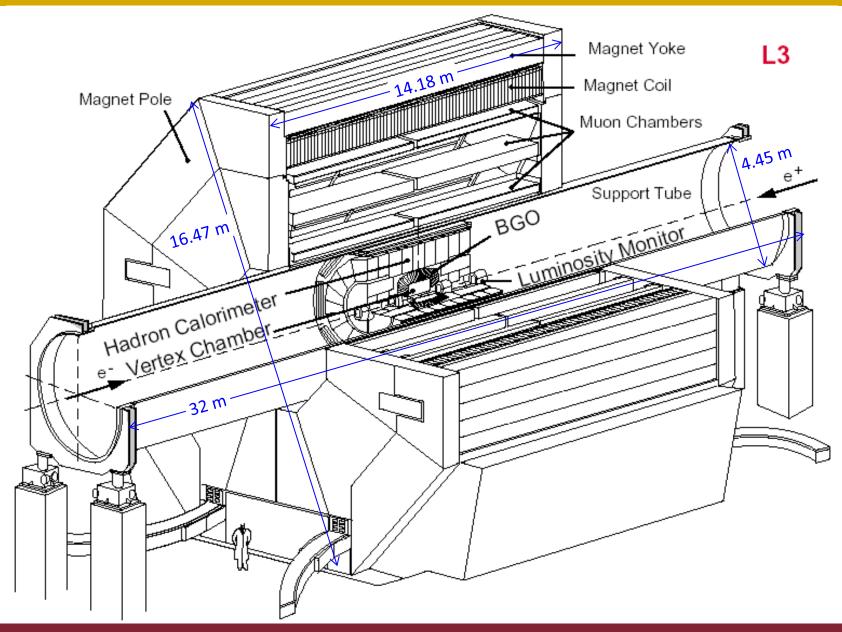
Detectors : DELPHI



Detectors : OPAL

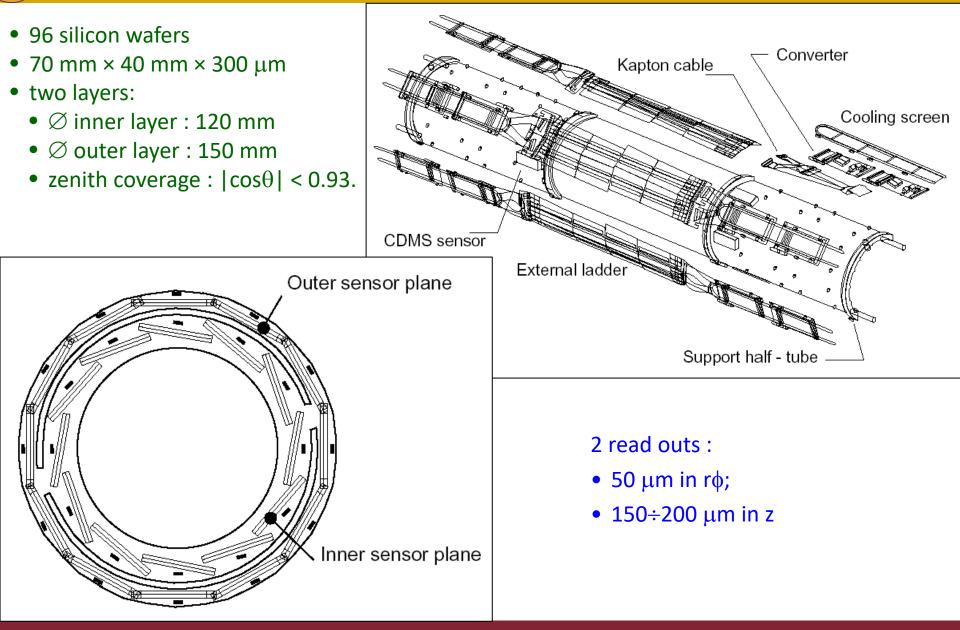


Detectors : L3



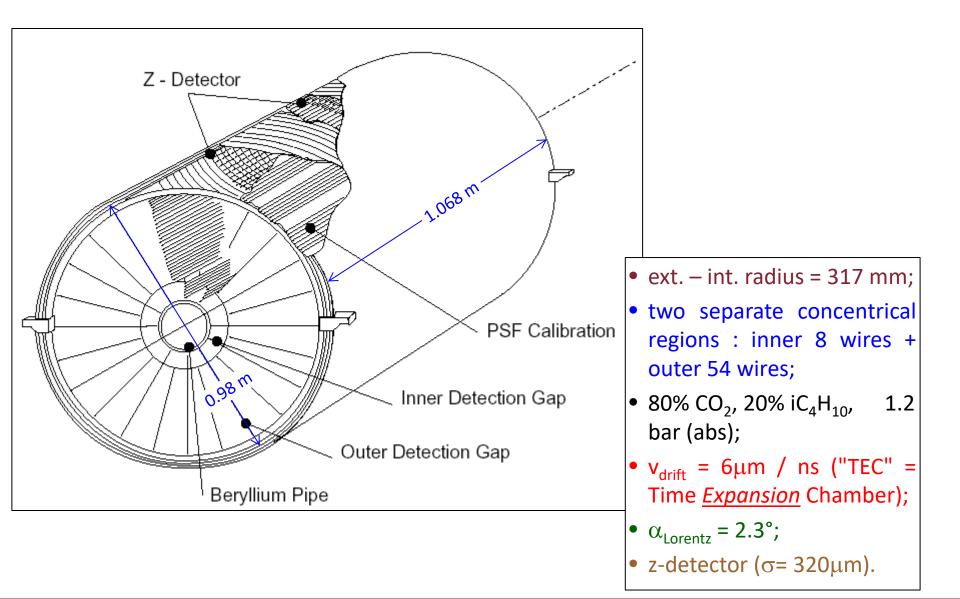


The L3 detector: SMD



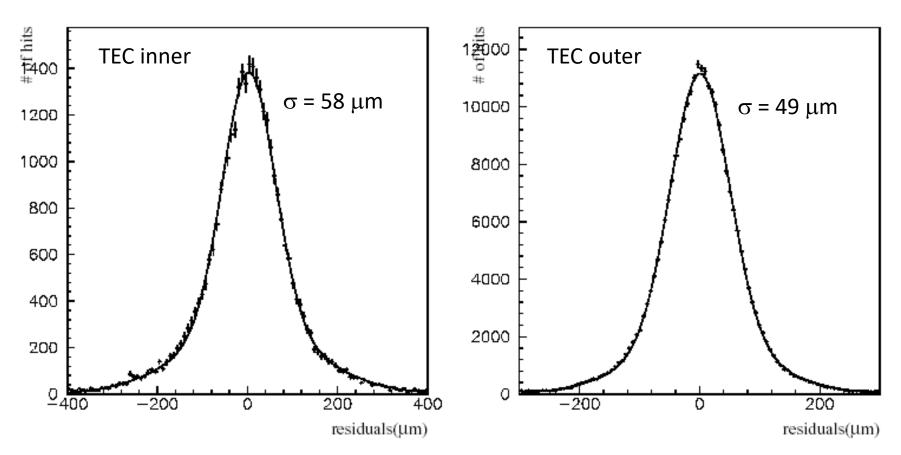


The L3 detector: TEC

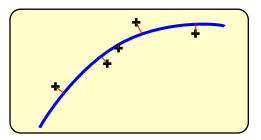




The L3 detector: TEC results

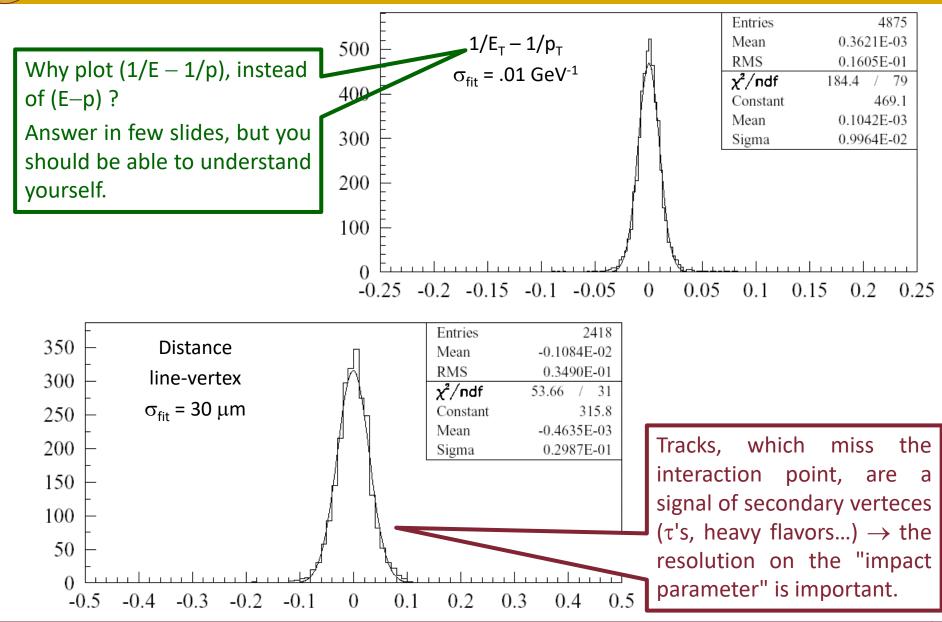


The *residuals* are the distances (with sign) between the measurements and the fitted trajectory. Assuming "many" measurements with the same resolution, their distribution is expected to be gaussian with mean=0 and RMS=resolution.



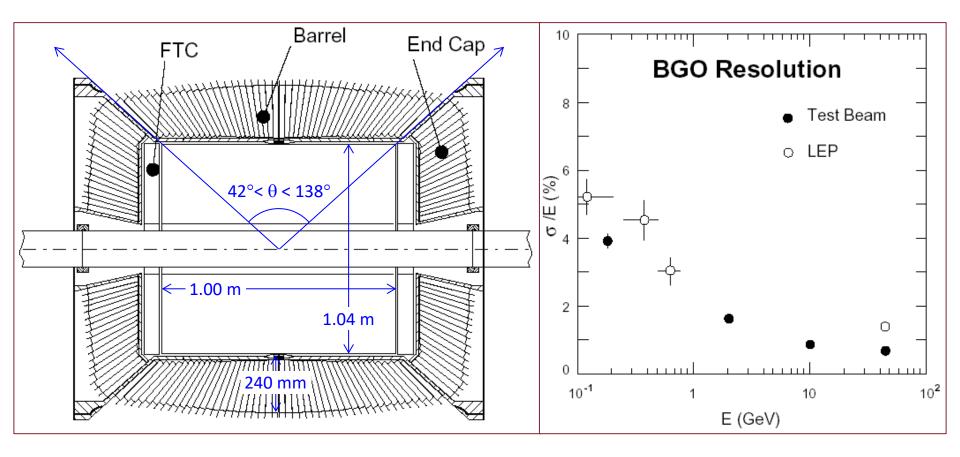


The L3 detector: SMD + TEC





The L3 detector: BGO

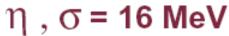


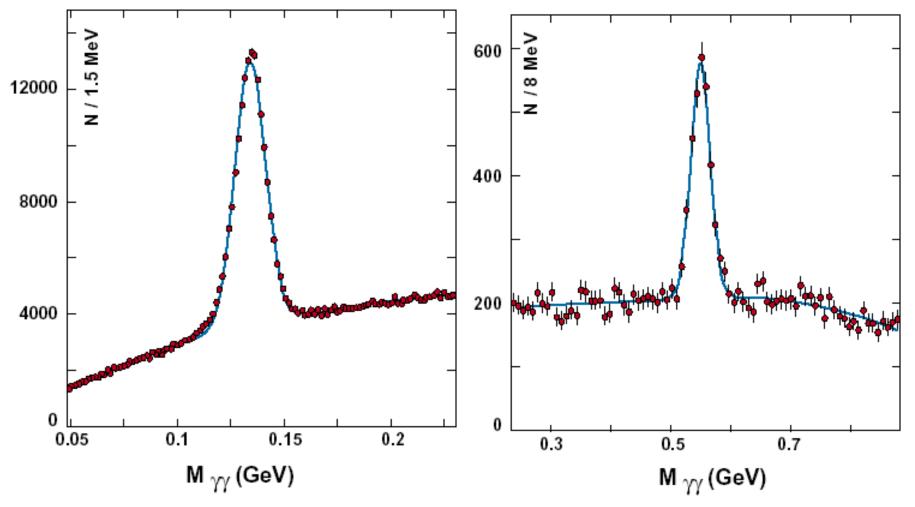
- 11,000 BGO (Bismuth germanium oxide Bi₄ Ge₃ O₁₂) scintillating crystals;
- pyramids $20 \times 20 \rightarrow 30 \times 30$ mm², length 240 mm;
- $X_0 = 11.3 \text{ mm} \rightarrow 21 X_0$.



The L3 detector: BGO results

 π°, σ = 7 MeV

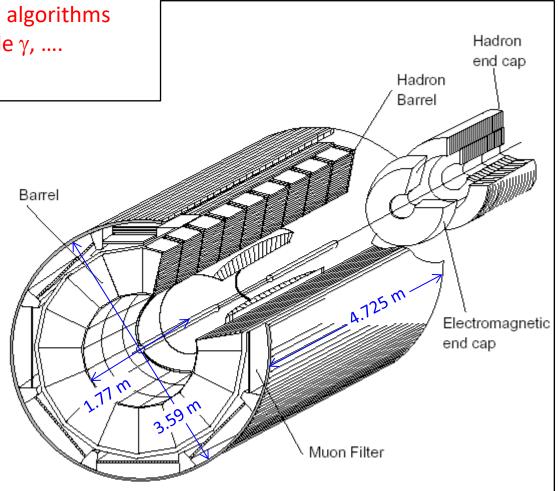




the mass resolution for particles decaying into γ 's is the traditional figure of merit of the e.m. calo (true also for H $\rightarrow \gamma\gamma$ at LHC !!!).

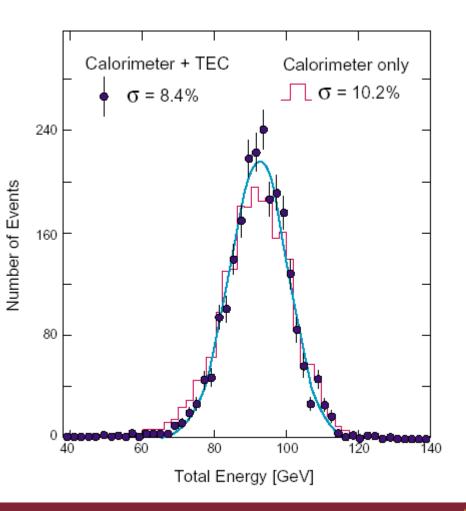


- plates of depleted U (U₂₃₈) + proportional wire chambers (370,000 wires);
- brass μ-filter (65%Cu, 35% Zn) + prop. tubes;
- BGO + hadcal in calo trigger (few algorithms in .OR., e.g. E_{tot}, E^{BGO}_{tot}, cluster, single γ,



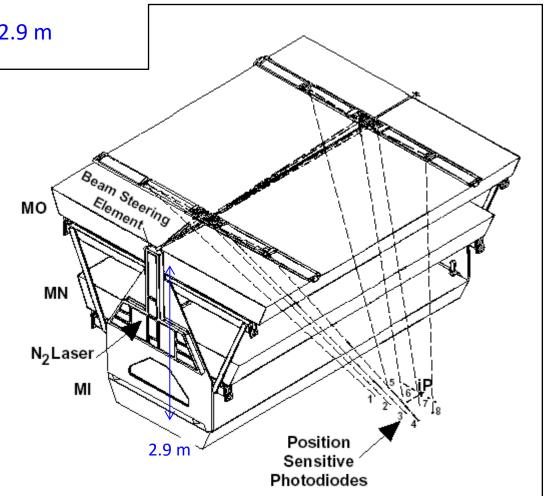


- $Z \rightarrow q\bar{q}$ at $\sqrt{s} = m_z$;
- E_{tot} is known and used to calibrate the detector;
- $E_{vis} / \sqrt{s} = \sum_{i} E_{i} / \sqrt{s}$ in two cases :
 - calo e.m. + had;
 - calo e.m. + had + TEC (- doublecounting);
 - resolution = 10.2% with calos only;
 - resolution = 8.4%, when TEC is also used (avoiding double counting).



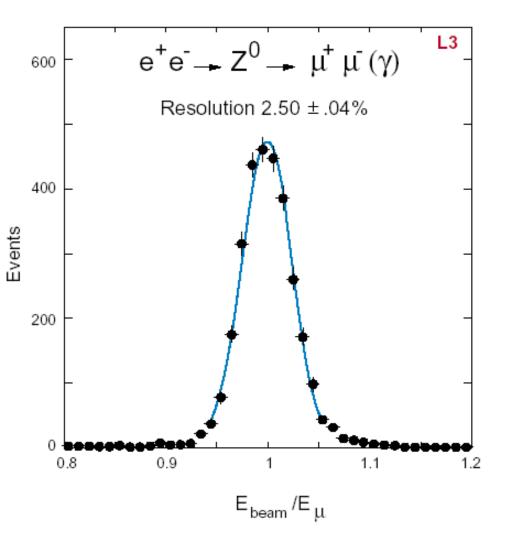


- octants, each with three chamber types : MO
 + MN + MI (16 + 24 + 16 wires);
- effective length of measurement: 2.9 m
- mechanical accuracy: ~10μm;
- alignment with optical sensors.





The L3 detector: µ chambers results



Why plot $E_{beam} / E_{measured}$?

- the sagitta (∞ 1/p) is the measured parameter;
- therefore 1/p expected gaussian, while p is strongly asymmetric in the tails;

•
$$E_{beam} / E_{\mu} = \sqrt{s} / (2 p_{\mu});$$

• $\sigma(m_z)/m_z = \sigma [E_{beam} / E_{\mu}] / \sqrt{2}$.

For Z events, error from the machine, i.e. $\sigma(m_z) = \sigma (\sqrt{s}) =$ few MeV.

This method is used to check \vec{p}_{μ} , which is used in other channels (e.g. Higgs search).

And why (1/E - 1/p), or $(1/E_T - 1/p_T)$?

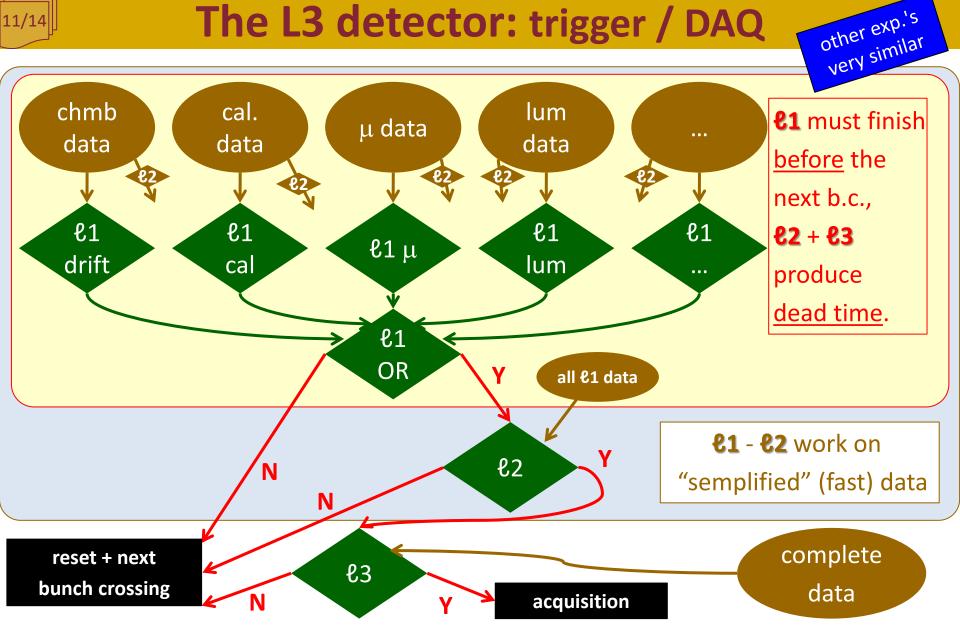
Similar, but more elaborated.

E (and E_T) comes from a calo, so it is normal, while p (and p_T) comes from a spectrometer, so it is normal in 1/p. Plot (E - p) if $\sigma(E) >> \sigma(p)$, but (1/E - 1/p) if

Plot (E – p) if $\sigma(E) >> \sigma(p)$, but (1/E – 1/p) if $\sigma(p) >> \sigma(E)$.



The L3 detector: trigger / DAQ





The L3 detector: trigger requirements

- crossing @ 44/88 KHz \leftrightarrow physics \leq 1 Hz, i.e. " μ " \approx 10^{-4} \div 10^{-5};
- event trigger (no selection on process type, <u>unlike LHC</u>);
- 3 levels of trigger;
- 1st level: simplified readout (e.g. faster ADC less precise), logical OR among:
 - > TEC (e.g. 2 opposite tracks);
 - μ (at least one candidate);
 - ≻...

<u>energy</u> (see next slides);

- 2nd level: same data as 1st lvl, but combine different detectors (e.g. a track + corresponding calo deposit);
- 3rd level: final data.

- fake triggers sources (~10÷20 Hz at 1st level) :
 - electronic noise;
 - > beam halo + "beam-gas"
 interactions , brem photons, ...;

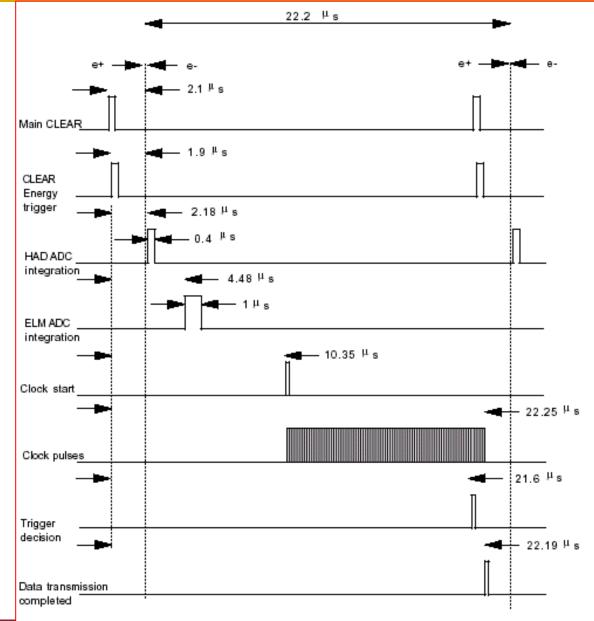
➤ cosmics, ...;

- 1st level is cabled + home-made processors [home : <u>THIS</u> building];
- 2nd level: (quasi-)commercial processor;
- 3rd level: standard computer (vaxstation at the time, today would use pc server + LINUX).
- \rightarrow inefficiency \leq 10⁻³ for Z \rightarrow e⁺e⁻, $\mu^{+}\mu^{-}$, hadrons;
- \rightarrow dead time \approx 5%.



