

# Search for the Higgs boson in the $H \rightarrow ZZ^* \rightarrow 4\text{-lepton}$ decay channel, with the ATLAS experiment at LHC

## Part 2: data analysis

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# Introduction

- In the previous seminar by Ludovico, you have seen how a detector (let's pick a random one: ATLAS @ LHC ) has been:
  - Designed
  - Built
  - Calibrated
- These are of course the first fundamental steps
- Today we'll see the following steps that lead to the Higgs boson discovery:
  - Design the analysis, collect the data and look for a signal
  - Did we really do a discovery ?
- And, we'll briefly see how some of the properties of the new resonance have been measured

# Designing an analysis

- What signal am I looking for ?
  - Define the signature in terms of the final state properties
- Is my trigger able to store the results ?
  - Particular important at high-luminosity colliders like LHC
- What are the backgrounds ?
  - Are there already known processes, that produce a signature exactly like the one I am looking for
  - What are the handles I can use to reject the backgrounds
  - Can I use Monte-Carlo (MC) or do I need to estimate the backgrounds from the data
- How much data do I need, to be able to say something ?
- How can I measure the properties of a possible discovery ?

# Outline

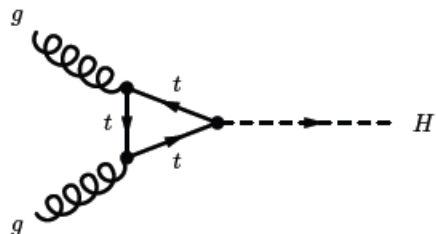
- A brief introduction on the SM Higgs search at LHC
  - Production mechanisms and decay channels
  - Description of main search channels and their characteristics
  - Assuming you already know the basics of Higgs Physics and its motivations
- The  $H \rightarrow ZZ^* \rightarrow 4\text{-lepton}$  channel (lepton = electron or muon)
  - Leptons reconstruction in brief
  - Signal signature and backgrounds
  - Event selection
  - Exclusion limits and signal significance
  - Measurement of the signal properties
- In the end, you should be able to see how the main results of the Higgs search at LHC Run 1 were derived at ATLAS

Section 1

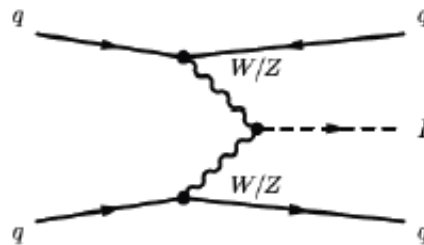
# INTRODUCTION

# Standard Model Higgs Boson @ LHC

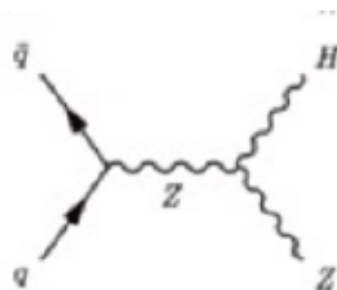
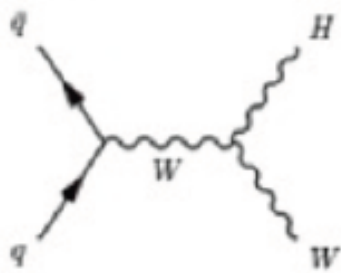
Production Feynman diagrams for a Higgs Boson at a p-p collider



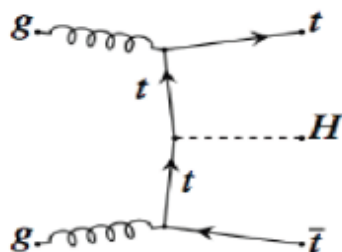
**Gluon-gluon fusion:**  
~87%  
Calculated with ~10%  
uncertainty  
(PDF and QCD scales)



**Vector Boson Fusion (VBF):**  
~7%  
Calculated with ~3%  
uncertainty

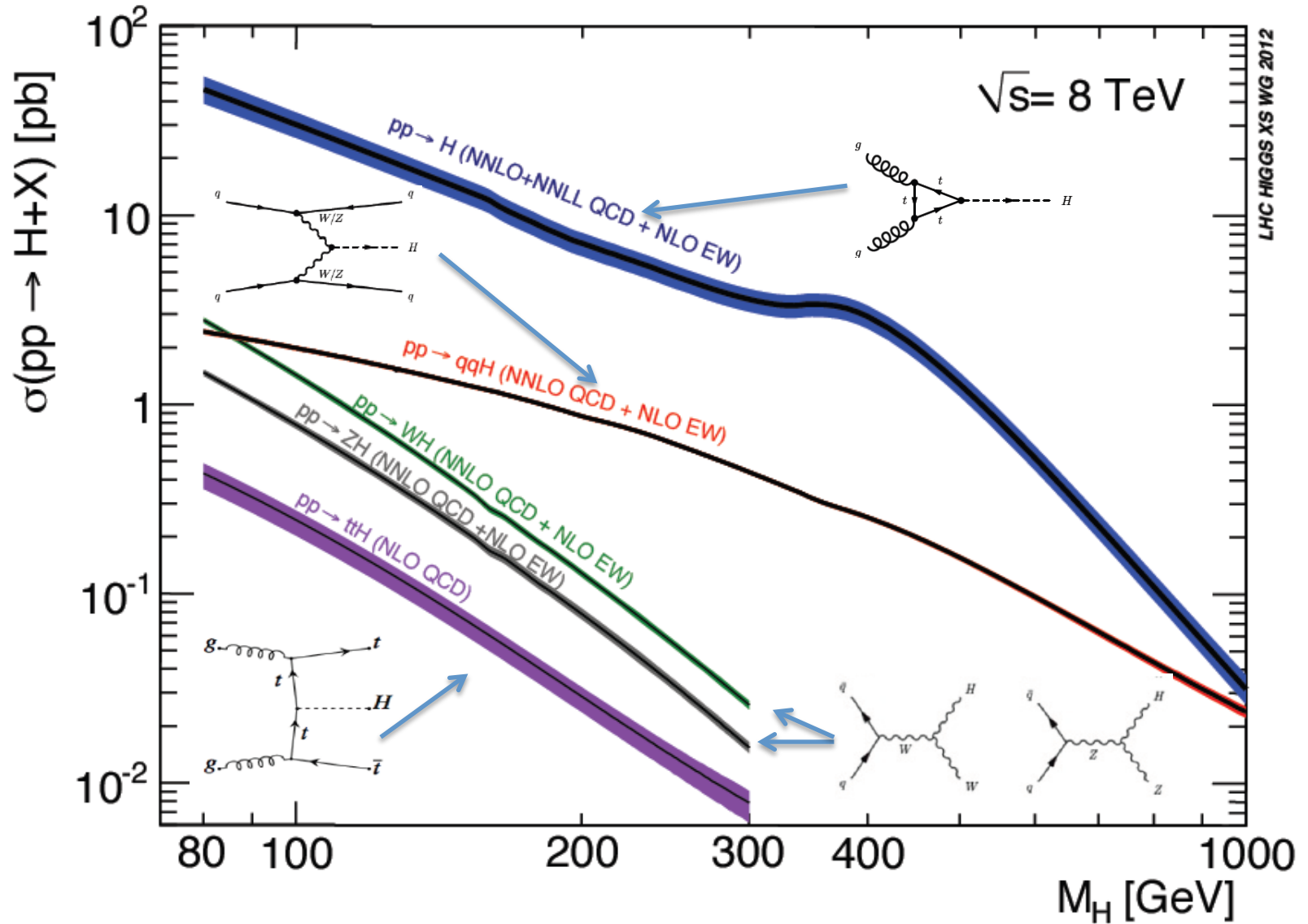


**Associated production (WH, ZH):**  
~5% Calculated with ~3%  
uncertainty



**tt-Higgs:**  
~1% Calculated with ~12%  
uncertainty

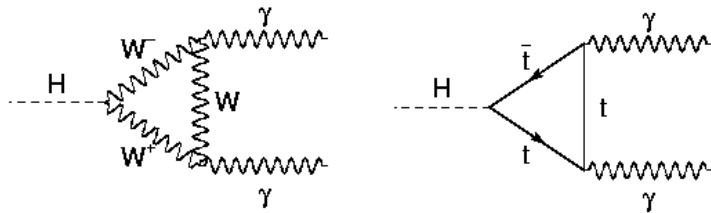
# Mass dependence of the cross sections



# Decay branching ratios

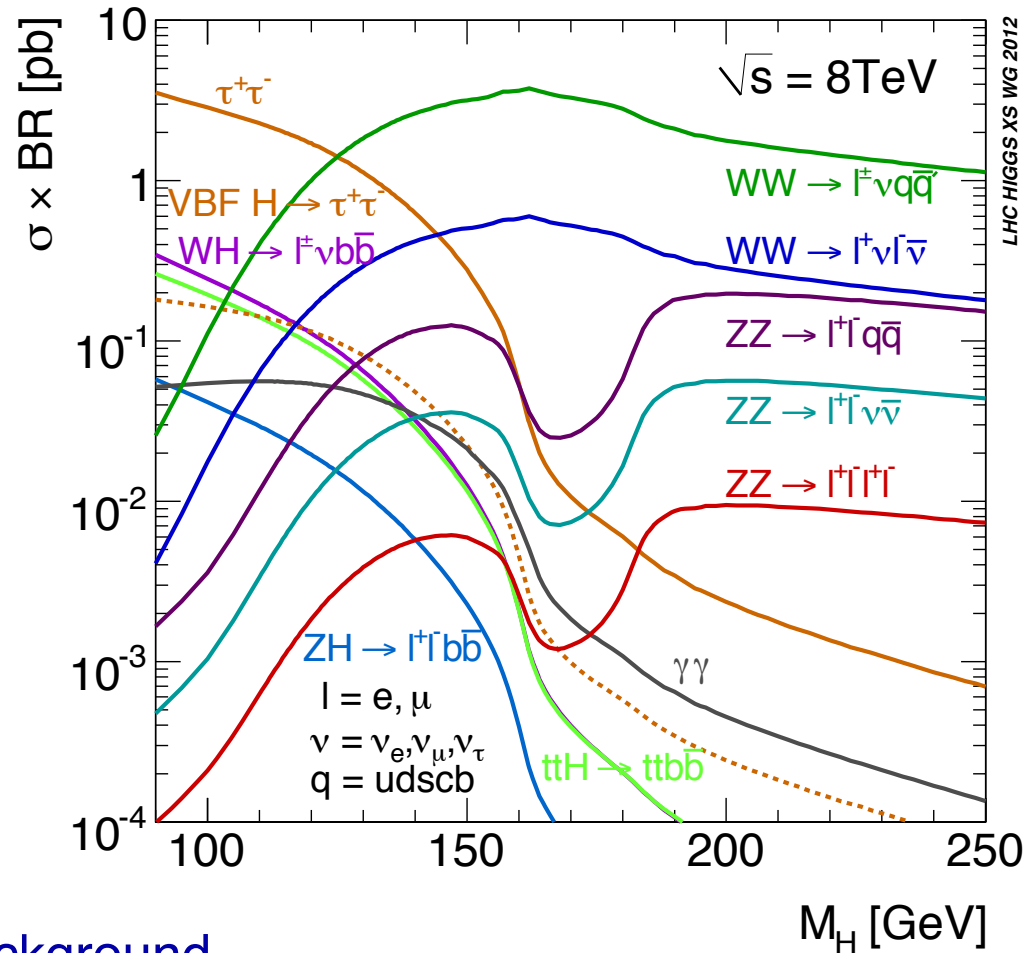
- Higgs coupling proportional to  $M_f, M_W, M_Z$

- The decay to a pair of photons is possible through W and top loops:



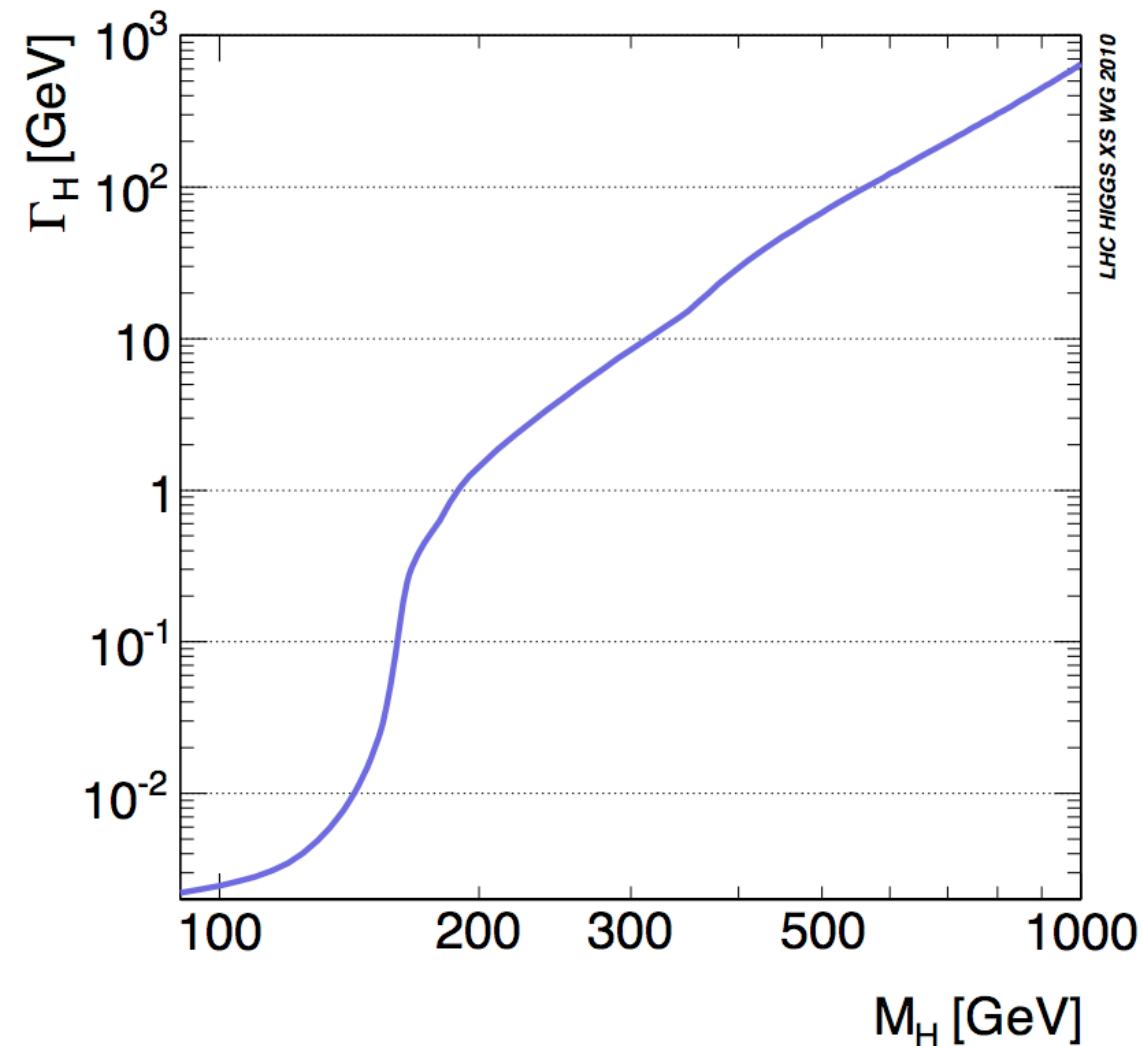
- In spite of the low BR, the 4-lepton decay channel is a fundamental one:

- Clean signature with low background
- Final state is fully reconstructed allowing the best measurement of the properties (mass, spin/parity, cross sections)





# Higgs width



In the low-mass region,  
i.e. below  $\sim 200$  GeV:

- natural width of the resonance negligible w.r.t. the typical resolutions of the “best” channels
- $H \rightarrow \gamma\gamma$  and  $H \rightarrow ZZ^* \rightarrow 4l$  have mass resolutions between  $\sim 1$  and  $\sim 2$  GeV

# Event rates

Number of signal events in  $20 \text{ fb}^{-1}$  at 8 TeV center of mass energy  
Standard Model Higgs with  $M_H = 125 \text{ GeV}$

Expected events before any selection

Channel	Events before selection
$H \rightarrow \gamma\gamma$	1000
$H \rightarrow WW \rightarrow lnl$	1200
$H \rightarrow ZZ^* \rightarrow 4l$ (Inclusive)	60
$H \rightarrow ZZ^* \rightarrow 4l$ (VBF)	3
$H \rightarrow ZZ^* \rightarrow 4l$ (VH)	2
$H \rightarrow \tau\tau$	30000

But, not only the signal rate is important of course.

What are the backgrounds ? What's their size with respect to the signal ?

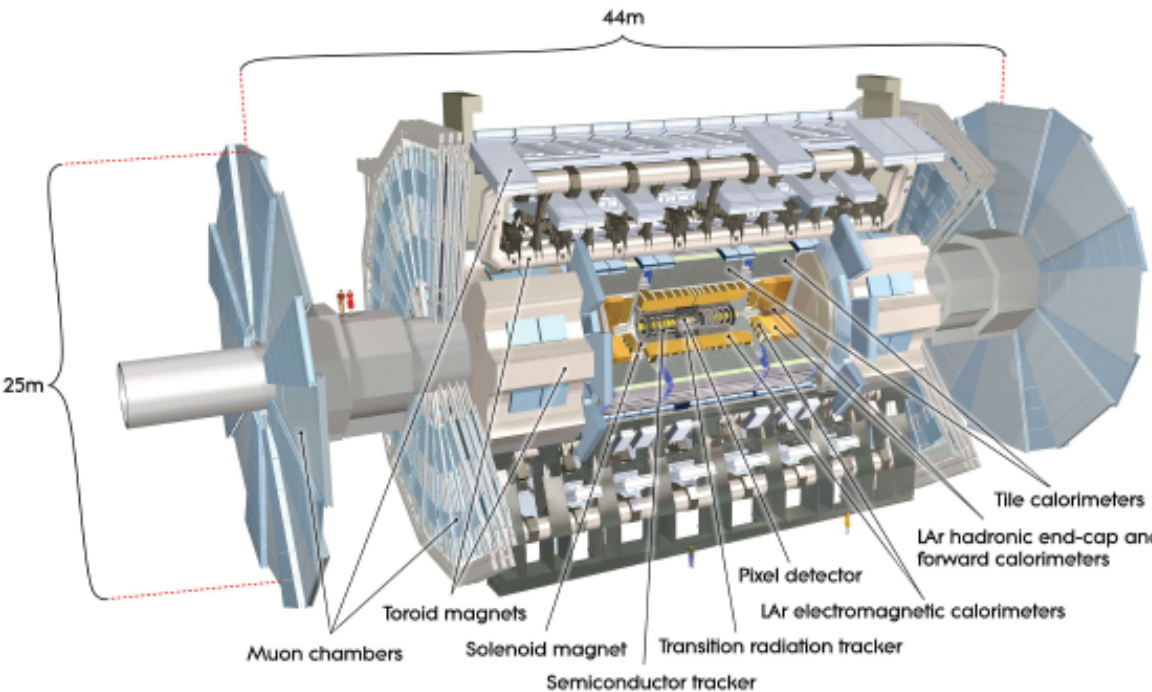
# Some remarks on the plots

- When looking at histograms of any distribution for different physics processes, one can usually use two approaches:
- Normalize each histo to given integral (usually 1) in order to look in detail at shape differences
  - I.e. to normalize to 1, weight each event with the factor:
    - $w=1/N_i$   
where  $N_i$  is the total number of events you have in your MC for the process  $i$
  - You will not see the actual number of expected events in the histo, but will be able to compare the shapes
- Normalize each histogram based on the cross section and a given integrated luminosity
  - This means to weight each event of the process  $i$  with a factor:
    - $w= \mathcal{L}\sigma_i / N_i$   
where  $\mathcal{L}$  is the integrated luminosity you want to normalize to,  $\sigma_i$  is the cross section of the process, and  $N$  is the tot number of MC events
- In the following you will see plots normalized in both ways

Section 2

# **THE ATLAS EXPERIMENT AND THE LHC RUN-1 DATASET**

# The ATLAS detector



Magnets

1 Central Solenoid (2 T)  
+ 3 air-core toroids

Tracking

Silicon+Transition radiation tracker

EM calo

Sampling LAr calo

HAD calo

Plastic scintillator (barrel)  
LAr technology (endcap)

Muon

Reco and trigger  
Standalone reco capabilities

## ATLAS p-p run: April-Sept. 2012

Inner Tracker			Calorimeters		Muon Spectrometer				Magnets	
Pixel	SCT	TRT	LAr	Tile	MDT	RPC	CSC	TGC	Solenoid	Toroid
100	99.3	99.5	97.0	99.6	99.9	99.8	99.9	99.9	99.7	99.2

**All good for physics: 93.7%**

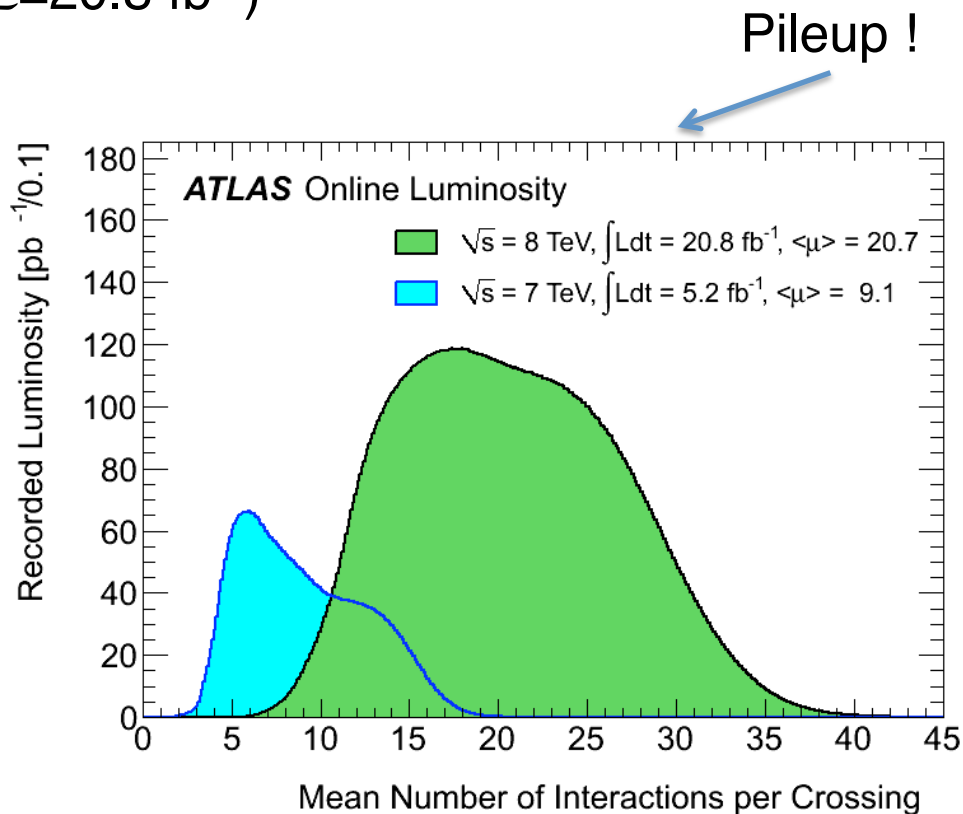
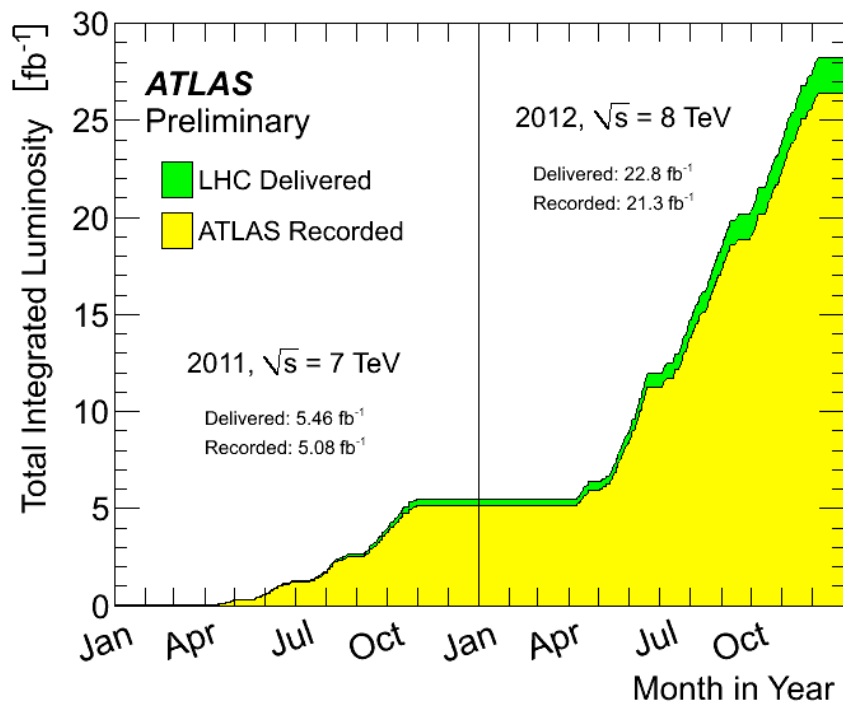
Luminosity weighted relative detector uptime and good quality data delivery during 2012 stable beams in pp collisions at  $\sqrt{s}=8$  TeV between April 4<sup>th</sup> and September 17<sup>th</sup> (in %) – corresponding to 14.0 fb<sup>-1</sup> of recorded data. The inefficiencies in the LAr calorimeter will partially be recovered in the future.

You have seen all the details in the seminar by Ludovico

2012 data  
→ 10 PB of data !

