

Challenges and opportunities in non-equilibrium soft matter

September 24, 2023 - September 27, 2023

Registration deadline: September 1, 2023

Location: Mont Sant Benet, Spain

Multinodal event: CECAM-UK-JCMAXWELL, CECAM-FR-MOSER, CECAM-FR-RA, CECAM-FR-GSO, CECAM-DE-JUELICH, CECAM-DE-MMS, CECAM-DE-SMSM, CECAM-IT-SISSA-SNS, CECAM-IT-SIMUL, CECAM-NL, CECAM-UK-DARESBUY, CECAM-AT

Daanentropy:
A disease spreading within the Computational Soft
Matter Community



Dedicated to Daan



Daanentropy

From Wikipedia, the free encyclopedia

Not to be confused with Entropy

Daanentropy is a sickness that is most commonly associated with the interest in states of disorder, randomness, or uncertainty. It has been observed in scientists working in diverse fields, from [classical thermodynamics](#), where it was first recognized, to the microscopic description of nature in [statistical physics](#), and to the principles of [information theory](#). It has found far-ranging spreading in [chemistry](#) and [physics](#), in biological systems and their relation to life, in [cosmology](#), economics, sociology, [weather science](#), [climate change](#), and [information systems](#).

Can you explain me what Daanentropy is ?



Free Research Preview. ChatGPT may produce inaccurate information about people, places, or facts. [ChatGPT August 3 Version](#)



- I have specific information about a sickness called "Daanentropy" that affects computational scientists. It appears that it spreads among scientists working in soft condensed matter associated with the repeated reading of some selected Daan Frenkel's articles. At an early stage it generates an uncontrollable need to calculate **entropic phase diagram**. At a later stage an urge to develop **novel computational methods** appears. The late stage involves a continuous mumbling of what **entropy-driven attraction** can do. Daanentropy has been first identified in Europe, but there are now propositions to consider it a pandemic infection.

A case study of a patient (FS) affected by
Daanentropy

Let's examin the different stages

A case study of a patient (FS) affected by
Daanentropy

Early stage: calculation of entropic phase diagram

Science **334**, 965 (2011);
DOI: 10.1126/science.1212648

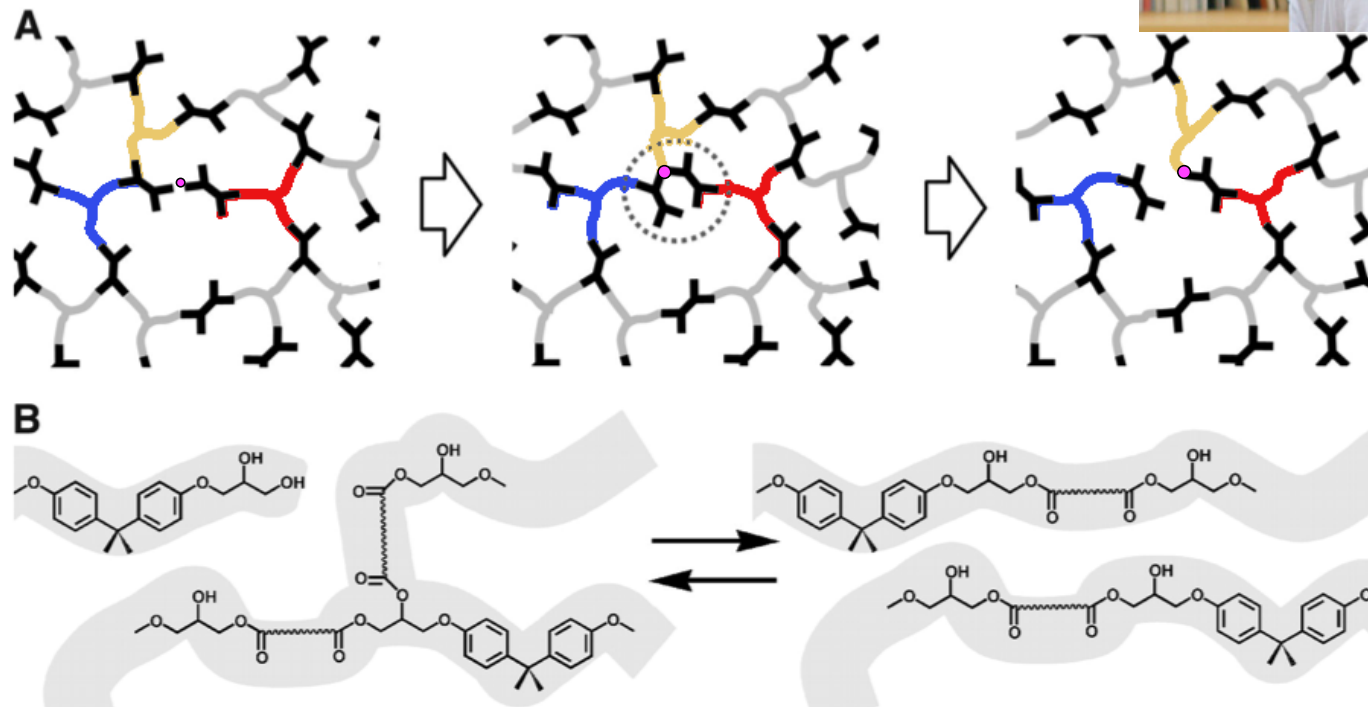
Silica-Like Malleable Materials from Permanent Organic Networks