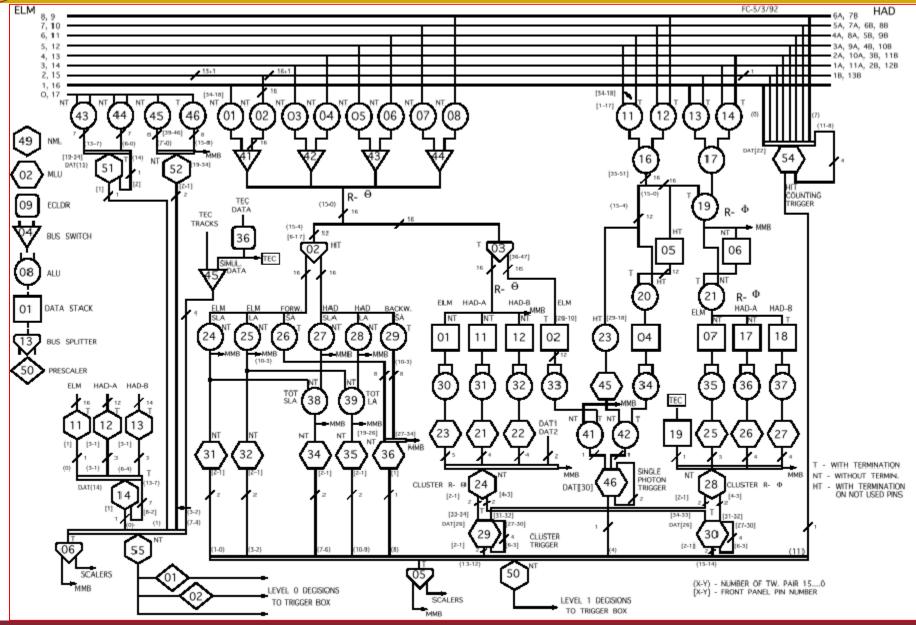
The L3 detector: energy trigger

- Roma : 1989-2000;
- CAMAC^(*) processor, built by "Sezione INFN" (this building, ground floor);
- fast digitization of calo signals;
- decision algorithm based on a digital programmable processor, realized with logic and arithmetic units;
- ~200 CAMAC modules;
- decision in ~22 μ s \rightarrow
- (*) CAMAC was an electronic standard, widely used in the '70s – 90's, now almost completely replaced by VME and other systems.



14/14

The L3 detector: energy trigger scheme





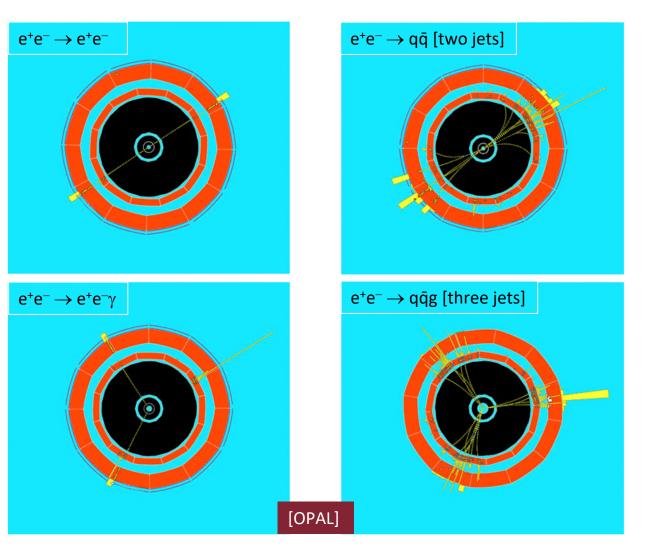
LEP events

The e⁺e⁻ initial state produces very clean events (parton system = CM system = laboratory, no spectators).

In these four LEP events the beams are perpendicular to the page.

The recognition of the events is really simple, also for non-experts.

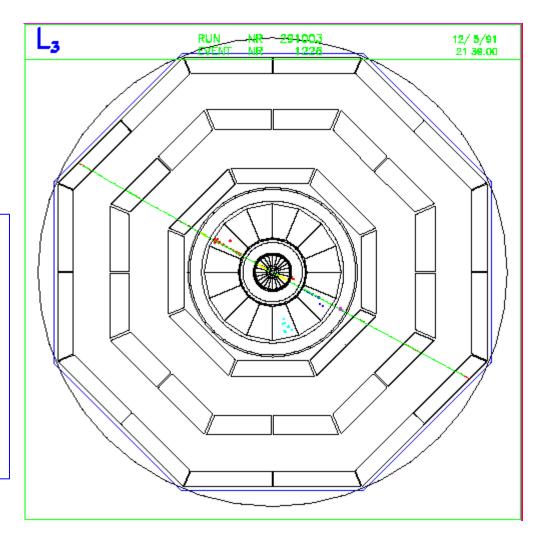
Great machines for high precision physics ...



LEP events: $\mu^+\mu^-$

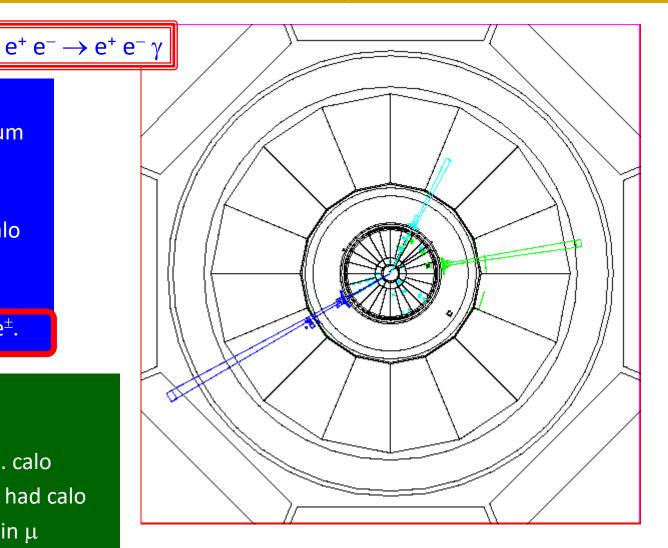
$e^+ e^- \rightarrow \mu^+$	μ-
-----------------------------	----

- + signals in SMD
- + track in TEC (→ momentum and charge)
- + mip in calos
- + signals in μ chambers (\rightarrow momentum and charge)
- = identified and measured μ^{\pm} .



LEP events : e⁺e⁻γ

- + signals in SMD
- + track in TEC (→ momentum and charge)
- + e.m. shower in e.m. calo
- + (almost) nothing in had calo
- + absolutely nothing in μ chambers
- = identified and measured e^{\pm} .
 - + no signal in SMD
 - + no signal in TEC
 - + e.m. shower in e.m. calo
 - + (almost) nothing in had calo
 - + absolutely nothing in μ chambers
 - = identified and measured γ .



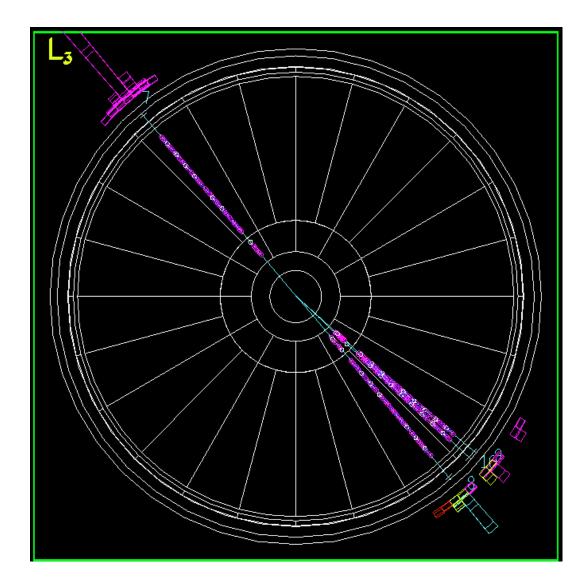
LEP events : $\tau^+\tau^-$

 $e^+ e^- \rightarrow \tau^+ \tau^-$

 τ^{\pm} id. does depend on decay:

- 1/3/5 had tracks;
- [or identified single ℓ^{\pm} ;]

(the evidence comes from the combination of the two decays in the opposite emispheres).

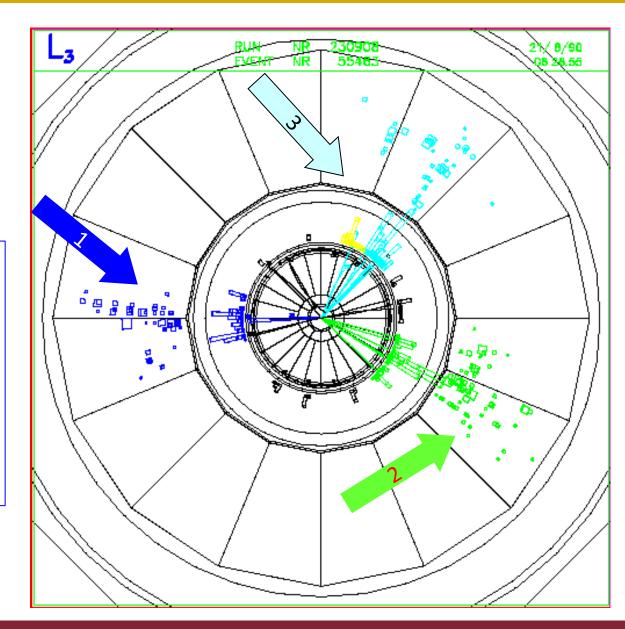


LEP events : 3 jets

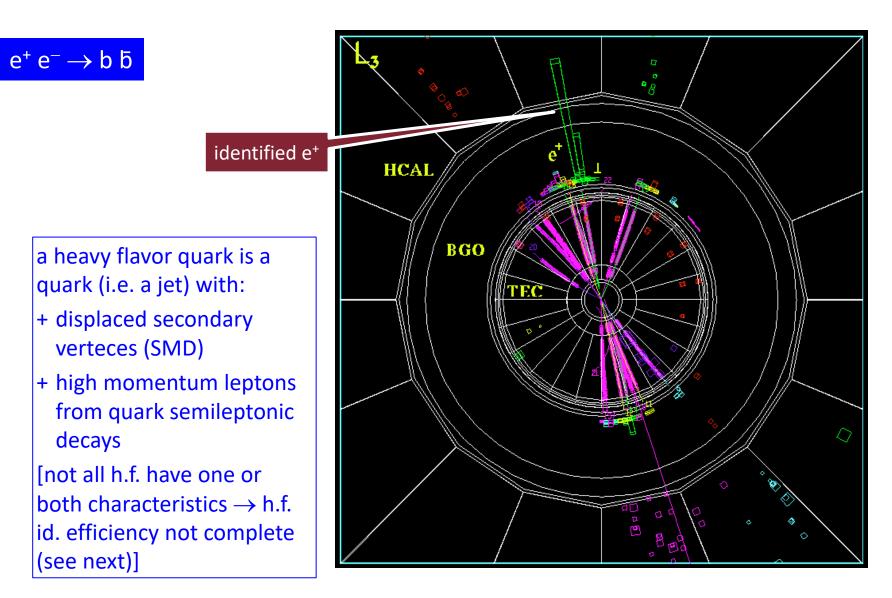
 $e^+ e^- \rightarrow q \bar{q} g$

a (anti-)quark or a gluon gives a hadronic jet:

- + many collimated tracks
- + large splashes in e.m. and had calos
- + (possibly) low momentum associated e^{\pm}/μ^{\pm}

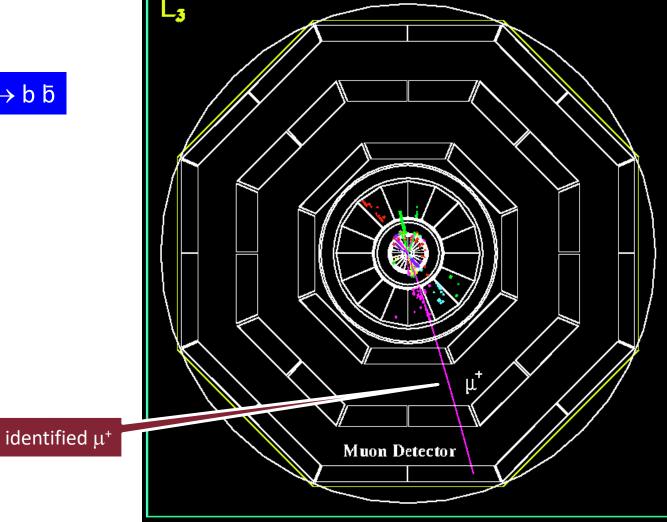


LEP events : $b\overline{b}$, $b \rightarrow e^-$









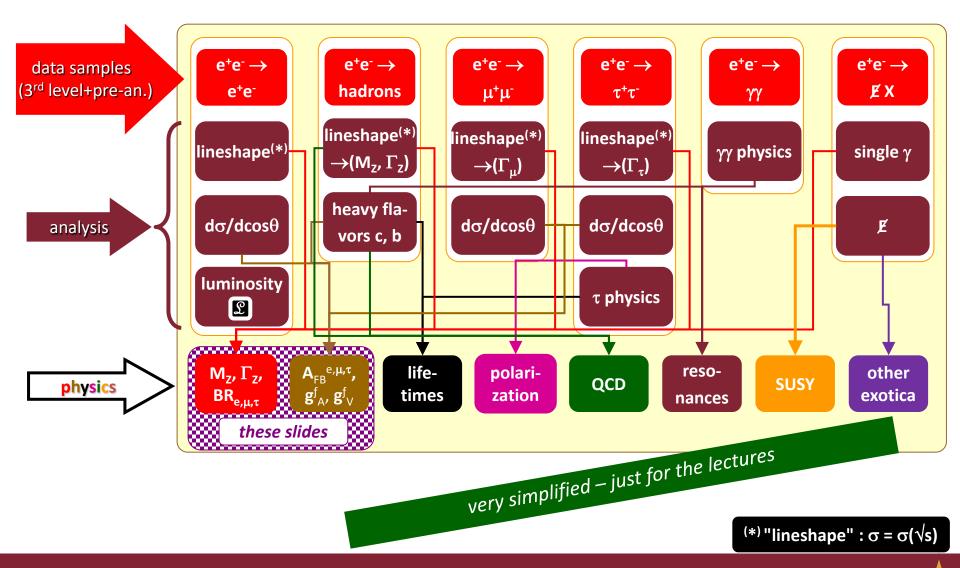
ii. Exp. methods

- 1. 4. [...]
- 5. Data analysis
- 6. Secondary verteces
- 7. Efficiency and purity
- 8. The luminosity
- 9. 16. [...]



data analysis





1/6

41 `

data analysis: events $\rightarrow \sigma$

- At LEP, as in any other experiment, a number of events N^{exp} has to be translated to a cross section σ_s ("signal");
- [also $dN^{exp}/d\Omega \rightarrow d\sigma_s/d\Omega$;]

2/6

- straightforward : $\sigma_s = N^{exp} / \mathcal{L}_{int}$;
- but (at least) two problems :
 - the selection algorithm loses trueand gains spurious-events: N^{exp} = N_{true} - N_{lost} + N_{sp.};
 - > the determination of \mathcal{L}_{int} , the **luminosity**.
- the experiment must measure/compute :
 - N^{exp} : number of selected events;
 - > σ_{b} : cross-section of bckgd;
 - $\succ \epsilon_{s,b}$: efficiency (signal and bckgd); <
 - > $\Delta N^{exp} = \sqrt{N^{exp}}$ (statistical error);
 - $\succ \Delta \varepsilon_{s,b}$ = "systematics";
 - \succ \mathcal{L}_{int} = int. luminosity.

- then (next slides) : > $N^{exp} = \mathcal{L}_{int} (\varepsilon_s \sigma_s + \varepsilon_b \sigma_b) \rightarrow \sigma_s = (N^{exp}/\mathcal{L}_{int} - \varepsilon_b \sigma_b) / \varepsilon_s; d\sigma_s/d... = [...];$
- the luminosity L_{int} is equal for signal and bckgd and <u>must be measured</u>;
- LEP measures L_{int} from a process ("lumi process"), with a calculable cross section, triggered and acquired at the same time as other data (→ so DAQ inefficiencies cancel out) :

 $\mathcal{L}_{int} = N_{lumi} / (\epsilon_{lumi} \sigma_{lumi} + \epsilon_{b-lumi} \sigma_{b-lumi})$

 $\begin{array}{ll} \bullet & \text{therefore three new errors}:\\ (\text{statistics}) & \Delta N_{\text{lumi}} = \sqrt{N_{\text{lumi}}},\\ (\text{sistematics}) & \Delta \epsilon_{\text{lumi,b-lumi}}, \Delta \sigma_{\text{b-lumi}},\\ ("\text{theory"}) & \Delta \sigma_{\text{lumi}} \overset{\text{theory}}{\overset{theory}}{\overset{theory}}}}}}}}}}}, \{$

NB. In an ideal experiment, $N_{lost} = N_{sp.} = 0 \rightarrow \varepsilon_s = 1$, $\varepsilon_b = 0$.

data analysis: theory \leftrightarrow exp. data

An example: $e^+e^- \rightarrow \mu^+\mu^-$:

3/6

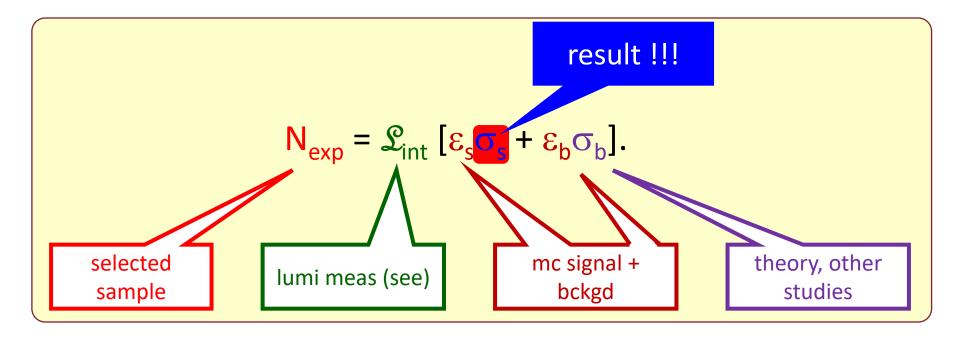
- studies for efficiency and purity with MC simulation [see later].
- <u>signal</u>: true events $e^+e^- \rightarrow \mu^+\mu^-$; the yield depends on m_Z , Γ_Z , Γ_μ (unknown);
- <u>bckgd</u>: events from other sources, with similar final state (because really the

same or similar in the detector), e.g. :

 $\begin{array}{l} \succ \ e^+e^- \rightarrow Z \rightarrow \tau^+\tau^- \rightarrow \\ \qquad \rightarrow (\mu^+\bar{\nu}_{\tau}\nu_{\mu}) \ (\mu^-\nu_{\tau}\bar{\nu}_{\mu}) \\ \qquad \rightarrow (\mu^+\mu^-) \ (+ \ not \ visible); \end{array}$

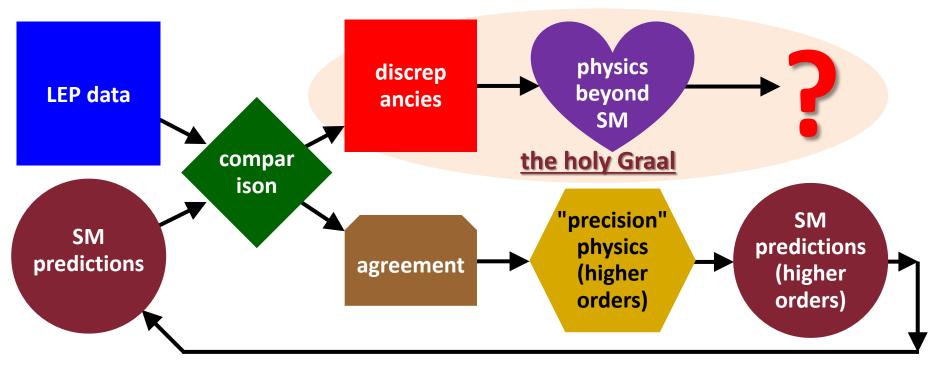
>
$$e^+e^- \rightarrow e^+e^-\mu^+\mu^- \rightarrow$$

→ $(e^+e^-)^{beam\ chamber}\ (\mu^+\mu^-)^{detected};$
→ $(\mu^+\mu^-)\ (+\ not-detected);$



data analysis: scheme



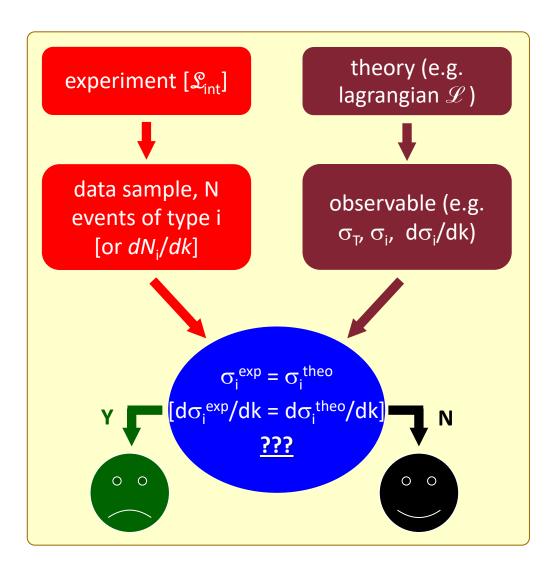


- In 1989, when LEP started, the SM was completely formulated and computed;
- the only missing pieces (at that time) were the top quark and the Higgs boson (both now discovered);
- the values of m_{top} and m_{Higgs} are such that they (in lowest order) have no role at LEP √s [but for H we did NOT know];

- twelve years of LEP physics gave <u>NO</u> major surprise, but general agreement with SM predictions;
- tons of measurements, a superb unprecedented work of precision physics : the <u>number of light v's</u> and the <u>predictions of m_{top} and m_{Higgs}</u> via higher orders are [*imho*] the LEP masterpieces.

data analysis: comparison theory ↔ data





Therefore, a *measurement* means :

- select a pure (as much as possible) sample of events N_i;
- measure the statistical significance of the experiment ($\rightarrow \mathcal{L}_{int}$);
- measure/compute the associated efficiency and purity ($\rightarrow \varepsilon$,p);
- compute $\sigma_i \equiv \sigma_i^{exp} = [previous slide]$ [or $d\sigma_i^{exp}/dk = (...)$];
- → finally **theory** ↔ experiment:
 - compute σ_i^{theo} from theory;
 - **<u>compare</u>** $\sigma_i^{\text{theo}} \leftrightarrow \sigma_i^{\text{exp}}$.

["<u>limits</u>" require a different method, see § limits].