# The Run-1 LHC dataset

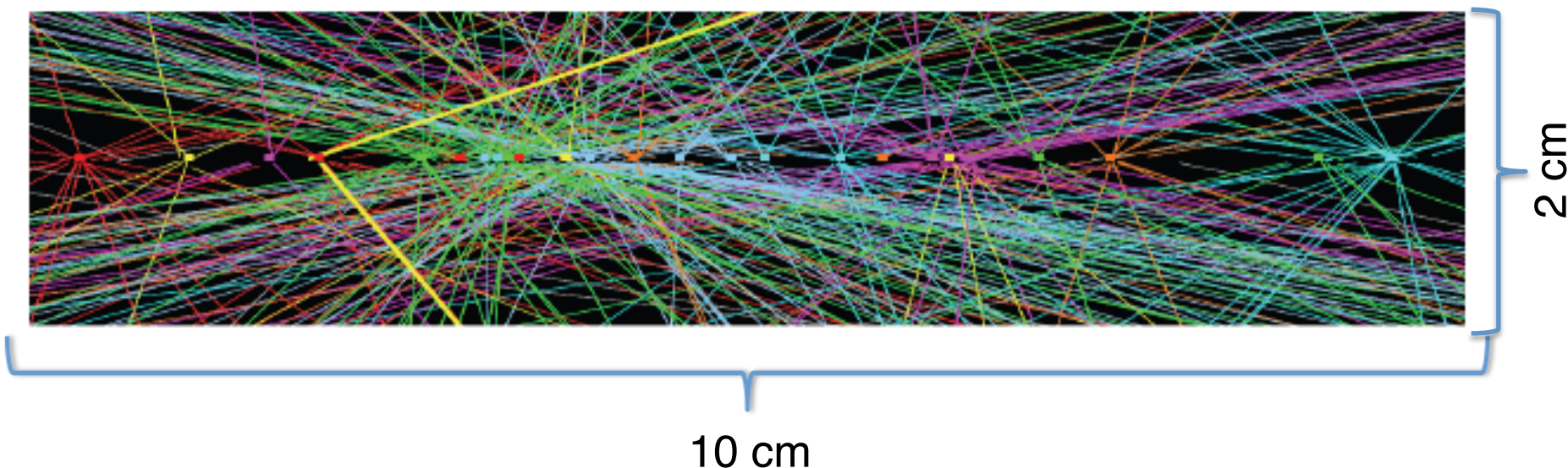
p-p center of mass energy at 7 TeV in 2011 ( integrated luminosity  $\mathcal{L}=5.08 \text{ fb}^{-1}$ ) and 8 TeV in 2012 ( $\mathcal{L}=20.8 \text{ fb}^{-1}$ )



Peak instantaneous lumi was  $7.7 \cdot 10^{33} \text{ cm}^{-2}\text{s}^{-1}$  in 2012

# Pileup

That's how a typical event at 8 TeV looks like, in the region around the primary vertex



The  $\sigma$  of the interaction point along the beam axis (z axis) is  $\sim 5$  cm, while the reconstruction resolution is  $\sim 90 \mu\text{m}$

→ The z IP is used to associate the tracks to each primary vertex

While on the x and y planes (transversal to the beam) the resolution is comparable to the spread of the interaction point ( $\sim 15 \mu\text{m}$ )

Section 3

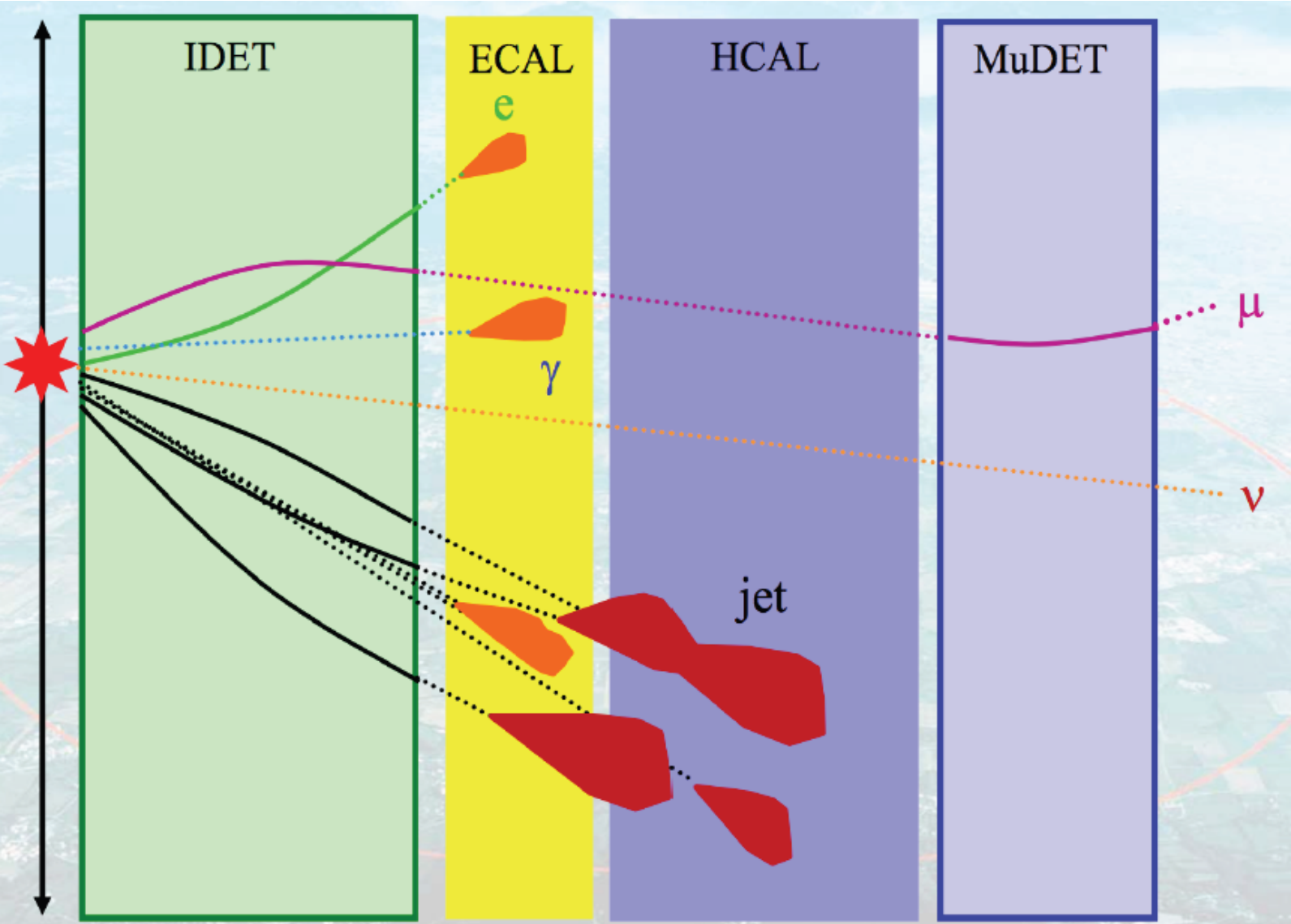
# SELECTION OF $H \rightarrow ZZ^*$ EVENTS, IN THE 4-LEPTON CHANNEL



# Steps for building an event selection - 1

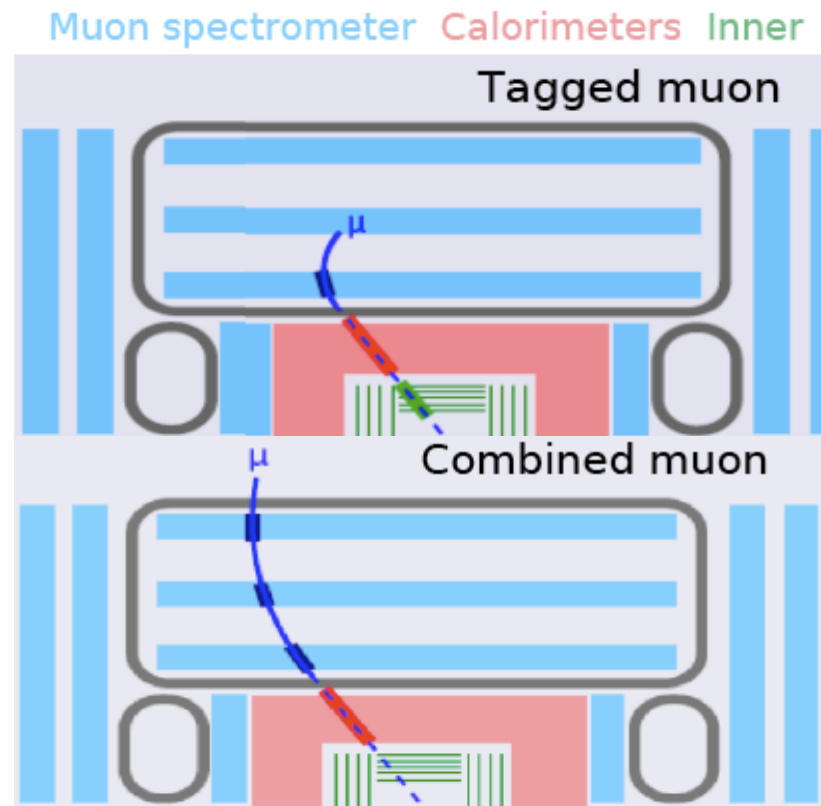
- When you think about an event selection, the first fundamental step is:
- Define the reconstructed “objects” that you will use in the analysis:
  - E.g. in the case of the  $H \rightarrow ZZ^* \rightarrow 4l$  search the relevant objects are muons and electrons
- Check the reconstruction performance
  - The MC models a perfect detector, in the best possible ways, some corrections might be needed
    - Which methods can be used to determine them

# Identification and reconstruction



# Muon identification and reconstruction

- Muons are identified by:
  - Tracks in the Muon Spectrometer
  - Segments of tracks in the inner station of the muon spectrometer ( low-pT muons not reaching all 3 stations)  
→ tagged muon
- Tracks in the MS are back-extrapolated to the ID, correcting for energy losses in the calo
  - Look for a matching ID track  
→ combined muon
- Tracks in the ID are out-extrapolated in the case of tagged muons



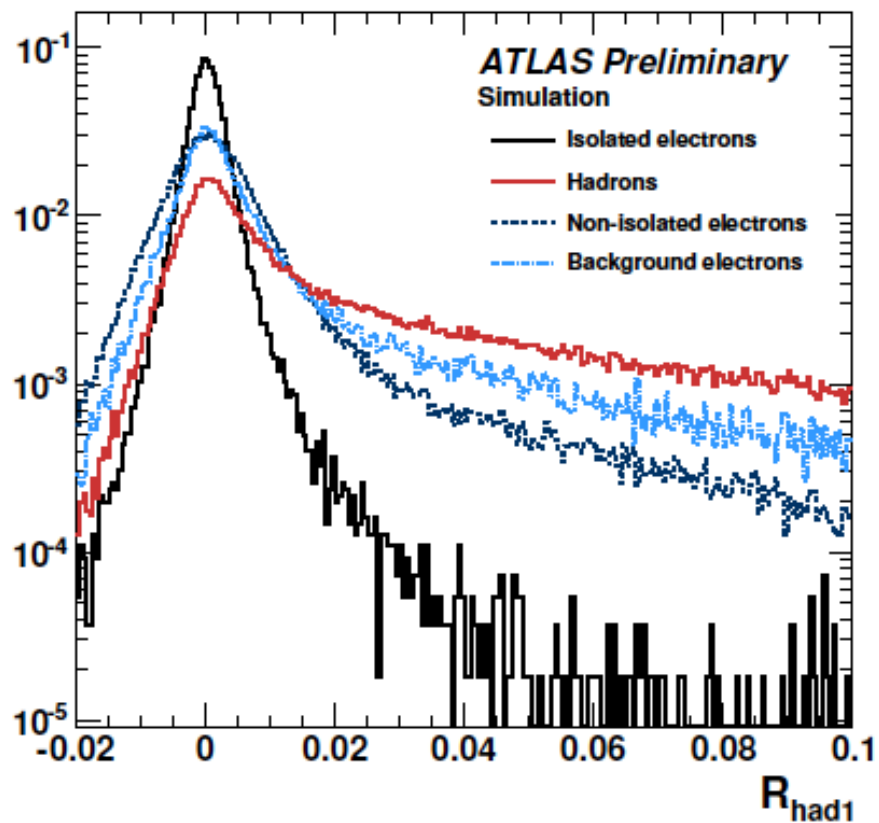
See the last seminar by Ludovico for all the details on the performance !

# Electron identification and reconstruction

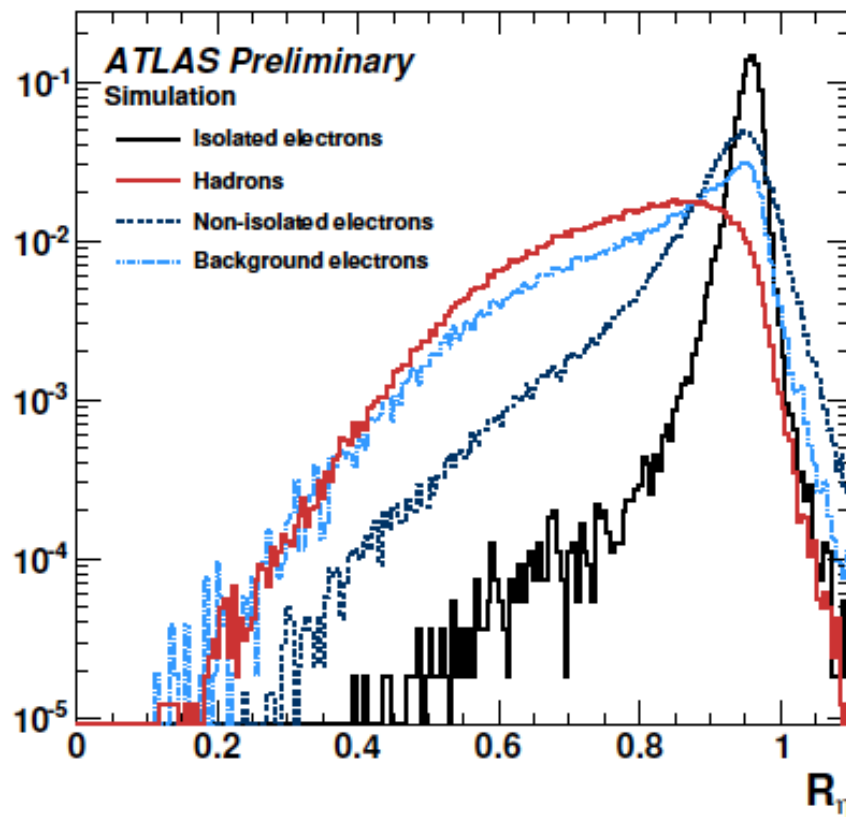
- Look for an ID track pointing to a cluster in the electromagnetic calorimeter
- Identification criteria must provide good separation with respect to jets faking electrons
- Some examples of general discriminating variables are:
  - Hadronic leakage:
    - ratio of energy in hadronic calorimeter / EM cluster energy ( $R_{had}$ )
  - Shower shape variables
    - Ratio of inner cluster cells/total cluster ( $R_{\eta}$ )
    - Ratio of last sampling / first samplings
  - Track / cluster matching:
    - $\Delta\eta$ ,  $\Delta\phi$  btw track and cluster
    - Ratio of cluster energy / track momentum
  - A few more ATLAS-specific variables (like hits in the TRT etc. )
- Either cut-based selection, or multi-variate
  - We'll discuss the difference in more detail later

# Electron discriminating variables – 1

Hadronic leakage



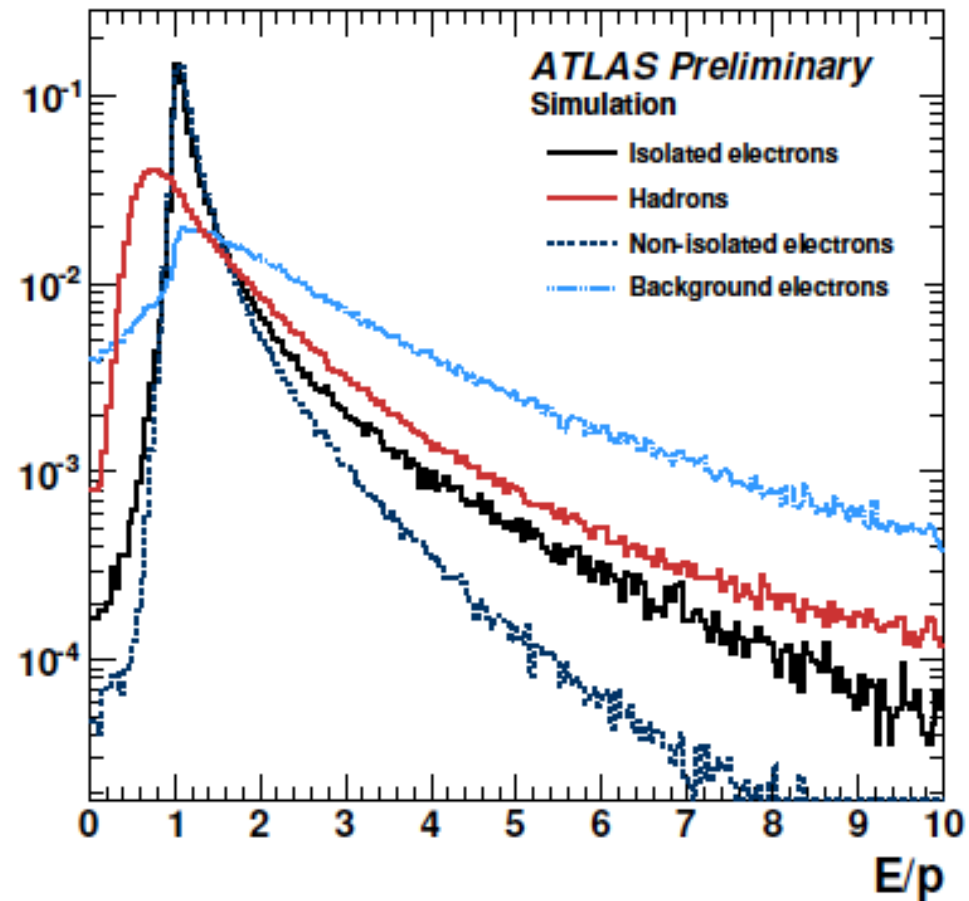
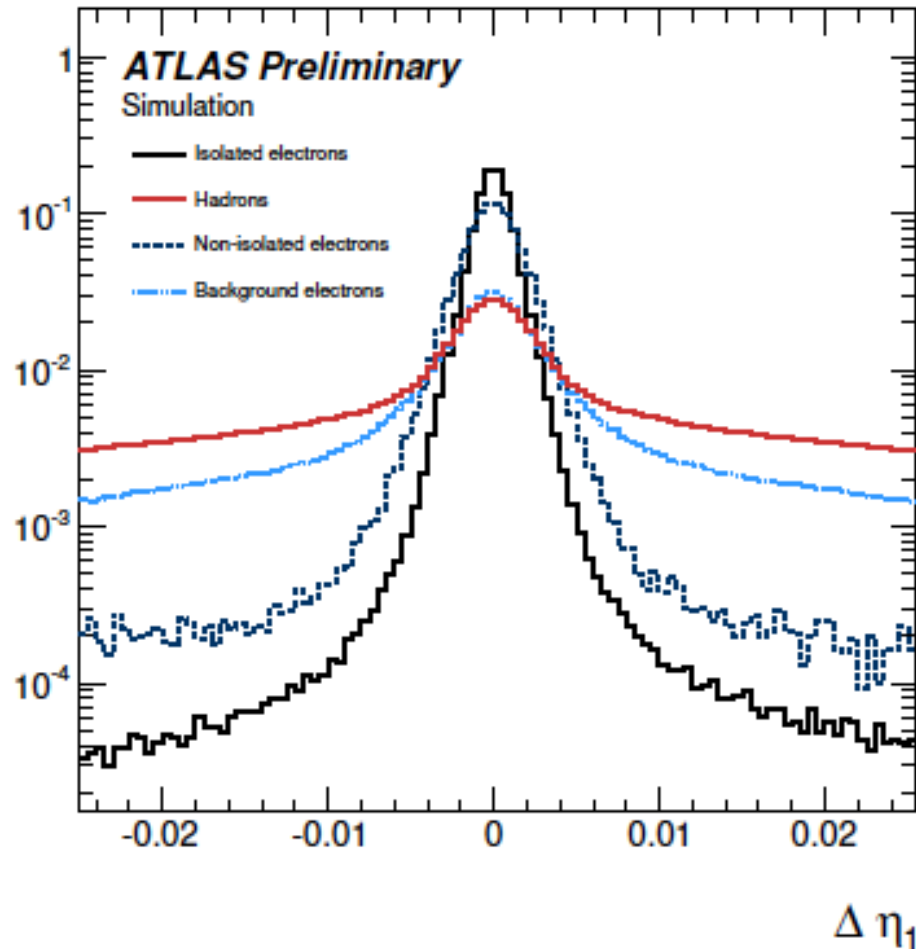
Inner cells / total cluster energy



# Electron discriminating variables - 2

$\Delta\eta$  between track and cluster

Cluster energy / track momentum

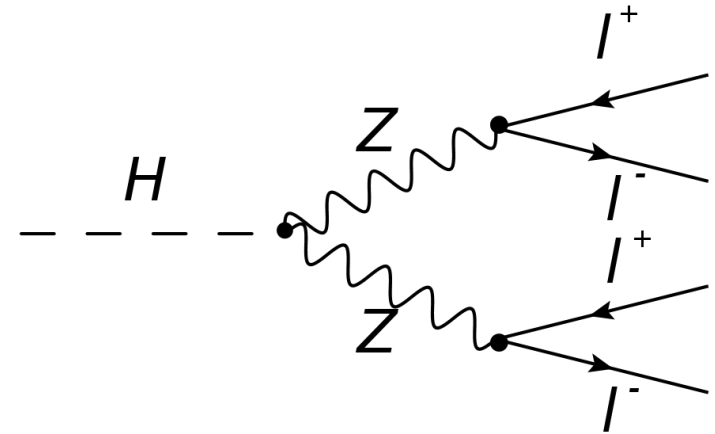


# Steps for building an event selection - 2

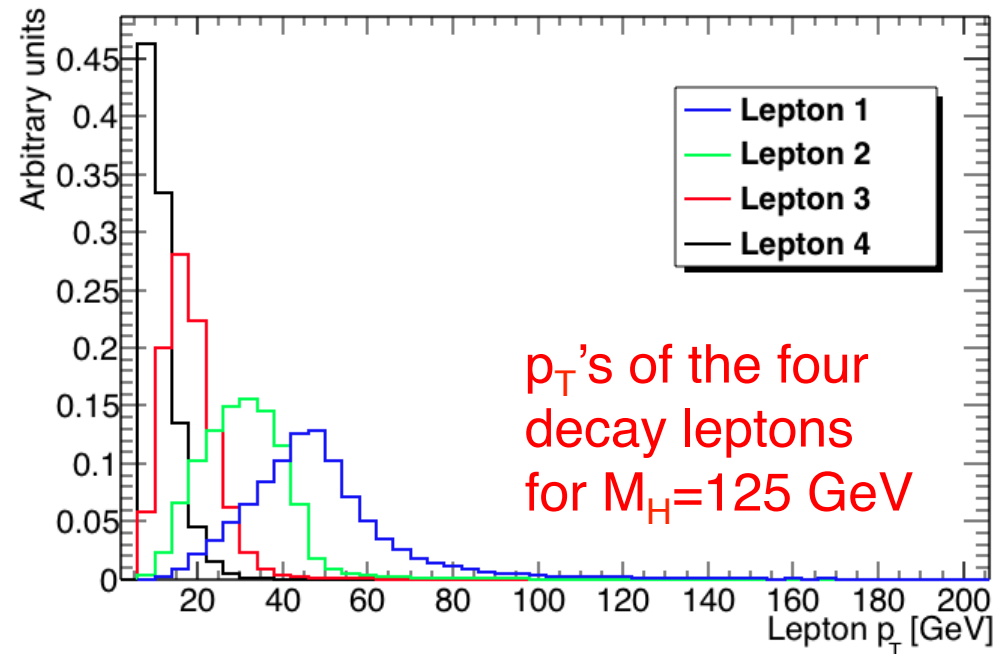
- In particular for searches, it is important to define the event selection **without looking at the data** (blind analysis)
  - Avoid biases in the definition of cuts: looking at the data one can pick excess regions and artificially enhance a significance
    - This should be avoided by all means
- So in general all the selection steps are defined using MC only
  - Data can also be used for some purposes, but in regions where the signal is not expected, the so-called control regions, or sidebands
- Once the selection is fully defined on MC:
  - Look at the data applying the cuts that you have defined

# Basic signal kinematics

- The Higgs decays to a pair of Z bosons
- For  $M_H < \sim 180$  GeV (smaller than twice the Z mass)
  - One Z is on-shell, the other is off-shell at lower masses
- For  $M_H > \sim 180$  GeV
  - Both Z's are on-shell
- Here we'll focus on the search in the low-mass region
  - Where the Higgs was actually found !



