Exercises on exact transformations

The general formula has been shown for two input variables that go to two output variables. Obvious it is very general. In particular it holds for one variable to one variable, thus becoming

$$f(y) = \int \delta(y - Y(x)) f(x) \, \mathrm{d}x \, .$$

Imagine X uniform in the range [0, 1],

1. apply the formula for the following transformations $1.1 \ Y = \sqrt{X};$ $1.2 \ Y = X^2,$

getting thus f(y) and also F(y).

- 2. For the each tranformed distribution:
 - 2.1 evaluate analitically expected value and standard deviation;
 - 2.2 write the code to generate random numbers, using the method of the inversion of the cumulative distribution;
 - 2.3 'check' the result by Monte Carlo extracting a sample of X and applying to it the above functions.

(This point is different from the the previous one, and

it is the easiest to accomplish.)