Ľ	-		
F		1	
F		1	
E		31	Ľ,
-		_	

SM predictions :

- σ(ff), σ(e⁺e⁻),
 dσ/dcosθ ... ("Born");
- radiative corrections;
- approximations;



experiment(s) (LEP, L3 as an example) :

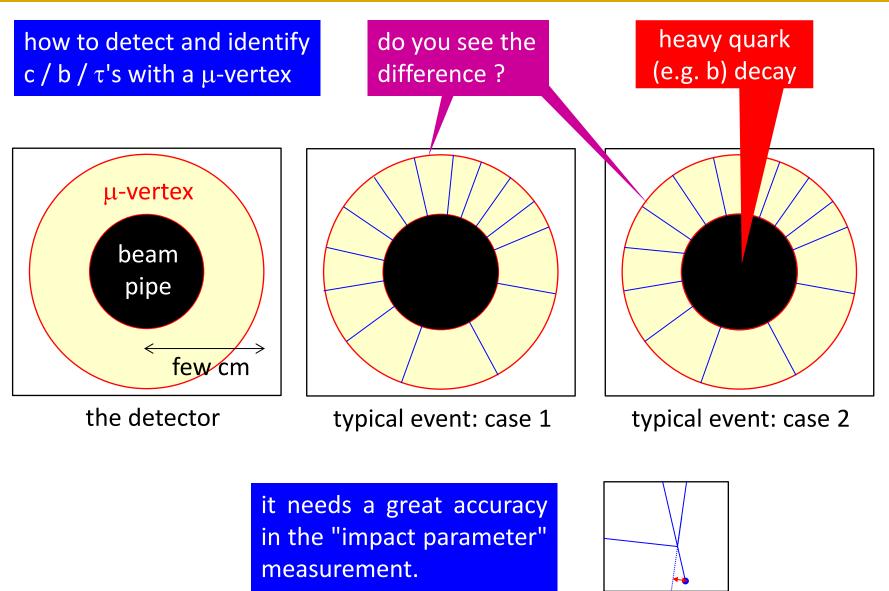
- cross sections $\sigma(e^+e^- \rightarrow e^+e^-, \mu^+\mu^-, \tau^+\tau^-, hadrons, \nu\bar{\nu});$
- differential cross sections $d\sigma(e^+e^- \rightarrow ...) / d \cos\theta$;
- "lineshape" (i.e. $\sigma(e^+e^- \rightarrow ...)$ as a function of \sqrt{s} [also $d\sigma(e^+e^- \rightarrow ...) / d\cos\theta$ vs \sqrt{s}].

data analysis and interpretations : global fit (4 exp. data) \leftrightarrow (SM):

- Z mass, full and partial width (m_z , Γ_z , Γ_f);
- number of v's from $\Gamma_{\text{invisible}}$ and from γ_{single} ;
- asymmetries $A_{forward-backward}$ for $e^+e^- \rightarrow e^+e^-$, $\mu^+\mu^-$, $\tau^+\tau^-$, hadrons;
- global fit data \leftrightarrow SM (\rightarrow consistency);
- global fit data \leftrightarrow SM (\rightarrow predictions of $m_{top}^{},\ m_{Higgs}^{}$ from radiative corrections).

secondary verteces





47

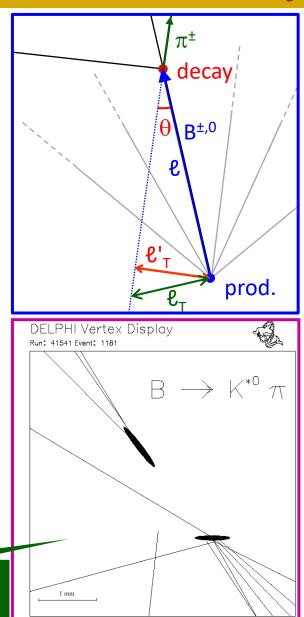
secondary verteces: kinematics



Analysis method (B as an example, similar for c-mesons/baryons, $\tau^{\pm}]$:

- [B conservation \rightarrow 2 B in the event \rightarrow 2 sec. vtxs];
- B ref. sys: $\tau(B^{\pm,0}) \approx 1.5 \times 10^{-12} \text{ s} \rightarrow \ell^* = c \tau_B \approx 500 \ \mu\text{m};$
- $\beta_{B} \approx 1 \rightarrow \ell (= \ell_{B}) = \ell^{*} \beta_{B} \gamma_{B} \approx c \tau_{B} \gamma_{B} \approx few mm [see];$ $\ell_{T} (= \ell \tan \theta)$ is invariant wrt a L-transform along β_{B} $\rightarrow \ell_{T} = \ell^{*}_{T} = \ell^{*} \sin \theta^{*} \approx 100 \div 500 \mu m$ (θ^{*} is the angle B/ π in the B ref. sys., **NOT** small);
- ℓ_T has large errors, but ℓ'_T, the <u>transverse distance</u> (extrapolation of a track) ↔ (primary vtx) can be meas.;
- $\theta \sim m_B/E_B \approx 1/\gamma_B = \text{small} \rightarrow \sin\theta \approx \tan\theta \rightarrow \ell'_T \approx \ell_T;$
- [call both ℓ'_{T} and ℓ_{T} "impact parameter ℓ_{T} "];
- > need a detector with an accuracy $\leq 100 \ \mu m$ in ℓ_T (i.e. in the extrapolation of the line of flight of a charged particle after 20÷30 mm from the last meas;
- **i.e.** a very precise microvertex detector may identify and reconstruct b, c, τ decays.

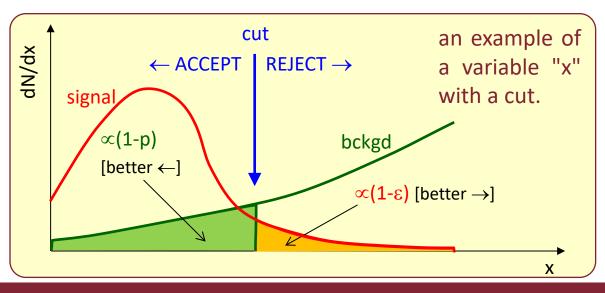
a real B⁰ decay in Delphi (only one B vtx shown]

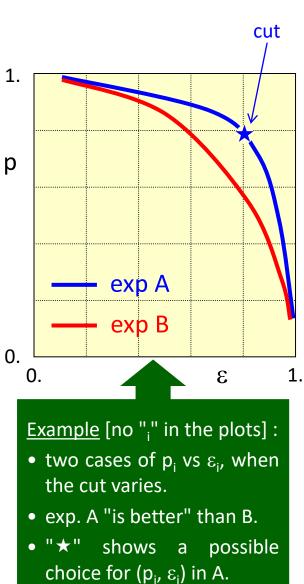


1/4

efficiency and purity

- <u>No selection method</u> is fully "pure" and "efficient", i.e. in a selected sample of events of type "i", there are some events "j" (j≠i), while some events "i" have been rejected;
- if N_i^{sel} is the number of events of the sample, define :
 - ▶ <u>efficiency</u> : $ε_i = N_i^{\text{sel,true}} / N_i^{\text{true,all}} < 1$ [ideally = 1];
 - > <u>purity</u> : $p_i = N_i^{sel,true} / N_i^{sel,all} < 1$ [ideally = 1];
 - $[\underline{contamination} : k_i = N_i^{\text{sel,false}} / N_i^{\text{sel,all}} = 1 p_i];$
- in general, $\boldsymbol{\epsilon}_{i}$ and \boldsymbol{p}_{i} are anti-correlated (see below);
- an algorithm (e.g. a cut in a kin. variable) produces $\epsilon_i + p_i$;
- the "optimal" <u>choice</u> depends on the analysis and on \mathcal{L}_{int} .





efficiency and purity: methods

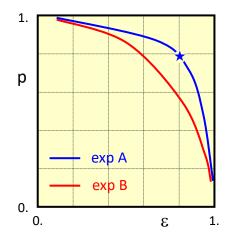


 $N_i^{sel,true}$ and $N_i^{true,all}$ are NOT directly measurable. Few methods to determine the relation ϵ / p, e.g. :

- > Montecarlo (commonly used) :
 - 3 steps : "<u>physics</u>" [→ 4-mom.] + <u>detector</u> [→ pseudo-meas.] + <u>analysis</u> [exactly the same as in real data];
 - pros : large statistics, flexible, easy;
 - cons : (some) systematics cannot be studied;
- ➤ test-beam :

- intrinsic purity + large statistics;
- pros : systematics;
- cons : not flexible, difficult, expensive;

- "data themselves"
 - [e.g. μ from Z $\rightarrow \mu\mu$ to study b $\rightarrow \mu$ X] :
 - "tag and probe" [p ≈ 1 even if ε small] to force purity;
 - ok for systematics;
 - difficult reproduction of the required case [in the example isolated μ's 45 GeV instead of low-p_T μ in a jet].
- ∴ Combination of the above, iterations, new ideas (i.e. <u>you </u>)...



efficiency and purity: example

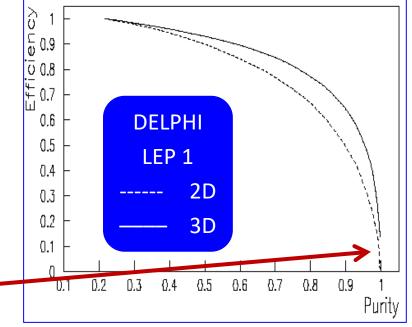


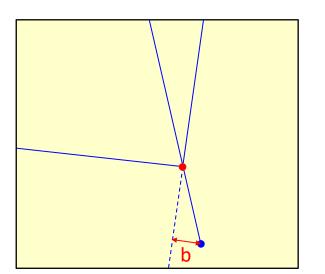
An example of the computation of ϵ vs p (secondary vtxs with impact parameter):

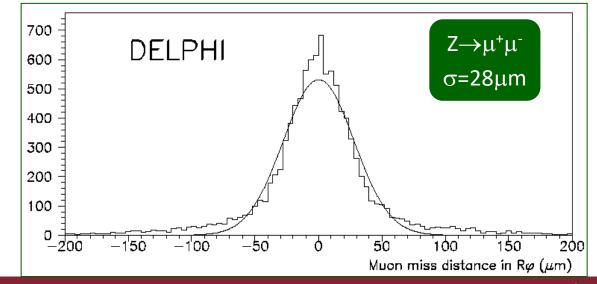
- use a mc (not shown) to define the distribution of impact parameter b in events with sec. vtxs;
- > a cut on b → ε = ε(b_{cut});

3/4

- use a process without secondaries (Z $\rightarrow \mu^+\mu^-$) to define the distribution of the variable b;
- > a cut on $b \rightarrow p = p(b_{cut});$
- $\varepsilon = \varepsilon(b_{cut}) \oplus p = p(b_{cut})$ are parametric equations;
- repeat with more info \rightarrow "3D" \rightarrow better curve.







51

efficiency and purity: the bckgd



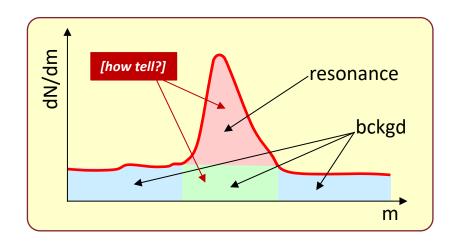
- The background ["bckgd"] may be conceptually divided into two categories :
 - irreducible bckgd^(*): other processes with the same final state [e.g. e⁺e⁻ →ZH, Z→µ⁺µ⁻, H→bb (signal) ↔ e⁺e⁻ →Z₁ Z₂, Z₁→µ⁺µ⁻, Z₂→bb (bckgd)];
 - reducible bckgd :

4/4

- badly-measured events,
- detector mistakes,
- physics processes which appear identical (with given selection criteria) to the process under study [e.g. because part of the final state is undetected, e⁺e⁻γ_{unseen} ↔ e⁺e⁻ν];
- the meaning of the distinction is that r.b. can be disposed with a better detector, or a more accurate selection (maybe with a loss in ε_s), while i.b. is intrinsic, and can only be subtracted statistically, by

comparing [$N^{exp} \leftrightarrow$ (expected bckgd)] and [$N^{exp} \leftrightarrow$ (expected signal+bckgd)];

(*) Similar to the "resonances" of the strong interactions, where a mass distribution exhibits peaks, interpreted as short-lived particles. However, it is impossible to assign single events to the resonating peak or to the non-resonant bckgd.



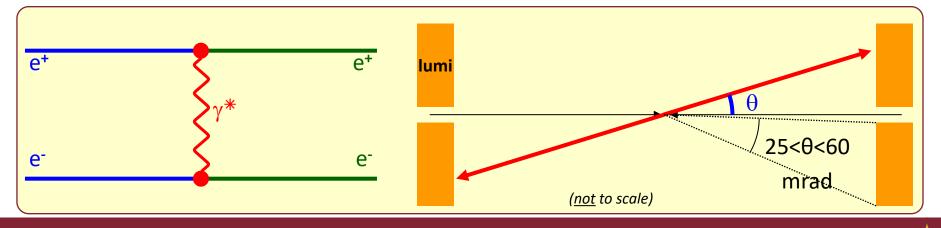
the luminosity

[few slides ago: LEP measures $\mathcal{L}_{int}^{\circ}$ from a process (...): $\mathcal{L}_{int} = N_{lumi} / (\varepsilon_{lumi} \sigma_{lumi} + \varepsilon_{b-lumi} \sigma_{b-lumi})$]

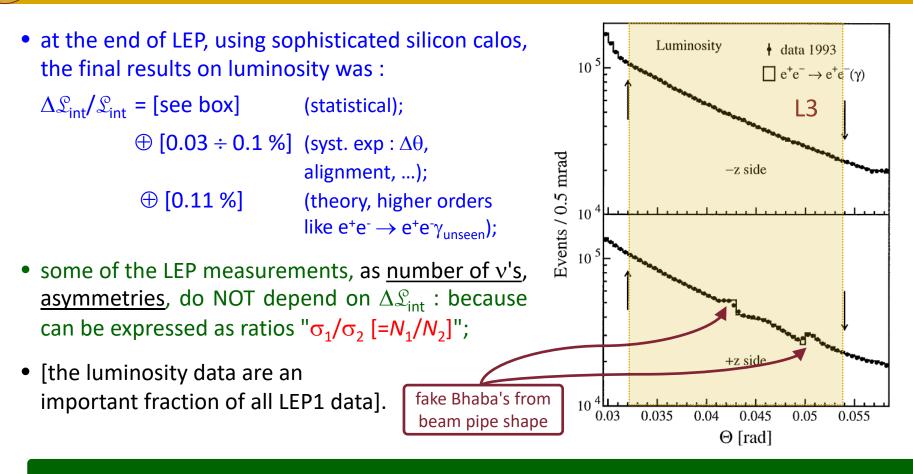
- the "lumi" process (σ_{lumi}) is $e^+e^- \rightarrow e^+e^-$ (Bhabha scattering) at small θ ;
- we <u>assume</u> that, when θ → 0°, the Bhabha scattering is dominated by the γ* exchange in the t-channel, while both (a) the γ*/Z exchange in the s-channel; (b) the Z^(*) exchange in the t-channel are negligible;
- therefore, the LEP experiments have e.m. calorimeters at small θ , to both

identify and measure e[±] ("luminometers", ring-shaped <);</pre>

- it is essential that the "ring" reaches very small θ , to minimize $\Delta \sigma_{stat}$ ($d\sigma_{Rutherford} / d\cos\theta \propto \theta^{-4}$);
- their position and efficiency must be known (= measured) very reliably, in order to minimize systematics;
- typically at LEP, $25 \le \theta_{\text{lumi}} \le 60 \text{ mrad}$: $\sigma_{\text{lumi}} = \frac{16\pi\alpha_{\text{em}}^2}{s} \left(1/\theta_{\text{min}}^2 - 1/\theta_{\text{max}}^2\right);$ $\Delta \mathcal{L} / \mathcal{L} = \Delta \sigma_{\text{lumi}} / \sigma_{\text{lumi}} \approx 2\Delta \theta_{\text{min}} / \theta_{\text{min}}.$



the luminosity L: results



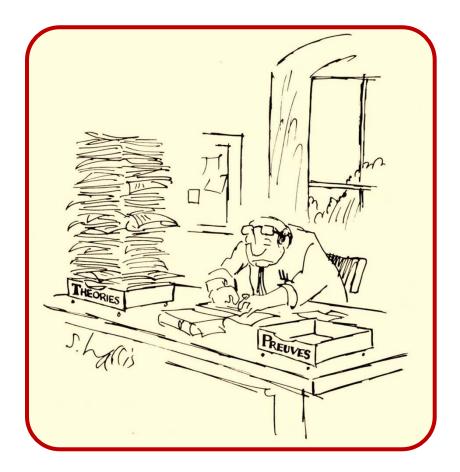
An estimate of the importance of the statistical error comes from the comparison :

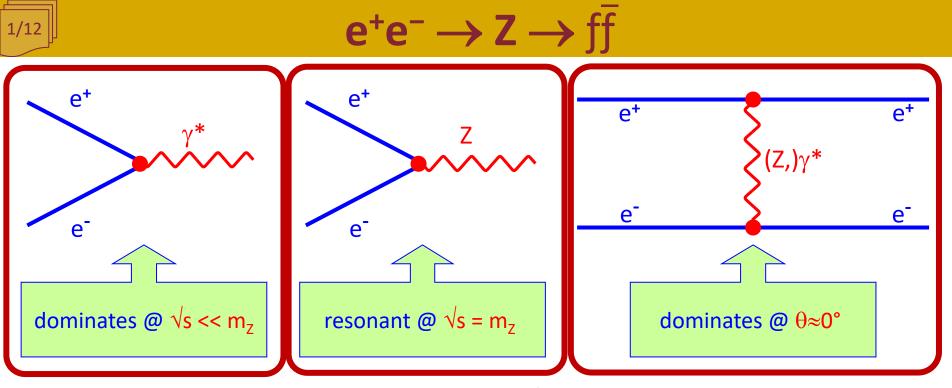
- $\sigma(e^+e^- \rightarrow hadrons, \sqrt{s} = m_z) \approx 30$ nb, the largest cross-section among all LEP processes;
- $\sigma(e^+e^- \rightarrow e^+e^-, 25 \le \theta \le 60 \text{ mrad}) \approx 100 \text{ nb}.$

Therefore the statistical error on the luminosity is negligible, but for the <u>hadronic cross section</u> at $\sqrt{s} = m_z$, where it is $\sim \sqrt{3/10}$ of the statistical error on the hadron data [but for this process the stat. error is irrelevant wrt systematics].

iii. Physics 1: Z & W

- 1. 8. [...]
- 9. $\underline{e^+e^-} \rightarrow Z \rightarrow f\bar{f}$
- 10. $d\sigma(e^+e^- \rightarrow f\bar{f}) / d\Omega$
- 11. $\underline{e^+e^- \rightarrow Z \rightarrow e^+e^-}$
- 12. <u>Radiative corrections</u>
- 13. LEP1 SM fit
- 14. $\underline{e^+e^-} \rightarrow W^+W^- @ LEP2$
- 15. Global LEP(1+2) fit
- 16. [...]





- Many possibility from e+e- initial state;
- similar couplings wrt already considered processes [§3, §4, §6, §7];
- at low energy, QED only (exchange of γ* in the s-channel);

• at $\sqrt{s} \approx m_z$:

- $\succ \ \sigma_{\rm res}(e^+e^- \rightarrow f\bar{f}) \propto \Gamma_f \, / \, [\, (s m_z^2)^2 + m_z^2 \Gamma_z^2 \,];$
- for each fermion pair, two (four for e⁺e⁻) diagrams + interferences);
- at higher energy, new phenomena (W[±], exchange, IVB pairs in the final state, ...).

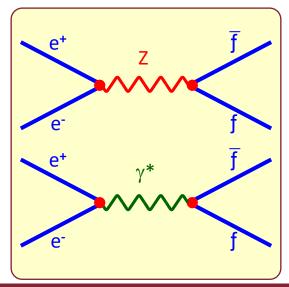
56



$e^+e^- \rightarrow Z \rightarrow f\bar{f}: \sigma_{Born}^{SM}$

In the SM, at lowest order, for
$$f \neq e^{\pm}$$
, $m_f \ll m_z$:
• $\sigma_{Born}(e^+e^- \rightarrow f\overline{f}) = \sigma_{zs} + \sigma_{\gamma s} + J_f$;
• $\sigma_{zs} = \frac{s\Gamma_z^2}{(s-m_z^2)^2 + s^2\Gamma_z^2/m_z^2} \frac{12\pi\Gamma_e\Gamma_f}{m_z^2\Gamma_z^2}$;
• $\sigma_{\gamma s} = \frac{4\pi\alpha^2}{3s}c_fQ_f^2$; $[c_f = 1 \text{ (leptons), 3 (quark)}]$;
• $\int_f = -\frac{(s-m_z^2)m_z^2}{(s-m_z^2)^2 + s^2\Gamma_z^2/m_z^2} \frac{2\sqrt{2}\alpha}{3}c_fQ_fG_Fg_v^eg_v^f$;
• $\Gamma_r = \Gamma_r = \sum \sum \Gamma/Z \rightarrow f\overline{f}$):

- $\Gamma_{z} = \Gamma_{tot} = \sum_{f} \Gamma(Z \rightarrow f\overline{f});$
- $\Gamma_{f} \equiv \Gamma(Z \rightarrow f\overline{f}) = \frac{G_{F}m_{Z}^{3}c_{f}}{6\sqrt{2}\pi} \left[g_{V}^{f^{2}} + g_{A}^{f^{2}}\right];$
- for $\sqrt{s} \approx m_z \rightarrow \text{interference and } \gamma^* \text{negligible;}$
- $\sigma_{\text{Born}}(e^+e^- \rightarrow f\overline{f}, \sqrt{s} = m_z) = \frac{12\pi\Gamma_e\Gamma_f}{m_z^2\Gamma_z^2}.$





$e^+e^- \rightarrow Z \rightarrow f\bar{f}: g_V^f$ and g_A^f

• the partial widths Γ_{f} (e.g. Γ_{μ}) are also easily computed in lowest order :

$$\Gamma_{f} = \frac{G_{F}m_{Z}^{3}c_{f}}{6\sqrt{2}\pi} \left[g_{V}^{f^{2}} + g_{A}^{f^{2}}\right] \rightarrow (f=\mu^{\pm}) \rightarrow \Gamma_{\mu} \approx \frac{1}{4} \frac{G_{F}m_{Z}^{3}}{6\sqrt{2}\pi} \approx 83 \text{MeV};$$

• for the other Γ 's it is found [lowest order values, NOT "the best"] :

f	Q _f	g ^f _A	g ^f _V	$\Gamma_{\rm f}$ (MeV)	$\Gamma_{\rm f}/\Gamma_{\mu}$	R _f (%)
$\nu_e \nu_\mu \nu_\tau$	0	+1⁄2	+1⁄2	166	1.99	6.8
e ⁻ μ ⁻ τ ⁻	-1	-1/2	038	83	[1]	3.4
u c [t]	2⁄3	+1⁄2	+.192	286	3.42	11.8
d s b	-1⁄3	-1/2	346	368	4.41	15.2

[\$v]: $g_{A}^{f} = t_{3L}^{f}$ $g_{V}^{f} = t_{3L}^{f} - 2Q^{f} \sin^{2}\theta_{w}$

In Born approx. [B = "Born"] :

>
$$\Gamma_{z}^{B}$$
 = 2423 MeV, $\Gamma_{hadr.}^{B}$ = 1675 MeV, $\Gamma_{invis.}^{B}$ = Γ_{v}^{B} = 498 MeV;

>
$$R_{hadr.}^{B}$$
 = 69.1 %, $R_{lept\pm}^{B}$ = 10.2 %, $R_{invis.}^{B}$ = 20.5 %,

>
$$R_{hadr.}^{B} / R_{vis.}^{B} = 87.0 \%$$
.