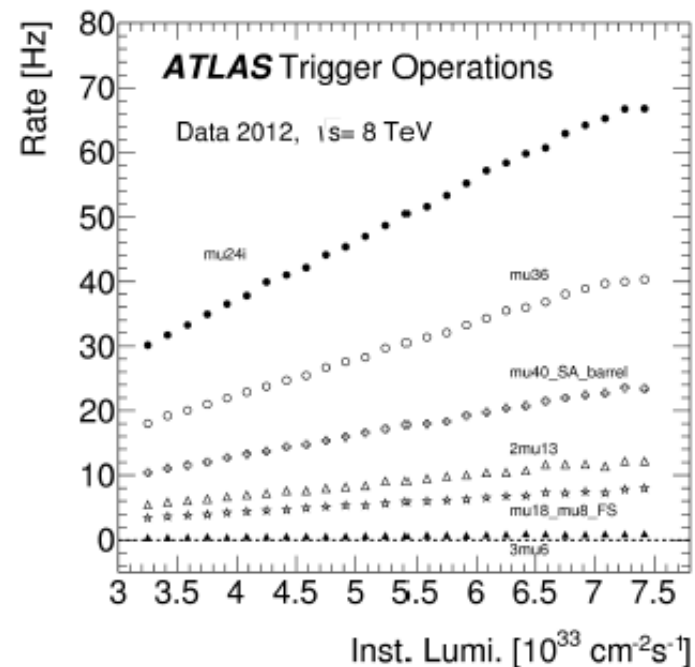
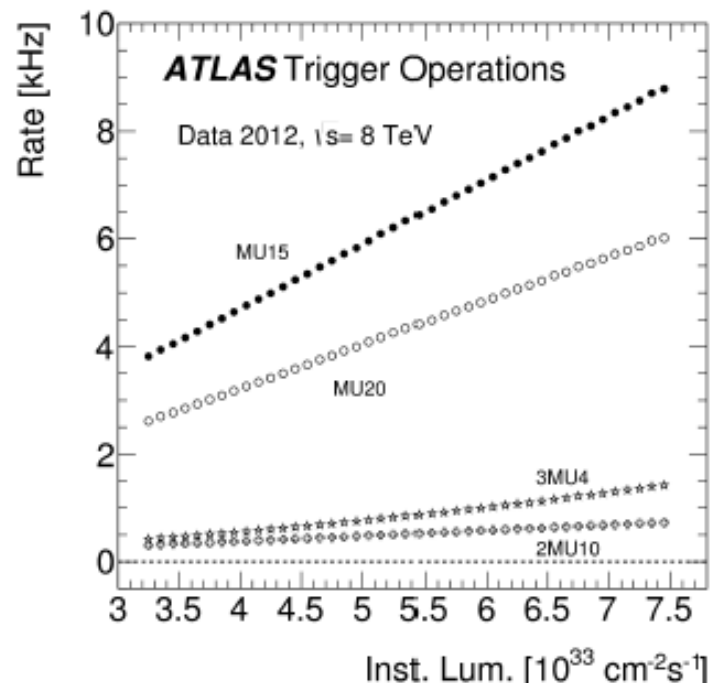
$p_T$ 's from  $\sim 5$  to 100 GeV





# The Trigger

- The trigger setup is the result of a compromise:
  - Keep the rate of accepted events at a level that can be sustained by the system:
    - Raise the thresholds
  - Keep high efficiencies for relevant Physics signals
    - Lower the thresholds
- Data Acquisition (DAQ) limits:
  - L1: 65-70 Hz
  - L2: 5 kHz
  - EF: 400 Hz
- Many signatures have to be combined in a menu, keeping the total rate within the DAQ limits
- Lepton thresholds always below 25 GeV during Run-1 ( or 12-15 GeV for di-lepton)
  - Not a problem for the 4l-channel
- Efficiency is important → more later

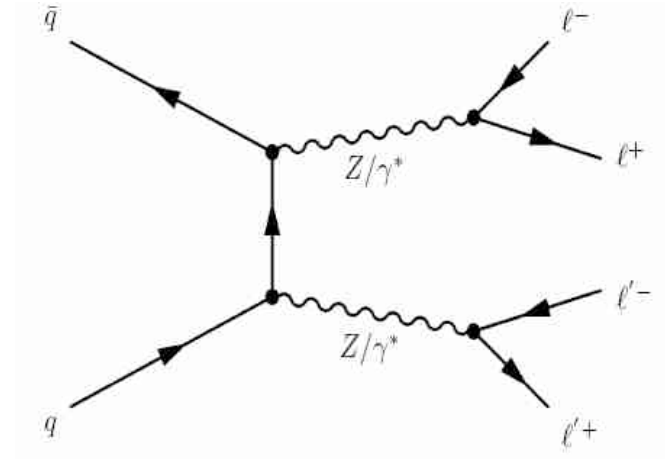


# Backgrounds

- When looking for a signal, most important thing is... the background
- Think of all possible processes that can give the same signature of your signal
- Can these events be rejected (fully or partially) ?
  - Identify any property of the background events, different from those of the signal → “reducible” background
  - If it can't be fully rejected, it will have to be taken into account in all following measures
- If instead the background signature is in everything identical to the signal, its events can't be rejected and will have to be taken into account later in the analysis
  - In this case → “irreducible” background

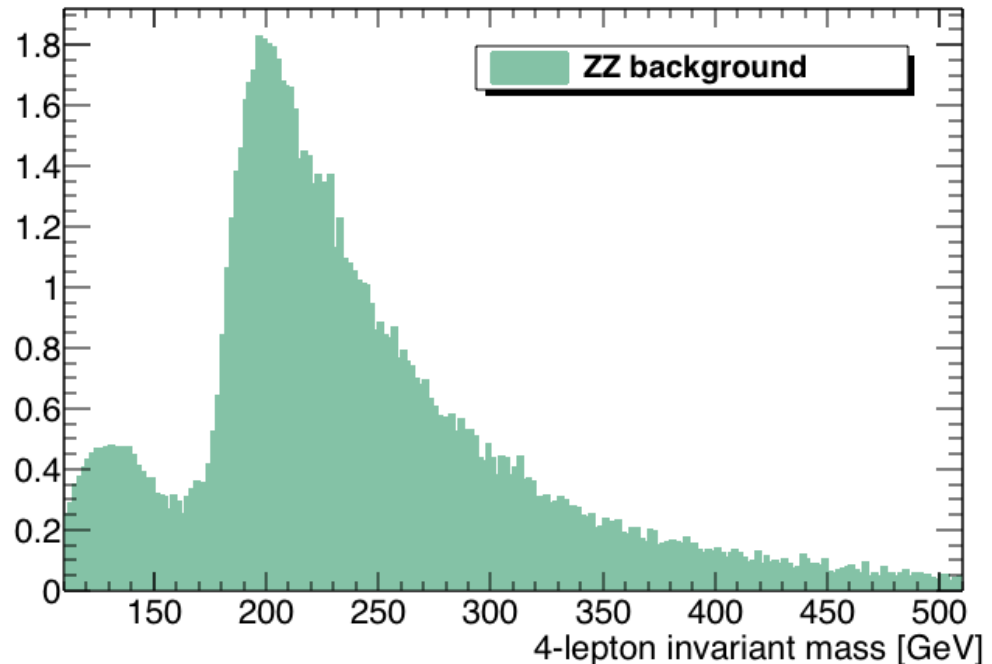
# Irreducible background

- The process  $q\bar{q} \rightarrow ZZ^{(*)} \rightarrow 4l$  has the same final state of the signal
- Only difference is the mass distribution
  - There are a couple of more subtle ones to which we'll come back later



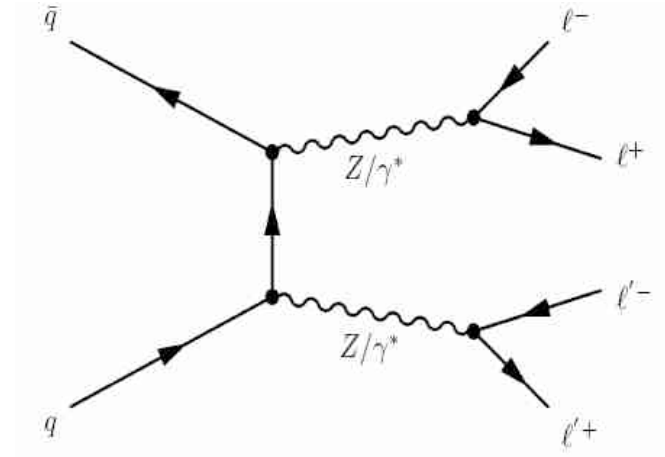
Onset of two on-shell  
Z's production from  $2 M_Z$ ,  
i.e. from about 180 GeV

Events are normalized to  
 $20 \text{ fb}^{-1}$  and based on each  
process cross section



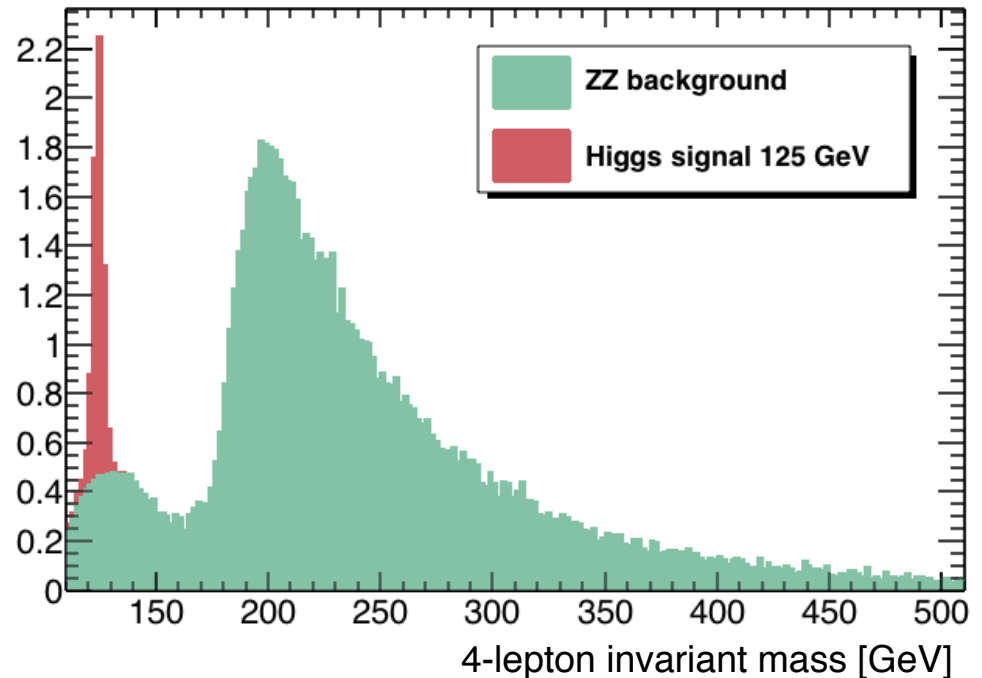
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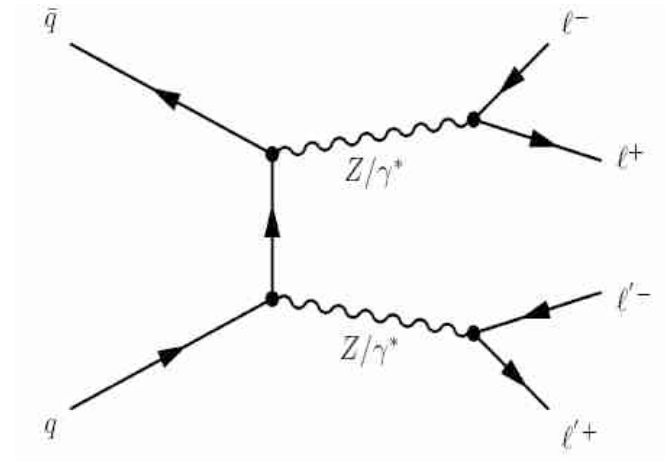
With the signal (@125 GeV)  
superimposed

Events are normalized to  
 $20 \text{ fb}^{-1}$  and based on each  
process cross section



# Irreducible background

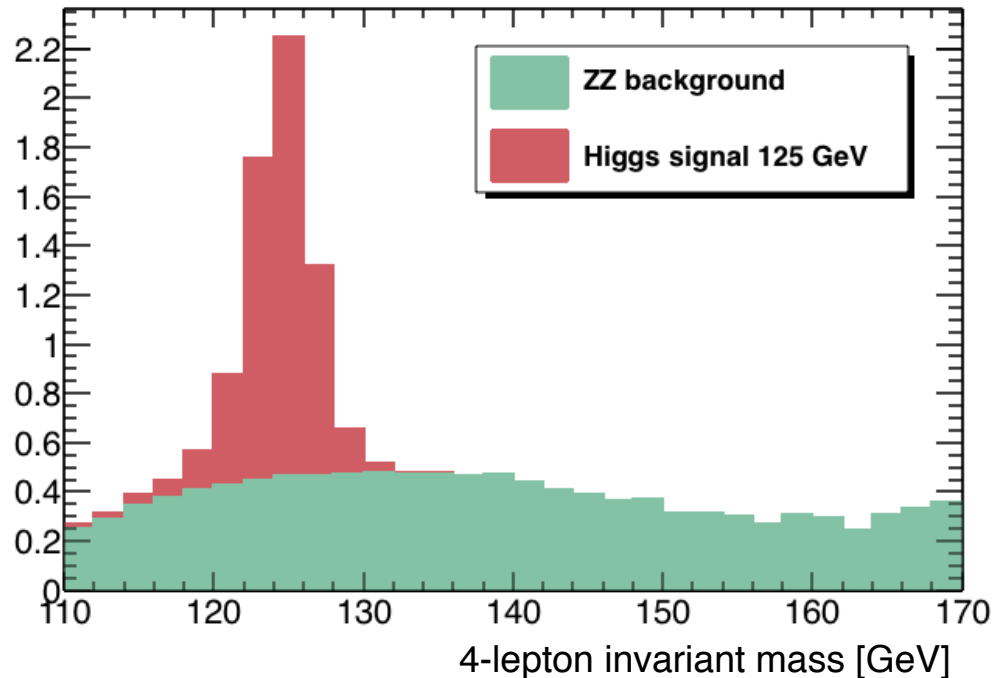
- The process  $q\bar{q} \rightarrow ZZ^{(*)} \rightarrow 4\ell$  has the same final state of the signal
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With the signal (@125 GeV)  
superimposed

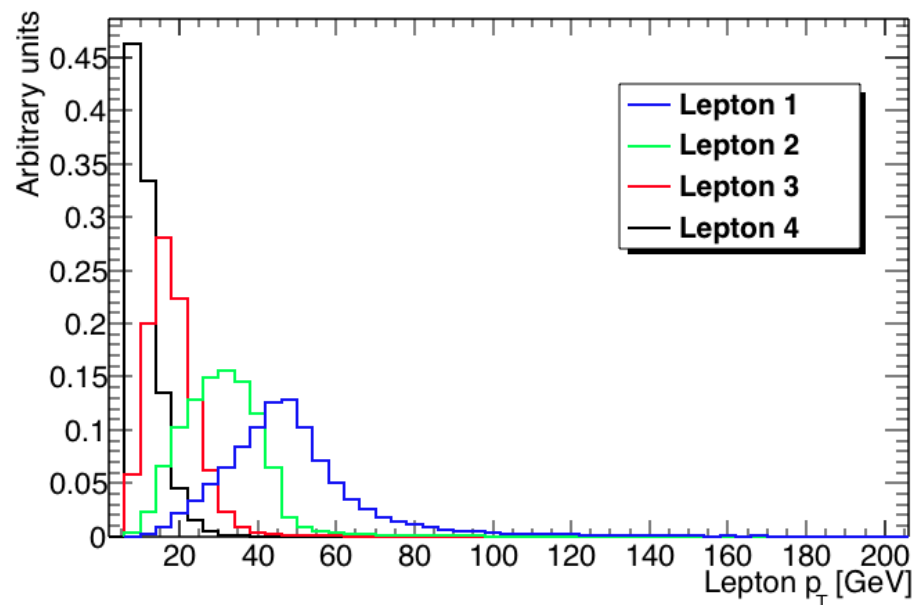
Events are normalized to  
 $20 \text{ fb}^{-1}$  and based on each  
process cross section

Zoom in the low-mass region  $\rightarrow$



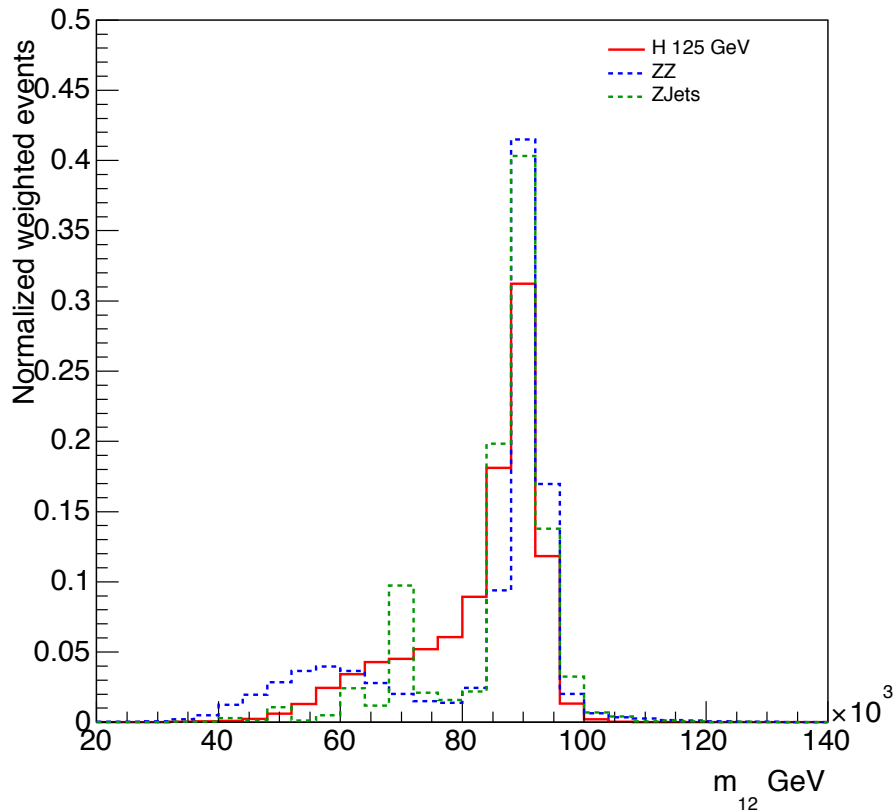
# First steps of the selection

- Require 4 reconstructed leptons (e or  $\mu$ ) coming from the same primary vertex
  - Some basic quality cuts are applied besides the standard identification:
    - Number of hits used for the reconstruction in each detector
- The composition of the quartet defines the decay channel
  - $4\mu$ ,  $4e$ ,  $2e2\mu$
- Apply the first cuts on the lepton  $p_T$ 's:
  - $p_T > 6$  (7 for e), 10, 15, 20 GeV
- Cut a little higher on electrons due to performance corrections ( more details later )

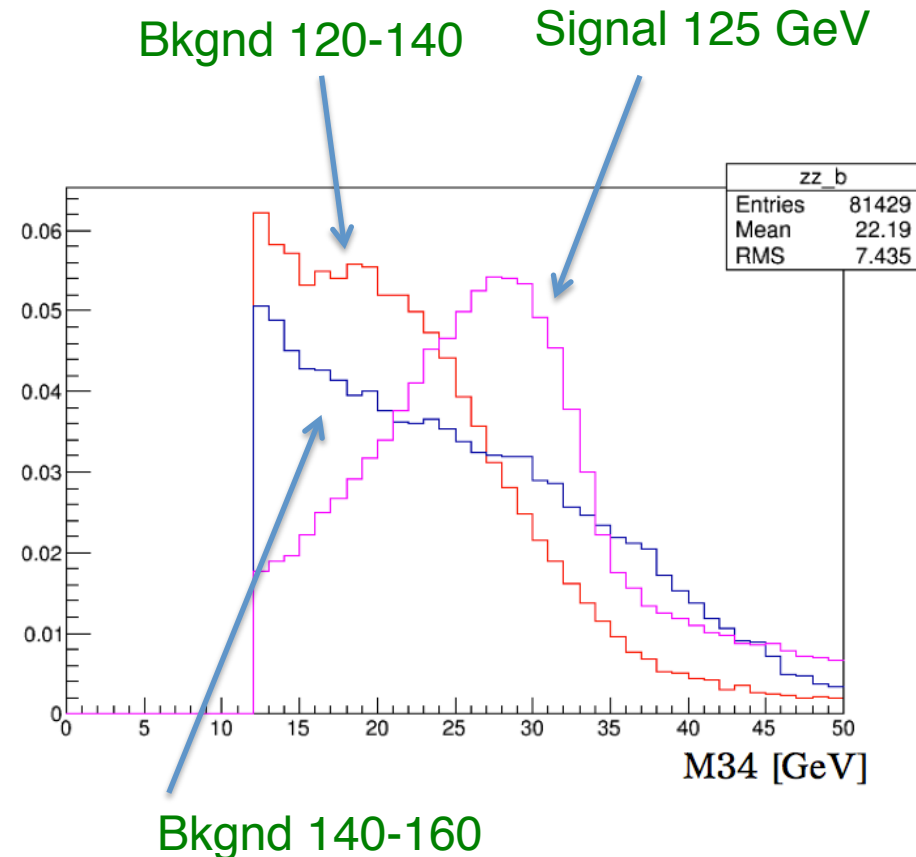


# Other kinematic cuts

## On-shell Z



## Off-shell Z



Leptons are paired according to type and charge, then for low-mass H search, the paired closer to the Z mass is called Z1 (on-shell Z), the other Z2 (off

# Significance

- When doing a search, the optimization of the cuts is driven by the maximization of the signal significance
- During the optimization, if the systematics are small one can normally use the simple expression you have seen in the lectures for the significance (n. of std. deviations):

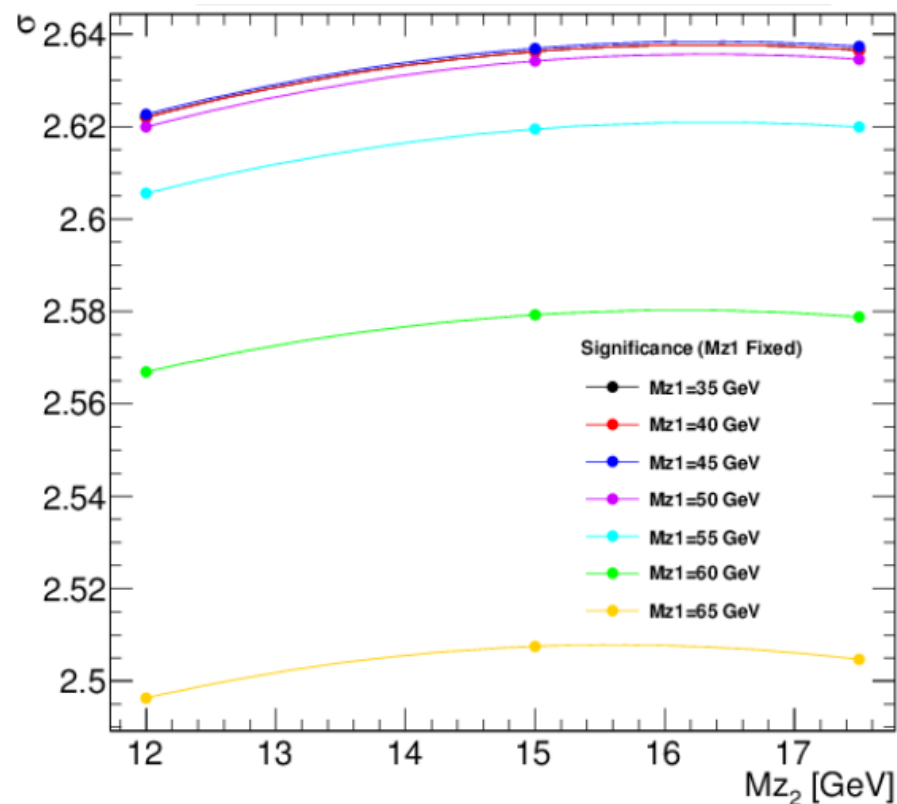
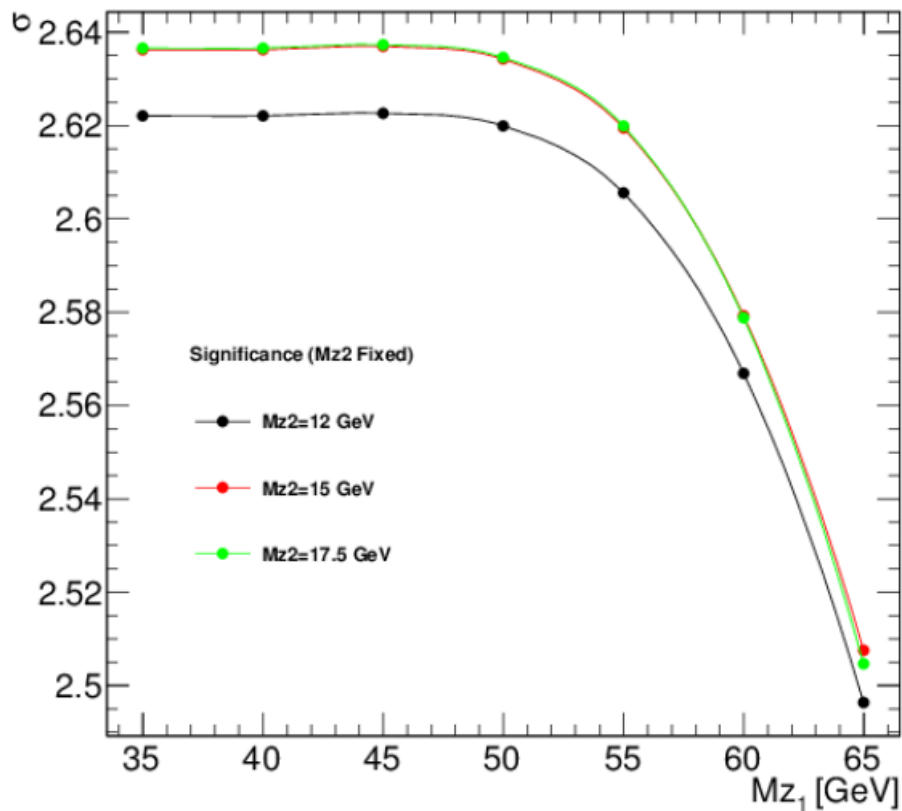
$$\frac{S}{\sqrt{S+B}}$$

- Or, in case of low statistics, using the likelihood ratio as test statistics:

$$\sqrt{2(S+B) \ln \left( 1 + \frac{S}{B} \right) - 2S}$$



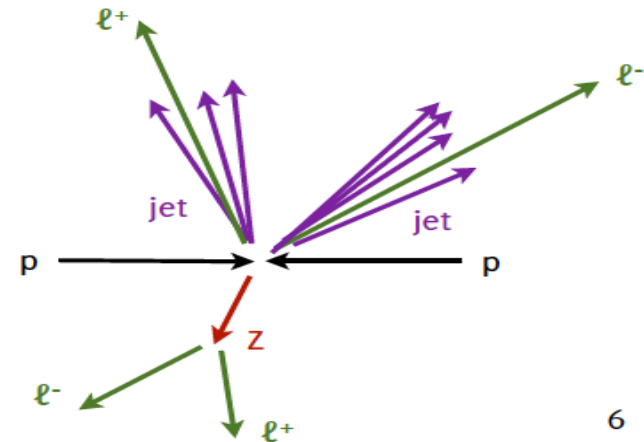
# Optimizing the cuts vs the significance



Significance vs the cuts on  $MZ_1$  and  $MZ_2$

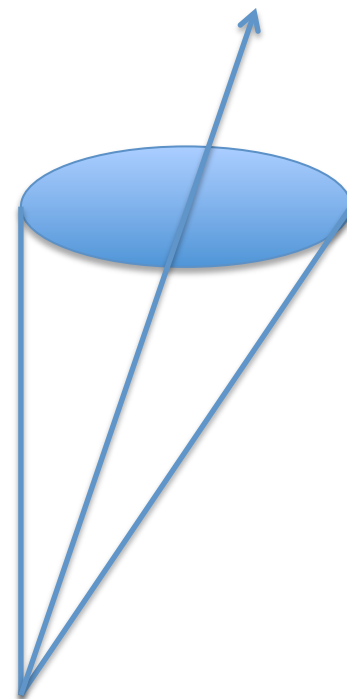
# Reducible backgrounds

- In this case, the final state is not exactly as your signal, but it has characteristics that can fake the signal final state
- In the 4-lepton example the main example of such background is the Z +jets process
- Cuts on the 3<sup>rd</sup> and 4<sup>th</sup> leading leptons are used for the rejection of these backgrounds
  - Z+light jets: the additional jets can fake electrons
    - Main handle to reject is an optimal electron identification
  - Z+bb: b leptonic decays produce leptons in the final state
    - Main rejection handle are the characteristics of leptons in jets from heavy quarks with long lifetime
      - Isolation
      - High impact parameter
- Processes with very large  $\sigma$  w.r.t. the signal, but easier to discriminate
  - E.g. Z inclusive  $\sigma$  is  $\sim 1$  nb, i.e.  $\sim 2 \cdot 10^5$  times the signal cross section !