Damien Montarnal, Mathieu Capelot, François Tournilhac, Ludwik Leibler*

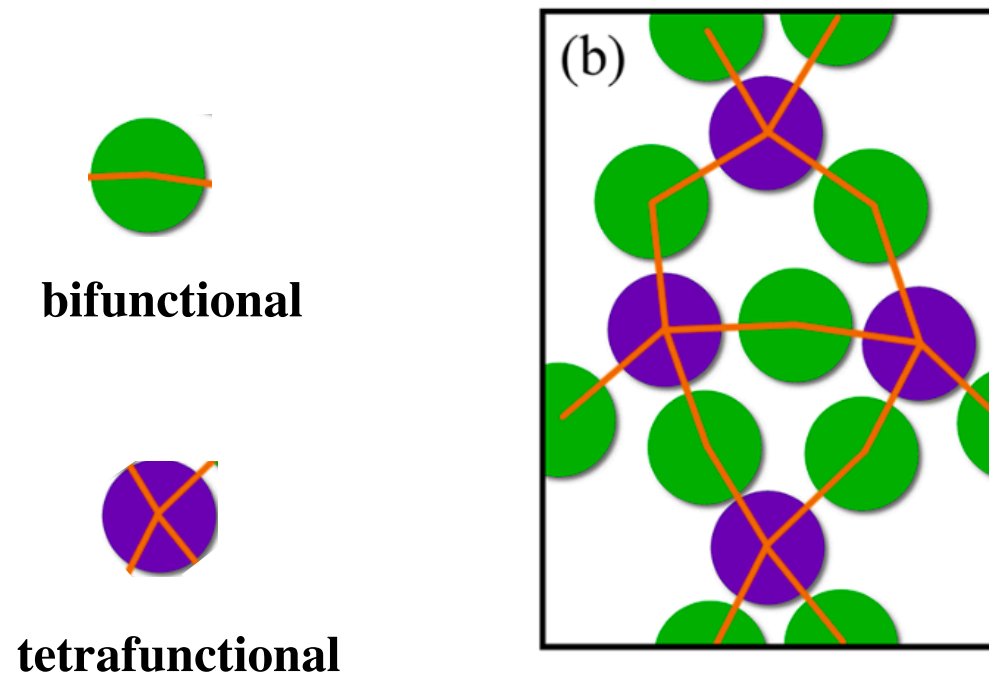


Non
stoichiometric
mixture of
4- and 3-
functional
Molecules

Always same
number of



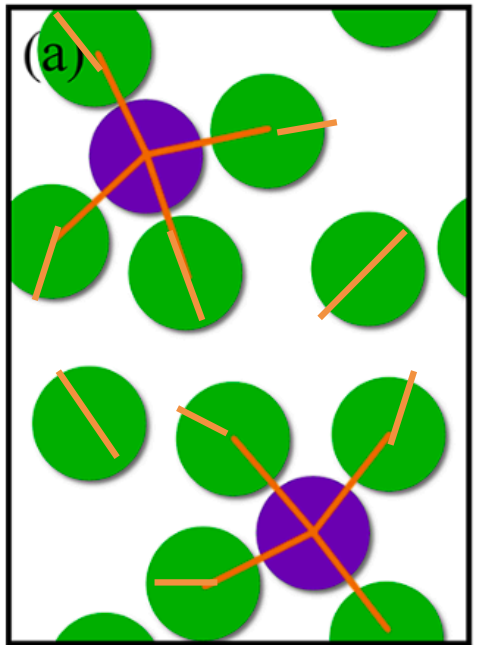
A simple (patchy particle-like) idea.



**Stoichiometric mixture of bifunctional and tetrafunctional
in the ground state ($kT \ll \epsilon$)**

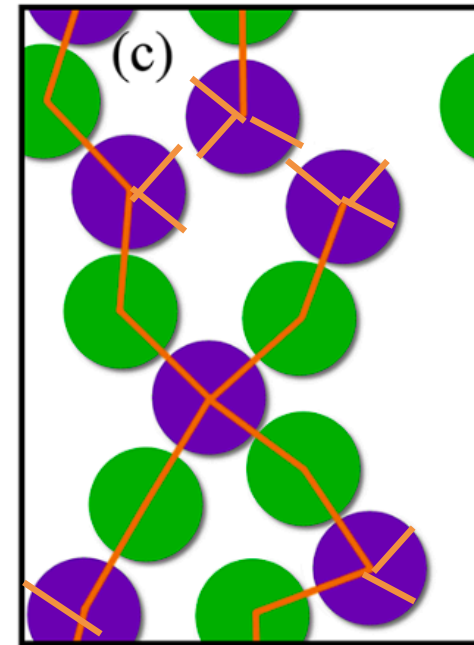
A simple idea. Non-stoichiometric binary mixtures at $T=0$ K

Excess of bivalent



All tetravalent are coordinated

Excess of tetravalent



All bivalent are coordinated

It is possible to control the number of saturated and non-saturated bonds !

Wertheim free energy

$$\beta F_{tot}/N = \beta f_{\text{bond}} + \beta f_{\text{HS}} + \beta f_{\text{mix}}$$

**Free energy change as a result of forming bonds
in the limit of T going to zero (strong bonds):**

$$f_{\text{bond}} = -\frac{T S_{\text{comb}}(4N_A, 2N_B)}{N} + \frac{n_b}{N} \left(-k_B T \log \frac{v_b(\rho)}{V} - \epsilon \right)$$

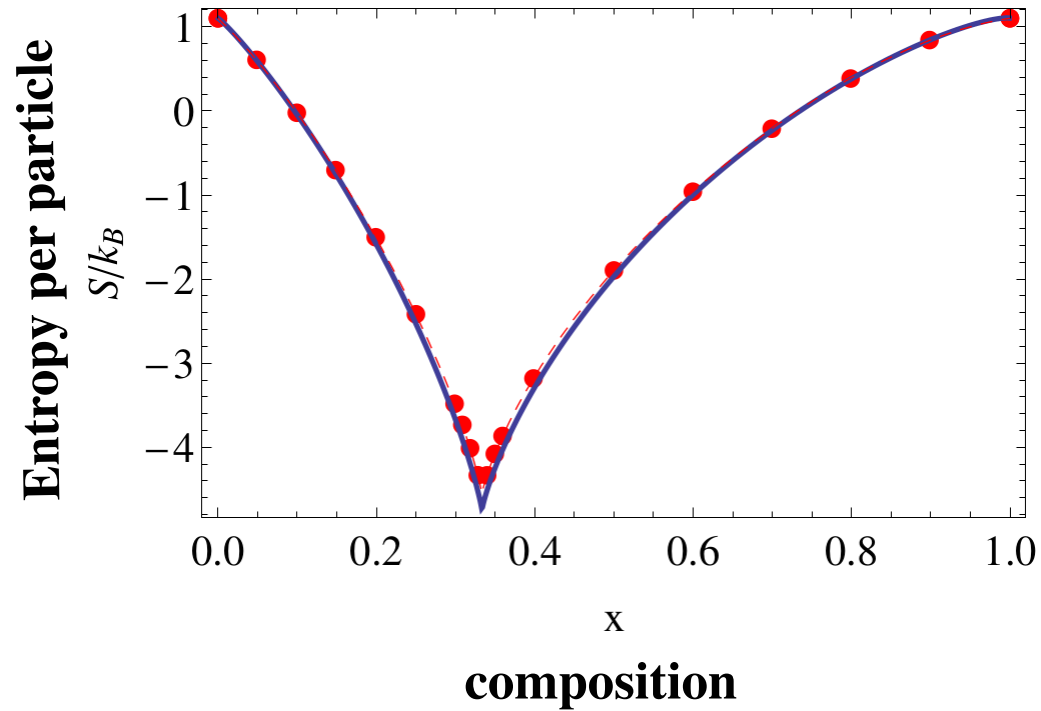
Combinatorial entropy term:

$$S_{\text{comb}}(n, m) = \begin{cases} k_B \log \frac{n!}{(n-m)!} & \text{if } n > m \\ k_B \log \frac{m!}{(m-n)!} & \text{otherwise} \end{cases}$$

Testing the theory

Comparison between the entropy from **simulations (red)** and **theory (blue)**.