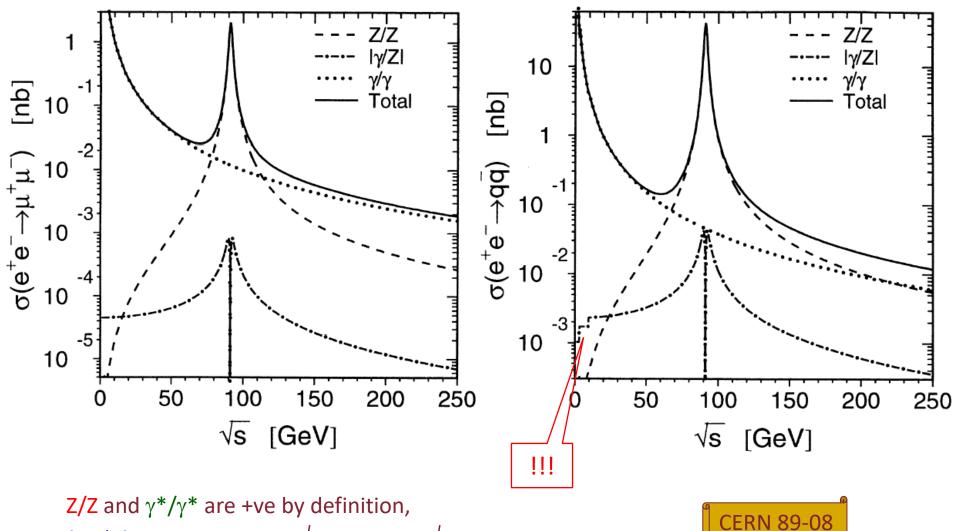
> $\Gamma_{\rm Z}$ \approx 2.4 GeV, $\Gamma_{\rm v}$ \approx 0.5 GeV,

remember !

→ $v: e^{\pm}: u: d \approx 2: 1: 3.4: 4.4$, hadr: $e^{\pm}: v \approx 70: 10: 20$.

 e^+ Z \overline{f} e^- f e^+ γ^* \overline{f} e^- f

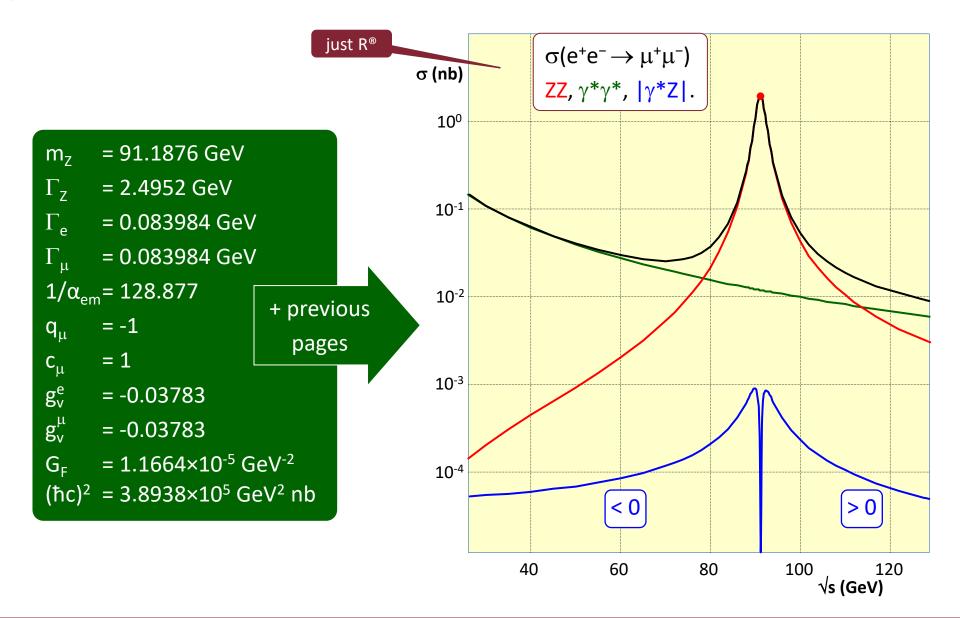
$e^+e^- \rightarrow Z \rightarrow f\bar{f}$: predictions



 $|\gamma^*/Z|$ is plotted (<0 @ $\sqrt{s < m_z}$, >0 @ $\sqrt{s > m_z}$).

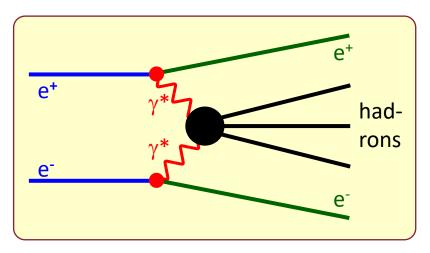


$e^+e^- \rightarrow Z \rightarrow f\bar{f}$: home-made predictions





$e^+e^- \rightarrow Z \rightarrow f\bar{f}: 2 \gamma \text{ physics}$



Introduce a different process: "2 γ physics":

- it is so called because the initial state of the hard collision is given by two γ's;
- the two e[±] of the initial state retain much of the energy, and in most cases escape undetected in the beam chamber;
- classify events in "untagged", "single tag" and "double tag", depending on whether 0, 1, 2 and e[±] are detected;
- lot of nice kinematics [try it];

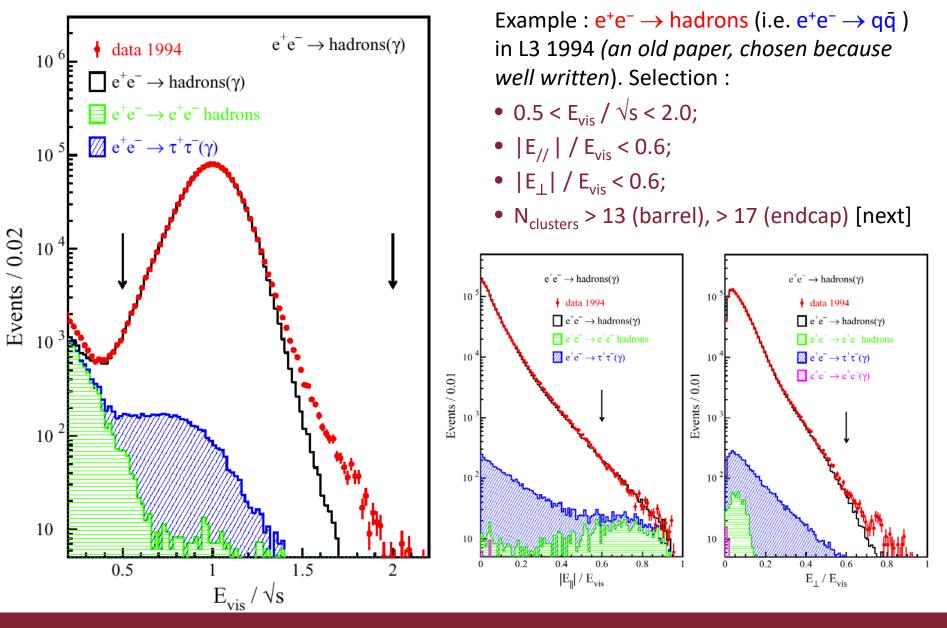
- events studied using two variables:
 - > $\sqrt{s} = m_{ini}(e^+e^-);$
 - > W = m($\gamma\gamma$) = m(hadrons);
- the study of $\sigma_{\gamma\gamma}$ requires a cut on W, i.e. $\sigma_{\gamma\gamma} = \sigma_{\gamma\gamma}(W > W_{cut})$, both for theory and detection:
 - > $\sigma_{\gamma\gamma}$ weakly dependent on \sqrt{s} ;
 - > $\sigma_{\gamma\gamma}^{''}$ strongly dependent on W, $\sigma_{\gamma\gamma} \sim e^{-W}$.

Why study "2 γ physics" ? Two main goals:

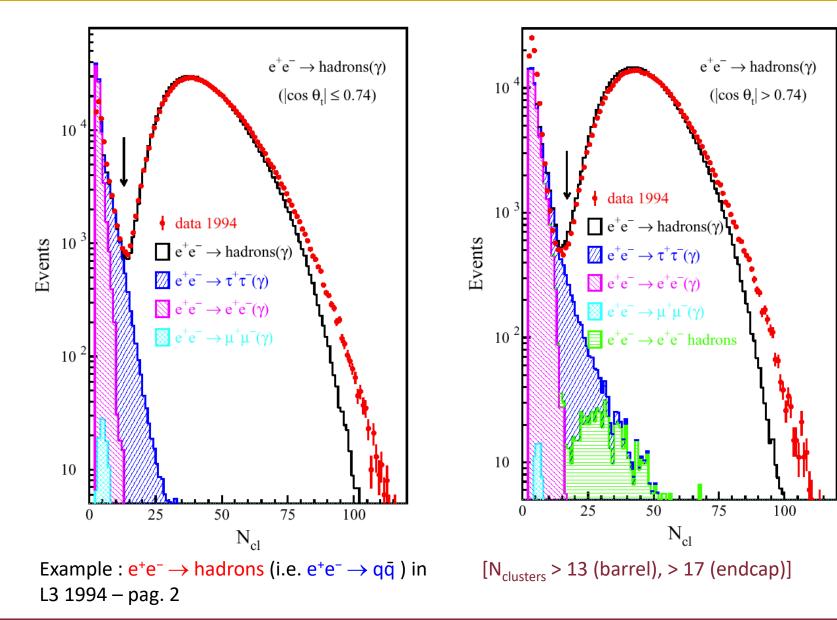
- 1. *intrinsic interest:*
 - any process deserves a study;
 - rich "factory" of hadron resonances;
 - other low-energy processes;
- 2. $\sigma_{\gamma\gamma}$ is large:
 - LEP1: subtract from high precision meas.;
 - LEP2: typically tiny cross sections → an important background, especially if large *E* required.



$e^+e^- \rightarrow Z \rightarrow f\bar{f}$: hadrons (1)

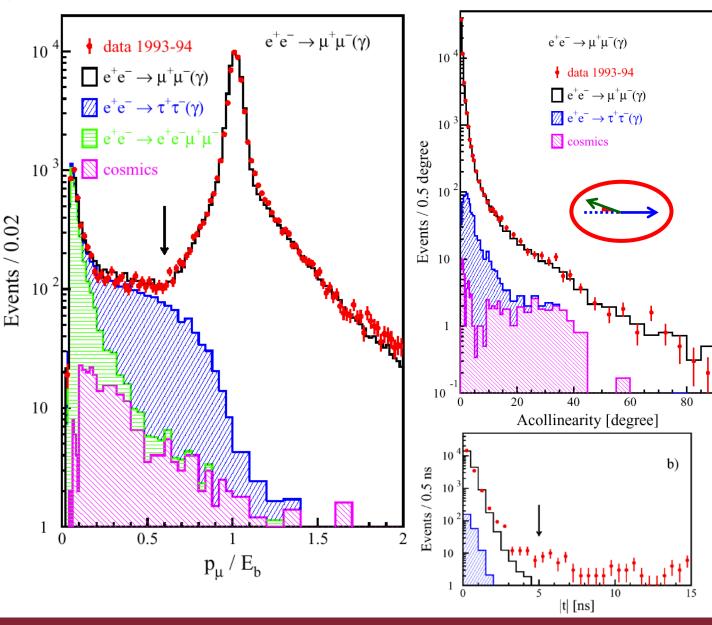


$e^+e^- \rightarrow Z \rightarrow f\bar{f}$: hadrons (2)





$e^+e^- \rightarrow Z \rightarrow f\bar{f}: \mu^+\mu^-$



Other example (same paper) : $e^+e^- \rightarrow \mu^+\mu^-$ Selection :

- \geq 1 μ identified;
- $|p_{\mu}| > 0.6 (\sqrt{s/2});$
- α(μμ) "small";
- N_{clusters} < 15;
- time_{scintillators}.

Q. : why μ's have smaller acollinearity than τ's ?

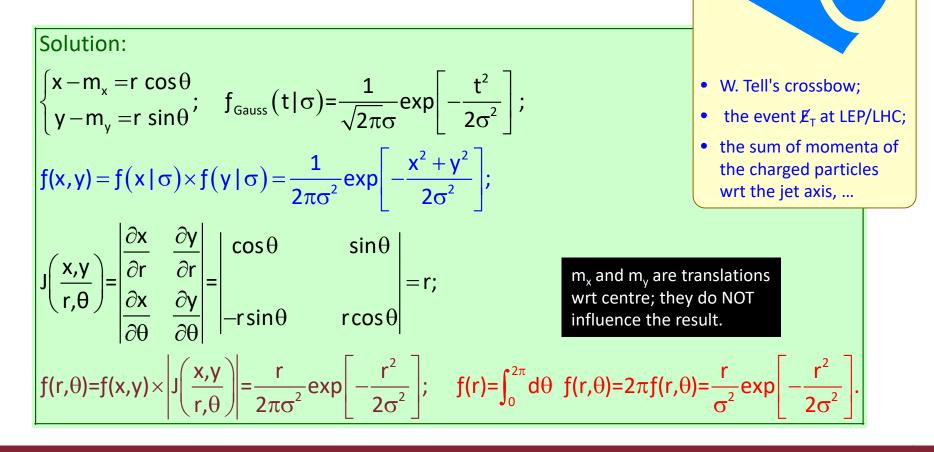


$e^+e^- \rightarrow Z \rightarrow f\bar{f}$: from W. Tell to LEP

X

Problem. Two variables (x, y) are normally (=Gauss) distributed with mean (m_x , m_y) and standard deviation $\sigma_x = \sigma_y = \sigma$. Find the distribution of the distance from the center

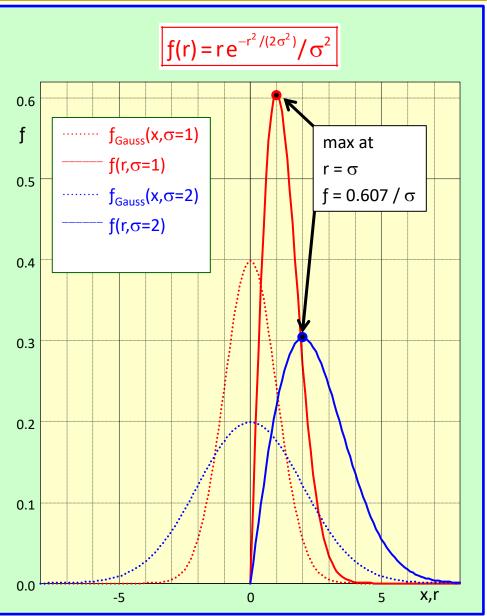
$$r = \sqrt{(x - m_x)^2 + (y - m_y)^2}.$$

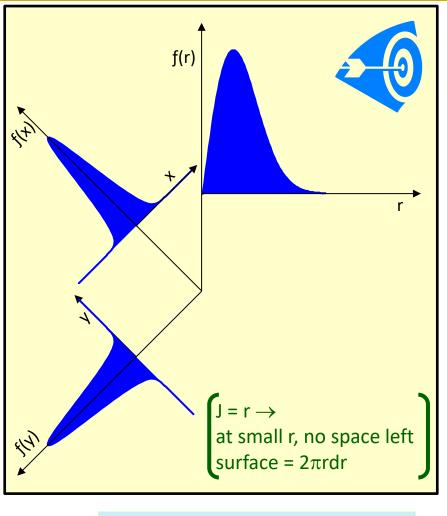




$e^+e^- \rightarrow Z \rightarrow f\bar{f}$: a W. Tell tale





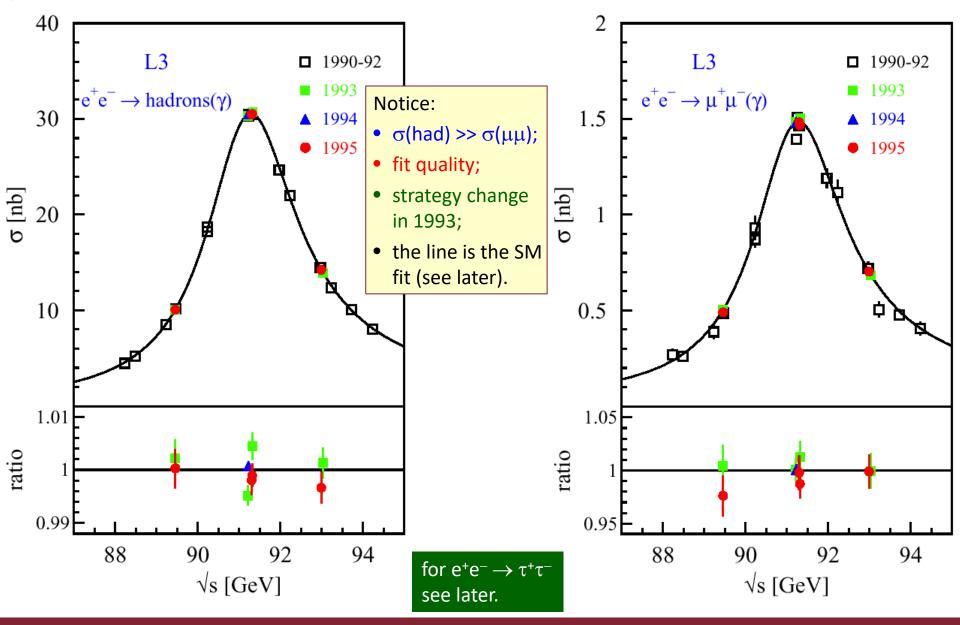


next question: the case $\sigma_x \neq \sigma_y$ [easy, needs only one smart trick]

66



 $e^+e^- \rightarrow Z \rightarrow f\bar{f}$: lineshape



PDG 2016, Differential cross-section in lowest (Born) order: 10.31-32-36 $\frac{\left|\frac{d\sigma_{Born}\left(e^{+}e^{-}\rightarrow f\overline{f}\right)}{d\cos\theta}=\frac{\pi\alpha^{2}(s)c_{f}}{2s}\right|^{\left(1+\cos^{2}\theta\right)\times}\left|\begin{array}{c}Q_{e}^{2}Q_{f}^{2}-2\left[\chi\right]Q_{f}Q_{e}g_{V}^{e}g_{V}^{f}\cos\delta_{R}+\\+\left[\chi^{2}\right]\left[\left(g_{A}^{e}\right)^{2}+\left(g_{V}^{f}\right)^{2}\right]\left[\left(g_{A}^{f}\right)^{2}+\left(g_{V}^{f}\right)^{2}\right]\right]^{+}\right\};$ $\chi = \frac{G_{F}}{2\sqrt{2}\pi\alpha(s)} \times \frac{Sm_{Z}}{(m_{Z}^{2} - s)^{2} + m_{Z}^{2}\Gamma_{Z}^{2}}; \qquad \tan \delta_{R} = \frac{m_{Z}T_{Z}}{m_{Z}^{2} - s};$ Z / γ^* $A_{f}^{FB}(\sqrt{s}) \equiv \frac{\sigma(\cos\theta > 0, \sqrt{s}) - \sigma(\cos\theta < 0, \sqrt{s})}{\sigma(\cos\theta > 0, \sqrt{s}) + \sigma(\cos\theta < 0,)};$ A^{FB}_f is the "forward-backward $A_{f}^{FB}(\sqrt{s} = m_{z}, Z_{s-channel} \text{ only}) =$ asymmetry" for $e^+e^- \rightarrow ff$. $=3\frac{g_{V}^{*}g_{A}^{*}}{(g_{V}^{e})^{2}+(g_{A}^{e})^{2}}\times\frac{g_{V}^{*}g_{A}^{*}}{(g_{V}^{f})^{2}+(g_{A}^{f})^{2}};$

 $d\sigma(e^+e^- \rightarrow ff) /$

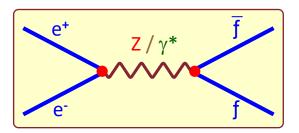
$d\sigma(e^+e^- \rightarrow f\bar{f}) / d\Omega$: comments

$$\frac{d\sigma_{Born}\left(e^{+}e^{-}\rightarrow f\overline{f}\right)}{d\cos\theta} = \frac{\pi\alpha^{2}(s)c_{f}}{2s} \begin{cases} \left(1+\cos^{2}\theta\right)\times \begin{bmatrix} Q_{e}^{2}Q_{f}^{2}-2[\underline{\chi}]Q_{f}Q_{e}g_{V}^{e}g_{V}^{c}\cos\delta_{R}+ \\ +[\underline{\chi^{2}}]\left[\left(g_{A}^{e}\right)^{2}+\left(g_{V}^{e}\right)^{2}\right]\left[\left(g_{A}^{f}\right)^{2}+\left(g_{V}^{f}\right)^{2}\right]\right]^{+} \\ +2\cos\theta\times\left[-2[\underline{\chi}]Q_{e}Q_{f}g_{A}^{e}g_{A}^{f}\cos\delta_{R}+4[\underline{\chi^{2}}]g_{A}^{e}g_{A}^{f}g_{V}^{e}g_{V}^{f}\right] \end{cases} + \end{cases};$$
$$A_{f}^{FB}\left(\sqrt{s}\right) = \frac{\sigma\left(\cos\theta>0,\sqrt{s}\right)-\sigma\left(\cos\theta<0,\sqrt{s}\right)}{\sigma\left(\cos\theta>0,\sqrt{s}\right)+\sigma\left(\cos\theta<0,\sqrt{s}\right)} \xrightarrow{\sqrt{s}\rightarrow m_{z}} 3\frac{g_{V}^{e}g_{A}^{e}}{\left(g_{V}^{e}\right)^{2}+\left(g_{A}^{e}\right)^{2}}\times\frac{g_{V}^{f}g_{A}^{f}}{\left(g_{V}^{f}\right)^{2}+\left(g_{A}^{f}\right)^{2}}.$$

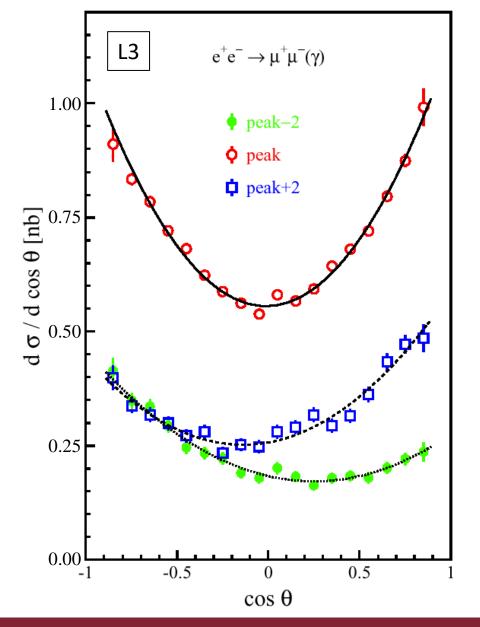
mediators : γ , Z [= Z_A + Z_V]; \mathbb{P} -cons : $\gamma\gamma$, γ Z_V, ZZ [= Z_A² + Z_V²]; \mathbb{P} -viol. : γ Z_A, Z_AZ_V.

- standard SM computation for $Z_s \oplus \gamma_s$ only (average on initial and sum on final polarization), then sum on φ :
- notice : the term ∞ (cos θ) is <u>anti-</u> <u>symmetric</u>; it does NOT contribute to σ_{tot} ($\int \cos\theta \ d\cos\theta = 0$), but only to the (\mathbb{P} violating) <u>forward-backward asymmetry</u>;
- the \mathbb{P} -violation clearly comes from the interference between the vector ($\gamma + Z_v$) and axial (Z_A) terms.