# Lepton isolation

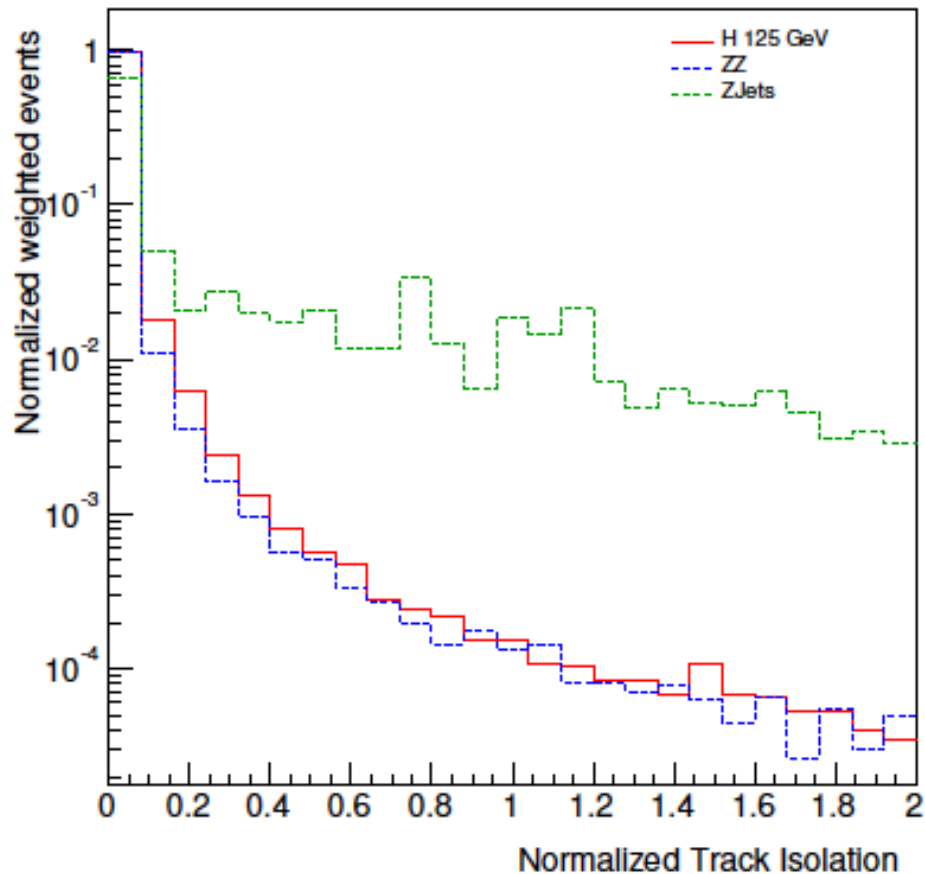
- Two possible ways of calculating it:
  - Sum of the tracks pT in a cone around the lepton track ( track isolation )
  - Sum of the calorimeter cells energy in a cone around the lepton track
- The two variables are correlated but can be used in a complementary way
- The cone is defined as:
$$\Delta R = \sqrt{(\Delta\eta)^2 + (\Delta\varphi)^2} < 0.2$$
- The size is optimized on the basis of efficiency and rejection
  - An important component is the impact of pileup events



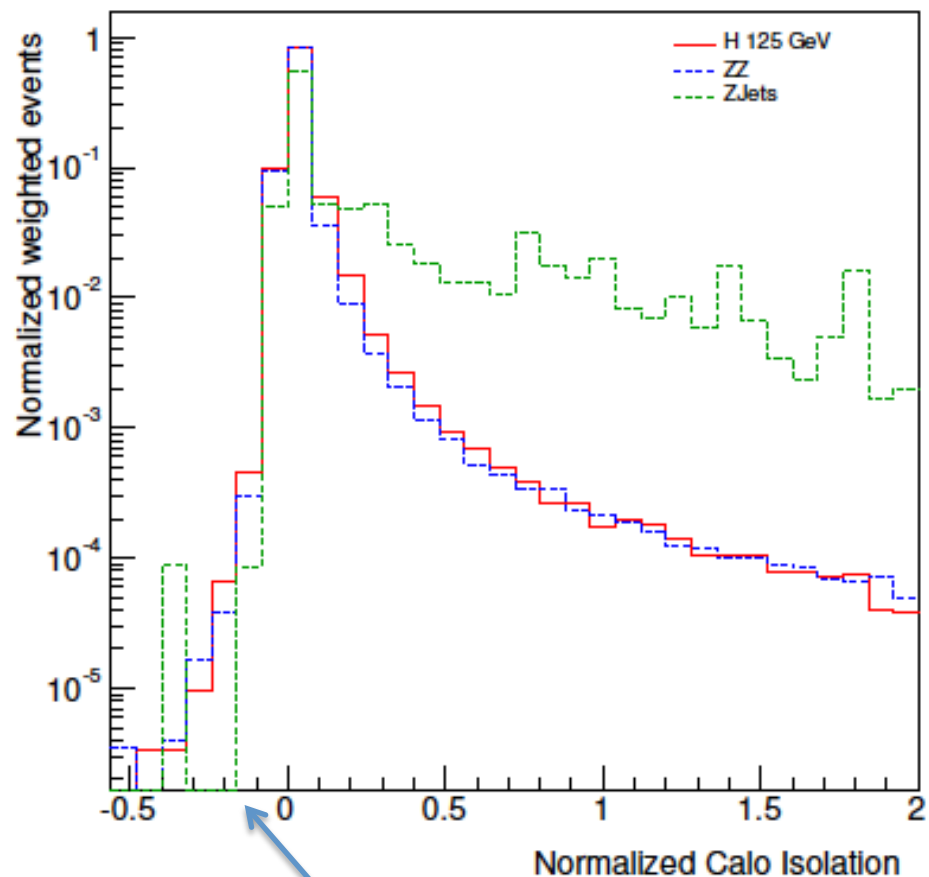
# Lepton isolation

- In both cases the isolation is normalized to the lepton  $p_T$

## Track isolation



## Calorimeter isolation

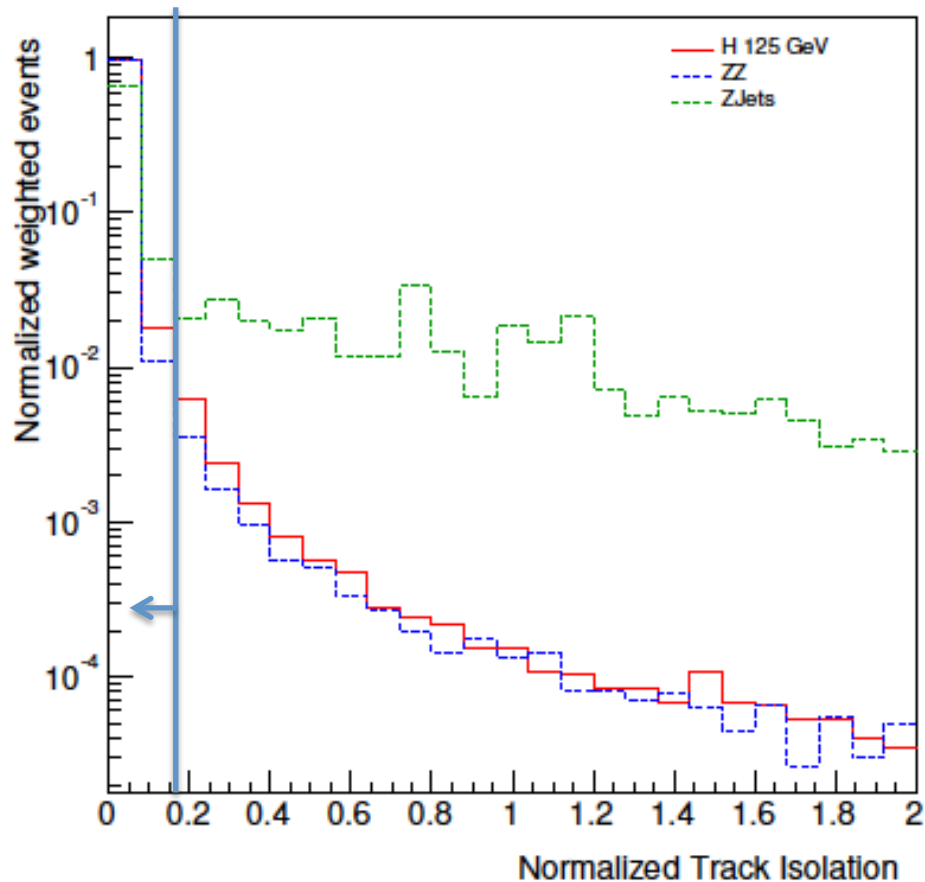


Noise subtraction

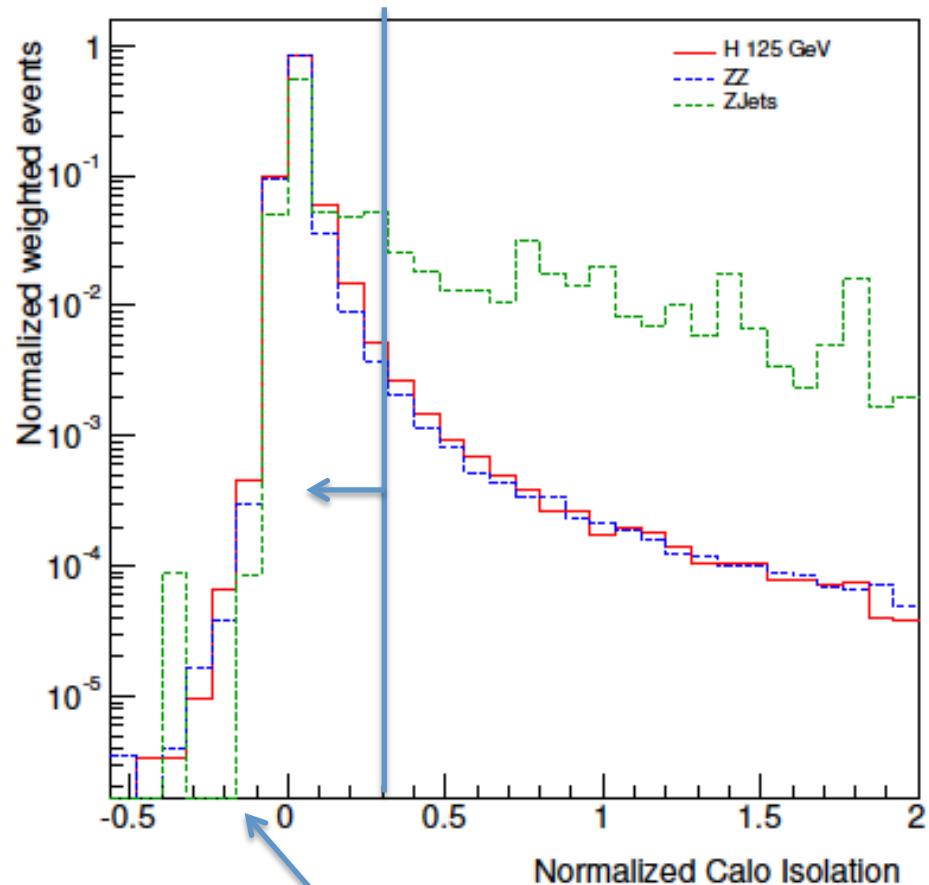
# Lepton isolation

- In both cases the isolation is normalized to the lepton  $p_T$

## Track isolation

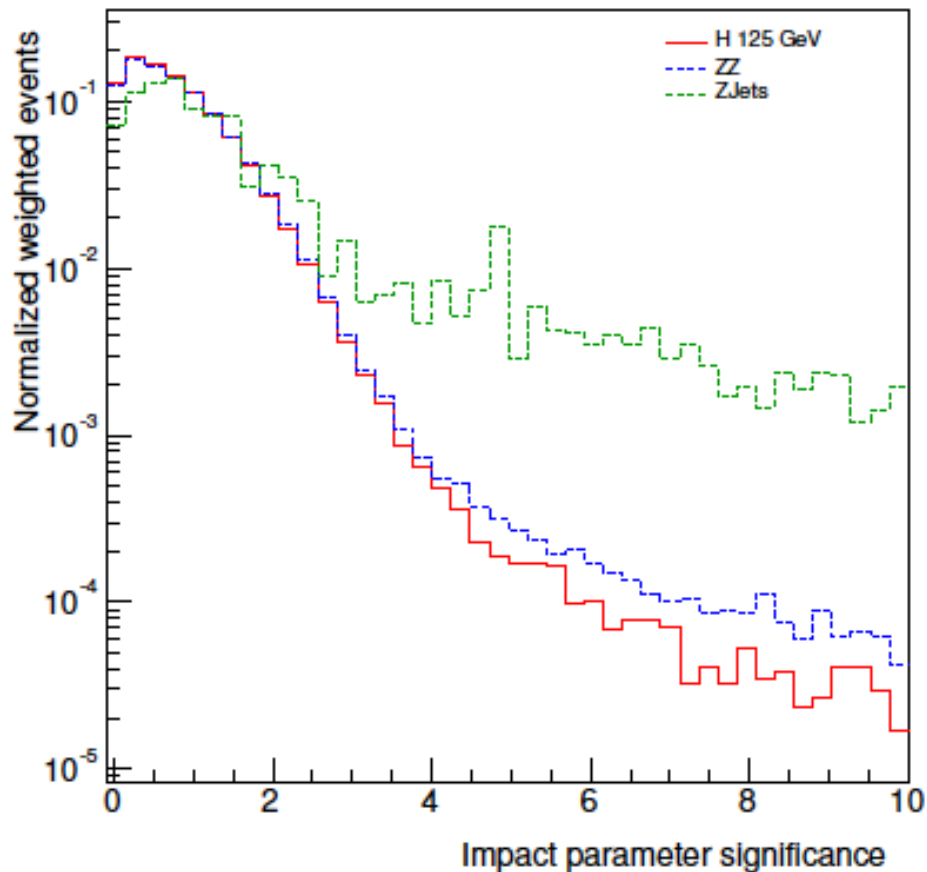


## Calorimeter isolation

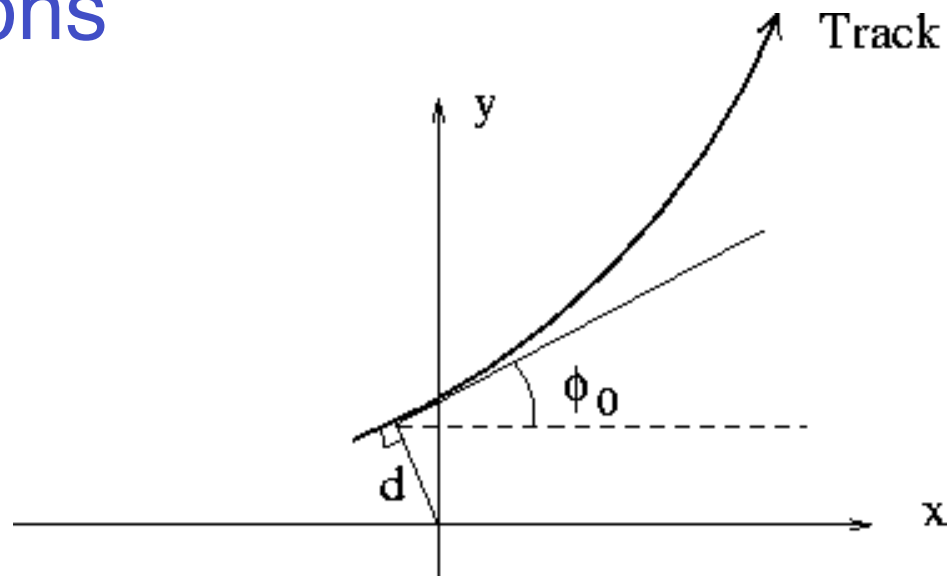


Noise subtraction

# Impact Parameter: muons



$$\text{IP significance} = d/\sigma_d$$

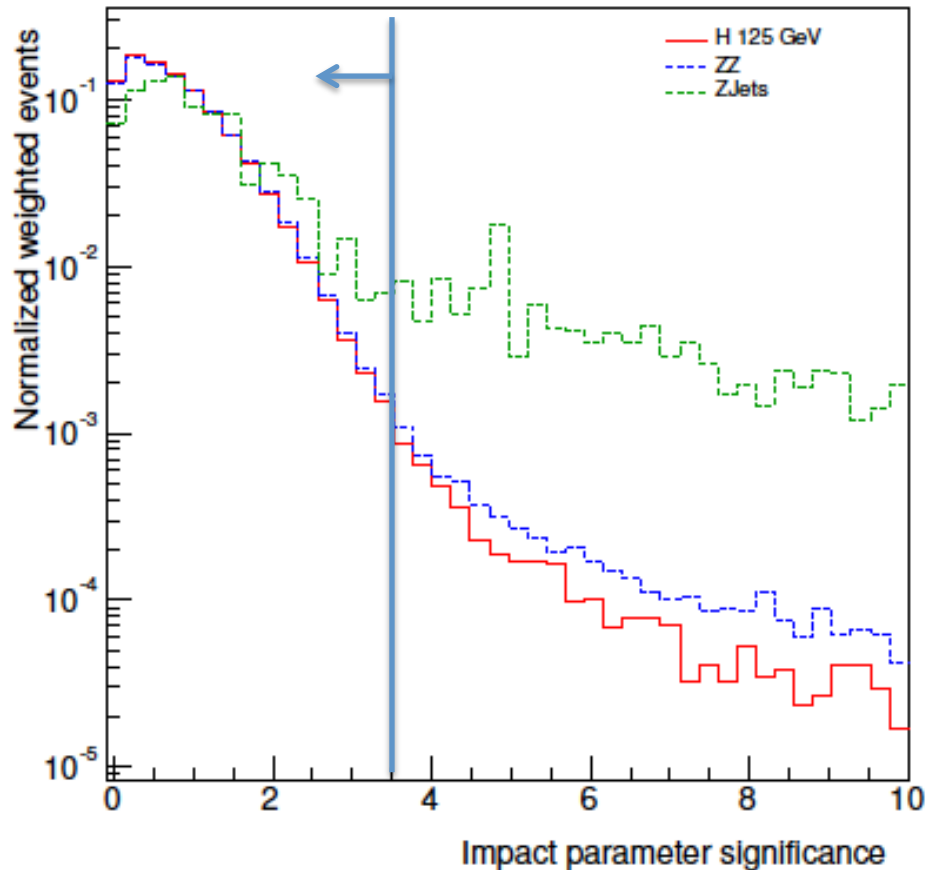


Long B mesons lifetime  $t \sim 1.5$  ps,  
i.e.  $\sim 750 \mu\text{m}$  at  $10 \text{ GeV } p_T$

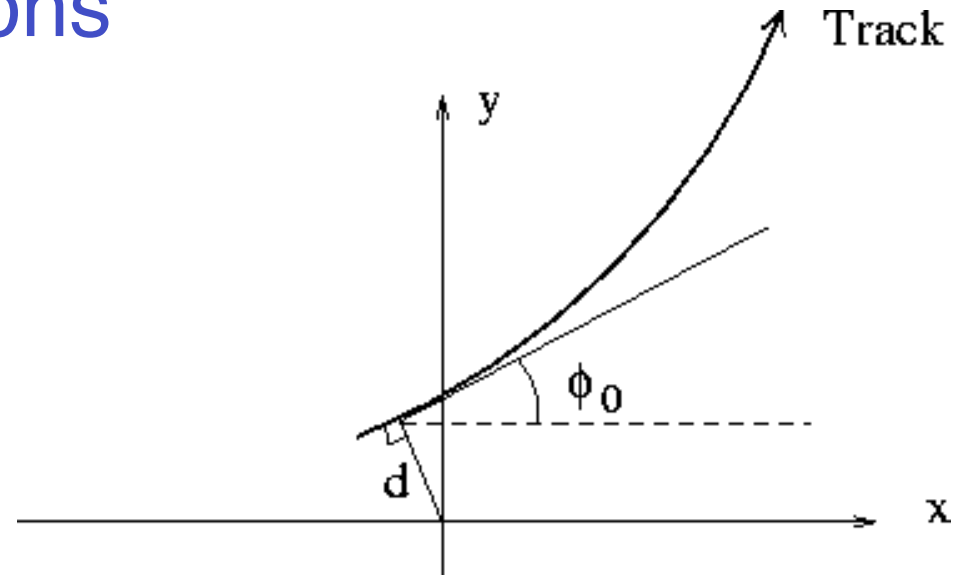
Transverse IP is used because  
of the much better resolution

Large IP of the sub-leading leptons  
can be used as a discriminating  
variable

# Impact Parameter: muons



$$\text{IP significance} = d/\sigma_d$$

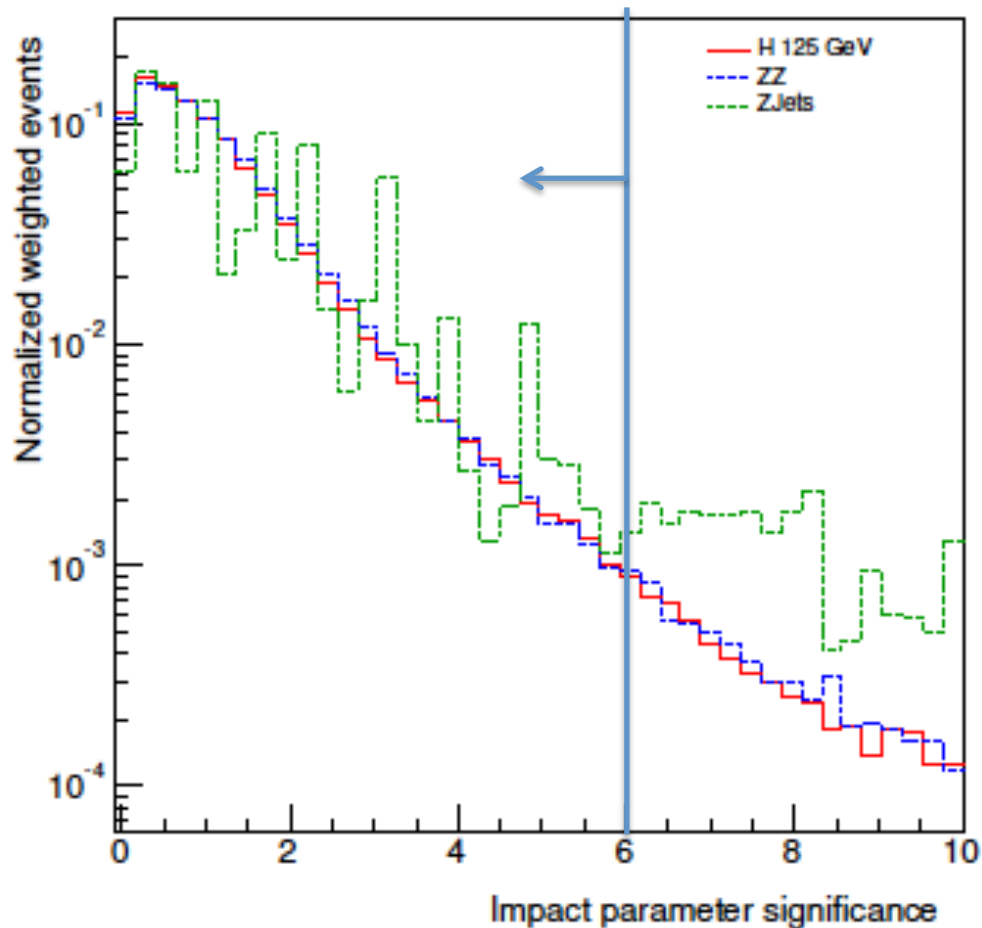


Long B mesons lifetime  $t \sim 1.5$  ps,  
i.e.  $\sim 750 \mu\text{m}$  at  $10 \text{ GeV } p_T$