Number density $\rho\sigma^3 = 0.35$

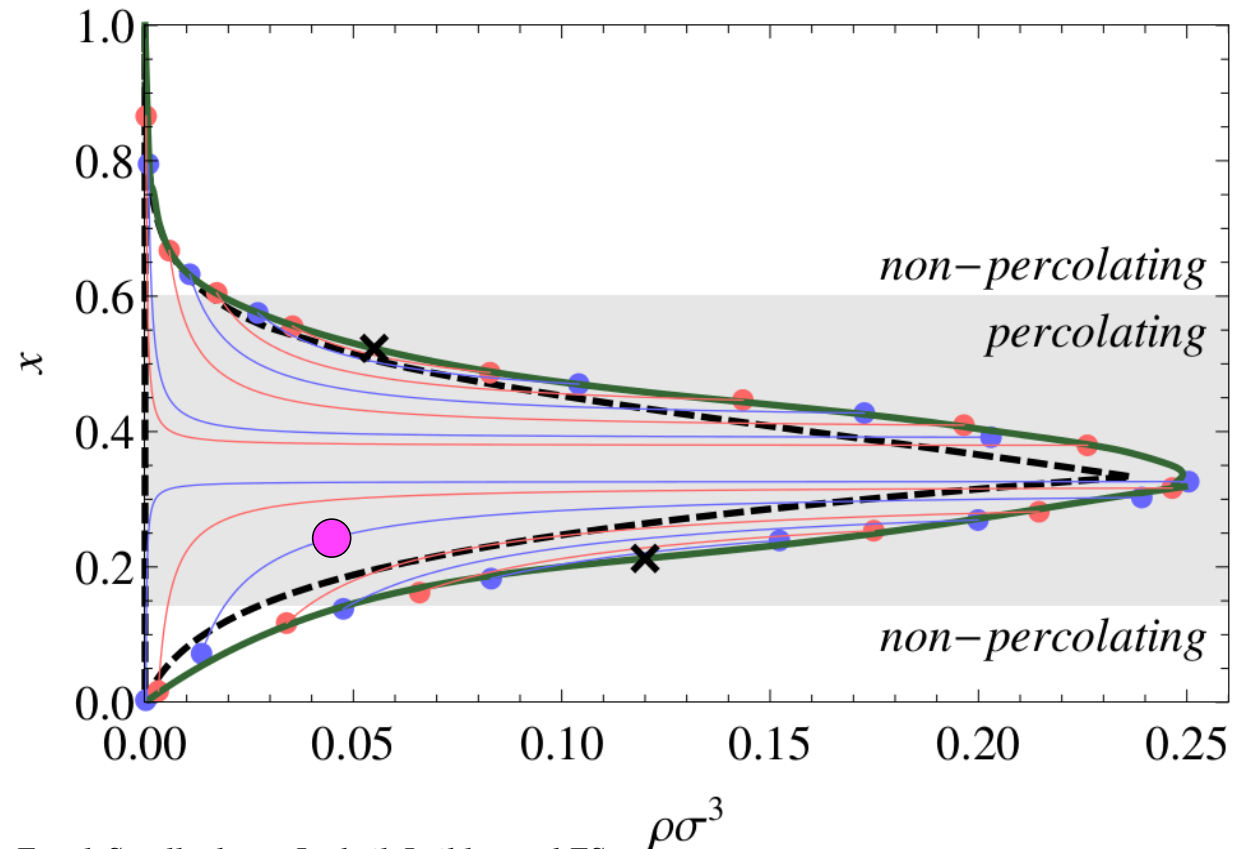


T=0 K Equilibrium phase diagram (Entropy Only!)

Placing a
vitrimers
network in a
good solvent
leads to swelling

The network
phase is closer to
the ideal x

the network
never fully
dissolves



Frank Smallenburg, Ludwik Leibler and FS
Patchy Particle Model for Vitrimers
Phys. Rev. Lett. 111, 188002 (2013)

$\rho\sigma^3$

Simulation: black dashed line
Theory: points, solid line

Merging two distinct pieces....



Early stage: calculation of entropic phase diagram

Another example of the early stage.....

If (a limited valence [patchy**]) liquid reaches a fully bonded state, then it has the same energy of the fully bonded crystal !**

(effectively an a-thermal system !)

Entropy decides the most stable phase (exactly as in HS!)