- at the pole ($\sqrt{s}=m_z$) :
 - $\succ \cos \delta_{R} = 0;$
 - > the asymmetry, i.e. the term $\propto \cos \theta$, is $\propto g_V^e$ (very small) for all fermions;
 - > for the $\mu^+\mu^-$ case [easily measurable], it is even smaller ($\propto g_V^e g_V^\mu$).

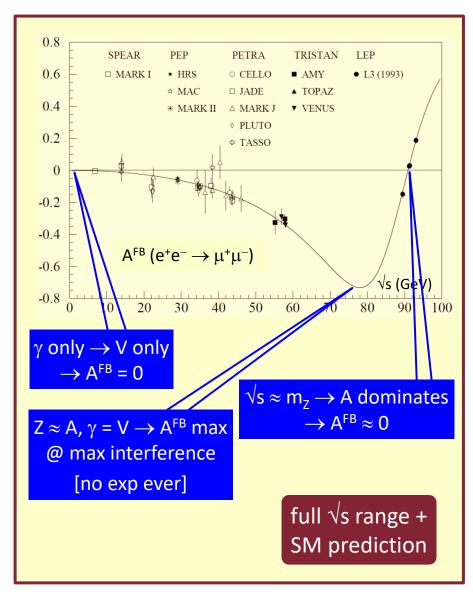


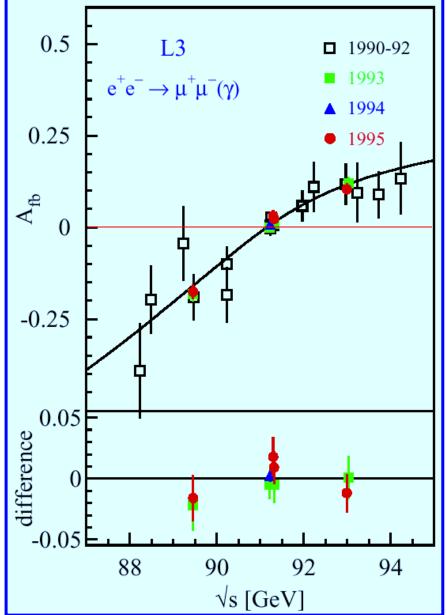
$d\sigma(e^+e^- \rightarrow f\bar{f}) / d\Omega$: data



- Experimentally, the main problem is the selection $f \leftrightarrow f$ (i.e. $\theta \leftrightarrow \pi \theta$). This is
 - > essentially impossible for light quarks u ↔ ū, d ↔ d (despite heroic efforts based on charge counting);
 - > difficult for heavy quarks c,b (based on lepton charge in semileptonic quark decays, e.g. c → sℓ⁺v, c → sℓ⁻v);
 - "simple" for μ[±] (only problem: wrong sagitta sign because of high momentum);
 - > best channel for $d\sigma/dcos\theta$ and A_{FB} : $e^+e^- \rightarrow \mu^+\mu^-(\gamma)$;
- unfortunately, $A_{FB}(\sqrt{s}=m_Z)$ is very small in the $\ell^+\ell^-$ channels, due to the extra small factor g_V^{μ} ;
- notice the asymmetry change for peak ±2 GeV.

$d\sigma(e^+e^- \rightarrow f\bar{f}) / d\Omega: A_{fb}(\mu^+\mu^-)$

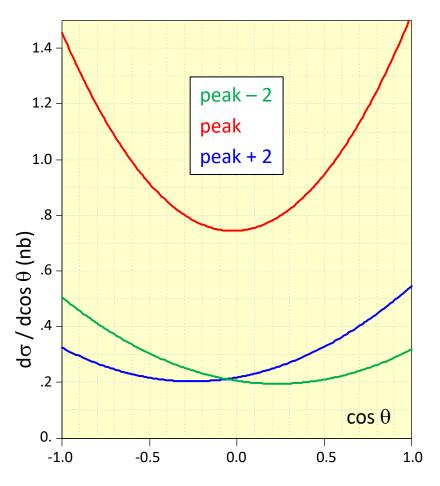




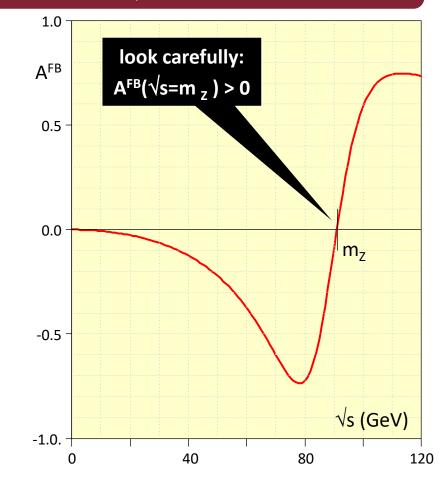
$d\sigma(e^+e^- \rightarrow f\bar{f}) / d\Omega$: problem

Problem. Compute $d\sigma/dcos\theta$ and A^{FB} at lowest order from the formulæ. This is a case where the "tree approx." fails. Explain where and why.

5/5



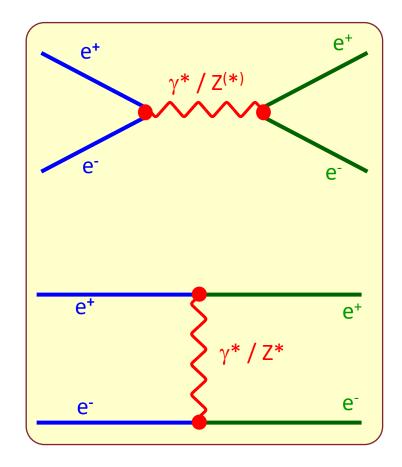
If no success, look to Grünewald, op. cit., pag. 230-232 [simplified explanation: higher orders and selection criteria are important, expecially for peak+2 (\rightarrow init. state brem). The correct approach is to use higher orders also in the prediction].



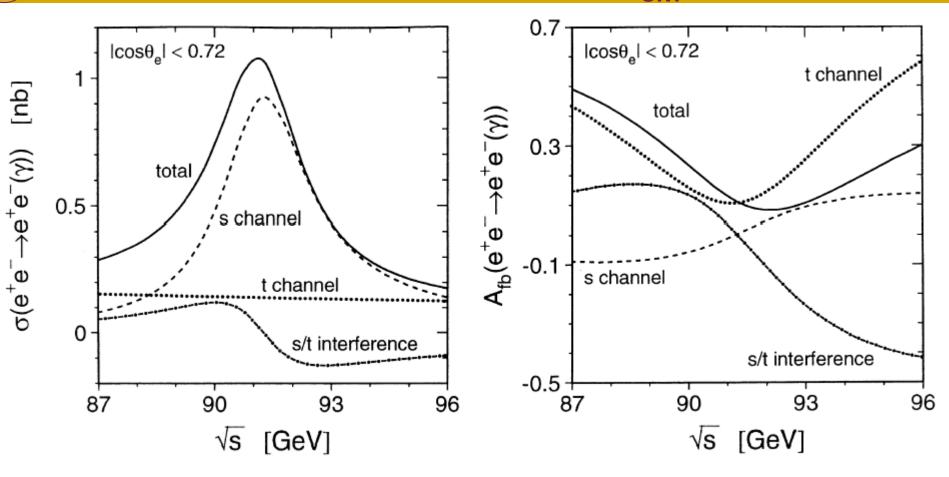
72

$e^+e^- \rightarrow Z \rightarrow e^+e^-$

- Bhabha scattering is more difficult, due to the presence of another Feynman diagram: the γ* / Z exchange in the t-channel;
- 4 Feynman diagrams \rightarrow 10 terms :
 - Z s-channel (Z_s);
 - > γ^* s-channel (γ_s);
 - Z t-channel (Z_t);
 - > γ^* t-channel (γ_t);
 - 6 interferences;
- qualitatively :
 - > @ $\sqrt{s} \approx m_z$ and θ >> 0°, Z_s dominates.
 - \triangleright @ θ ≈ 0°, γ_t dominates for all √s;
 - > @ $\sqrt{s} \ll m_z$ and $\theta \gg 0^\circ$, γ_s and γ_t are both important, while Z_s is negligible.

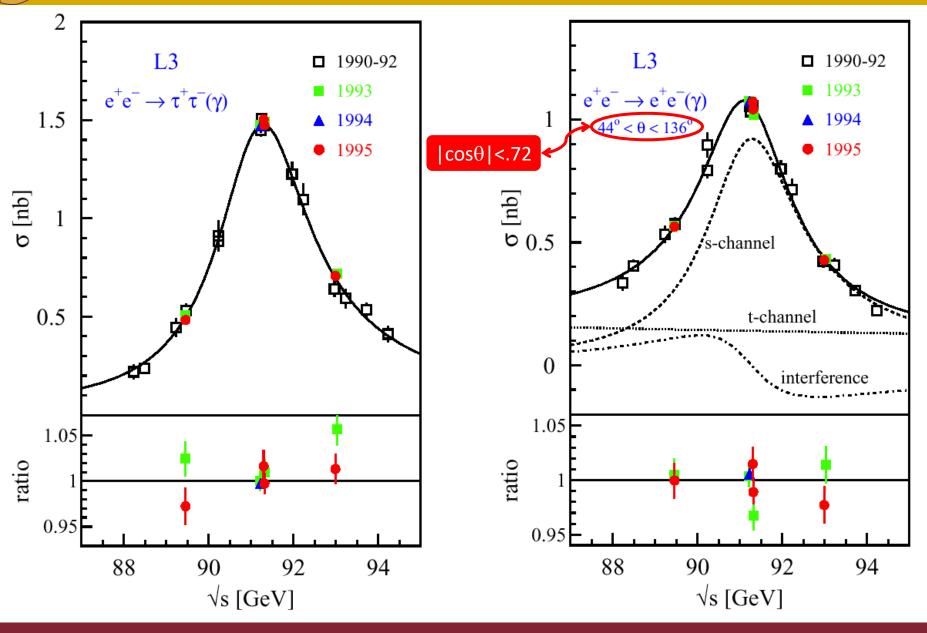


 $e^+e^- \rightarrow Z \rightarrow e^+e^-$: σ_{SM}



- s, t, interference vs \sqrt{s} , with a θ cut $(|\cos\theta| < 0.72, i.e. 44^{\circ} < \theta < 136^{\circ});$
- data @ |cosθ| ≈ 1 taken, but not used here [used for lumi];
- notice : the cut on $\cos\theta$ is NOT instrumental, but used OFFLINE to enhance Z_s over γ_t , considered as bckgd.

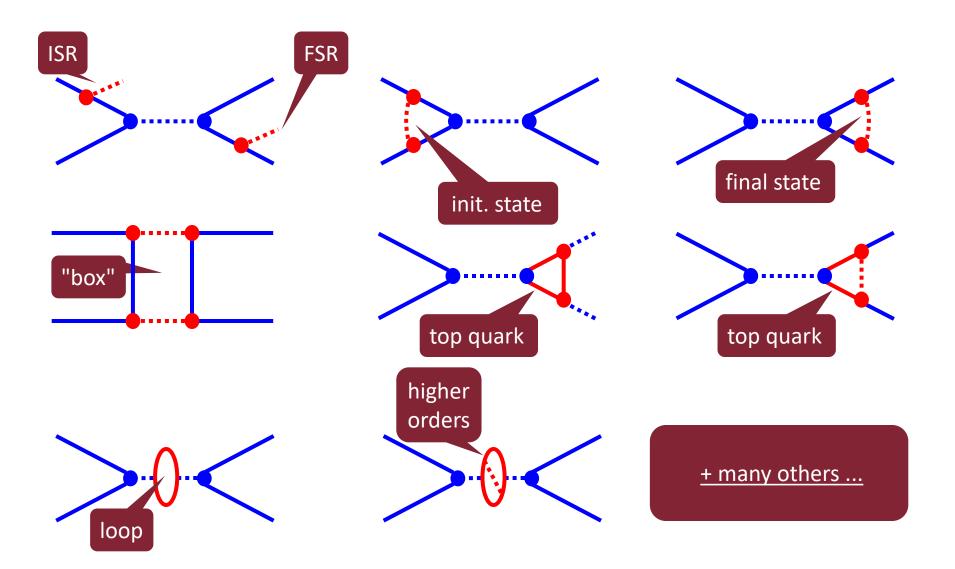
$e^+e^- \rightarrow Z \rightarrow e^+e^-$: results





radiative corrections





radiative corrections: what ? why ?



what?

2/7

- higher orders (both SM and bSM);
- dependent on <u>full</u> SM, QCD included;
- conventionally, classified into QED, weak, QCD, bSM (if any);
- ... or initial and final state;
- > also particles <u>not kinematically</u> <u>allowed at lower \sqrt{s} (e.g. top, Higgs);</u>

<u>computable ?</u>

- in principle <u>yes</u>, if all parameters known;
- in practice, <u>successive approximations</u> ("order n");

necessary ?

yes, because required by the measurement accuracy;

<u>useful ?</u>

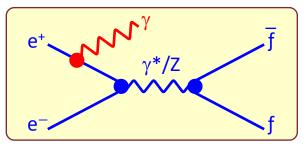
- yes, because they give an indirect access to higher energy, by making lower energy observables (like m_z) dependent on higher energy parameters (like m_{top} or m_H);
- \succ i.e., they "raise" the accessible \sqrt{s} ;
- + more accurate and powerful test of the theory;
- [much work, theses, papers, ...];

how to use the bSM part (e.g. SUSY), both tree-level and higher orders ?

- first, do not include it, and look for discrepancies;
- if disagreement (εὕρηκα !!!), include physics bSM and look for agreement;
- ➢ if not → put a <u>limit</u> on physics bSM.

3/7

radiative corrections: ISR kinematics



One of the simplest r.c. is the QED brem of a (real) γ from one of the initial state e[±] : **ISR** (Initial State Rad.);

• the kinematics is :

$$e^{+}e^{-}(\sqrt{s}, 0, 0);$$

$$\gamma (E_{\gamma}, E_{\gamma}\cos\alpha_{\gamma}, E_{\gamma}\sin\alpha_{\gamma});$$

$$f\overline{f} (\sqrt{s} - E_{\gamma}, -E_{\gamma}\cos\alpha_{\gamma}, -E_{\gamma}\sin\alpha_{\gamma});$$

$$s' \equiv m_{f\overline{f}}^{2} = (\sqrt{s} - E_{\gamma})^{2} - E_{\gamma}^{2} = s(1 - 2E_{\gamma}/\sqrt{s});$$

$$z \equiv s'/s = 1 - 2E_{\gamma}/\sqrt{s}; [s' < s \rightarrow z < 1]$$

$$E_{\gamma} \text{ is fixed and } \alpha \text{-independent:}$$

$$E_{\gamma} = \frac{\sqrt{s}}{2} \frac{s-s'}{s} = \frac{s-s'}{2\sqrt{s}} = \frac{s-m_{f\bar{f}}^2}{2\sqrt{s}}.$$

- **<u>LEP 1</u>** ($\sqrt{s} < m_z + \text{few GeV}$) :

 - > α_{γ} small (brem. dynamics), γ 's mostly in the beam pipe;
 - ▶ condition : $2m_f \le \sqrt{s'} \le \sqrt{s}$;
- <u>LEP 2</u> (√s >> m_z) :
 - $√s' ≈ m_z$ (because of resonance), known as "return to the Z";
 - photon is really monochromatic
 (Γ_z << E_γ) and very energetic;
 - α_γ small (brem. dynamics), γ's mostly in the beam pipe, Z's with high longitudinal momentum, event very unbalanced;
 - vevents easily removed in the analysis, but it decreases the effective event yield.

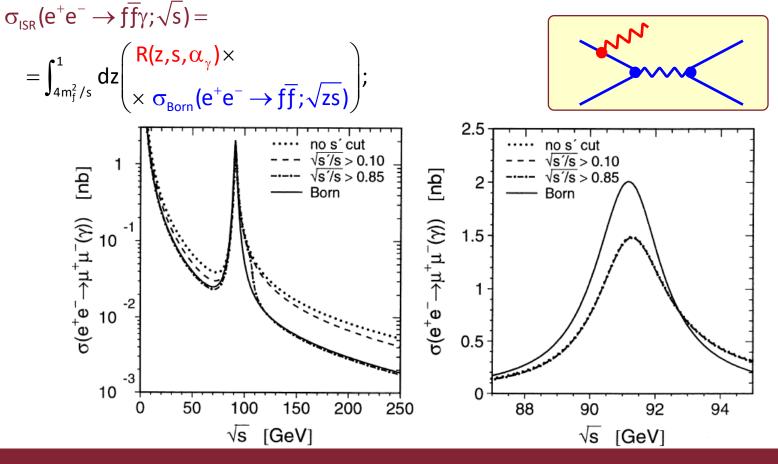
radiative corrections: ISR results

Theoretical treatment :

4/7

- ➤ assume factorization (ISR) ↔ (Z formation);
- > the Z formation at √s' is equivalent to the standard process at √s, without ISR :
- > $R(z,s,\alpha_{\gamma}) = radiator$, i.e. probability (function of \sqrt{s} , z, α_{γ}) for γ brem;
- > <u>R calculable</u> in QED at a given order.

At LEP 2, cut on z ($\approx E_{vis}/\sqrt{s}$), tipically z<0.85).



radiative corrections: results for m_z

A precise computation requires much tedious work : these values are just for understanding [see fig.] :

- $$\begin{split} \bullet \ \sqrt{s} \, |_{\text{Born}}^{\text{max}} &\approx m_{Z} \, (1 + \gamma^{2})^{\frac{1}{4}} \approx m_{Z} \, (1 + \frac{1}{4} \, \gamma^{2}) \approx \\ &\approx m_{Z} + 17 \, \text{MeV}; \\ & \text{[slightly larger]} \end{split}$$
- $\sqrt{s}|_{ISR}^{max} \approx m_z (1 \frac{1}{4} \gamma^2) + \pi \beta \Gamma_z / 8$ $\approx m_z + 89 \text{ MeV};$ [slightly larger];

•
$$\sigma_0^f \equiv \sigma_{Born}(e^+e^- \rightarrow f\bar{f}; \sqrt{s=m_z}) =$$

= $12\pi\Gamma_e\Gamma_f/(m_z^2\Gamma_z^2);$

•
$$\sigma(e^+e^- \rightarrow f\bar{f})|_{Born}^{max} \approx \sigma_0^f (1 + \frac{1}{4}\gamma^2) \approx \approx \sigma_0^f (1 + .00019)$$

[slightly larger];

•
$$\sigma(e^+e^- \rightarrow f\bar{f})|_{ISR}^{max} \approx \sigma_0^f \gamma^\beta (1 + \delta_{sup}) \approx 0.75 \sigma_0^f$$

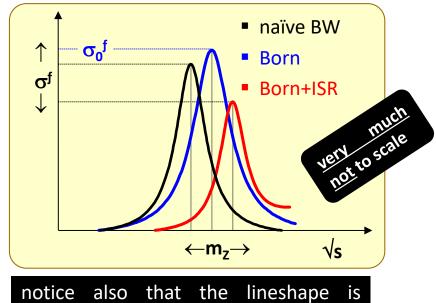
[much smaller]:

the most important effect

5/7

- similar method for $\Gamma_{\rm Z}$:
 - \succ Γ_z s-dependent : Γ_z → sΓ_z / m_z²;
 - > (references);
- $\gamma \equiv \Gamma_z / m_z \approx 0.027;$
- $\beta \equiv 2\alpha [2\ell n (m_z / m_e) 1]/\pi \approx 0.108;$

 $\delta_{sup} \equiv [soft- and virtual-\gamma's, calculable].$



notice also that the lineshape is dependent on the type of the fermion (e.g., for $e^+e^- \rightarrow v\bar{v}$ no γ in final state).

radiative corrections: parameter Δr

[an example : radiative corrections for W^{\pm} and Z mass]

• in the SM, m_w and m_z are related by:

6/7

$$m_{w}^{2} \sin^{2} \theta_{w} = \frac{\pi \alpha}{\sqrt{2} G_{F}}$$
; $\sin^{2} \theta_{w} = 1 - \frac{m_{w}^{2}}{m_{Z}^{2}}$;

- radiative corrections modify the formulæ;
- <u>define</u> the parameters Δr (<u>radiative</u> <u>correction parameter</u>), $\Delta \alpha$ (<u>QED rad. corr.</u>), Δr_w (<u>weak rad. corr.</u>) :

$$m_{W}^{2} \sin^{2} \theta_{W} \equiv \frac{\pi \alpha}{\sqrt{2} G_{F}} \times \frac{1}{1 - \Delta r} \rightarrow$$
$$\Delta r = 1 - \frac{\pi \alpha}{\sqrt{2} G_{F}} \times \frac{m_{Z}^{2}}{m_{W}^{2} (m_{Z}^{2} - m_{W}^{2})};$$
$$\frac{1}{1 - \Delta r} \equiv \frac{1}{1 - \Delta \alpha} \times \frac{1}{1 - \Delta r_{W}};$$

• $\Delta \alpha$ is reabsorbed in $\alpha_{(s)}$, <u>running coupling</u> <u>constant</u> [the _(s) means "function of \sqrt{s} "] : $\Delta \alpha_{(s)} = (\alpha_{(s)} - \alpha_{(s=0)}) / \alpha_{(s)};$ • from QED :

 $\begin{array}{l} \Delta \alpha_{(m^2_z)} \approx 0.07 \rightarrow \alpha_{(m^2_z)} \approx [128.89 \pm 0.09]^{-1}; \\ \mbox{[error from } \int \sigma(e^+e^- \rightarrow hadr.) @ $\sqrt{s} << m_z$] \end{array}$

• the equation with m_w + m_z becomes :

$$m_{W}^{2}\left(1-\frac{m_{W}^{2}}{m_{Z}^{2}}\right)=\frac{\pi\alpha_{(s=m_{Z}^{2})}}{\sqrt{2}G_{F}}\times\frac{1}{1-\Delta r_{W}};$$

• [to select top and Higgs terms] expand Δr_w into parts, dependent on $m_t (\propto m_t^2)$ and $m_H (\propto \ell n m_H)$, and the rest $(\Delta \bar{r}_w)$:

$$\Delta \mathbf{r}_{w} = \Delta \overline{\mathbf{r}}_{w} \Big|_{\mathbf{m}_{t} = \hat{\mathbf{m}}}^{\text{calc.}} + \frac{\partial \Delta \mathbf{r}_{w}}{\partial \mathbf{m}_{t}} \Big|_{\mathbf{m}_{t} = \hat{\mathbf{m}}} \delta \mathbf{m}_{t} + \frac{\partial \Delta \mathbf{r}_{w}}{\partial \mathbf{m}_{H}} \delta \mathbf{m}_{H};$$
$$[\hat{\mathbf{m}} = \mathbf{175 \ GeV}].$$

⁷⁷ radiative corrections: method \rightarrow discovery

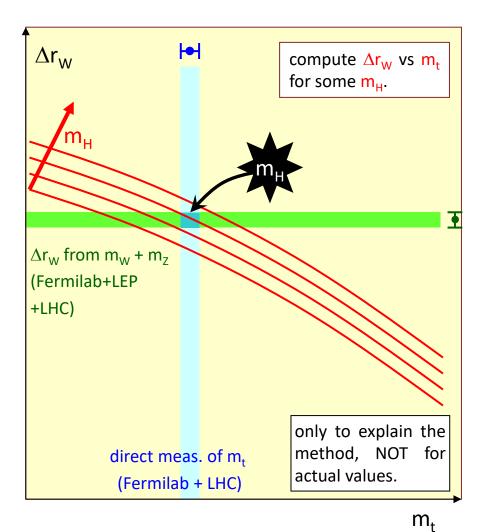


- assume we are in the "post-top, pre-Higgs" era [i.e. 1995-2011] :
- numerically, the sensibility is :

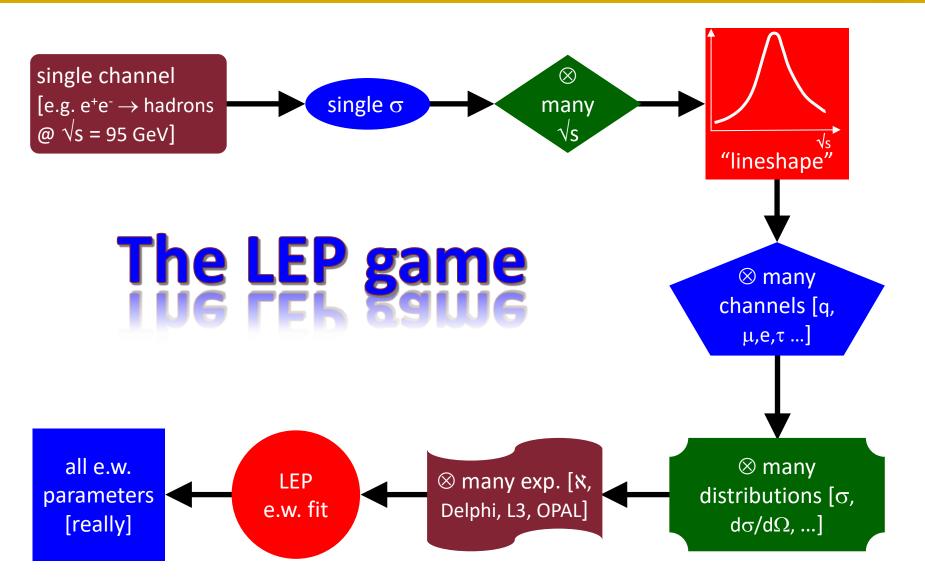
$$\begin{split} \Delta r_{W} &\approx \Delta \overline{r}_{W} \Big|_{\text{calc.}}^{+} \\ &- 0.0019 \Bigg(\frac{m_{t}}{175 \text{GeV}} \Bigg) \Bigg(\frac{\delta m_{t}}{5 \text{GeV}} \Bigg) + \\ &+ 0.0050 \Bigg(\frac{\delta m_{H}}{m_{H}} \Bigg); \end{split}$$

[the two terms have <u>opposite sign</u> and <u>very different size</u>]

- <u>the meas. of</u> m_w, m_z, m_t + the calculation of higher orders of SM allow for a "measurement" of m_H á la Hollik;
- in reality, many observables → global fit.