Transverse IP is used because  
of the much better resolution

Large IP of the sub-leading leptons  
can be used as a discriminating  
variable

# Impact parameter: electrons



Because of the bremsstrahlung, the performance on IP reconstruction is much worse for electrons

It can still be used, but the cut has to be re-tuned to a looser value

→ keep a high enough efficiency

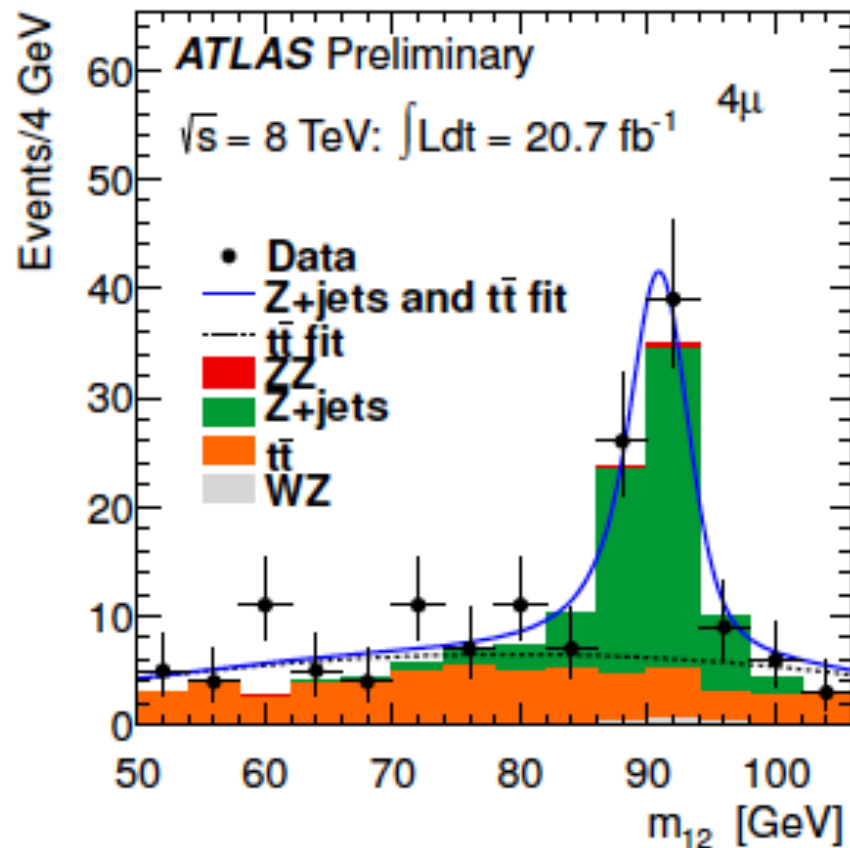


# Derive backgrounds from data

- In some cases, the cross section of a background is so large, that it is not possible to generate enough MC events to determine its characteristics precisely
- E.g. for Z+jets one would need  $\sim 2 \cdot 10^5$  the signal statistics
- To derive signal normalization and/or shapes, and in general to cross check all backgrounds, the so-called Control Regions (CR) are built, by removing, or reverting some of the selection cuts
  - Create background-enhanced CRs
- The MC can then be used to extrapolate from the CR to the Signal Region (SR) via some transfer factors or functions
  - But in some cases just the data are used, and also the transfer functions are derived from the data
  - Various methods that we'll not have time to cover in detail

# Example of a background CR

- Obtained by removing/reverting the cuts on isolation and IP
- Signal and irreducible background are in this way completely removed
- An almost pure Z+jets +  $t\bar{t}$  (another irreducible background that we didn't cover here) sample is obtained



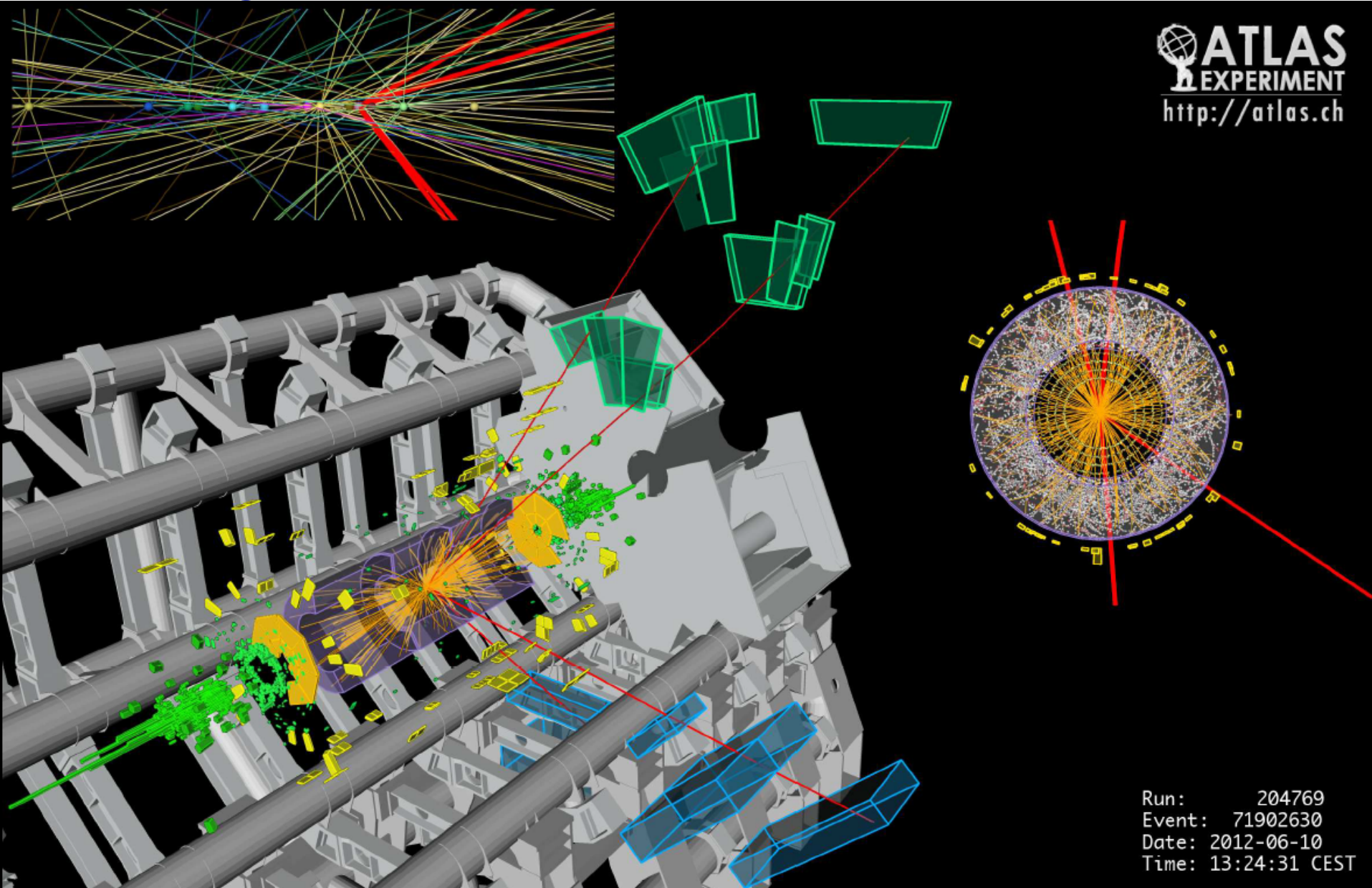
By fitting the data with two template functions:

→ Breit-Wigner + Gaussian ( Z-peak from the Z+jets)

→ Polynomial (~flat  $t\bar{t}$  component)

The two contributions can be disentangled and each MC separately rescaled to the data

# A $4\mu$ signal candidate

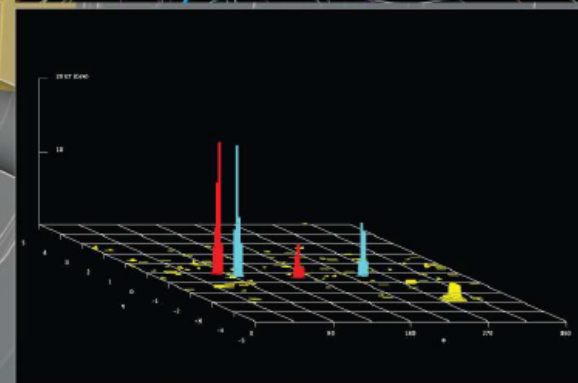
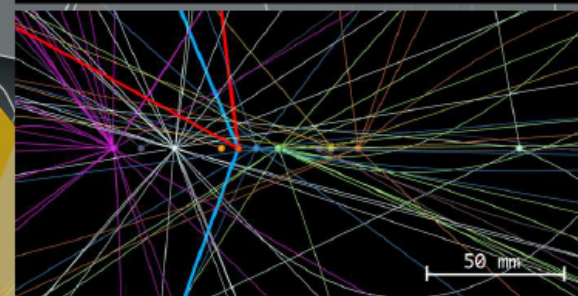
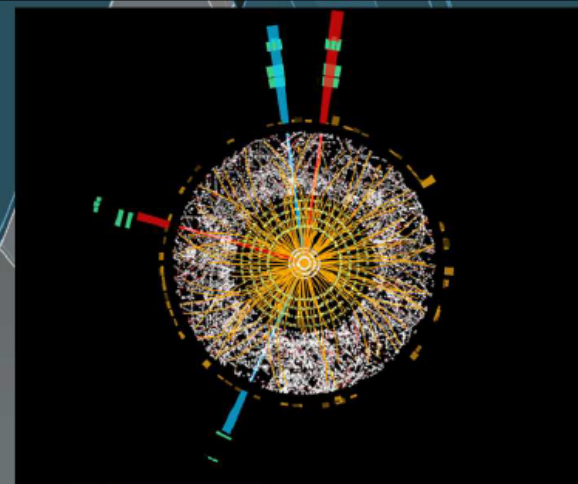
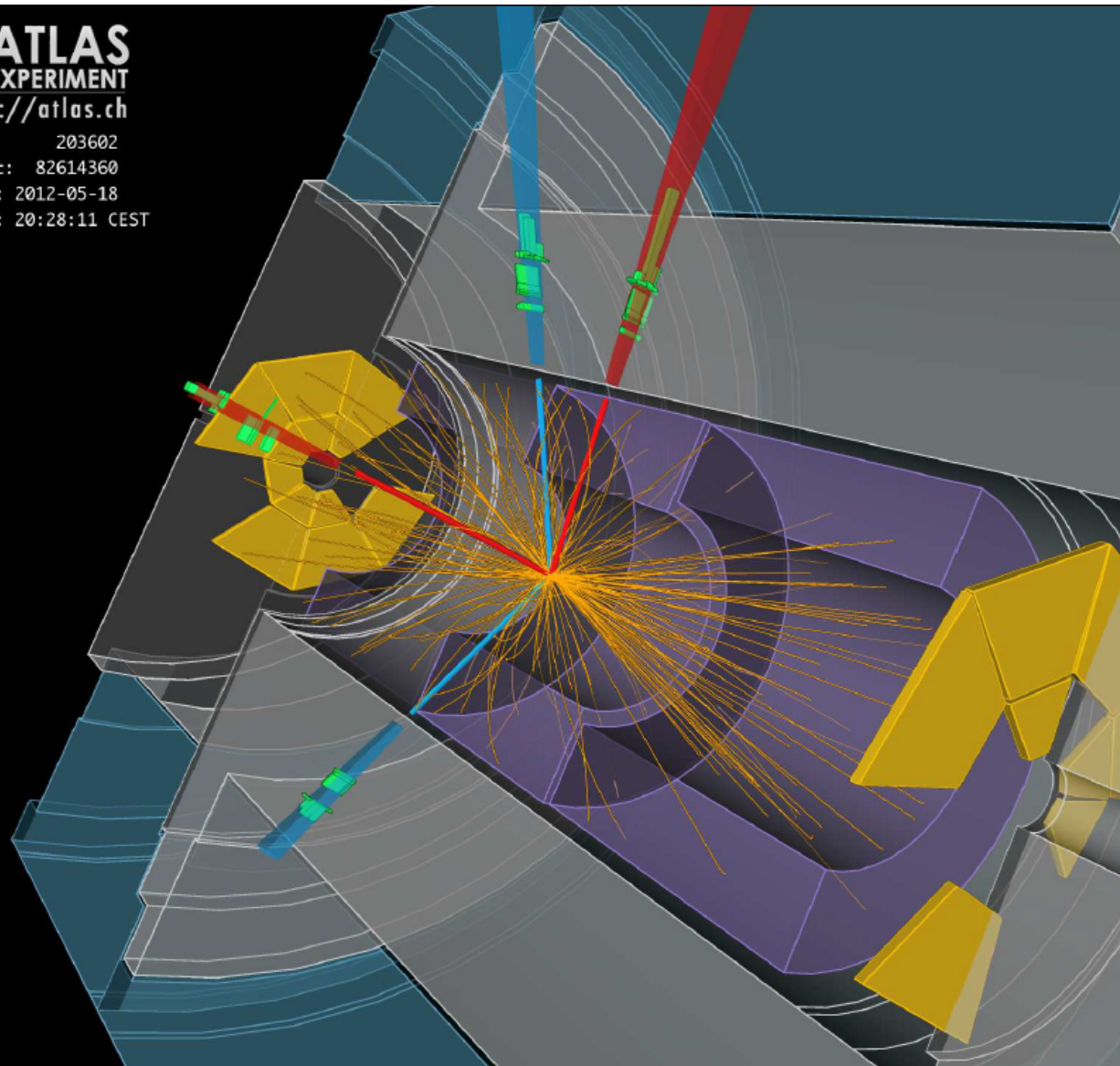


Run: 204769  
Event: 71902630  
Date: 2012-06-10  
Time: 13:24:31 CEST

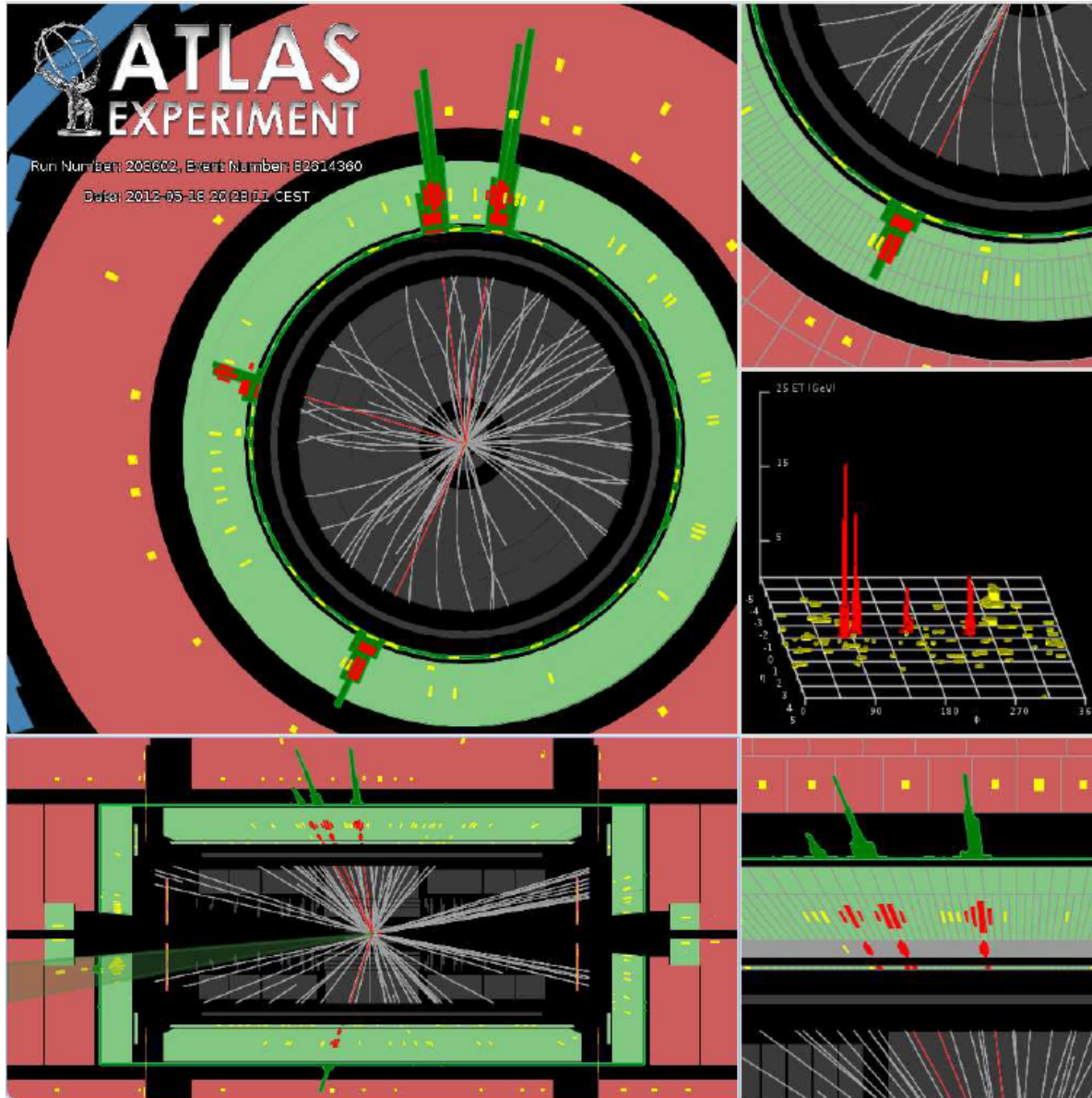
# A 4e signal candidate

**ATLAS**  
EXPERIMENT  
<http://atlas.ch>

Run: 203602  
Event: 82614360  
Date: 2012-05-18  
Time: 20:28:11 CEST



# Another view

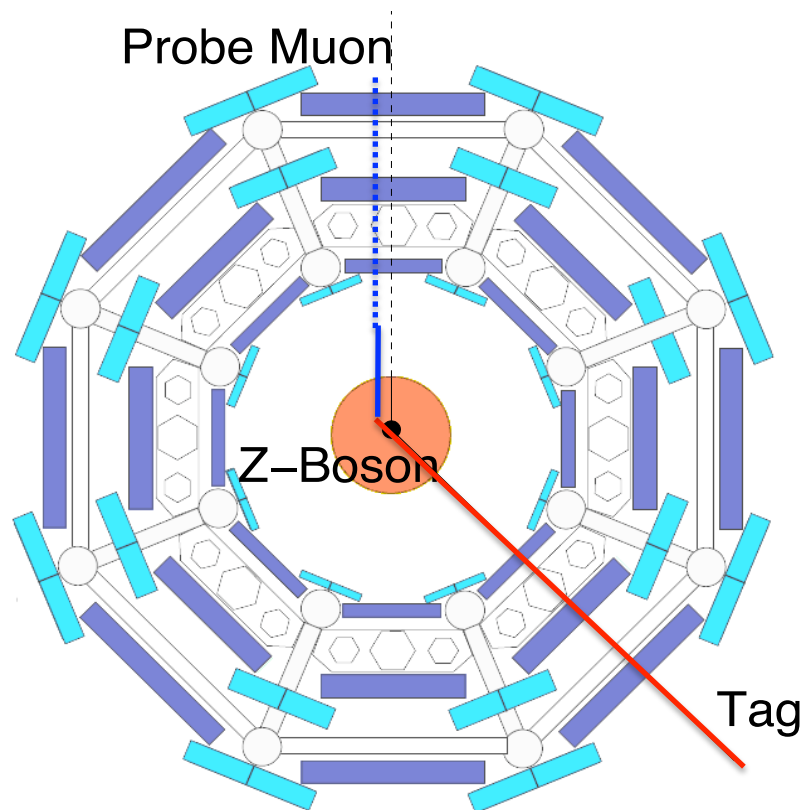


# Modeling of the detector performance

- The MC models the detector performance with great accuracy
- Still some effects might not be perfectly modeled and will need some data-driven tuning
  - Need to make sure that the MC models data correctly, before claiming that any difference comes from new physics
- Fine-tuning of small local effects, or time-dependent detector issues:
  - E.g. if one part of the detector becomes inefficient for a limited data taking interval
- Typical effects to take into account are:
  - Trigger and reconstruction efficiencies
  - Momentum and energy resolutions
  - Momentum and energy scales
- This is a very important ingredient in all Physics analyses and implies:
  - Develop methods to measure data-driven performances
  - Apply corrections to the MC or to the data

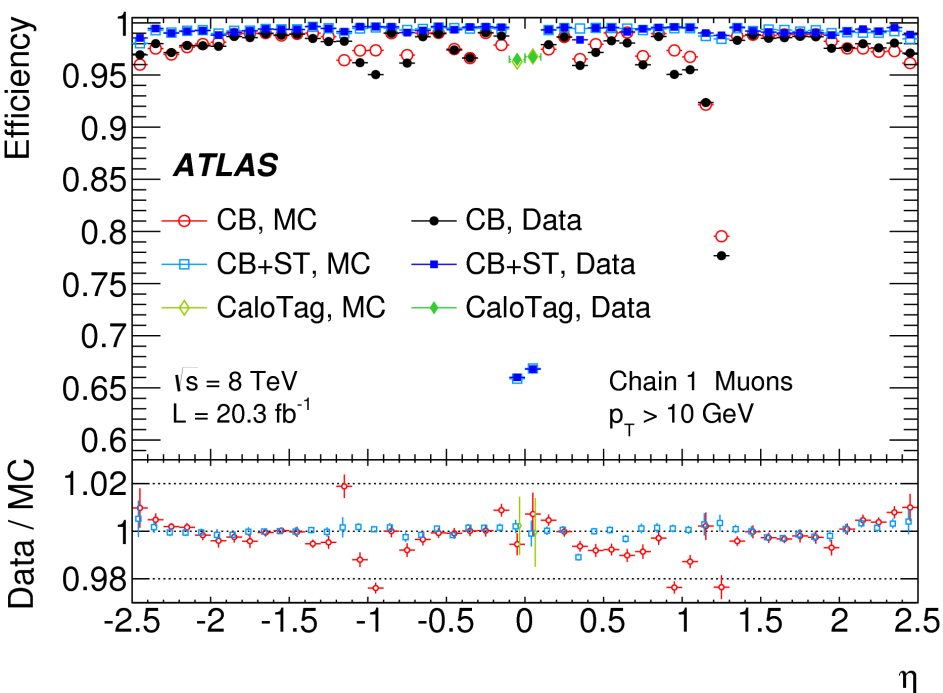
# Efficiencies

- Use known process/resonances decaying to electrons or muons
  - $Z \rightarrow \ell\ell$  ( $p_T > \sim 10$  GeV) and  $J/\psi \rightarrow \ell\ell$  ( $p_T < \sim 10$  GeV)
- Look for a reconstructed muon, which also provided the trigger (tag muon)
- Look for a track in the Inner Detector (probe):
  - Same vertex as the tag
  - Isolated (reject tracks in jets)
  - $M(\text{tag}, \text{probe})$  close to  $M_Z$  or  $M_{J/\psi}$
- Check if the probe ID track matches a reconstructed muon (or a muon trigger element)
  - The efficiency is given by  $N_{\text{matching}}/N_{\text{total probes}}$
- Same method used also for electrons (look for matching tracks/calorimeter clusters)