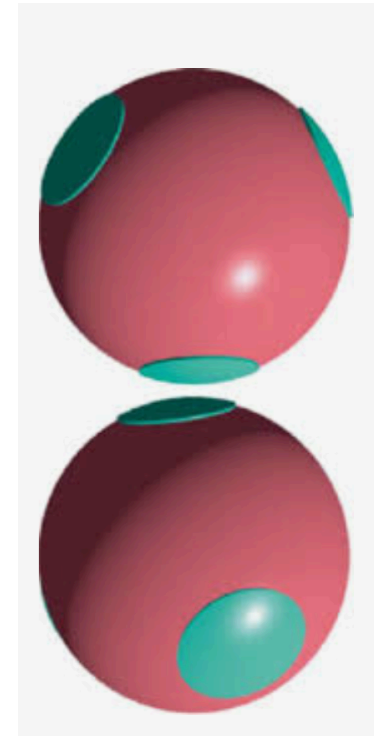
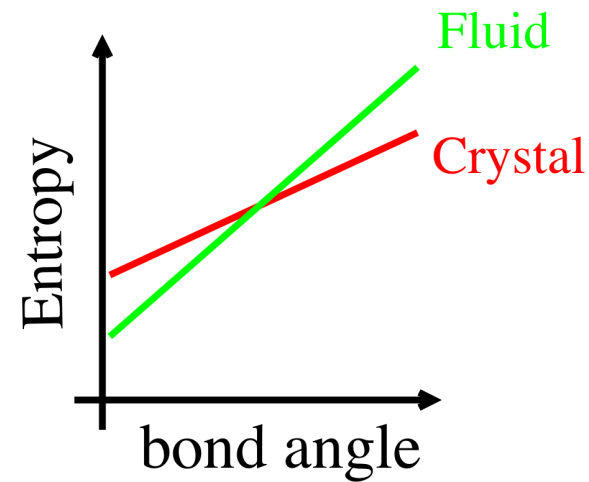
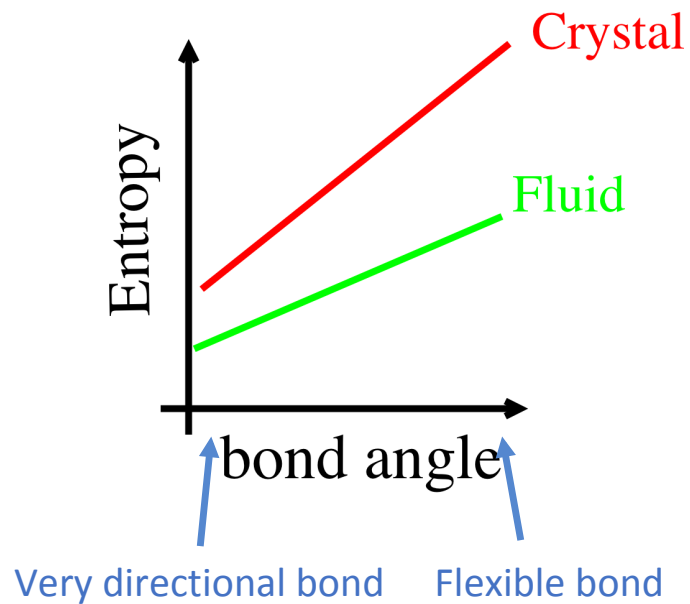
Competition between:

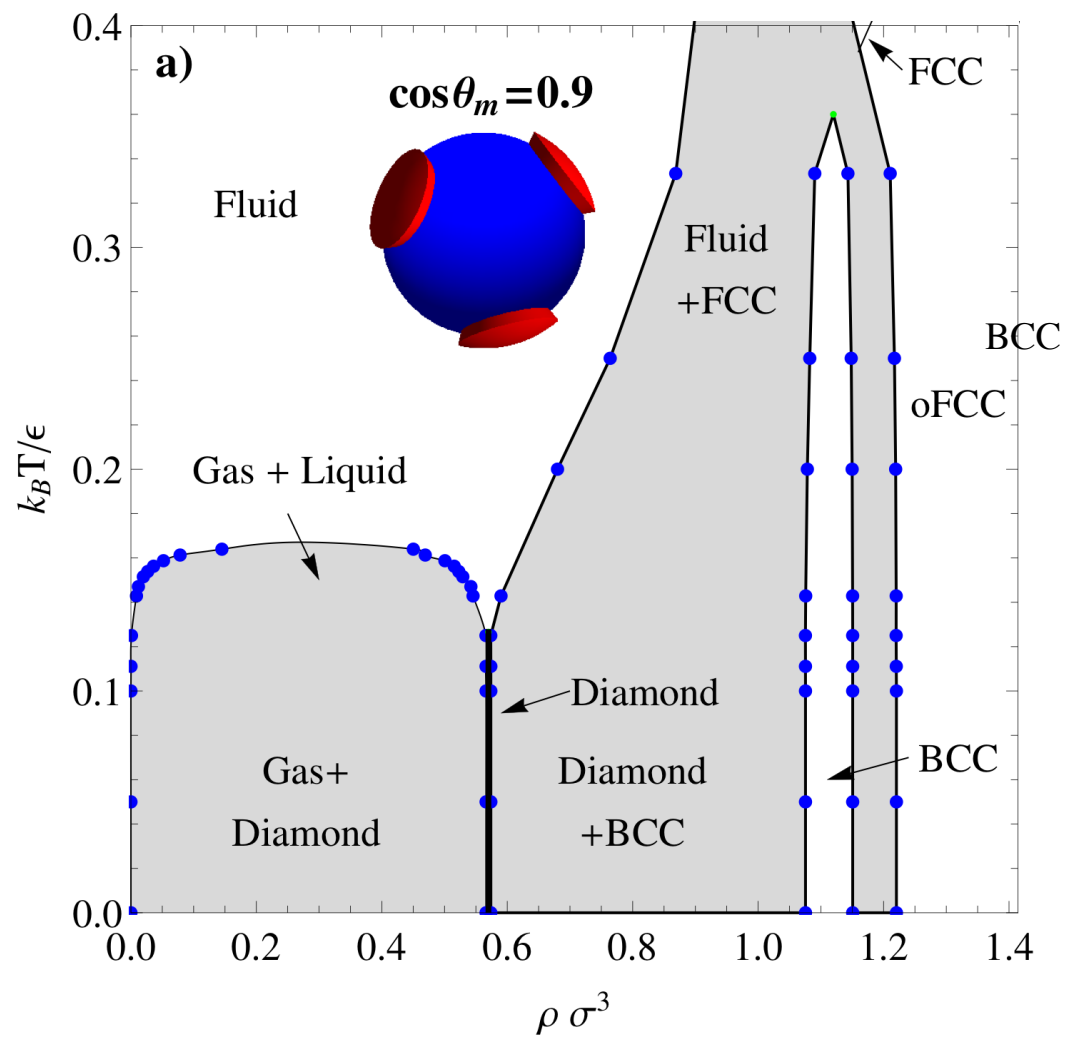
- **Number of microstates accessed at
“fixed bonding” (vibrational entropy)
(both crystal and fully bonded liquid)**
- **Number of different bonding
topologies (configurational entropy)
(only fully bonded liquid)**