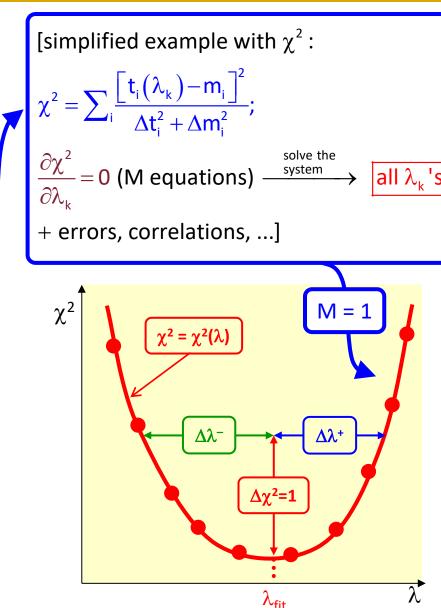
LEP1 SM fit



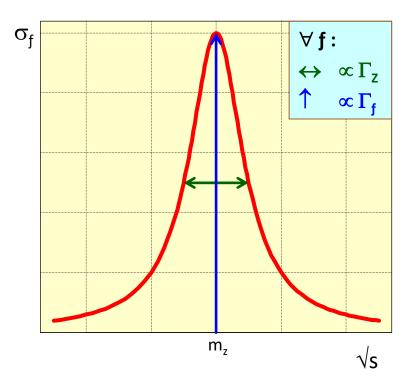
LEP1 SM fit: explanation

- in the SM, the observables [e.g. σ's, dσ/dcosθ's, asymmetries, ...] are (functions of few) parameters like m_z, Γ_z, Γ_f, θ_w ...;
- in an experiment: N observables t_i (i = 1, ..., N) and M SM parameters λ_k (k=1,...,M);
- [at LEP 1, N = few×100, M \leq 10, see later);
- [M is fixed, but the choice is free, e.g. one among m_z , m_w and θ_w is redundant]
- the dependence of t_i from λ_k is known: $t_i = t_i(\lambda_k) \pm \Delta t_i$ (Δt_i = the theoretical error);
- the N observables are measured : m_i ± Δm_i (Δm_i = the convolution of stat. and sys.);
- a (difficult) numerical program computes the "best" λ_k 's which <u>fit</u> the observations;
- then the same values of λ_k are used for all the computations (shown as the "SM fits").
- [since N>>M, the dependence of any λ_k on the single ith meas. is very small.]
- [also test the agreement SM \leftrightarrow data.]

Paolo Bagnaia – PP – 10



LEP1 SM fit: σ vs Γ

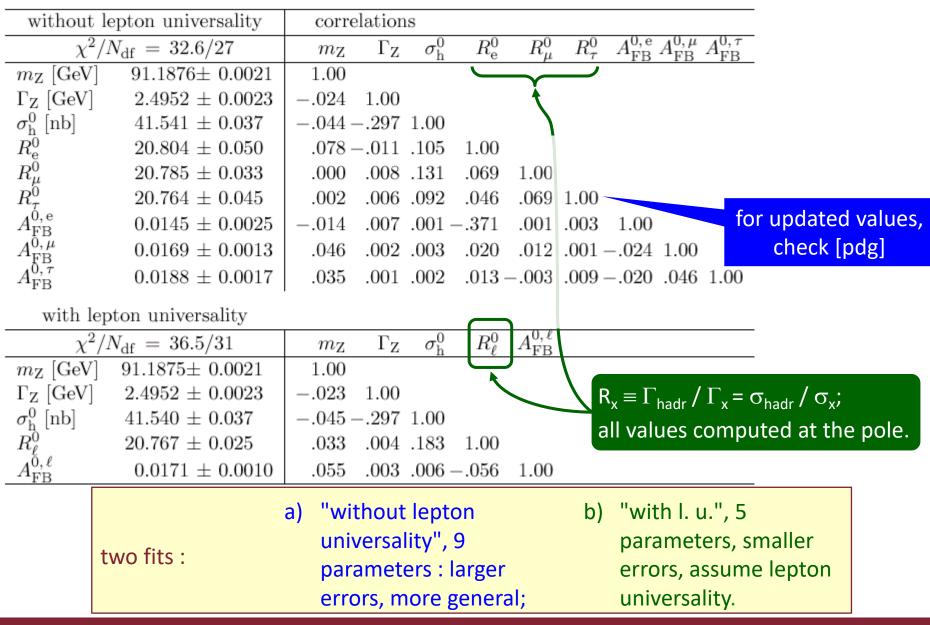


$$\sigma_{Born}(e^+e^- \rightarrow f\overline{f}, \sqrt{s} = m_z) = \frac{12\pi\Gamma_e\Gamma_f}{m_z^2\Gamma_z^2}.$$

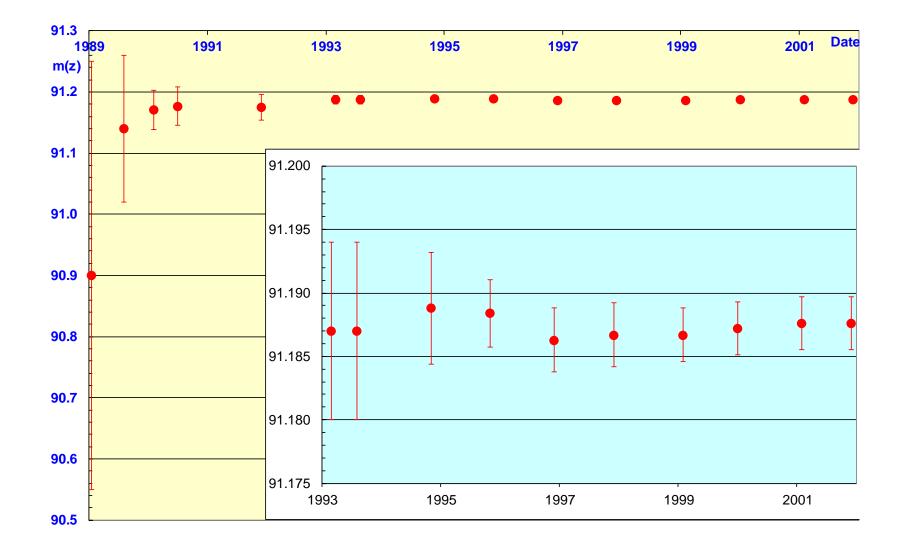
- in LEP jargon, "lineshape" means $\sigma(e+e- \rightarrow Z \rightarrow f\bar{f})$ vs \sqrt{s} (*) for a given fermion pair of type f;
- the lineshape shows the characteristic "bell shape", due to the resonance;
- both the height and the width of the bell depend on the e.w. parameters;
- the strategy is
 - a) first, <u>measure</u> mass, full and partial widths of the Z;
 - b) then, <u>fit</u> :
 - > number of light v's (= fermion families);
 - electro-weak couplings.

(*) warning : NOT " $d\sigma/d\sqrt{s}$ ", which is meaningless.

LEP1 SM fit: m_z , Γ_z

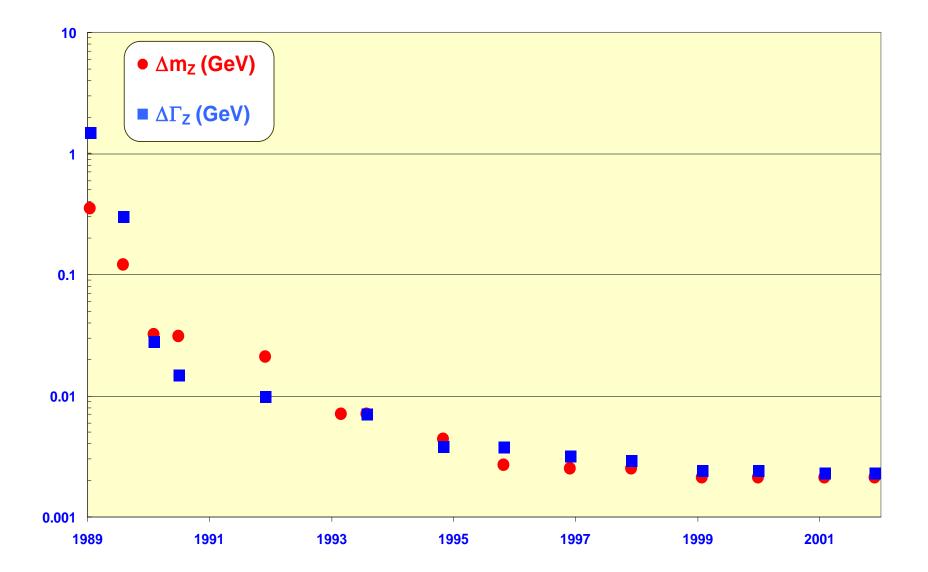


LEP1 SM fit : m_z





LEP1 SM fit: Δm_z , $\Delta \Gamma_z$



7/9

LEP1 SM fit: n_v

- Neutrinos are the lightest component of the fermion families [in SM no theor. explanation, just matter of fact];
- assuming this case also for (hypothetical) further families, i.e. additional v's lightest member of a family;
- the decay Z → vv̄ is important (~20%), but not observable (but "single γ", not treated here);
- but it contributes to Γ_z (observable);
- indirect detection: measure Γ_z , subtract the contribution of observable decays (" $\Gamma_{visible}$ "), get " $\Gamma_{invisible}$ " and compute n_v (more precisely the number of <u>light</u> v, i.e. $m_v < m_z/2$):

$$\begin{split} \Gamma_{\text{inv}} &\equiv \Gamma_z - \sum_{j=q,\ell^{\pm}} \Gamma_j = \Gamma_z - \Gamma_{\text{hadr}} - 3\Gamma_{\ell^{\pm}};\\ n_v &= \frac{\Gamma_{\text{inv}}}{\Gamma_v^{\text{SM}}} = \left(\frac{\Gamma_{\text{inv}}}{\Gamma_z^{\text{exp}}}\right) \left(\frac{\Gamma_z^{\text{SM}}}{\Gamma_v^{\text{SM}}}\right). \end{split}$$

- [the last step to decrease stat and syst errors]
- it turns out :

 $n_v = 2.9840 \pm 0.0082$

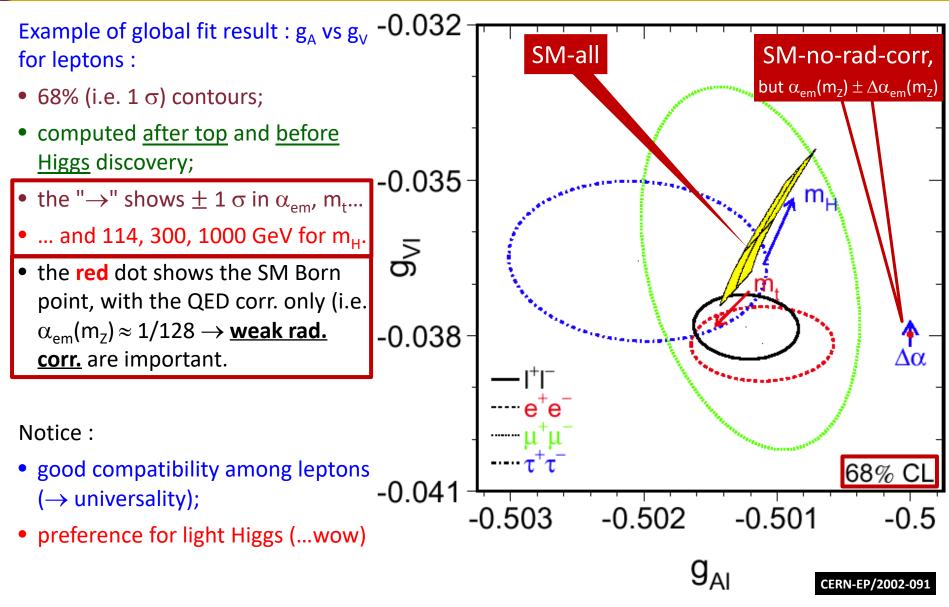
i.e. $n_v = 3$, no other families

[probably the best, most known, most quoted LEP result, see <u>fig on pag. 2</u>].

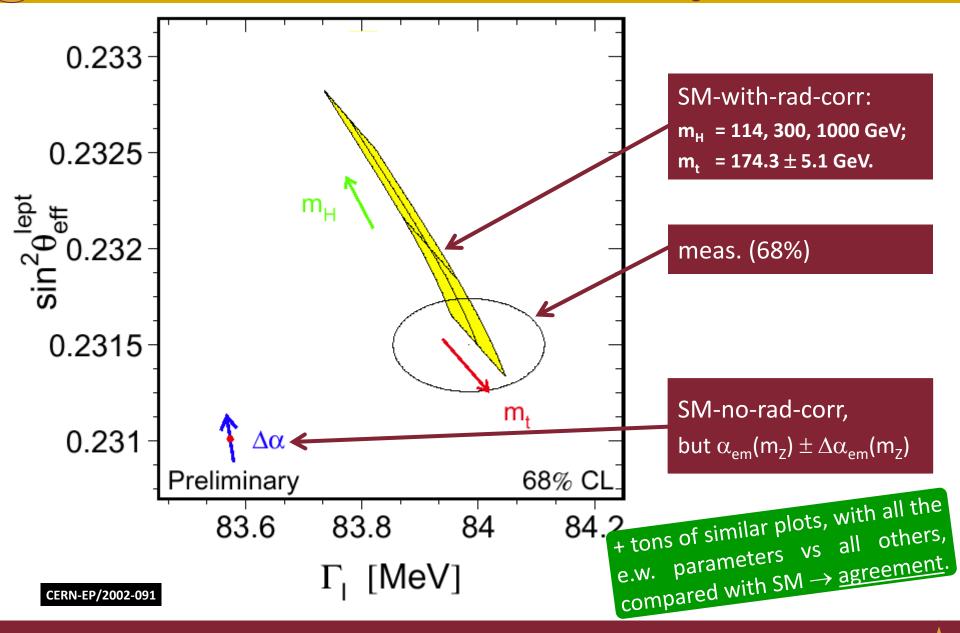
NB strictly speaking, $n_v =$ width of invisible decays normalized to Γ_v ; i.e. it could get contributions from other invisible decays (physics bSM, e.g. neutralino); in such cases, <u>" n_v " not an integer</u>.

$$\begin{split} \sigma_{\text{Born}}(e^{+}e^{-} \rightarrow f\overline{f}, \ \sqrt{s} = m_{z}) = & \frac{12\pi\Gamma_{e}\Gamma_{f}}{m_{z}^{2}\Gamma_{z}^{2}}; \\ \Gamma_{v}^{\text{SM}} = & \frac{G_{F}m_{z}^{3}c_{f}}{12\sqrt{2}\pi}; \qquad \Gamma_{z} = \sum_{i}\Gamma_{i}. \end{split}$$

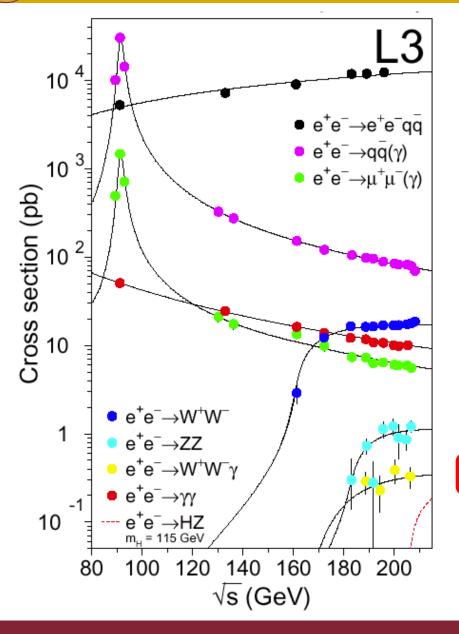
LEP1 SM fit : g_A vs g_V for leptons



LEP1 SM fit : $sin^2\theta$ vs Γ_e



$e^+e^- \rightarrow W^+W^- @$ LEP2: LEP2 processes

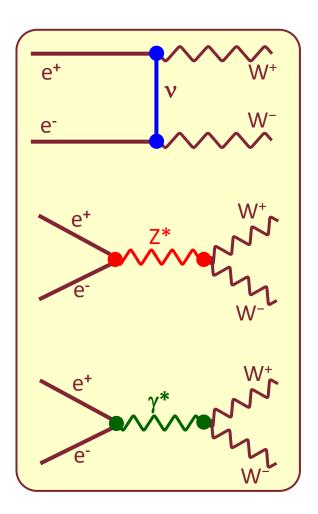


In 1994-2000 LEP gradually $\sqrt{s} = m_z \rightarrow 200 \text{ GeV}$

- LEP1 was dominated by the Z pole;
- on the contrary, LEP2 is "democratic";
- many final states :
 - > "2 photons", e.g. $e^+e^- \rightarrow e^+e^- q\bar{q}$;
 - \succ "2 fermions", e.g. e⁺e⁻ → Z^{*}/ γ^{*} → qq̄;
 - \succ "4 fermions", e.g. $e^+e^- \rightarrow W^+W^- \rightarrow q\bar{q} q\bar{q}$;
 - $ightarrow e^+e^- \rightarrow \gamma\gamma;$
 - > Higgs searches (special case of 4 fermions).
- only W⁺W⁻ and Higgs in these lectures.

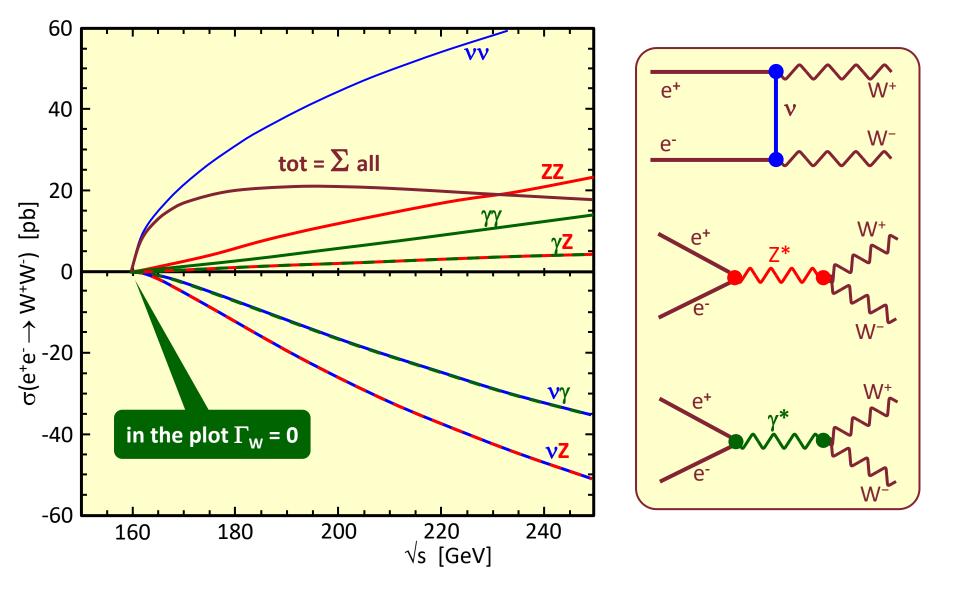
$e^+e^- \rightarrow W^+W^-$ @ LEP2: Feynman diagrams

- the process $e^+e^- \rightarrow W^+W^- \rightarrow f\bar{f}f\bar{f}$ dominates the 4 fermions sample;
- in lowest order, there are three Feynman diagrams;
- all the vertices of the e.w. theory: ffW, ffZ, ff γ , ZWW, γ WW;
- the overall (finite) cross section results from delicate cancellations among the 6 terms (3 |module|² + 3 interferences) [next slide];
- therefore, any possible anomaly (discrepancy wrt SM, e.g. an anomaly in the couplings) would result in evident deviations from the predictions.

