After a brief overview of the MSSM and its Higgs sector, we discuss the role of indirect constraints from flavour physics and other observables (dark matter and electroweak precision tests). The results of a recent global fit in a constrained version of the MSSM (the mSUGRA scenario) are also presented: within this minimal framework indirect constraints can easily be satisfied, and the lightest Higgs boson mass is predicted to be just above the LEP exclusion bound.