Like in HS, the crystal (diamond for tetrahedral particles) is stable because

$$S_{\text{vib crystal}} > (S_{\text{vib}} + S_{\text{conf}})_{\text{liquid}}$$

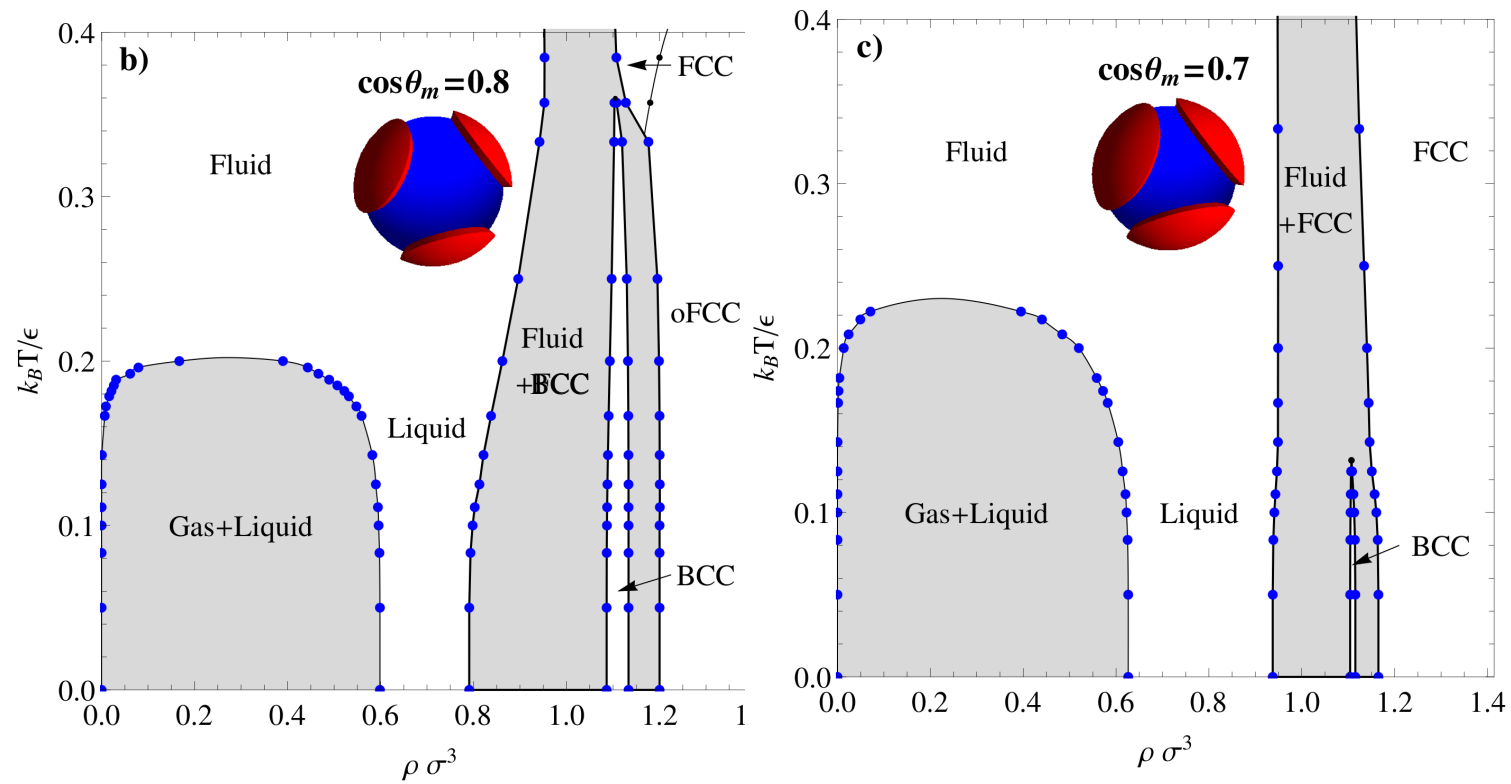
What happen when the angular width of the patch increases (but single bond per patch) ?