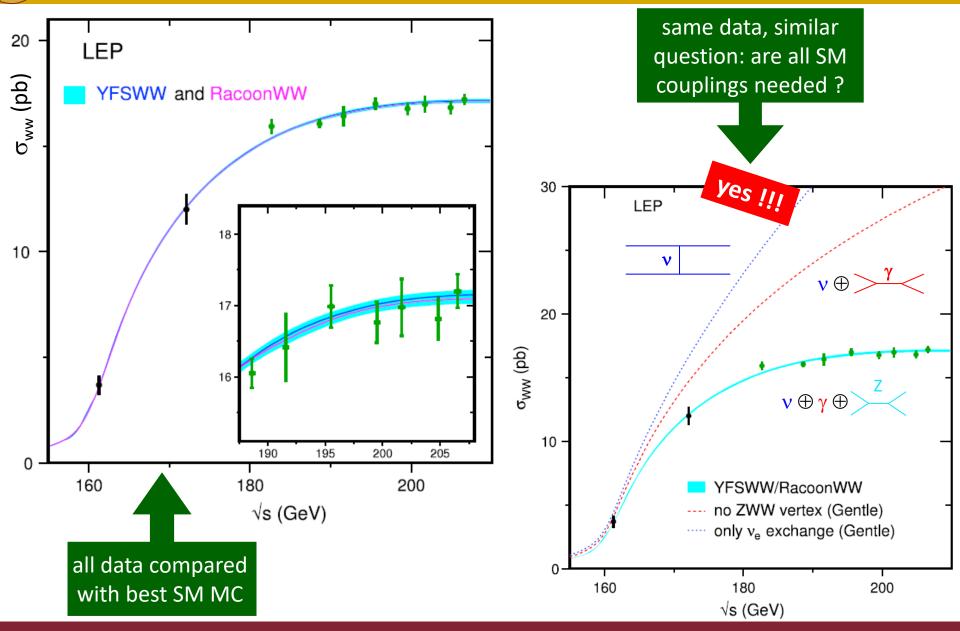




$e^+e^- \rightarrow W^+W^-$ @ LEP2: cross section



$e^+e^- \rightarrow W^+W^- @ LEP2: cross section results$

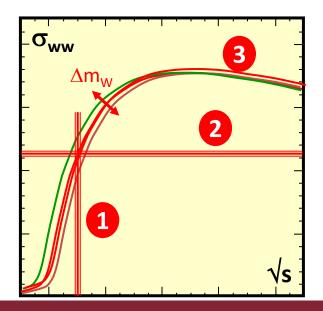


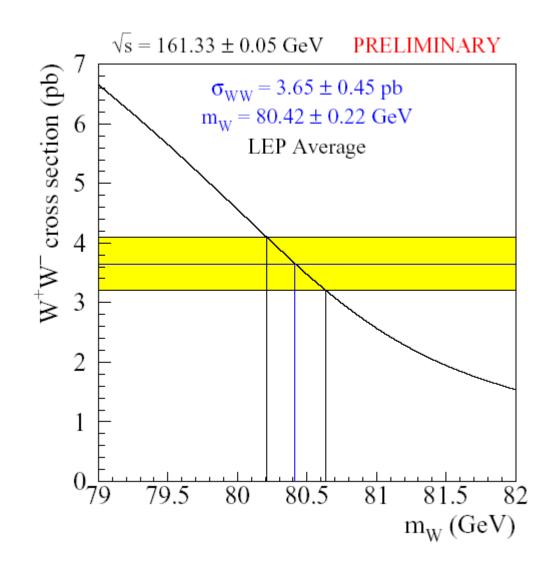
$e^+e^- \rightarrow W^+W^-$ @ LEP2: W mass from σ

Technically clever and simple :

- compute $\sigma(e^+e^- \rightarrow W^+W^-) = \sigma(m_W)$;
- compute the "best" \sqrt{s} , by combining
 - > sensitivity $(\partial \sigma / \partial m_w = max) \rightarrow \sqrt{s} \approx$ threshold;
 - (Δσ^{stat} ↓) → (σ ↑) → (√s ↑);
 - \succ take into account Δ_{theory} and syst.;

• <u>measure</u>.



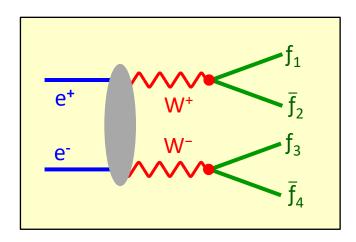






- kinematical constraints (e.g. 4-mom conservation) help in the analysis :
 - selection criterion (rejection of bad measurements or event classification in other processes);
 - improve resolution (see next);
- this case as an example : likelihood fit to m_w, $\Gamma_{\rm w}$;
- compare analysis/fit on real data wrt same procedure on "pseudo-events" (physics + detector mc);
- $\Gamma_{\rm W}$ strongly (anti-)correlated with experimental resolution ["pessimistic" detector mc $\rightarrow \sigma_{\rm meas}$ too large $\rightarrow \Gamma_{\rm W}$ too small !!!];

- systematics from:
 - ISR/FSR parameterization;
 - reconstruction algorithms (expecially jets, ex. color reconnection, Bose-Einstein correlations);
 - many other sources...
- consistency checks : in this case m_z , Γ_z from $e^+e^- \rightarrow ZZ$ (with smaller stat).



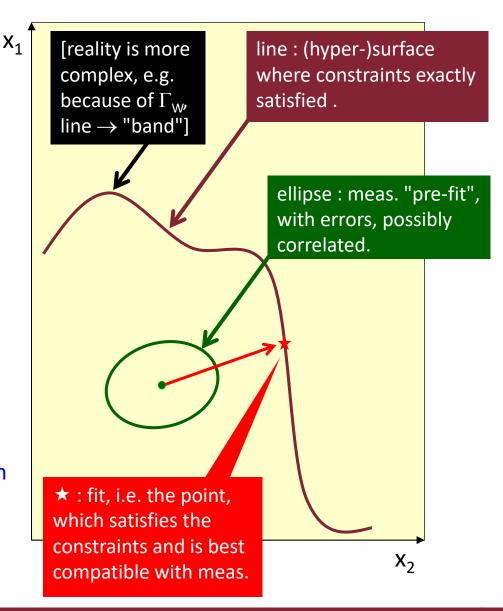


In the parameter space :

- n unkn. = 4 * n_{body} = 16;
- N meas. [e.g. E, \vec{p} for jets / ℓ^{\pm} 's];
- K equations [= 4 mom + masses^(*)];
- C (=N+K-n) constraints;
- E.g. : $e^+e^- \rightarrow W^+W^- \rightarrow f_1f_2f_3f_4$, n=16 :
 - > 4 jets : N=16, K=5 → <u>C = 5</u>;

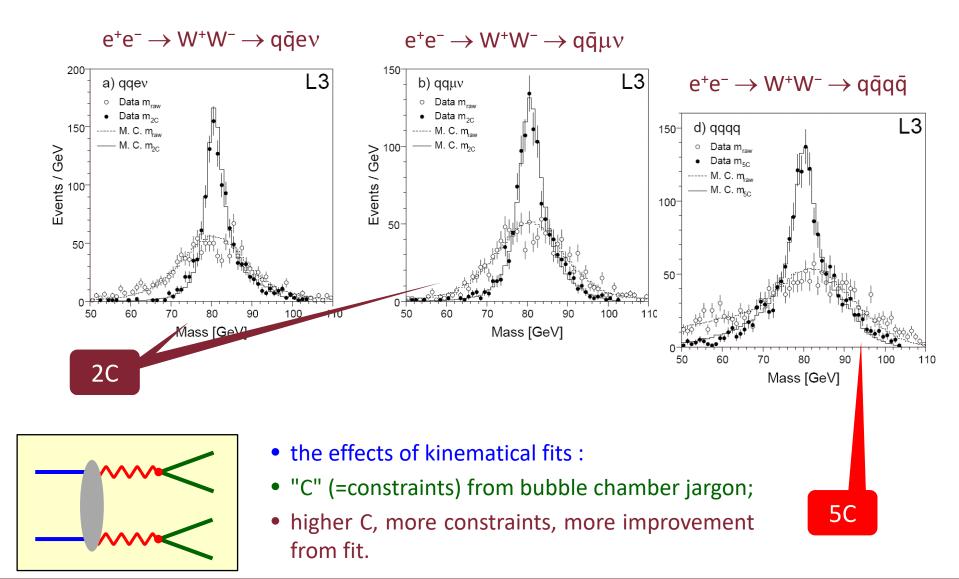
 - > $\ell^+\nu\ell^-\bar{\nu}$: N=8, K=7 → <u>C < 0</u>;
- If C > 0, a kinematical fit is possible (a simplified sketch in x₁, x₂, i.e. n=2)

[the red arrow " \rightarrow " represents a statistical estimate (χ^2 , likelihood) and a computation method (e.g. Lagrange multipliers)].



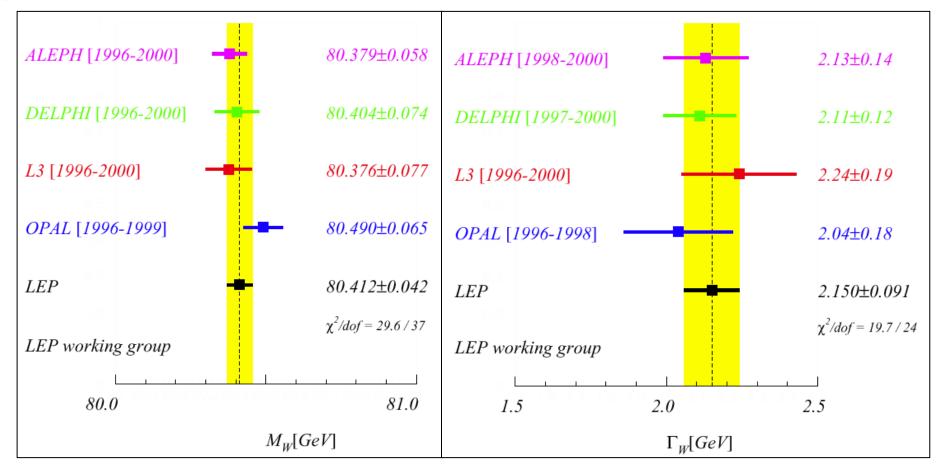
^(*) $m_{W^+} = m_{W^-}$ and $m_v \approx 0$.

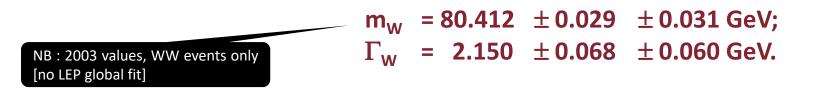






$e^+e^- \rightarrow W^+W^- @ LEP2: m_w, \Gamma_w results$







$e^+e^- \rightarrow W^+W^- @ LEP2: W^{\pm} decay$

- in the SM the W[±] boson decays through CC interactions (V-A);
- therefore the coupling is the same for all ff' pairs, providing :
 - > m($f\bar{f}$) < m_w (→ no t decays);
 - > qq mixing (à la CKM) must be used;
- ASSUMING (*just for the discussion*) a diagonal CKM matrix, W⁺ decays into e⁺ν, μ⁺ν, τ⁺ν, ud, cs̄, (tb̄ forbidden);
- [if W⁻, then corresponding antiparticles];
- (m_f << m_w and CKM ≈ diagonal) → same BR for all channels (but color factor);
- the V-A theory gives in lowest order : $\Gamma(W \rightarrow ff') = G_F m_W^3 / (6\sqrt{2\pi}) \approx 226 \text{ MeV};$
- (3 leptons + 2 quarks × 3 colors = 9) :

 $\Gamma_{W} = \Sigma \Gamma_{i}(W \rightarrow ff') \approx 9 \times 226 \text{ MeV} =$ = 2.05 GeV;

BR(W $\rightarrow \ell^{\pm} \nu$) $\approx 1/9 \approx 0.11$;

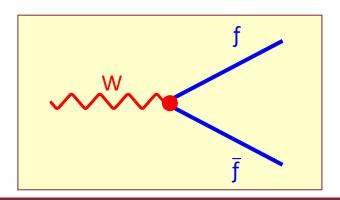
 $BR(W^+ \rightarrow u\bar{d}) \approx BR(W^+ \rightarrow c\bar{s}) \approx 1/3 \approx 0.33;$

 if the correct quark mixing is used, the CKM matrix element V_{qq'} must be considered :

 $\Gamma(W \rightarrow q\bar{q}') = |V_{qq'}|^2 G_F m_W^3 / (6\sqrt{2\pi});$

 $\Gamma_{W} = \Sigma \Gamma_{i}(W \rightarrow ff') = \underline{unchanged};$

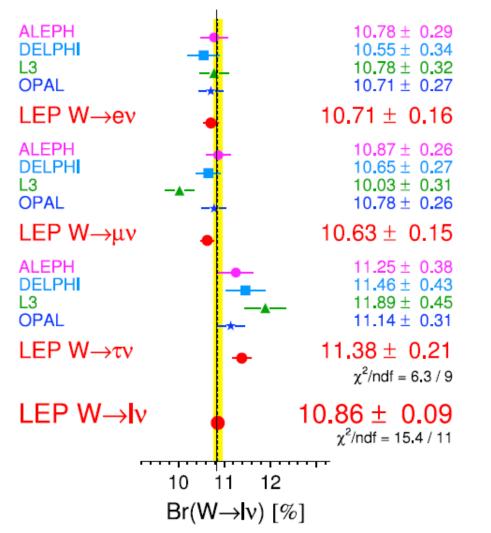
 $\mathsf{BR}(\mathsf{W} \rightarrow \mathsf{q}\bar{\mathsf{q}}') \approx |\mathsf{V}_{\mathsf{q}\mathsf{q}'}|^2 / 3.$

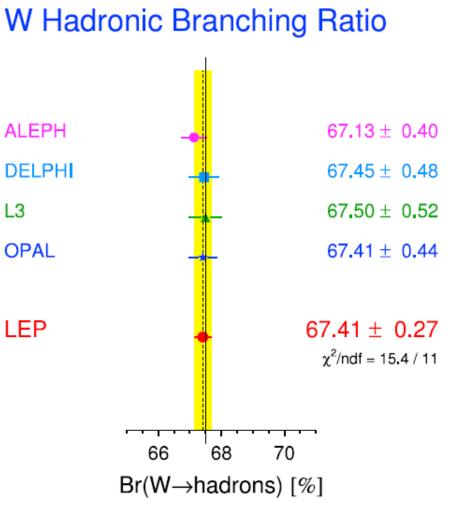


11/12

$e^+e^- \rightarrow W^+W^- @ LEP2: W^{\pm} decay results$

W Leptonic Branching Ratios







$e^+e^- \rightarrow W^+W^- @ LEP2: m_w vs \Gamma_w$

In the SM, $m_{\rm W}$ and $\Gamma_{\rm W}$ are correlated:

- are the previous measurements consistent ?
 - > <u>yes</u>, see the plot;
- can do better ? i.e. check the SM with all the LEP measurement ?

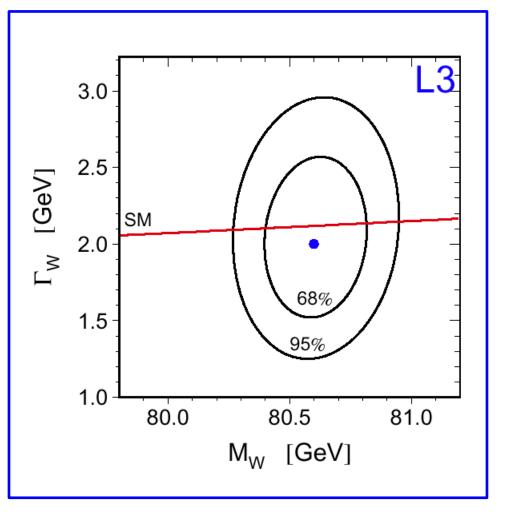
➢ yes;

 even better ? i.e. add also the other SM non-LEP measurement, i.e. v's and low-energy ?

yes, see next slide;

 is the fit producing a value for the (still) unknown parameters, e.g. m_H ?

➢ yes.



global LEP(1+2) fit

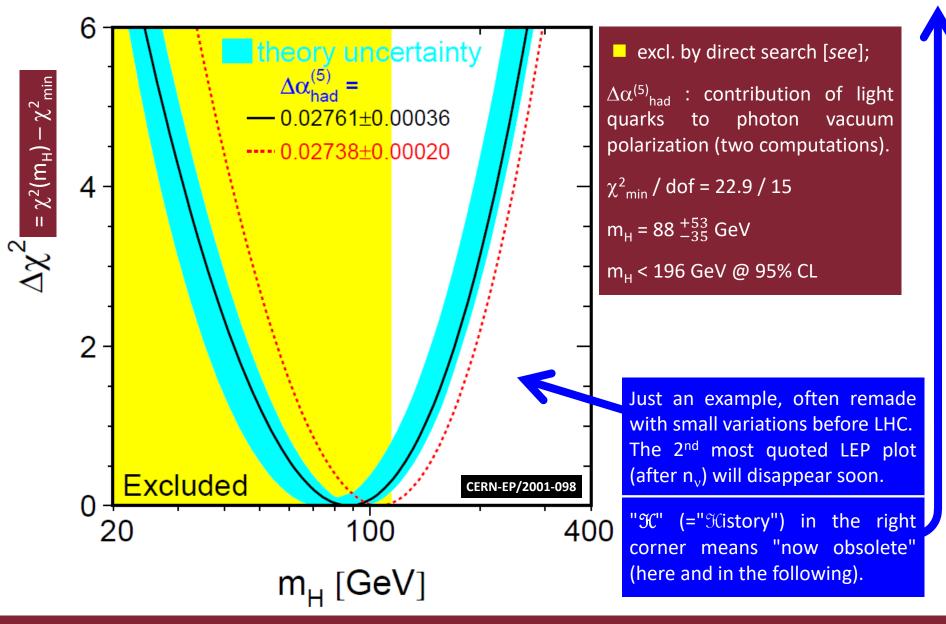
	Measurement	Pull	(O ^{meas} –O ^{fit})/σ ^{meas} -3 -2 -1 0 1 2 3	9
$\Delta \alpha_{had}^{(5)}(m_Z)$	0.02761 ± 0.00036	-0.16	-3-2-10123	circa A.D. 2000, at the end of LEP era.
m _z [GeV]	91.1875 ± 0.0021	0.02		the end of LEP and
Γ _z [GeV]	2.4952 ± 0.0023	-0.36	•	SI Era.
σ_{had}^{0} [nb]	41.540 ± 0.037	1.67		
R _I	20.767 ± 0.025	1.01	-	
A ^{0,I}	0.01714 ± 0.00095	0.79	-	experiment - theory
A _I (P _τ)	0.1465 ± 0.0032	-0.42	-	error ,
R _b	0.21644 ± 0.00065	0.99		
R _c	0.1718 ± 0.0031	-0.15		expected gaussian, μ =0, σ =1;
A ^{0,b}	0.0995 ± 0.0017	-2.43		
R _c A ^{0,b} A ^{0,c} _{fb}	0.0713 ± 0.0036	-0.78	-	$\chi^2 = \sum_i (\text{pull}_i)^2;$
A _b	0.922 ± 0.020	-0.64	-	
A _c	0.670 ± 0.026	0.07		χ^2 / dof = 25.5 / 15 \rightarrow $\mathcal{P}(\chi^2)$ =4.4%.
A _I (SLD)	0.1513 ± 0.0021	1.67		
$sin^2 \theta_{eff}^{lept}(Q_{fb})$	0.2324 ± 0.0012	0.82	-	
m _w [GeV]	80.426 ± 0.034	1.17		
Г _w [GeV]	2.139 ± 0.069	0.67	-	This nice agreement was
m _t [GeV]	174.3 ± 5.1	0.05		NuTeV $\sigma_{CC,NC}(vN)$ mainly used to:
sin²θ _w (νN)	0.2277 ± 0.0016	2.94	4	 claim the quality of the
Q _W (Cs)	-72.83 ± 0.49	0.12	*	SM (and exp.'s);
			-3 -2 -1 0 1 2 3	• predict the (unknown) mass of the Higgs.

1/2



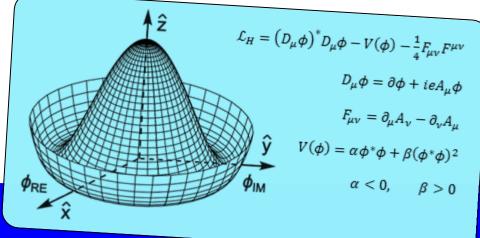
global LEP(1+2) fit : m_H prediction





iv. Physics 2 : Higgs

- 1. 15. [...]
- 16. Higgs search at LEP1
- 17. <u>Higgs search at LEP2</u>
- The Higgs boson has been (*very likely*) discovered at LHC, definitely not at LEP.
- Why remember an old and not-so-nice story, like the LEP search of the Higgs ?
- Because it is very instructive almost all searches are unsuccessful → in practice limits and exclusions are much more frequent than discoveries;
- [also, in the past fluctuations/mistakes have been rare, but not null]



• go \rightarrow § 11, then come back;

- Higgs properties are treated in § LHC [+ RQM + EWI];
- here only an incomplete discussion for Higgs production in e⁺e⁻ at LEP1 & LEP2 energies.

Higgs search @ LEP1

- In the SM the Higgs boson is at the origin of fermion masses;
- at least one H, neutral, spin-0;
- only 1 H → "minimal SM" (<u>MSM</u>, the case discussed in these lectures);
- m_H <u>free parameter</u> of SM (but m_H < 1 TeV);
- in the MSM, if m_H is given, <u>the dynamics is</u> <u>completely determined and calculable</u> (couplings, cross sections, BR's, angular distributions, ...);
- properties :
 - charge : 0; spin : 0; J^P = 0⁺;
 - coupling with fermions f :

$$\Gamma(H \rightarrow f\overline{f}) = \frac{c_f}{4\pi\sqrt{2}} G_F m_H m_f^2 \beta_f^3;$$

$$\beta_f = \sqrt{1 - 4m_f^2 / m_H^2}; \quad c_f = \begin{cases} 1 \text{ [leptons]} \\ 3 \text{ [quarks]} \end{cases};$$

- > [notice: $\Gamma_f \propto m_f^2$);
- therefore, H decays mainly in the fermion pair of highest mass kinematically allowed;
- ➤ therefore, if $m_H > 2m_b$ (i.e. > 10 GeV), mainly <u>H → bb</u>.
- Z \rightarrow HH (spin-statistics, like $\rho^0 \rightarrow \pi^0 \pi^0$);
- in lowest order only:
 - > Z \rightarrow H γ (Z, H neutral !!!) [or H \rightarrow Z γ];

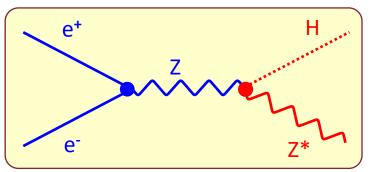
however, (H $\rightarrow \gamma\gamma$) essential for the discovery (see § LHC).

- ➤ H → gg (no strong interactions);
- > but $H \rightarrow Z\gamma$, $\gamma\gamma$, gg through higher order processes.

more complete discussion in § LHC, e.g. discussion of $H \rightarrow Z$, W decays.