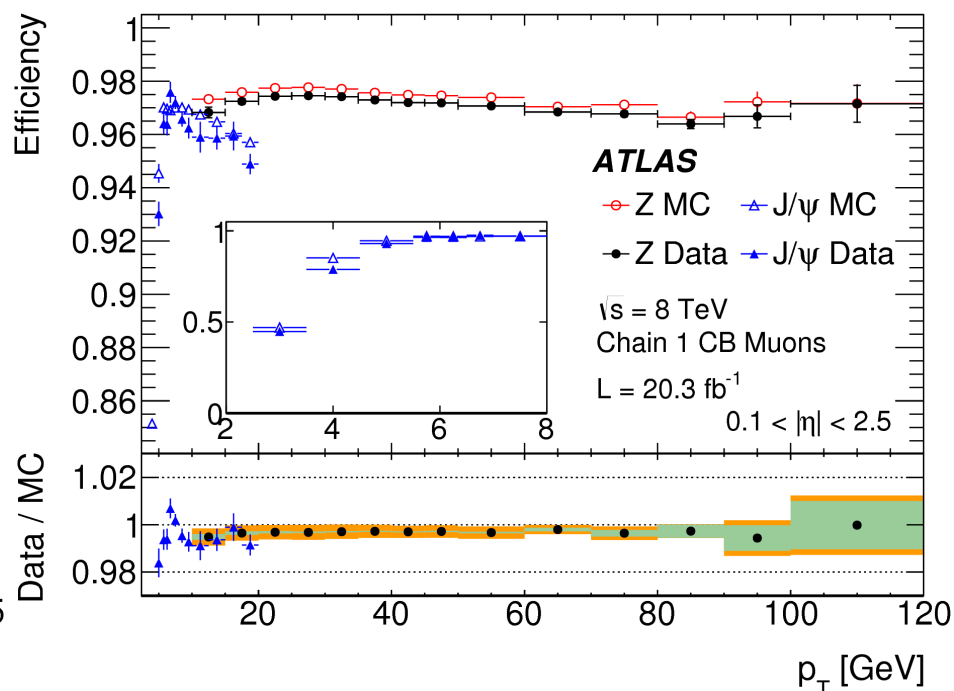


# Some example results for muons

Efficiencies vs  $\eta$  for various types of reconstructed muons



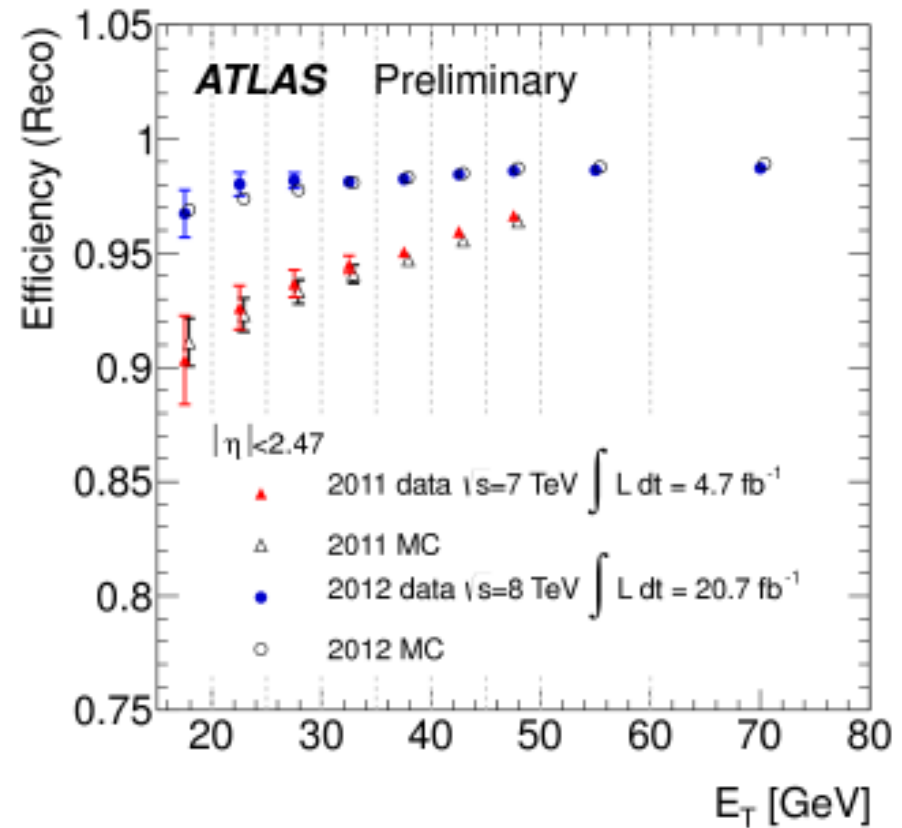
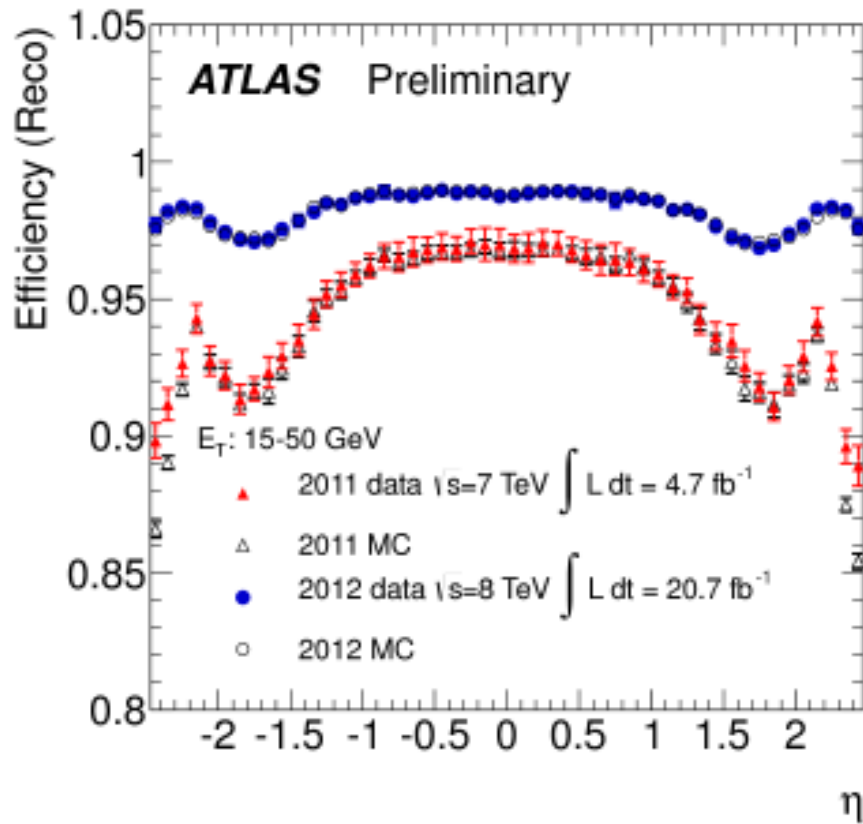
Efficiencies vs  $p_T$  for combined muons



Local Efficiencies are calculated for single muons in bins of  $p_T$ ,  $\eta$ ,  $\phi$ , chosen with the proper granularity, depending on detector structure, or known inefficiency regions



# Efficiencies corrections for electrons



Also in this case, the efficiencies are calculated in bins of the phase-space  
Large improvement in 2012 reconstruction

# Efficiency reweighting

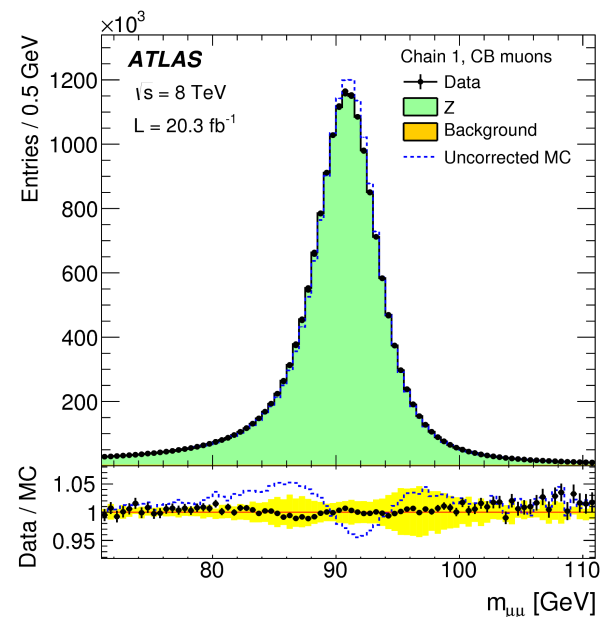
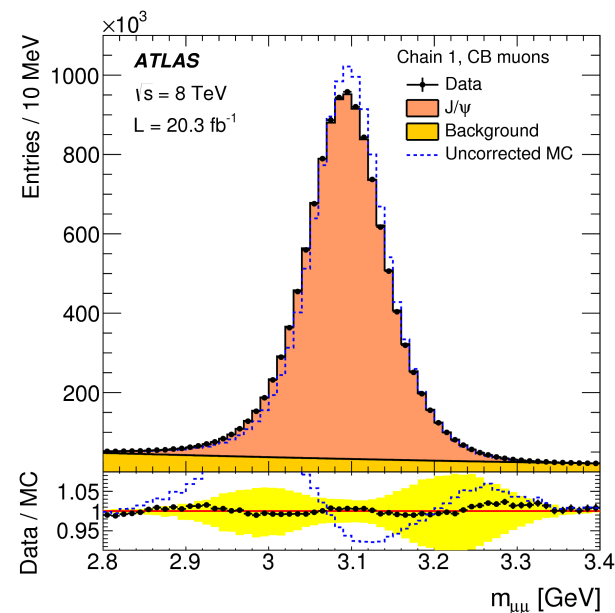
- Efficiency is corrected by giving to each event a weight
- Get for each bin:
  - $\varepsilon_i^{\text{data}}$ : efficiency in data
  - $\varepsilon_i^{\text{MC}}$ : efficiency in MC
- In 4-lepton events:
- Reconstruction efficiency
  - Reweight each MC event according to: 
$$w = \prod_{i=1,n} \frac{\varepsilon_i^{\text{DATA}}}{\varepsilon_i^{\text{MC}}}$$
  - Where the product runs over all reconstructed leptons entering in the analysis
- Trigger efficiency: just need at least one lepton triggering
  - Reweight each MC event according to:

$$w = \frac{1 - \prod_{i=1,N} (1 - \varepsilon_i^{\text{DATA}})}{1 - \prod_{i=1,N} (1 - \varepsilon_i^{\text{MC}})}$$

Ratio of the probabilities that at least one lepton is passing the trigger

# Momentum scales and resolutions

- Scales of momentum and energy are determined by comparing to the MC distributions of known resonances
  - $Z$ ,  $J/\psi$ ,  $\Upsilon$
- The very well known masses and widths allow the precise determination of momentum and energy scales
  - Same method used for muons and electrons
  - Just the level of backgrounds is different
- Scales are determined in bins of  $p_T$ ,  $\eta$ ,  $\phi$
- **Systematic uncertainties on scales are a fundamental ingredient in the mass measurement**



Section 4

# ANALYSIS RESULTS

# Results of July 2012 – the discovery !

Number of events in a mass window 120-130 GeV around the signal peak

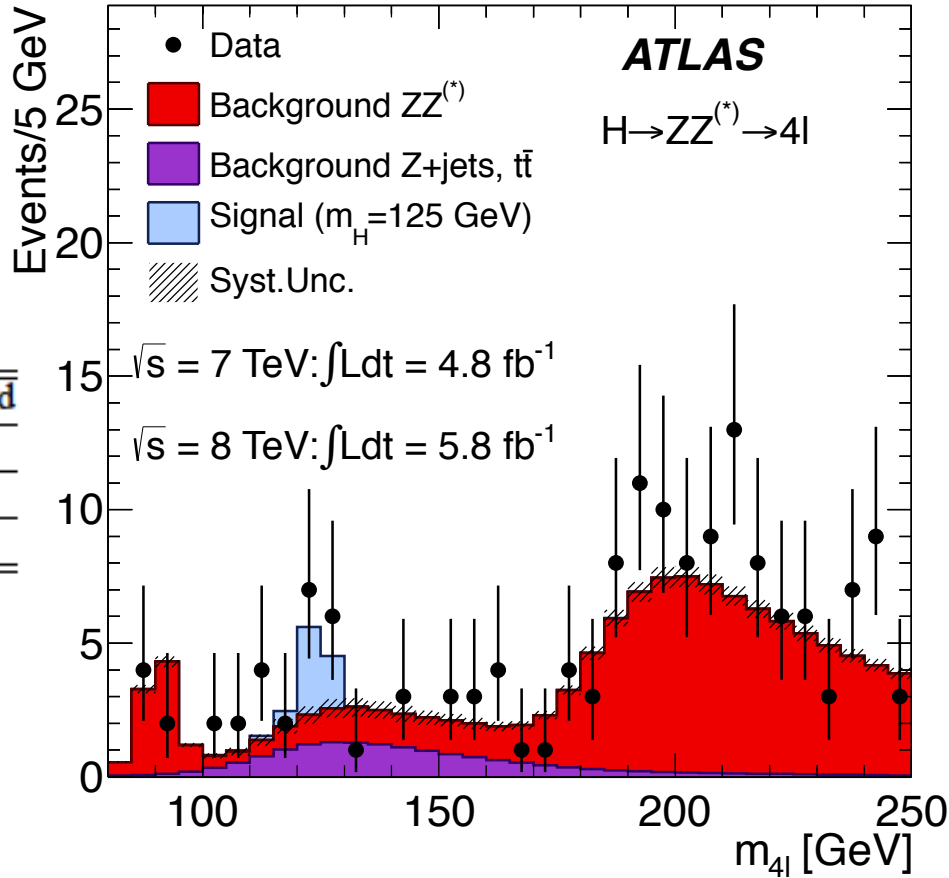
Theory error on the  $\sigma$

	Signal	$ZZ^{(*)}$	Z + jets, $t\bar{t}$	Observed
$4\mu$	$2.09 \pm 0.30$	$1.12 \pm 0.05$	$0.13 \pm 0.04$	6
$2e2\mu/2\mu2e$	$2.29 \pm 0.33$	$0.80 \pm 0.05$	$1.27 \pm 0.19$	5
$4e$	$0.90 \pm 0.14$	$0.44 \pm 0.04$	$1.09 \pm 0.20$	2

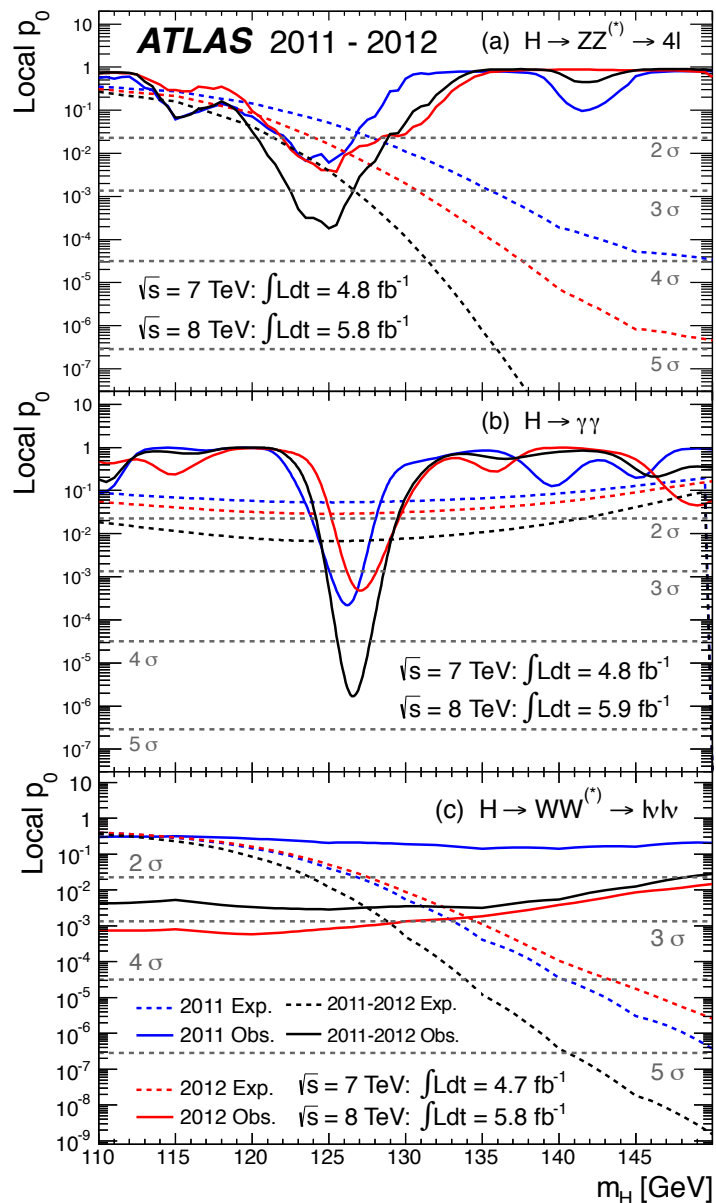
Total expected signal: 5.3 events  
 Total expected background: 4.9 events

Total observed events in data: 13 !

Already a simple calculation shows you something: probability to observe 13 events when you expect 4.9 is **0.17 %** ( of course no errors no syst here )



# Significance of the first observation

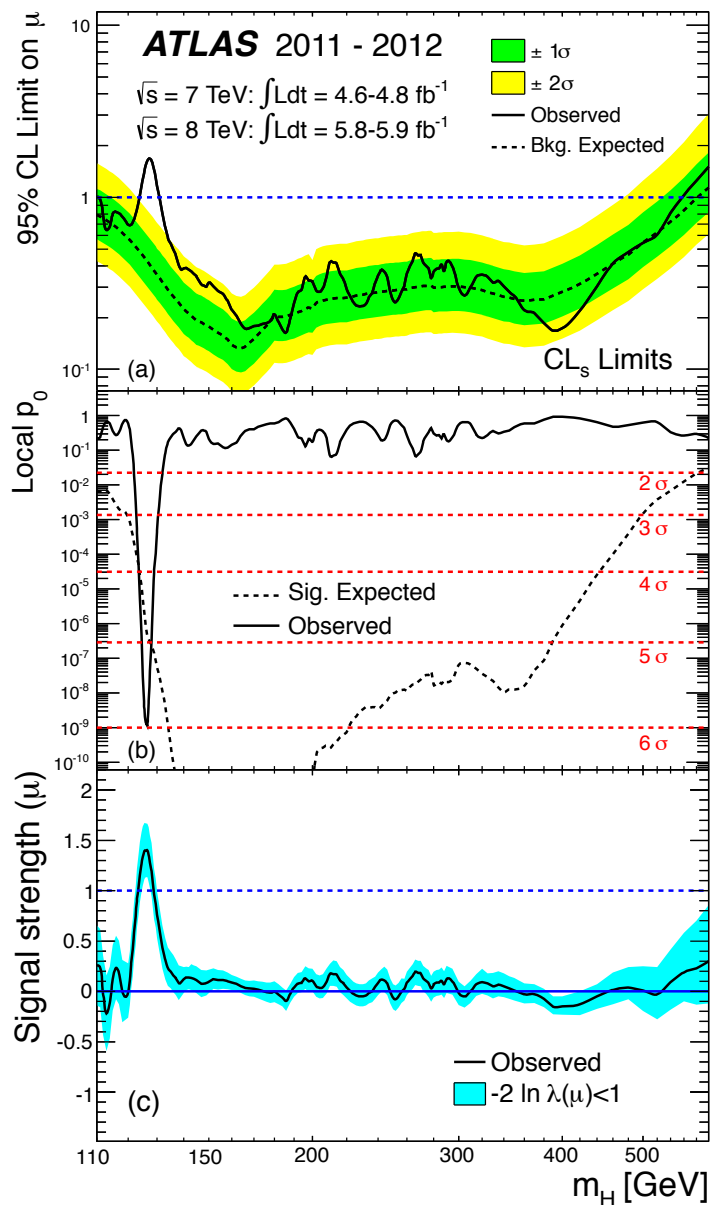


- Test of the background only hypothesis using the test statistics that you've seen the lectures:

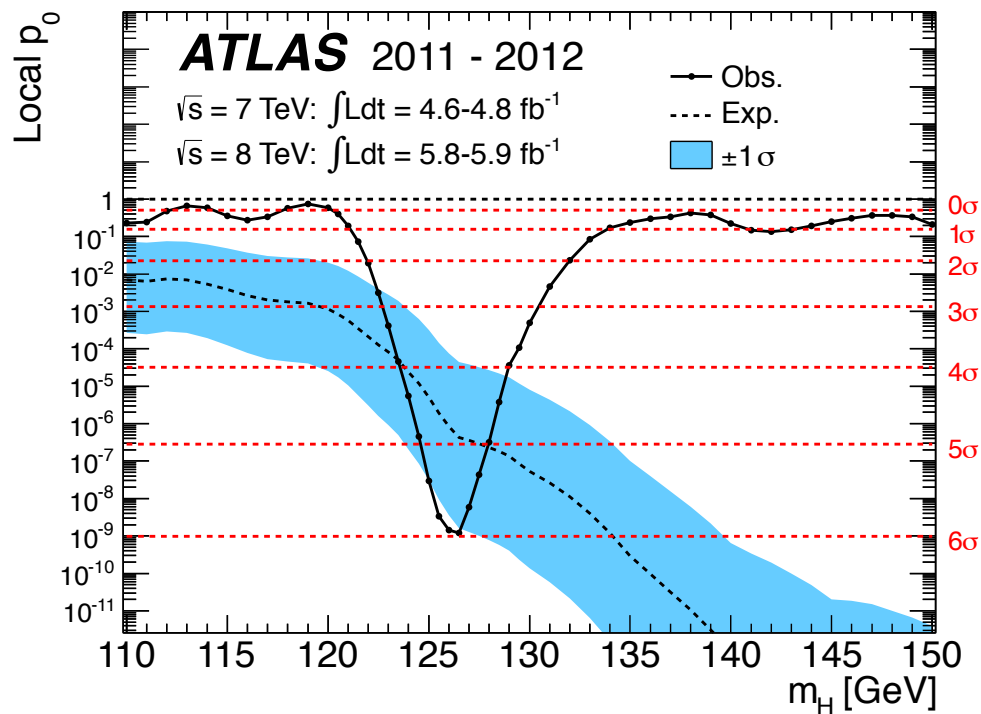
$$q_0 = -2 \ln \frac{L(0, \hat{\underline{\theta}})}{L(\hat{\underline{\mu}}, \hat{\underline{\theta}})}$$

- The  $p_0$  is the probability that a background fluctuation is more signal-like than expected for the signal (or than the data for the observed)
- The expected curves correspond to the  $p_0$  vs mass in case of a SM signal

# Combined limits and significance

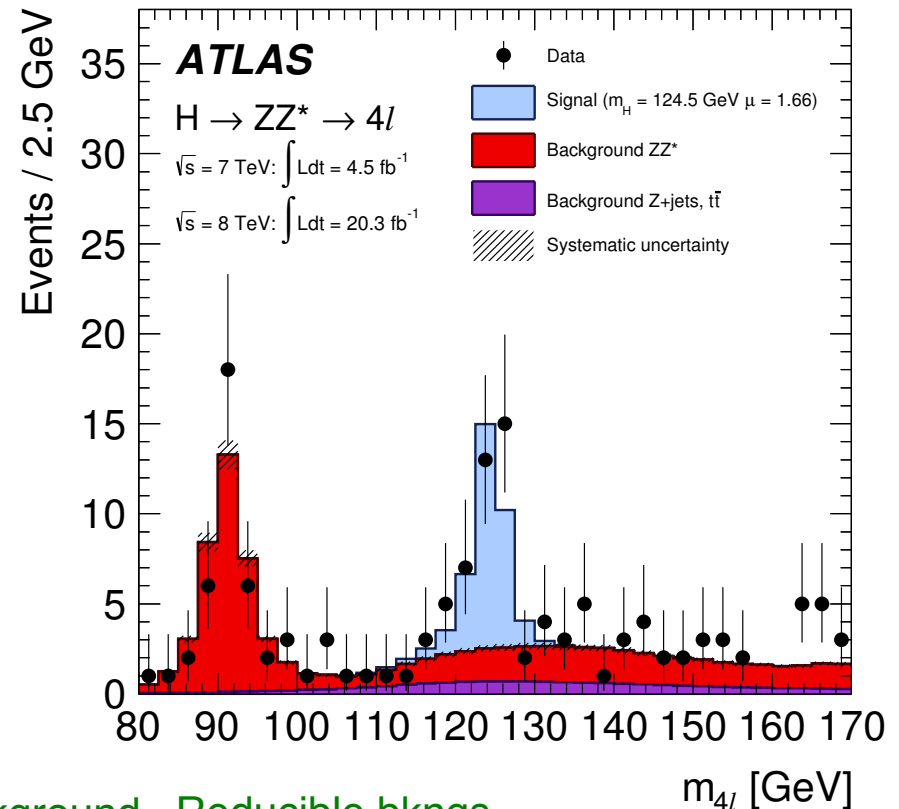


## Combined $p_0$ in the low-mass region



# The new resonance, with the full run1 dataset

- At the end of the run-1 data taking (end of 2012)
  - 4.5 fb<sup>-1</sup> at 7 TeV and 20.3 fb<sup>-1</sup> at 8 TeV
- In the 120-130 GeV mass window:
  - 37 observed events with 10.4 expected from background only ( well above 5-sigma significance )
    - Light excess w.r.t. expected SM signal