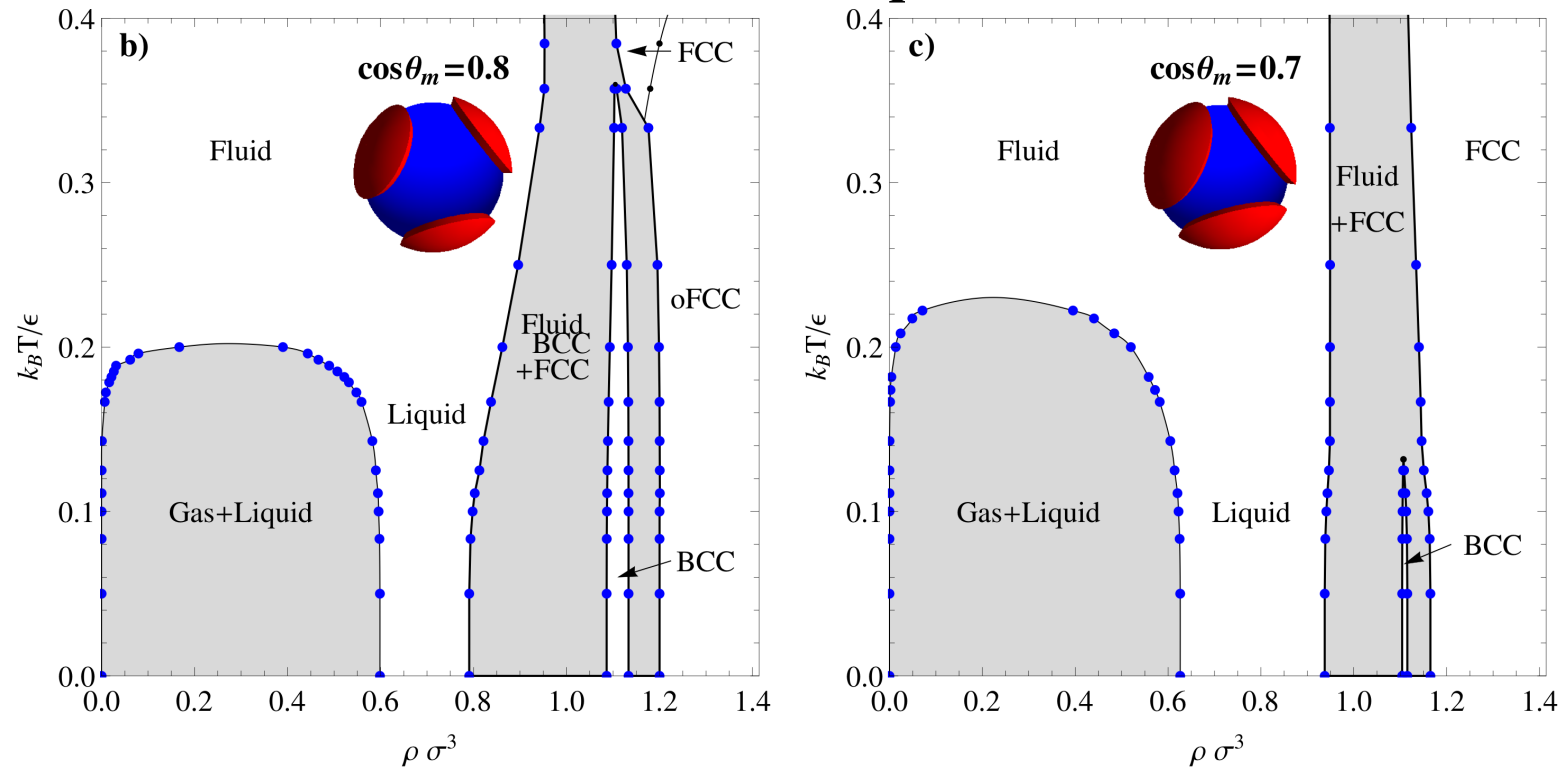


Liquids more stable than crystals in particles with limited valence and flexible bonds

Frank Smallenburg* and Francesco Sciortino



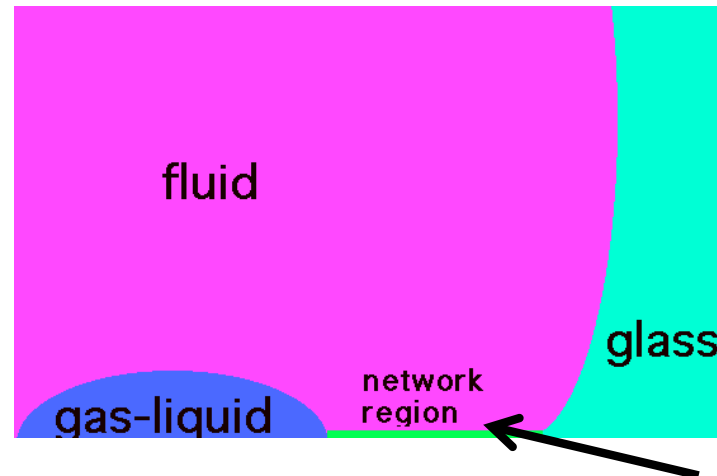
Ultrastable liquids !



Also 3 patches

Martinez-Veracoechea, F. J., Mladek, B. M., Tkachenko, A. V. & Frenkel, D. Design rule for colloidal crystals of dna-functionalized particles. *Phys. Rev. Lett.* 107, 045902 (2011).

Key elements for liquid stability at $T=0$ K: (ultrastable liquids !)



Thermodynamically stable !

- * **Patchiness - Low valence.** Small density of the coexisting liquid phase
- * **Large flexibility of the angular interactions:** (wide variety of networks, increasing S_{conf})

Intermediate stage in Daanentropy:

(urge to develop smart equilibration methods)

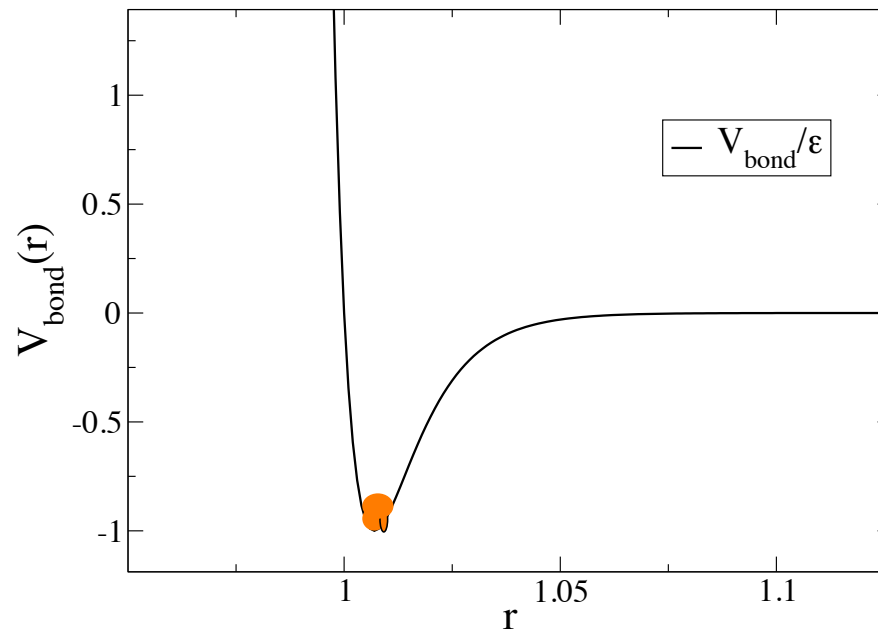
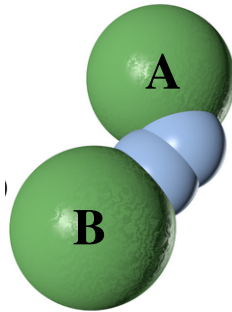
How to equilibrate networks at low temperature