Higgs search @ LEP1: Bjorken process





• LEP 1 ($\sqrt{s} \approx m_z$) : $e^+e^- \rightarrow Z \rightarrow HZ^* \rightarrow (f\overline{f})(f\overline{f})$;

i.e. the Higgs production is one of the possible Z decays :

$$\frac{1}{\Gamma(Z \to f\overline{f})} \frac{d\Gamma(Z \to Hf\overline{f})}{dx} =$$

$$= \frac{G_F m_Z^2}{24\sqrt{2}\pi^2} \frac{(12 - 12x + x^2 + 8y^2)\sqrt{x^2 - 4y^2}}{(x - y^2)^2};$$

$$x = \frac{2E_{H}}{m_{z}} = \frac{m_{z}^{2} + m_{H}^{2} - m_{f\bar{f}}^{2}}{m_{z}^{2}}; \quad y = \frac{m_{H}}{m_{z}}.$$

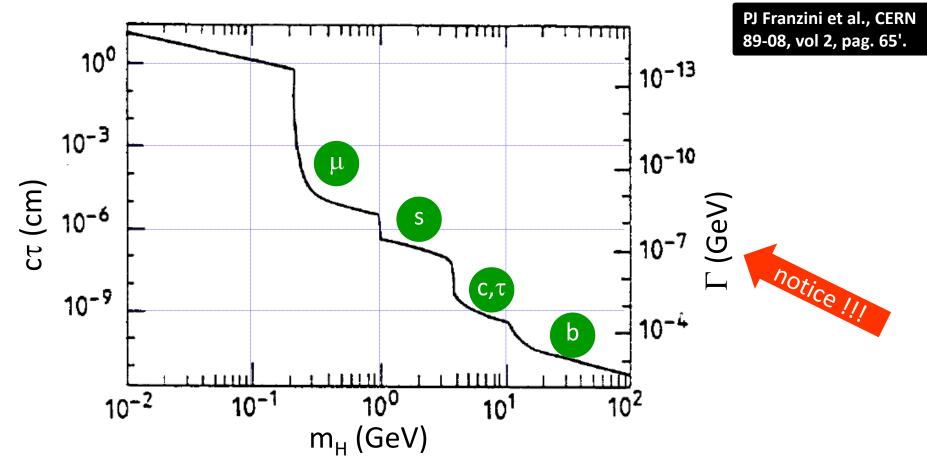
 $e^+e^- \rightarrow Z \rightarrow HZ^*$ [Bjorken process]

- kinematical constraint : $\sqrt{s} \approx m_Z > m_{Z^*} + m_H \rightarrow m_H < m_Z$
- best observable when $Z^* \rightarrow \ell^+ \ell^-$ (no bckgd), $H \rightarrow b \overline{b}$ (BR $\ge 80\%$);

• Kinematics not difficult, e.g. $Z^* \rightarrow \mu^+ \mu^-$, m(Z*) = m_{µµ}, E(Z*) = E_{µµ}, m_H² = s + m_{µµ}² - 2 $\sqrt{s}E_{µµ}$. ok ?

Higgs search @ LEP1: decay predictions

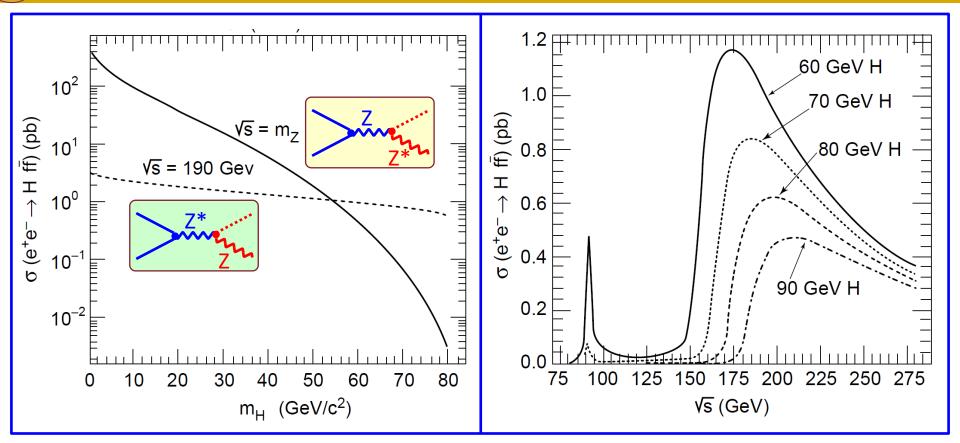




The main decay product of H is the $f\bar{f}$ of largest mass compatible with $m_{\rm H}$: e.g. means H \rightarrow ss.

When a new threshold opens up, there is a "step" in $c\tau$ (~1/ Γ), rounded by phase space.

Higgs search @ LEP1: predictions



For $\sqrt{s} \approx m_z$ (real Z) and $m_H \ll m_z$, the Bjorken process ($e^+e^- \rightarrow Z \rightarrow HZ^*$) has a sizeable cross section, but at larger m_H it essentially disappears \rightarrow go to larger \sqrt{s} . The predictions at $\sqrt{s} \gg m_Z$ come from a similar process ($e^+e^- \rightarrow Z^* \rightarrow HZ$, virtual Z*), known as "<u>higgs-strahlung</u>" [*next slides*].

Higgs search @ LEP1: results

expected

events

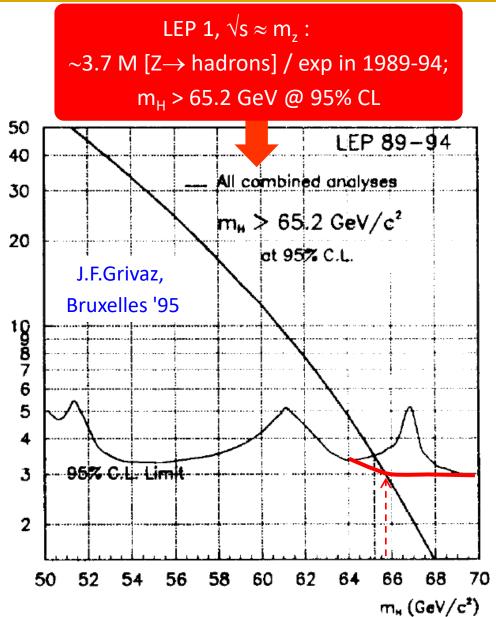
n ber

- <u>this</u> plot summarizes the limits of the four experiments :
 - A :63.1 GeV
 - D:55.4

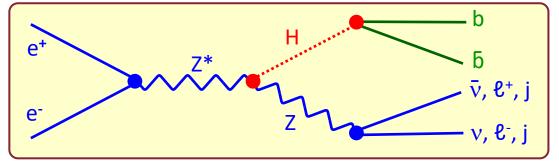
5/5

- L : 60.2
- O : 59.1 ";
- the candidate @ m_H = 67 GeV (OPAL) reduces the limit by few × 100 MeV;
- a test case for the method, discussed in § limits; notice :
 - the <u>combined</u> limit is "better" than any single exp.;
 - the "worst" <u>observed</u> limit does not come necessarily from the "worst" exp.;
 - … because it is a random variable;

conclusion: move to higher √s, i.e.
 Bjorken process → higgs-strahlung.



Higgs search @ LEP2

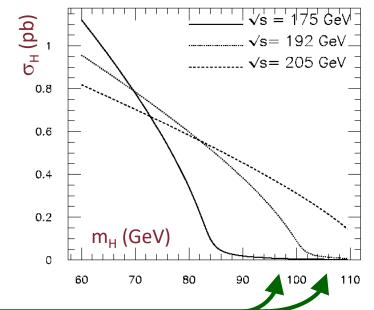


$e^+e^- \rightarrow Z^* \rightarrow HZ$ [higgs-strahlung]

- LEP 2 : process of "higgs-strahlung" (= radiative emission of a Higgs boson from a Z*);
- i.e. the higgs production is a 4fermion final state, mediated by a virtual Z* [like e⁺e⁻ → W⁺ W⁻ → 4f];
- kinematical constraint :

 $\sqrt{s} = m_{Z^*} > m_Z + m_H$

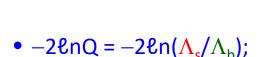
• [no *K* here, because of possible future colliders, see later].



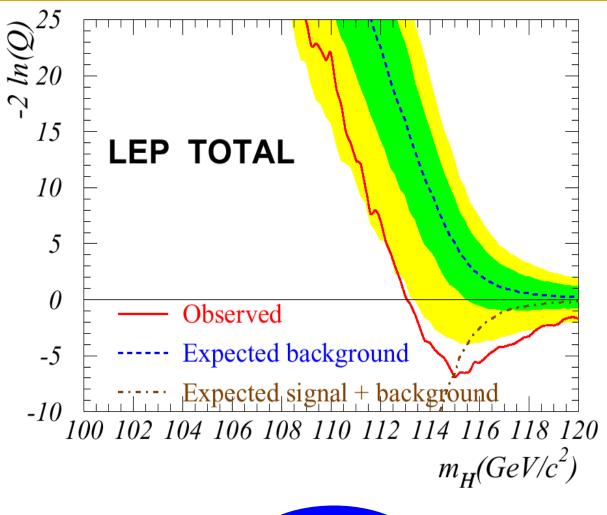
$$\begin{split} & \left[\begin{array}{c} \sigma_{0}(e^{+}e^{-}\rightarrow Z^{*}\rightarrow ZH) = \\ & = \frac{G_{F}^{2}m_{Z}^{4}}{24\pi s} \Big[\left(g_{V}^{\ell}\right)^{2} + \left(g_{A}^{\ell}\right)^{2} \Big] \sqrt{\lambda} \frac{\lambda + 12m_{Z}^{2}/s}{\left(1 - m_{Z}^{2}/s\right)^{2}}; \\ & \left[\lambda \right] & = \left(1 - m_{H}^{2}/s - m_{Z}^{2}/s\right)^{2} - 4m_{H}^{2}m_{Z}^{2}/s^{2}; \\ & \left[\frac{1}{\sigma_{0}} \frac{d\sigma_{0}}{d\cos\theta} = \frac{\lambda^{2}\sin^{2}\theta + 8m_{Z}^{2}/s}{4\lambda^{2}/3 + 16m_{Z}^{2}/s} \xrightarrow{s \text{ large}}{3} \frac{3}{4}\sin^{2}\theta. \end{split}$$

Higgs search @ LEP2: LEPC 3/11/2000





- -2ℓnQ(m_H=115) = -7;
- if interpreted as a discovery
 - > $m_{H} = 115^{+1.3}_{-0.9} \text{ GeV};$
 - > $1-CL_{b} = 4.2 \times 10^{-3};$
 - ≻ i.e. "2.9 σ";
- if interpreted as a limit :
 - ▷ m_H > 113.5 GeV @ 95%CL.





Higgs search @ LEP2: LEPC 3/11/2000

20 A PARTY ON

IB 100

Total Current DELPHI LUMINOSIT

RECOMMENDATION

Given the consistency for the combined results with the hypothesis of the production of a SM Higgs boson with a mass of 115 GeV, and an observed excess in the combined data set of 2.9 a. a further run with 200 pb⁻¹ per experiment at 208 GeV would enable the four experiments to establish a 5 discovery.

The four experiments consider the search for the SM Higgs boson to be of the highest importance, and CERN should not miss such a unique opportunity for a discovery.

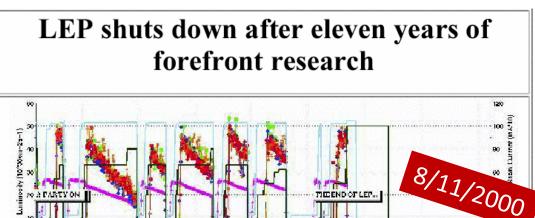
Therefore, we request to run LEP in 2001 to collect $\mathcal{O}(200 \text{ pb}^{-1})$ at $\sqrt{s} \ge 208 \text{ GeV}$.



3/6

ALEPH, DELPHI, L3, OPAL The LEP Higgs Working Group

P. Igo-Kemenes - LEP Seminar - Nov. 3, 2000



TIECEND OF LEP.

00:00

12:00

OPALLUMINOSITY.

15:00

OC: BR

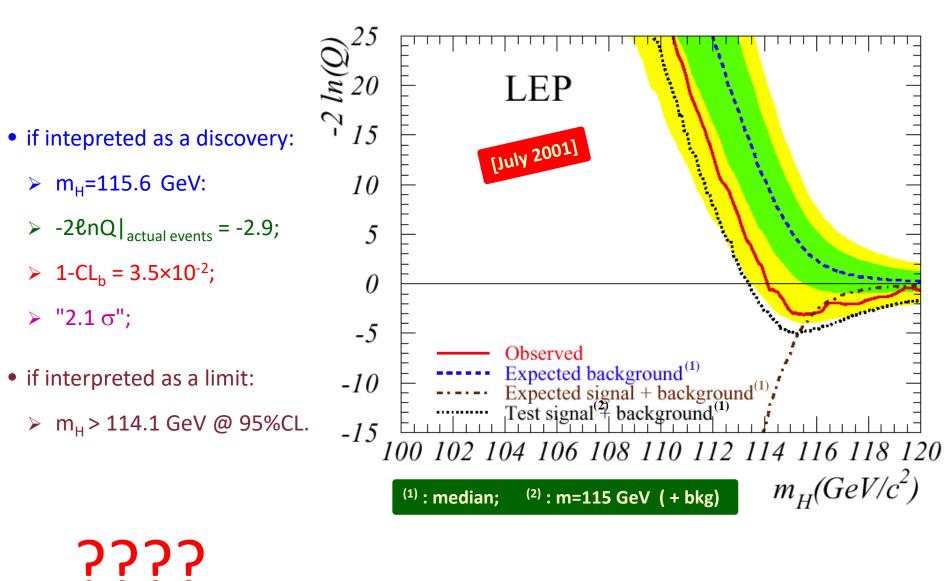
These are the measurements taken of LEP's final beam. The accelerator was switched off for the last time at 8:00 am on 2 November. (Click on photo for enlargement)

After extended consultation with the appropriate scientific committees, CERN 's Director-General Luciano Maiani announced today that the LEP accelerator had been switched off for the last time. LEP was scheduled to close at the end of September 2000 but tantalising signs of possible new physics led to LEP's run being extended until 2 November. At the end of this extra period, the four LEP experiments had produced a number of collisions compatible with the production of Higgs particles with a mass of around 115 GeV. These events were also compatible with other known processes. The new data was not sufficiently conclusive to justify running LEP in 2001, which would have inevitable impact on LHC construction and CERN's scientific programme. The CERN Management decided that the best



4/6





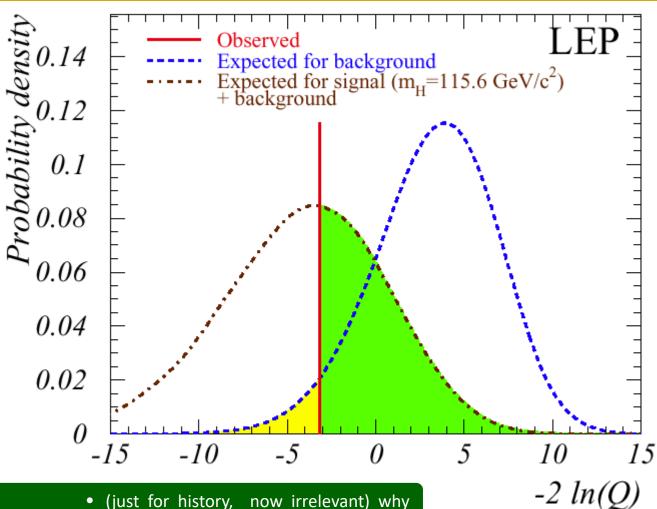
- - - -

Higgs search @ LEP2: the end

- method "gedankenexperiment" [i.e. produce via mc many experiments, with the same quality and L_{int} of the present one] :
- $m_{\rm H}^{\rm test}$ = 115.6 GeV;

5/6

- $\int f_{b,s} d(-2 \ln Q) = 1;$
- "•" = 1-CL_b= 3.5%;
- "•" = CL_{s+b}= 43%.



Comments/questions (<u>imho</u>):

- if this result had been presented in November 2000, there would have been no problem: no one would have claimed the need for further studies.
- (just for history, now irrelevant) why was the first analysis wrong ? well, ... ?
- why to show it to students ? because it is very instructive, normal classes see only the standard (discovery vs limits).

6/6

Higgs search @ LEP2: conclusion



- the "LEPC result" is difficult to explain (NOT only to students) : stat. fluctuations, mistakes, systematics out-of-control, ...
- the CERN management (L. Maiani) took the right decision at a high risk;
- the real threat was a delay of LHC, a huge human and economic price;
- instead, the final results are relatively simple to explain: a honest fluctuation at 3.5% does not deserve a discussion;
- the Higgs boson search crossed the ocean, but the TeVatron did not really enter in the game;
- and finally LHC ... [you know].

27

Other more personal comments:

- unlike theoretical physics, statistics (and human behavior) require risk evaluation;
- experimental physics lies in the middle;
- you should understand and judge the decisions of the experiments and the management (often they did NOT agree);
- ... while the landscape was changing (November '00, July '01, post-LEP, now);
- you might conclude that the "right decision" is a function of role and time (???);
- ... and that searches are risky, not for gutless people.

the Higgs boson @ LEP : $\sigma(e^+e^-\rightarrow HZ)$



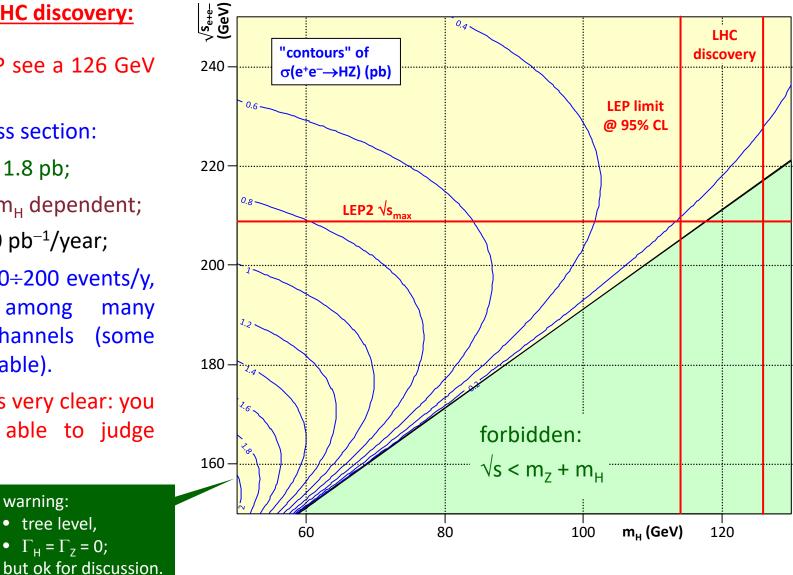
AFTER the LHC discovery:

A/1

- Q: could LEP see a 126 GeV Higgs?
- plot the cross section:
- $\sigma = 0.2 \div 1.8 \text{ pb};$
- strongly m_{μ} dependent;
- $\mathfrak{L}_{int} \approx 200 \text{ pb}^{-1}/\text{year};$
- i.e. $n = 40 \div 200 \text{ events/y}$, shared among many decay channels (some undetectable).
- A: the plot is very clear: you should be able to judge yourself !

warning: • tree level,

• $\Gamma_{\mu} = \Gamma_{7} = 0;$



the Higgs boson @ LEP : higgs-strahlung

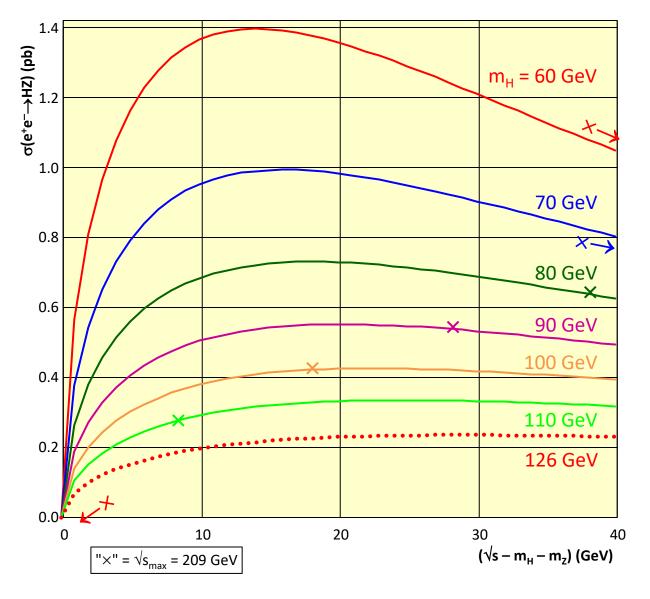


Plot $\sigma(e^+e^- \rightarrow Z^* \rightarrow HZ)$ vs the "kinetic" energy, i.e. $(T = \sqrt{s} - m_H - m_Z)$, in the approx. $\Gamma_Z = \Gamma_H = 0$:

A/2

- T \leq 0 \rightarrow σ = 0 (obvious);
- the ×'s show \sqrt{s} = 209 GeV;
- $\sigma_{max}(T)$ at T \approx 15÷20 GeV, slightly increasing with m_H;
- σ_{max}(m_H) decreases a lot when m_H increases;
- for $\sqrt{s} >> m_H + m_Z$, $\sigma \propto s^{-1}$ (obvious);
- for m_H > 110 GeV, other processes (not shown), other than higgsstrahlung;

if m_H = 126 GeV (LHC), H
 not produced at LEP 2.



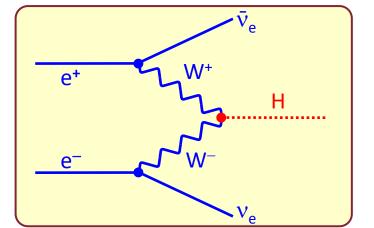
the Higgs boson @ LEP : the future in e⁺e⁻

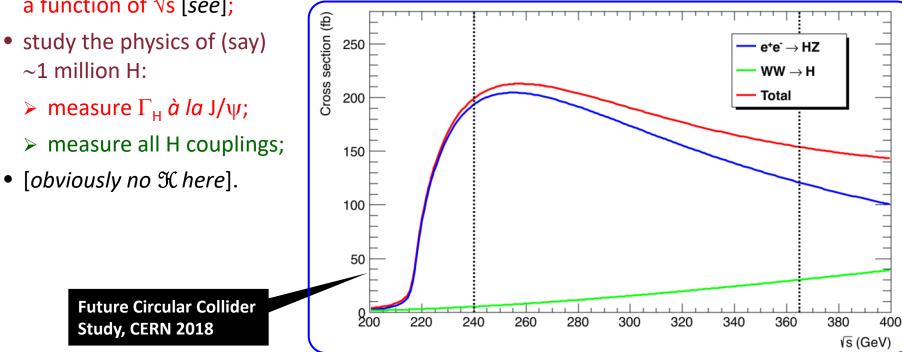
In the post-LEP (and post-H-discovery) era, the interest has shifted to a possible higher energy e^+e^- collider (circular or linear).

In this case:

A/3

- consider also other processes (e.g. the so called "WW-fusion" $e^+e^- \rightarrow H\bar{v}_e v_e$ [see];
- compute the cross-section for m_H=126 GeV, as a function of √s [see];





References

- 1. LEP predictions from SM : Yellow report CERN 89-08.
- L3 results @ LEP1 : Phys. Rep. 236 (1993) 1.
- 3. L3 results 1994 : Eur.Phys.Journ. C16 (2000) 1.
- 4. M.W.Grünewald, Phys. Rep. 322 (1999) 125.
- 5. Z pole results : Phys.Rep. 427 (2006) 257.
- 6. WW results : Phys.Rep. 532 (2013) 119.
- 7. Higgs @ LEP : Ann. Rev. Nucl. Part. Sci. 2002.52:65.



Jan Brueghel the Elder and Hendrick de Clerck – Abundance and the Four Elements – 1606 – Prado Museum



SAPIENZA Università di Roma

End of chapter 10