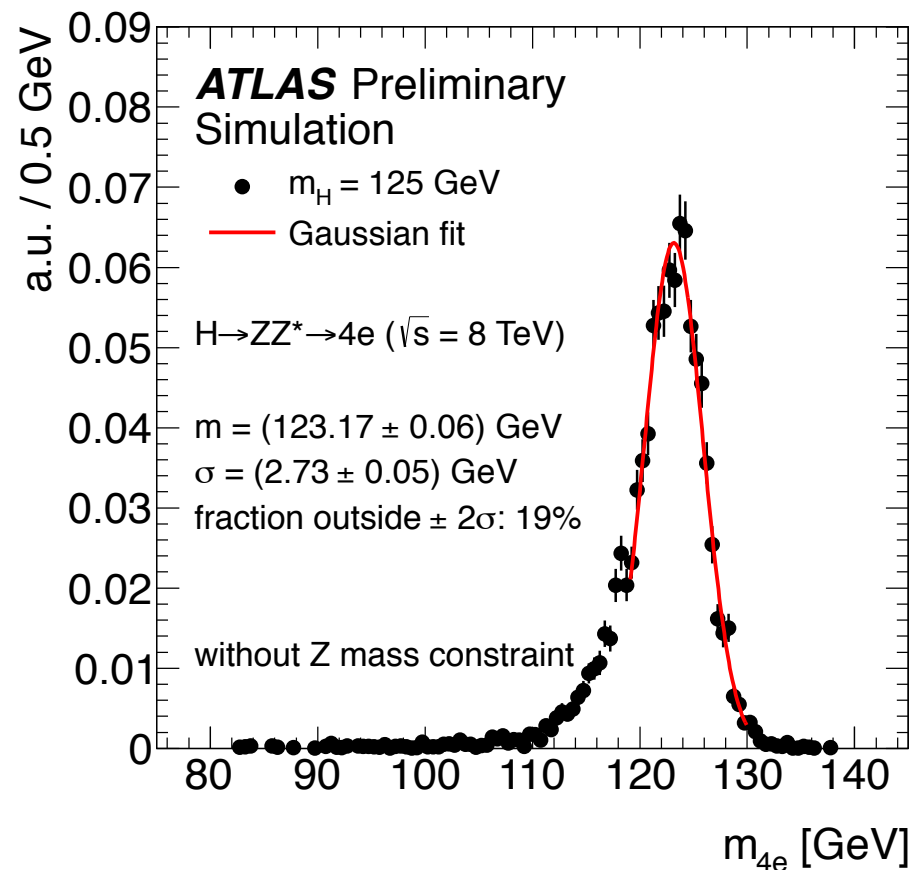
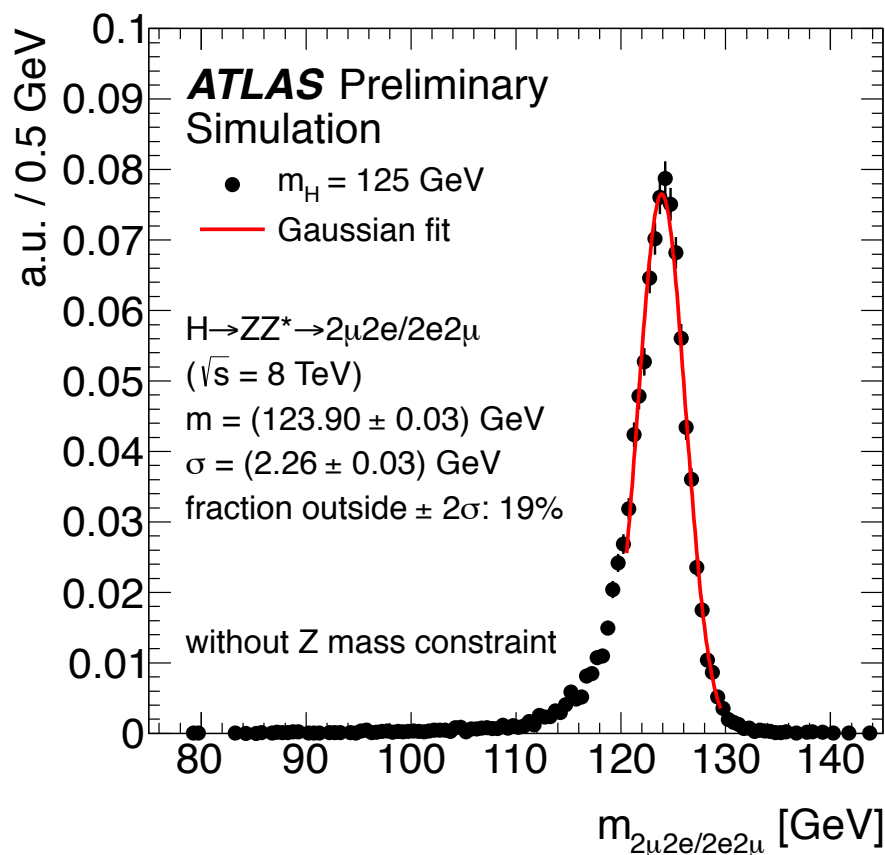
Signal 120-130    ZZ background    Reducible bkngs

Total signal     $\sqrt{s} = 7 \text{ TeV}$  and  $\sqrt{s} = 8 \text{ TeV}$

4 $\mu$	6.80 ± 0.67	6.20 ± 0.61	2.82 ± 0.14	0.79 ± 0.13	1.7	9.81 ± 0.64	14
2e2 $\mu$	4.58 ± 0.45	4.04 ± 0.40	1.99 ± 0.10	0.69 ± 0.11	1.5	6.72 ± 0.42	9
2 $\mu$ 2e	3.56 ± 0.36	3.15 ± 0.32	1.38 ± 0.08	0.72 ± 0.12	1.5	5.24 ± 0.35	6
4e	3.25 ± 0.34	2.77 ± 0.29	1.22 ± 0.08	0.76 ± 0.11	1.4	4.75 ± 0.32	8
Total	18.2 ± 1.8	16.2 ± 1.6	7.41 ± 0.40	2.95 ± 0.33	1.6	26.5 ± 1.7	37



# Mass resolution



Natural width @ 125 GeV is 4 MeV

→ The reconstructed peak width is completely determined by the experimental resolution

→ It's important to reduce it as much as possible (mass measurement)

# Z mass constraint

- The resolution can be improved by applying the so-called Z mass constraint
  - The signal decay must have the two leading leptons having an invariant mass close to an on-shell Z
  - Rescale the lepton momenta so that the invariant mass of the leading lepton pair corresponds to the Z mass
- Simplest way is to rescale the momenta minimizing a chi-sq and imposing a constraint to the Z mass

$$M_{ll}^2 = p1 \cdot p2 \cdot (1 - \cos \theta_{12})$$

$$M_{ll}^{2'} = k1 p1 \cdot k2 p2 \cdot (1 - \cos \theta_{12}) = M_Z^2$$

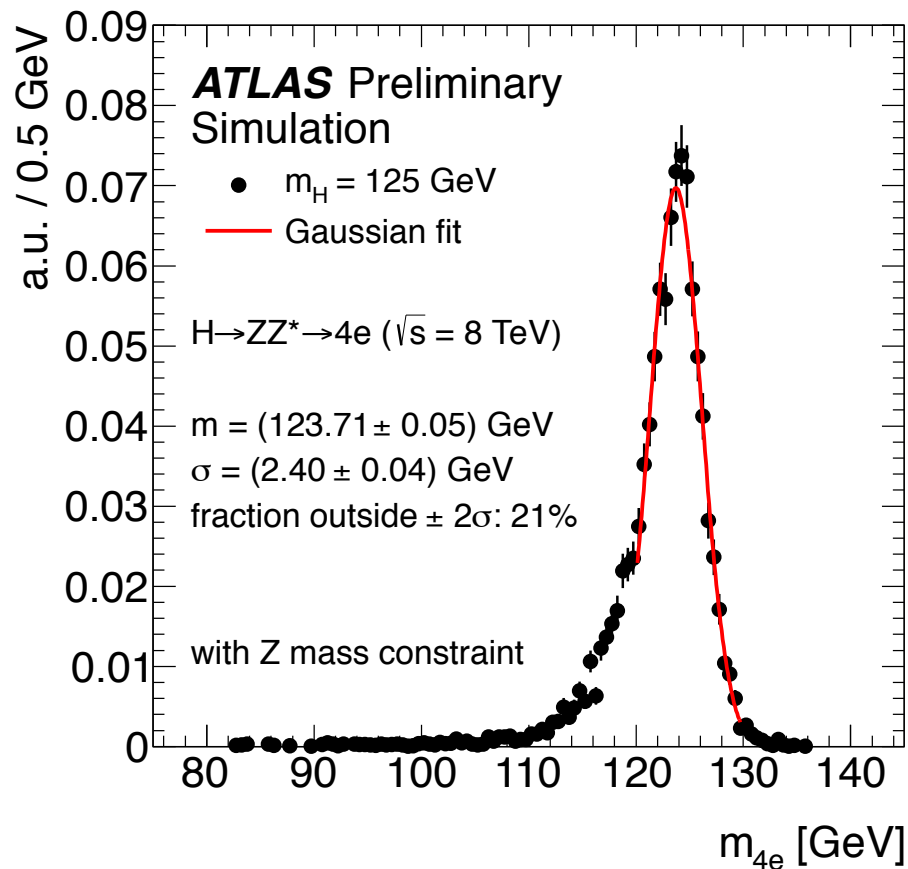
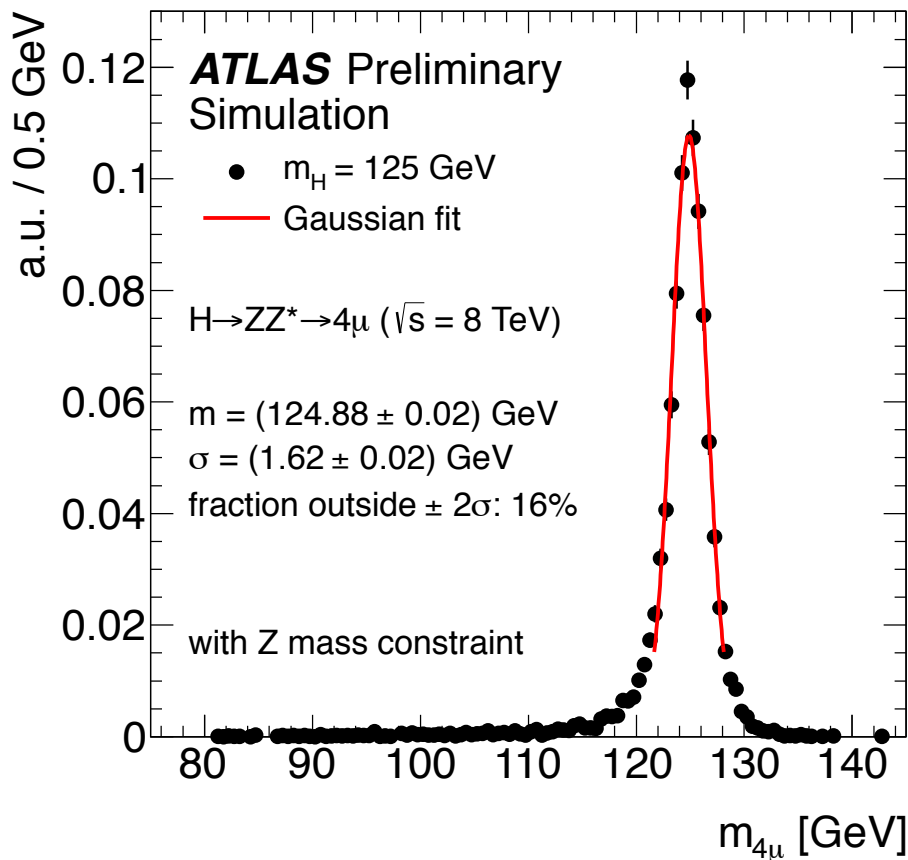
$$k1 \cdot k2 = M_Z^2 / M_{ll}^2$$

$$\chi^2 = \frac{(k1 p1 - p1)^2}{\sigma_{p1}^2} + \frac{(k2 p2 - p2)^2}{\sigma_{p2}^2}$$

Or, a more complex  
Constrained kinematic fit,  
taking into account also the  
Z natural width

# Signal mass resolution with mass constraint

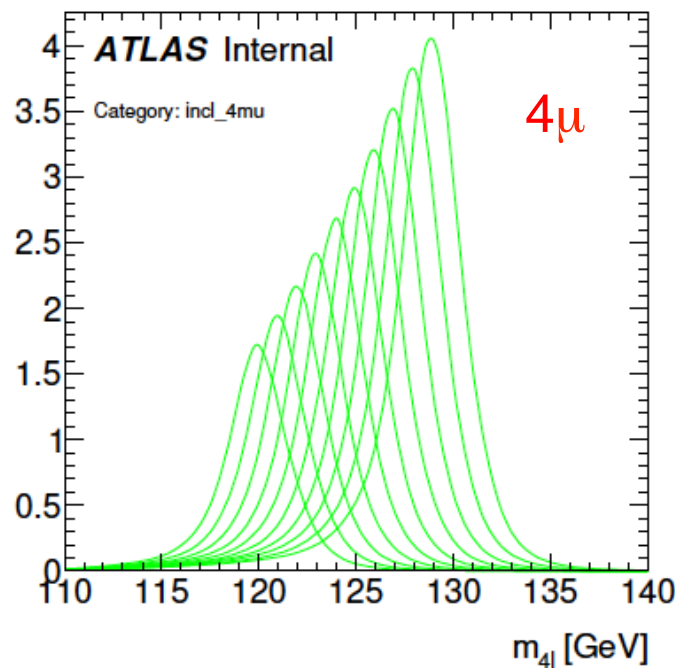
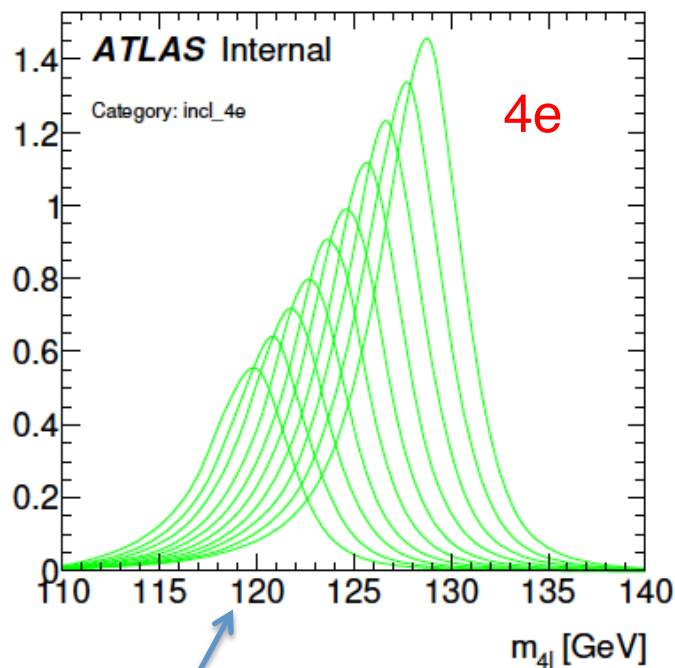
For  $M_H=125$  GeV



The Higgs mass is a free parameter of the theory → its precise measurement it's fundamental

# Mass measurement

Template fit: build a MC model of the signal mass distribution  
 Continuous variation of the distribution vs  $M_H$  and  $\sigma_H$  via a morphing function (basically an interpolation among the fixed points)



Of course, only the signal depends on  $M_H$

In the same fit, both mass and “signal strength” extracted:

$$\mu = \frac{\sigma_{Observed}^{Signal}}{\sigma_{SM}^{Signal}} = \frac{N_{Observed}^{Signal}}{N_{SM}^{Signal}}$$

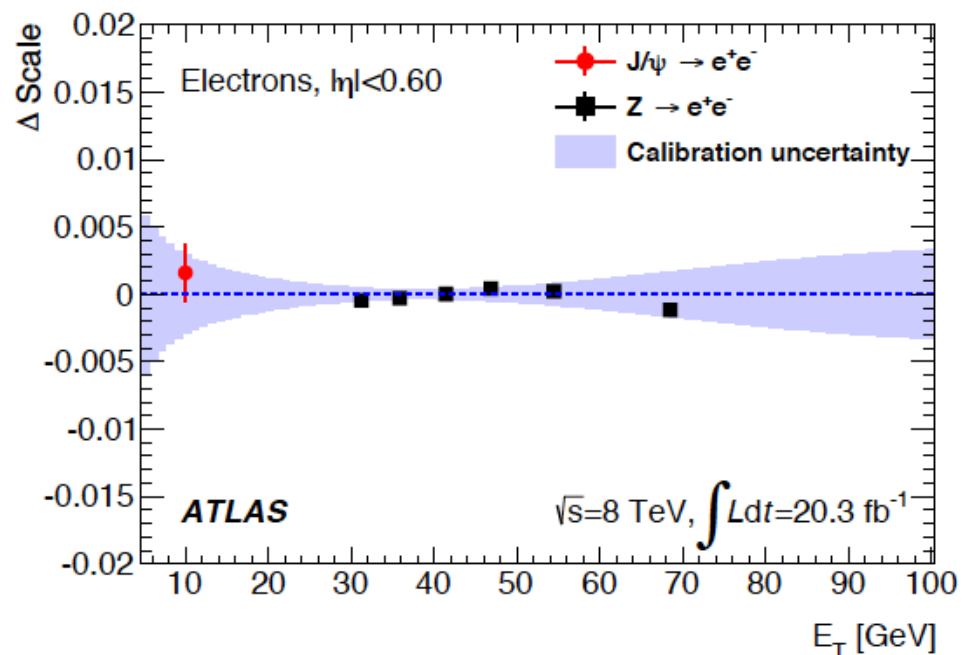
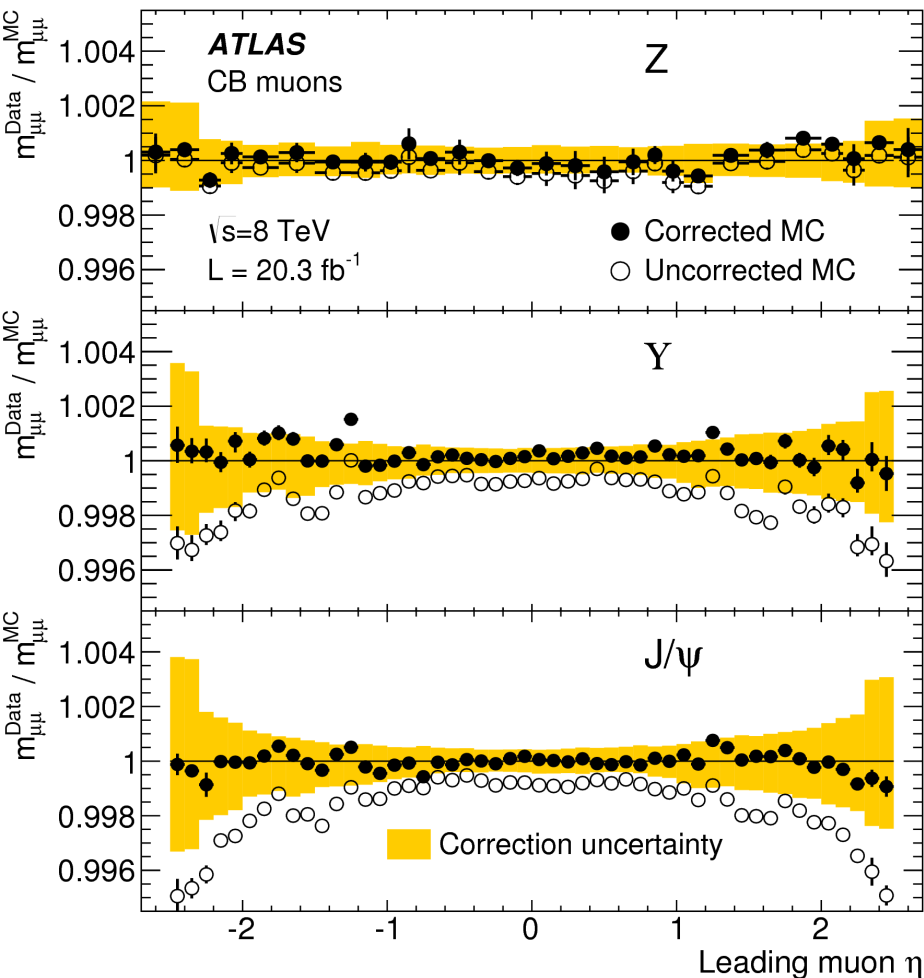
# Systematics

Systematics on the energy scales are:

→ 0.04% - 1% for electrons

→ 0.07% - 0.2% for muons

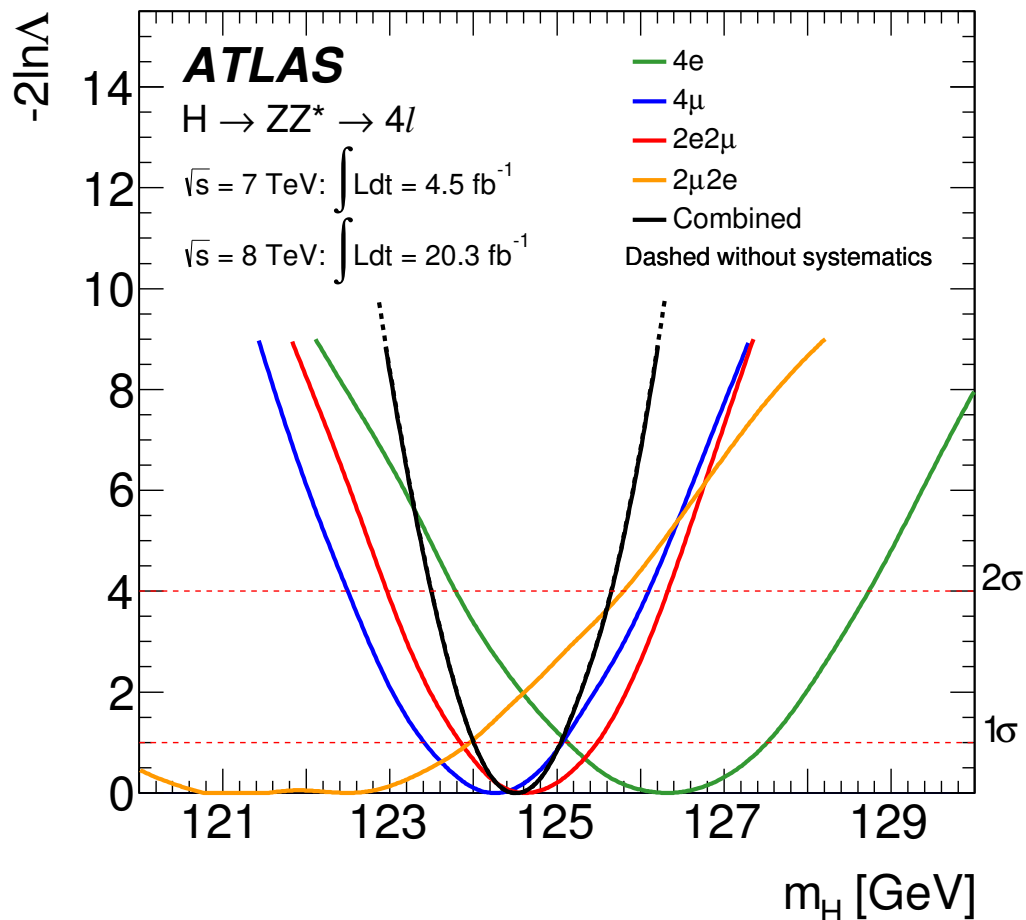
Thanks to the large stat of the resonance and the extensive work on calibrations



# Statistical and systematic errors

- The error on a measurement has:
  - A statistical component, i.e. depending only on the number of events entering in the measurement
  - A systematic component, i.e. connected to the methods and assumptions used in the measurement (e.g. the energy scales, the errors on the background knowledge)
- Due to the limited statistics the  $H \rightarrow ZZ^* \rightarrow 4l$  channel is not strongly affected by systematics
- Mass measurement main errors:
  - Momentum and energy scales
  - Background shapes
- Signal strength measurement:
  - Backgrounds normalizations (and shape)
  - Theoretical error on the SM signal cross section

# Mass fit results



$$M_H = 124.51 \pm 0.52 \text{ (stat)} \pm 0.6 \text{ (syst)}$$

The impact of the scale syst. on the mass is negligible

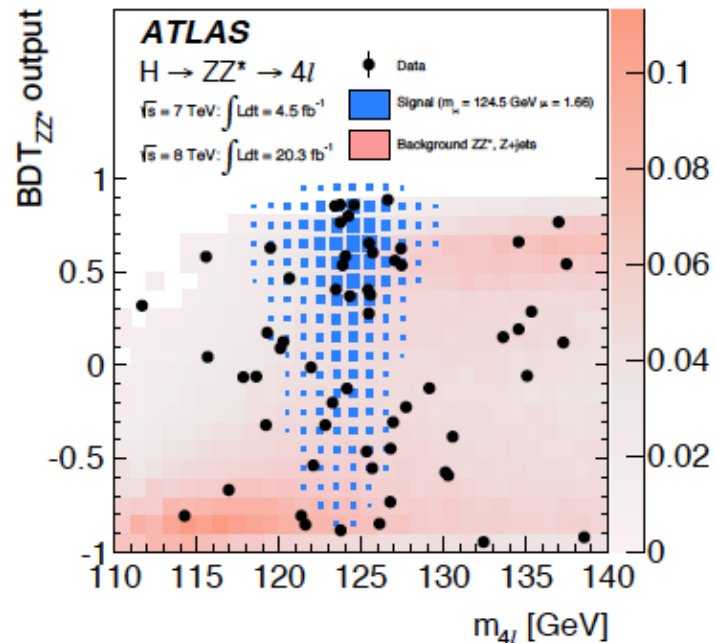
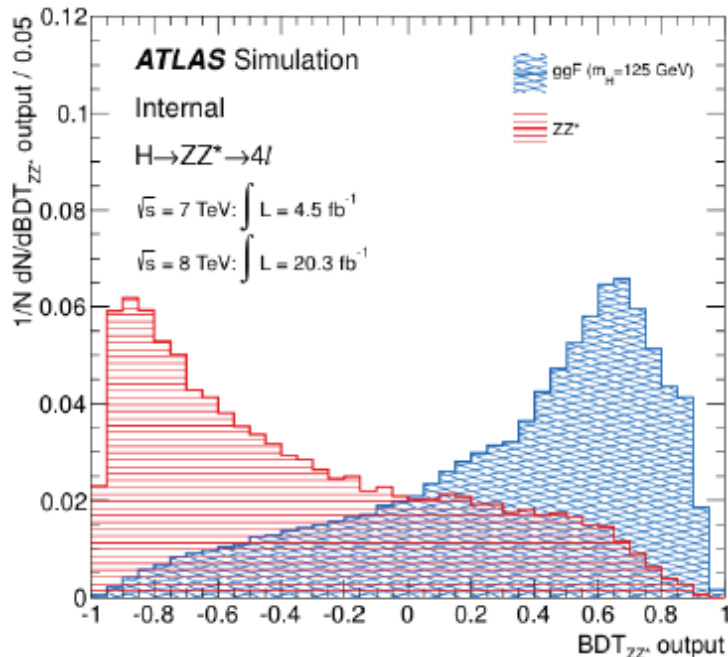
Signal strength compatible with the SM:

$$\mu = 1.44 \text{ }^{+0.40}_{-0.33}$$

In the case of  $m$  the impact of the systematics is larger mainly due to the theory uncertainties on the signal cross section