Swapping instead of breaking

See Bortolo Moggetti work for MC methods

Molecular Dynamics of Swap Events

Short-range with clear minimum and cut-off

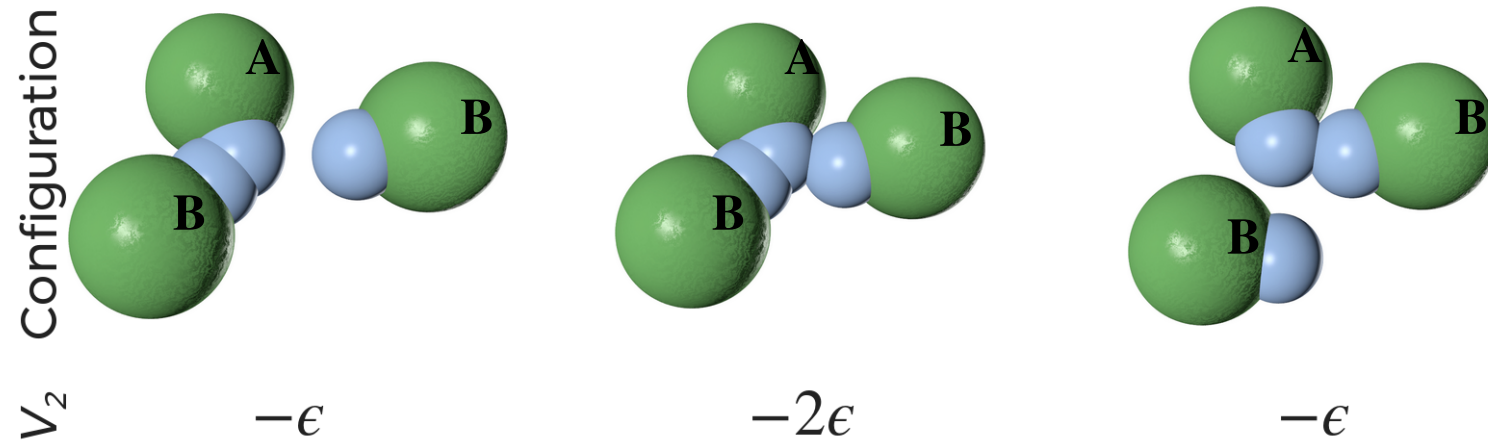


Three-body potential for simulating bond swaps
in molecular dynamics

Eur. Phys. J. E (2017) 40: 3

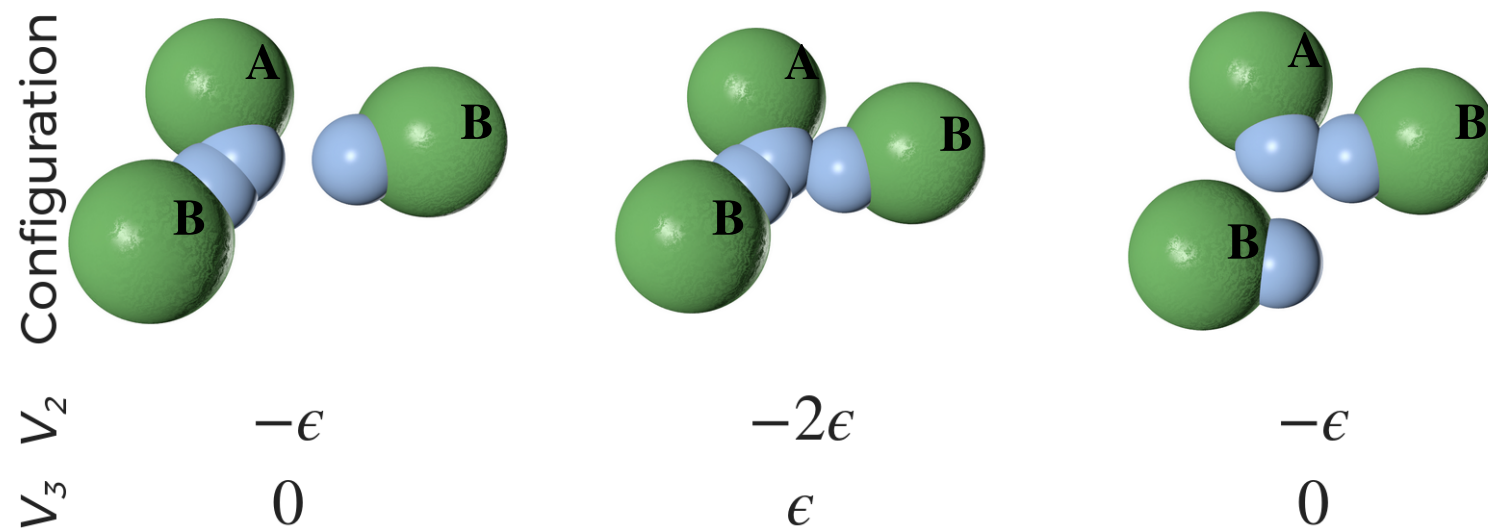
$$kT < \epsilon$$

Molecular Dynamics of Swap Events



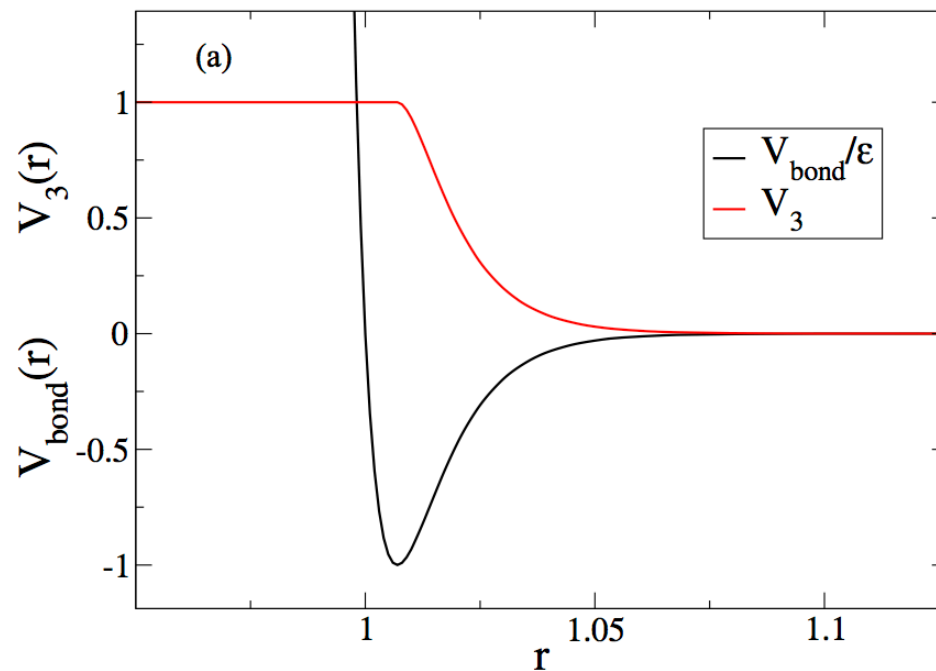
We need a flat energy surface for swap

Molecular Dynamics of Swap Events



We need a flat energy surface for swap

Molecular Dynamics of Swap Events



$$V_3(r) = \begin{cases} 1, & r \leq r_{\min}, \\ \frac{-V_{\text{bond}}(r)}{\epsilon}, & r_{\min} \leq r \leq r_{\text{cutoff}} \end{cases}$$

$$V_{\text{threebody}} = \lambda \sum_{ijk} \epsilon V_3(r_{ij}) V_3(r_{ik}) \quad (\text{always positive})$$

The late stage: Entropy Attracts !