# Improving the mass fit

- The fit of the mass peak that we just saw, is model-independent, i.e. does not make assumptions on the spin/parity quantum numbers of the resonance
  - The fit can be improved by assuming SM hypothesis  $J^P=0^+$  for the decaying resonance
  - This hypothesis has been verified on data (see in the following)
- While, the ZZ background has a different composition of Z's polarization states (total J not forced to be 0)
  - This feature can be used to build a discriminant variable between the signal and the irreducible background, and include it as additional dimension in the fit





Section 5

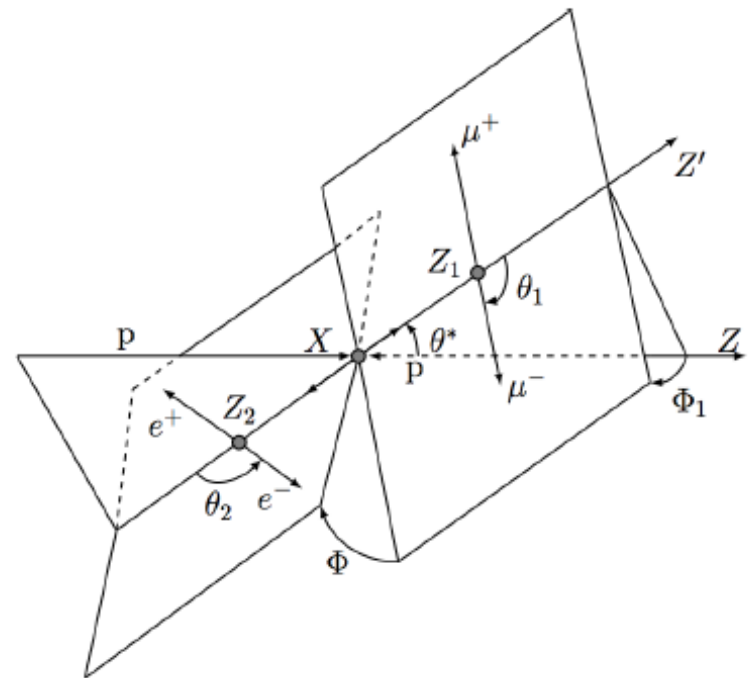
# MULTI-VARIATE ANALYSES

# Multivariate Analyses

- It is not always possible to place a cut on a discriminating variable
  - The level of discrimination doesn't always allow to remove the background keeping a high efficiency
- In some cases, the discrimination is just in tiny shape differences, or even in the correlation among various variables
  - More sophisticated methods have to be applied
  - Multi-Variate Analyses are very powerful in this cases
  - We'll see here just an example (the Boosted Decision Tree) of many different methods available

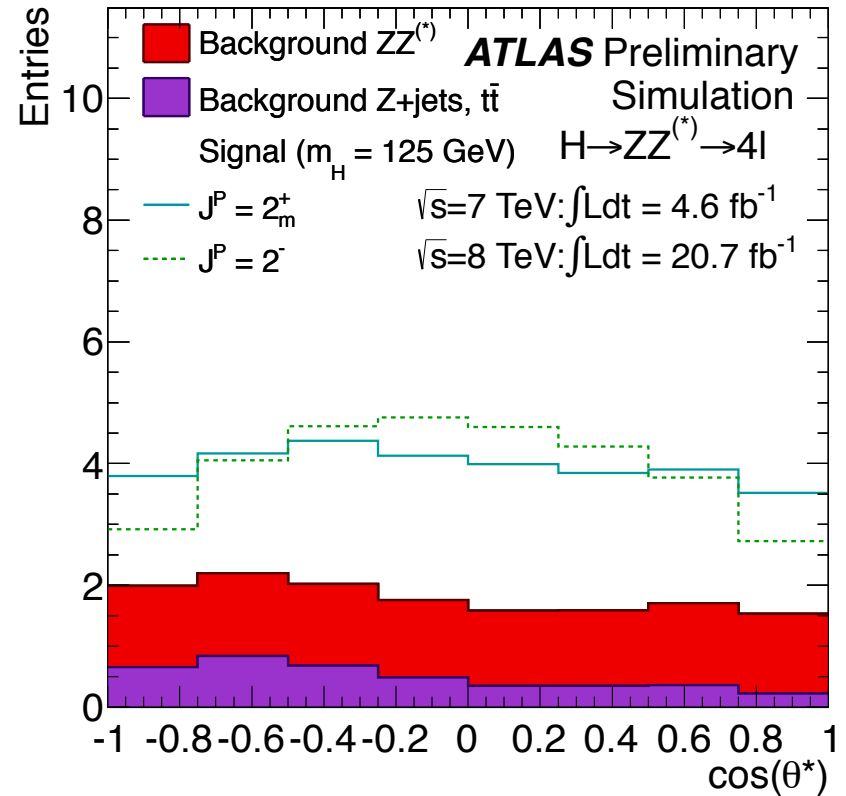
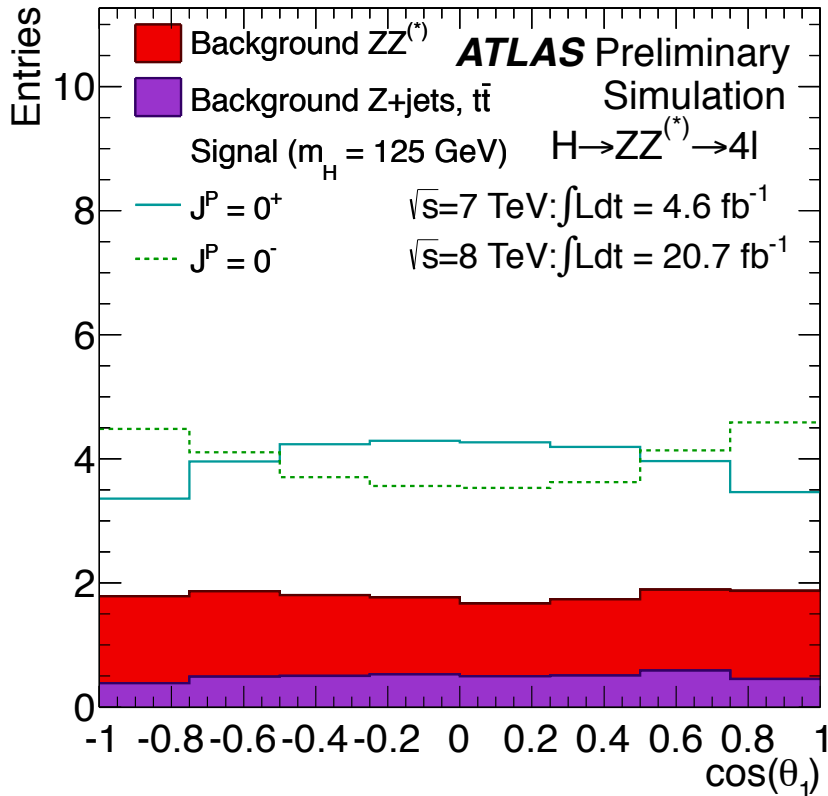
# Measurement the spin and parity quantum numbers

- The  $H \rightarrow ZZ^* \rightarrow 4l$  channel allows the full reconstruction of the final state
  - It's one of the most important channels for the measurement of the resonance properties
- Spin and parity of the decaying resonance affect the polarization of the two  $Z$ 's in the final state
  - Angular distributions can be used to test spin and parity quantum numbers of the decaying resonance



# Example of sensitive variables

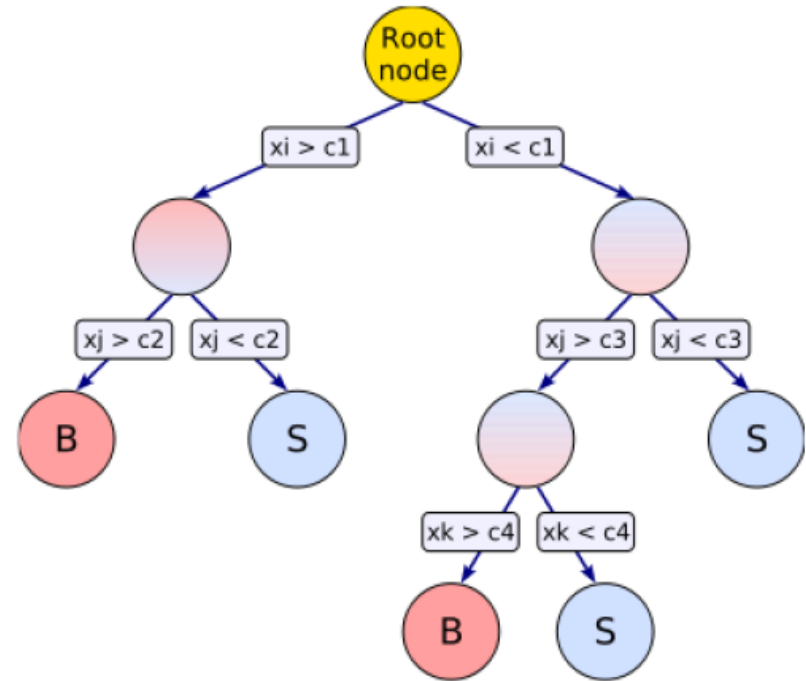
## Decay angle of the first $l^+l^-$ pair



- The variables are discriminant, but not enough to be able to just place a cut.
  - Any cut would not remove much more background than signal
- Need a so-called multi-variate analysis (MVA)

# Building a Boosted Decision Tree (BDT)

- A BDT is a sequence of binary cuts on one of the selection variables
- At each step, the variable providing the best S / B separation, and the optimal cut is chosen
- At each S/B split the procedure is repeated for each of the two subsets obtained
- The procedure stops when the subsets become so small, that the statistical fluctuations are larger than any improvement in separation
- The nodes of the final level (“leaves”) are classified as S or B according to the class the majority of the events belongs to.



# Examples of MVA: BDT

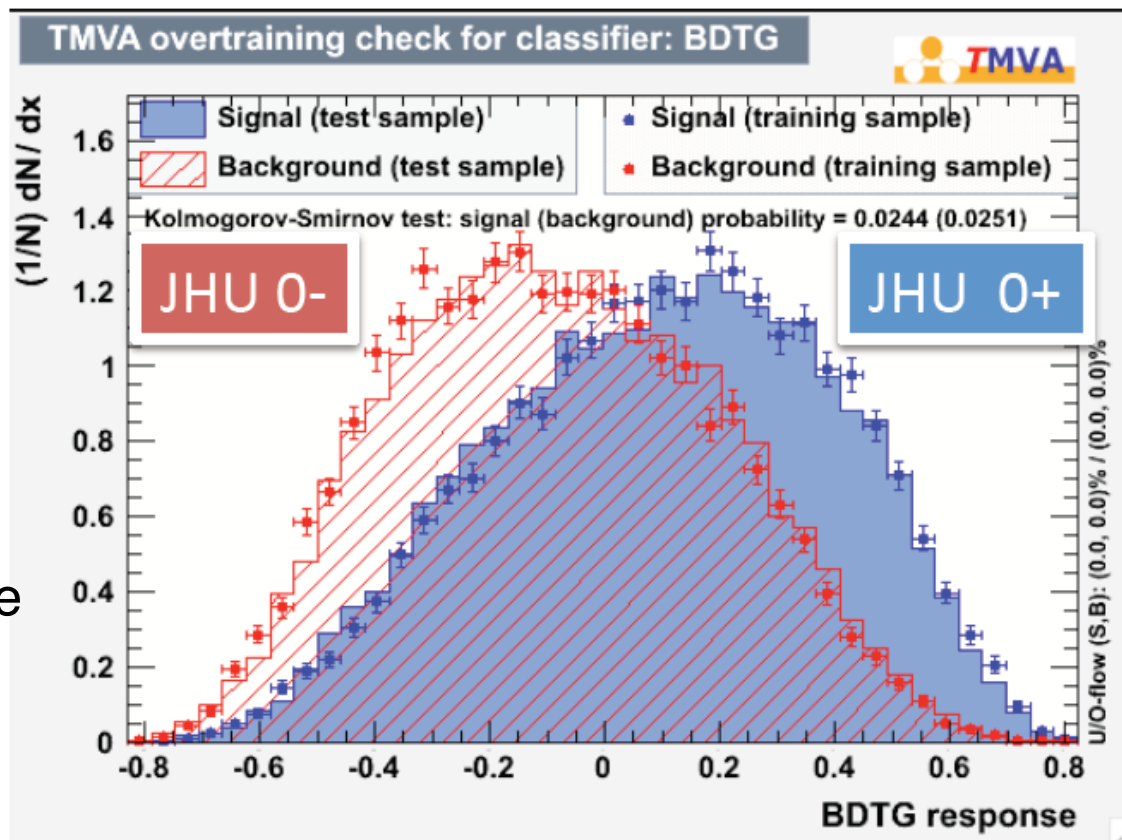
- Boost: optimize the sensitivity
- Use multiple trees:
  - Each can be trained with the same dataset, but reweighted in order to optimize the sensitivity
- An example (Adaptive Boost)
  - Train the first tree with the original weights (e.g. with the cross sections)
  - The subsequent tree is trained reweighting the previously misclassified events with a weight  $\alpha=(1-\text{err})/\text{err}$ , where **err** is the mis-classification rate
- The number of trees and their depth, must be chosen according to the available MC training statistics

# More on MVA analyses

- The “training” of the method is usually performed on MC events
- To correctly evaluate the separation, divide the sample in two sub-sets: **training and test samples**
- This is also done in order to avoid the over-training
  - The MVA might “learn” the fluctuations of your training sample

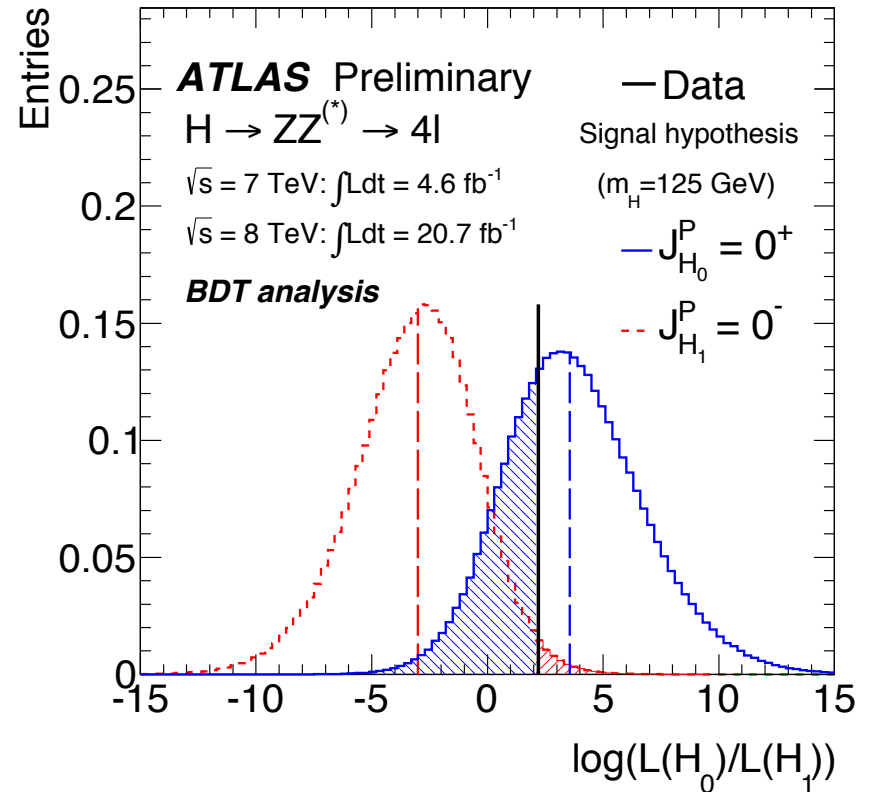
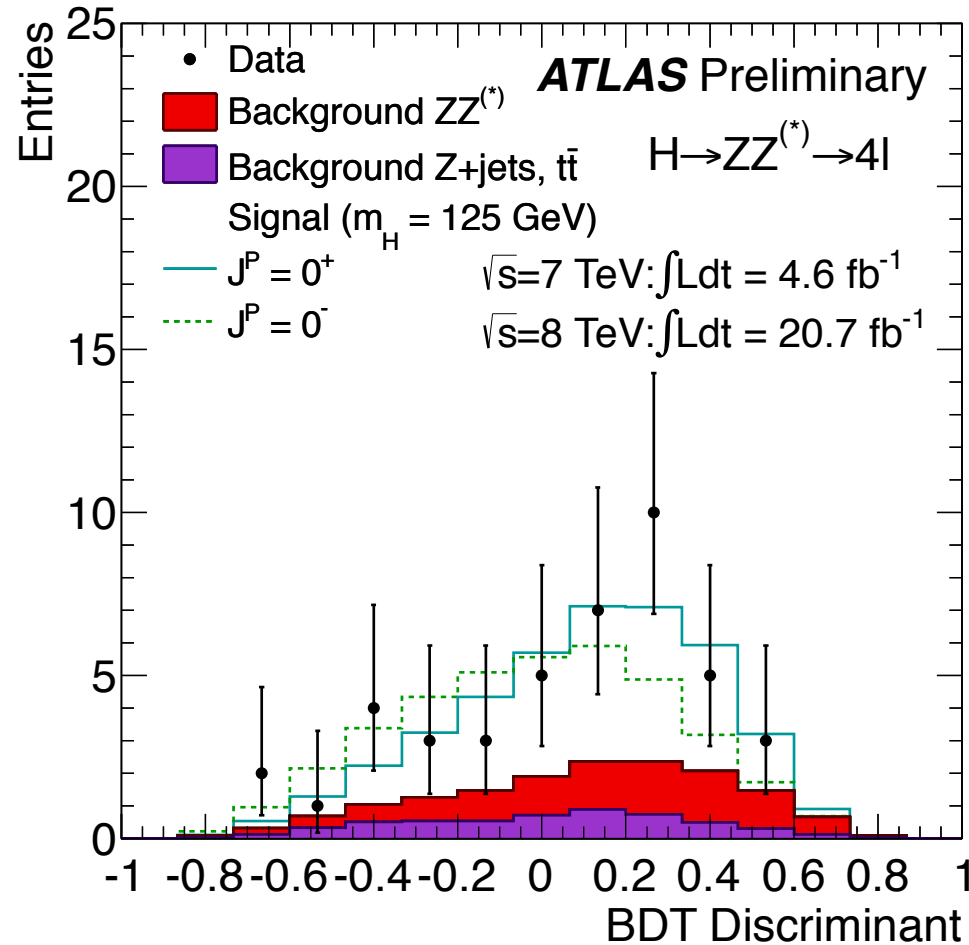
This is an example of a light overtraining  
→ the separation between the training samples is slightly better than for the test samples

In this case one should increase the MC stat, or decrease the number of trees



# Discriminant distribution and hypothesis test

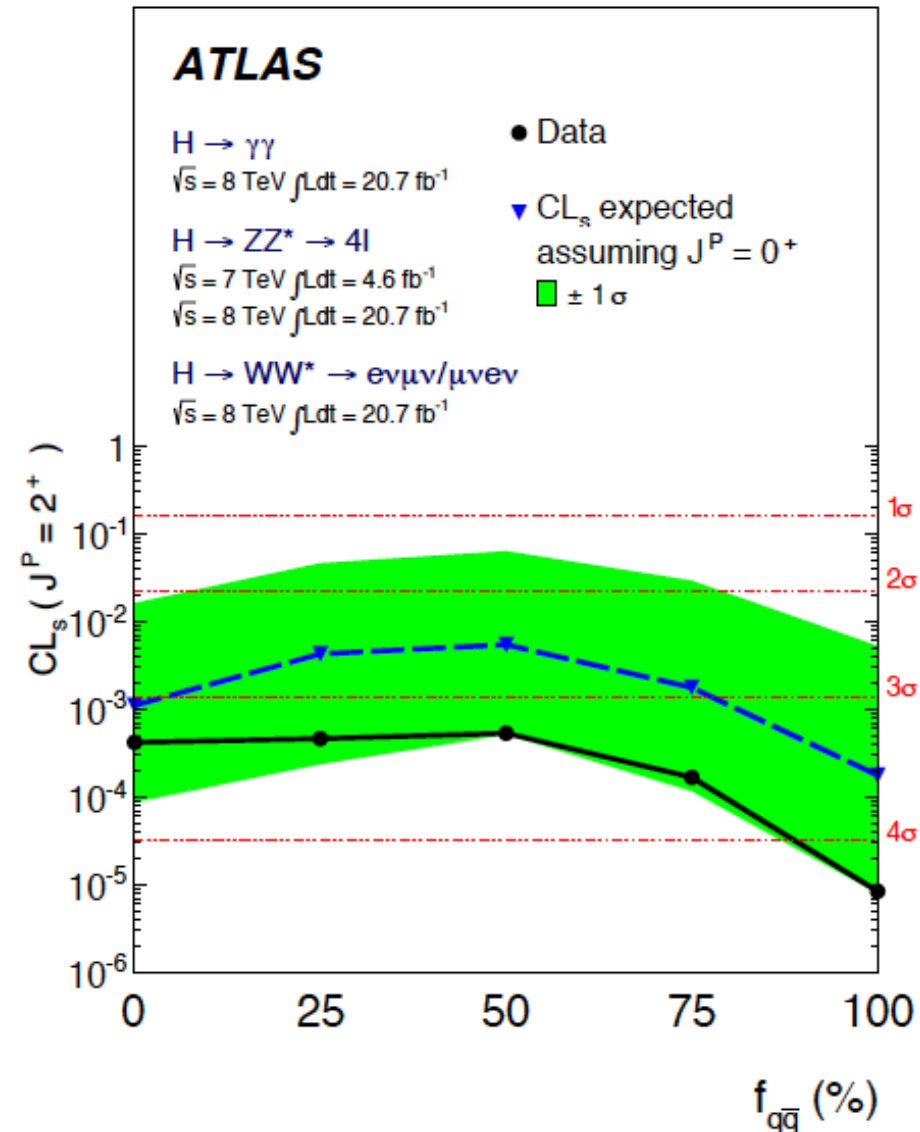
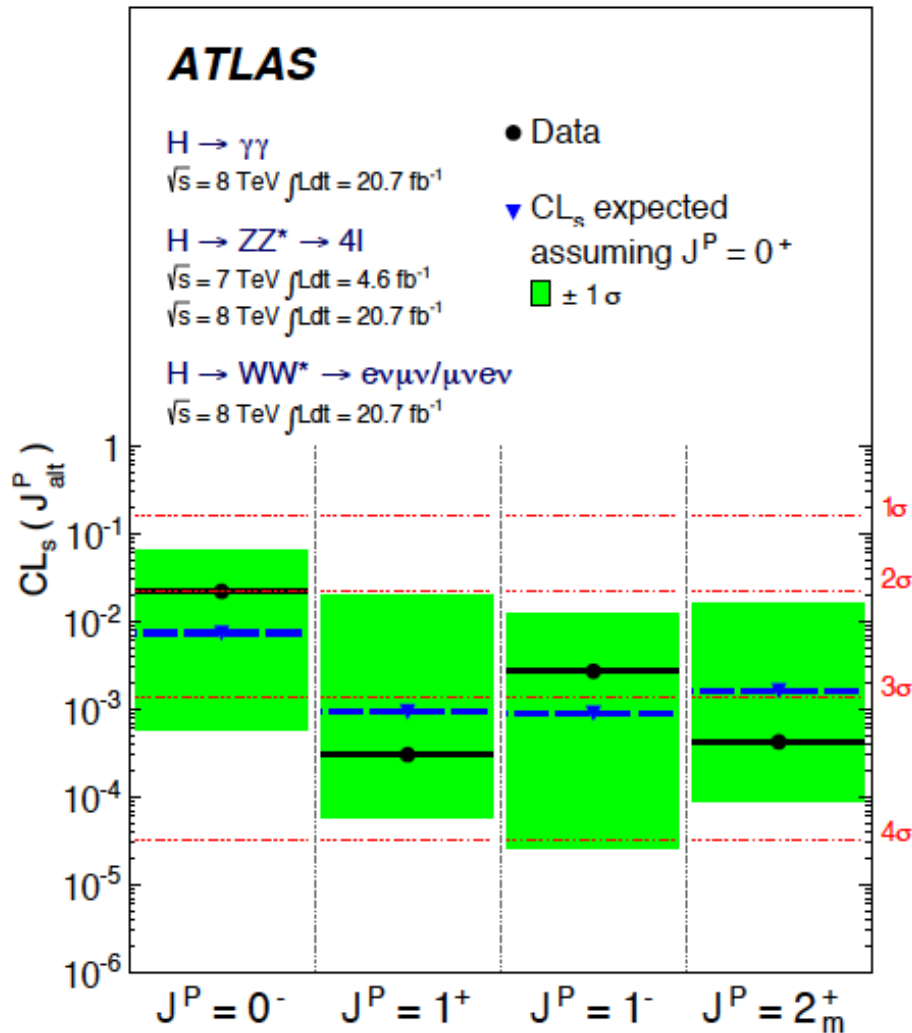
- Log-likelihood ratio as test statistics
- Generate pseudo-experiments assuming each of the two hypotheses
- Median of  $0^+ \rightarrow$  SM expected  $p_0$
- Data value  $\rightarrow$  Observed  $p_0$





# Final results on spin and parity

$$CL_s = \frac{p_0(J_{alt}^P)}{1 - p_0(J^P = 0^+)}$$



# CONCLUSIONS

# Conclusions

- This was an attempt to consider one real example of an analysis and follow all the aspects of its development
  - Initial thoughts
  - Designing the analysis
  - Applying it to the data → the discovery
  - Measurements of the new resonance properties
- Due to lack of time, I couldn't give you many details, and a real summary of the results, but in case you would like to discuss more please do not hesitate to contact me:
  - Mail: [stefano.rosati@cern.ch](mailto:stefano.rosati@cern.ch)
  - Office: **Building Marconi, 2<sup>nd</sup> floor, 229-b**
- And in general if you are interested in having a thesis with the ATLAS group, many topics available both on data analysis and detector development