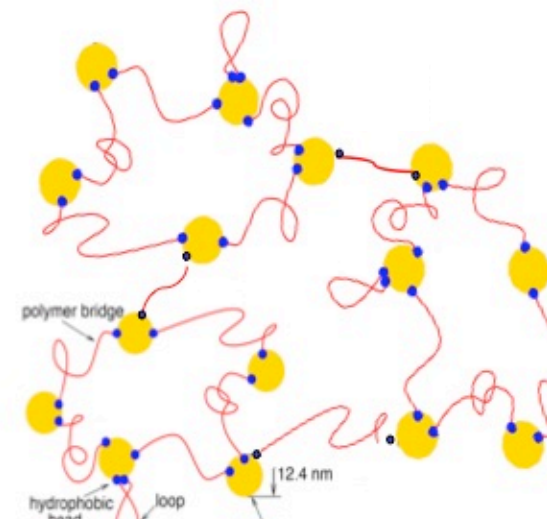
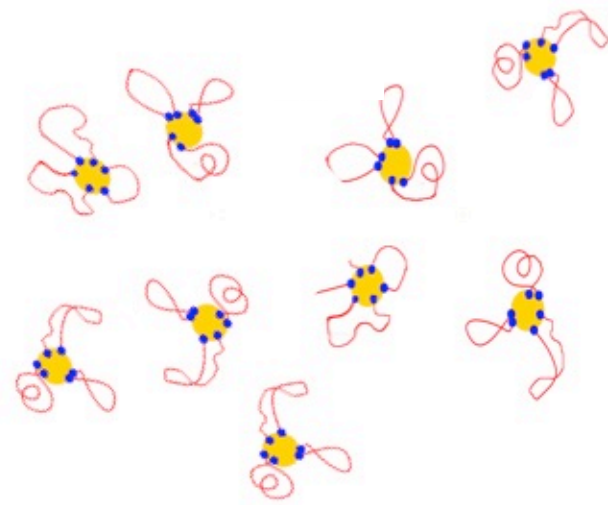
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Useful for students:

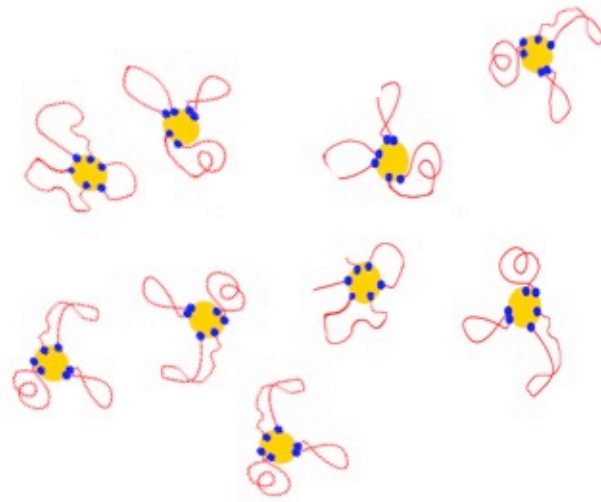
Francesco Sciortino

[Entropy in self assembly](#)

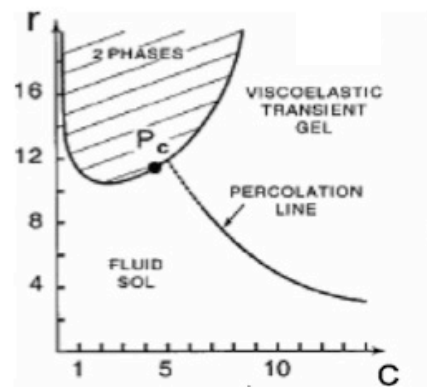
Riv. Nuovo Cimento, Vol. 42 (2019) 511, DOI: 10.1393/ncr/i2019-10165-1



Another important source of entropy: Combinatorial Entropy



(Exp)

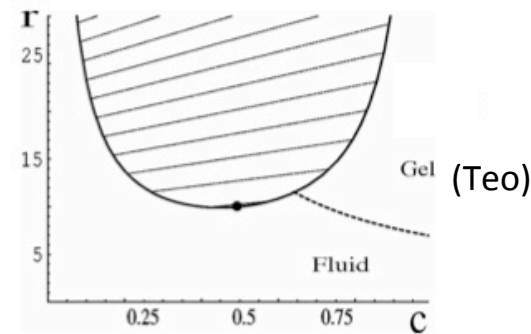
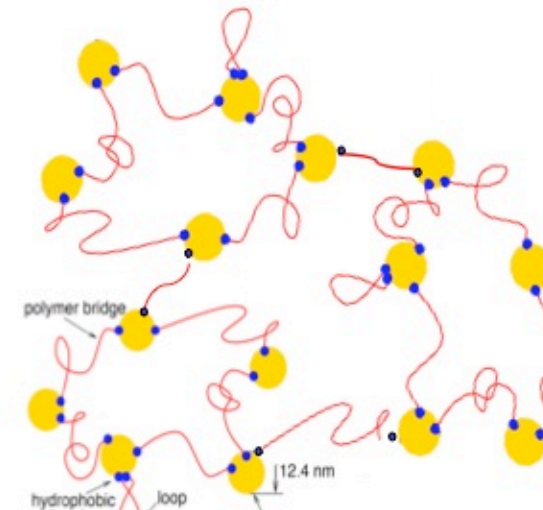


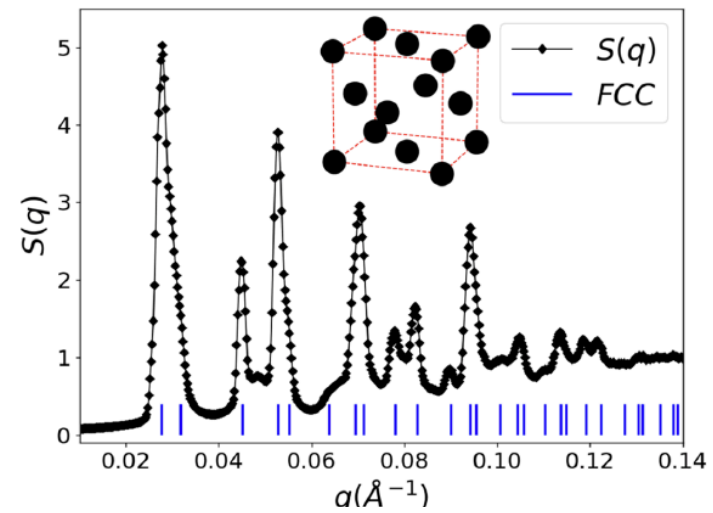
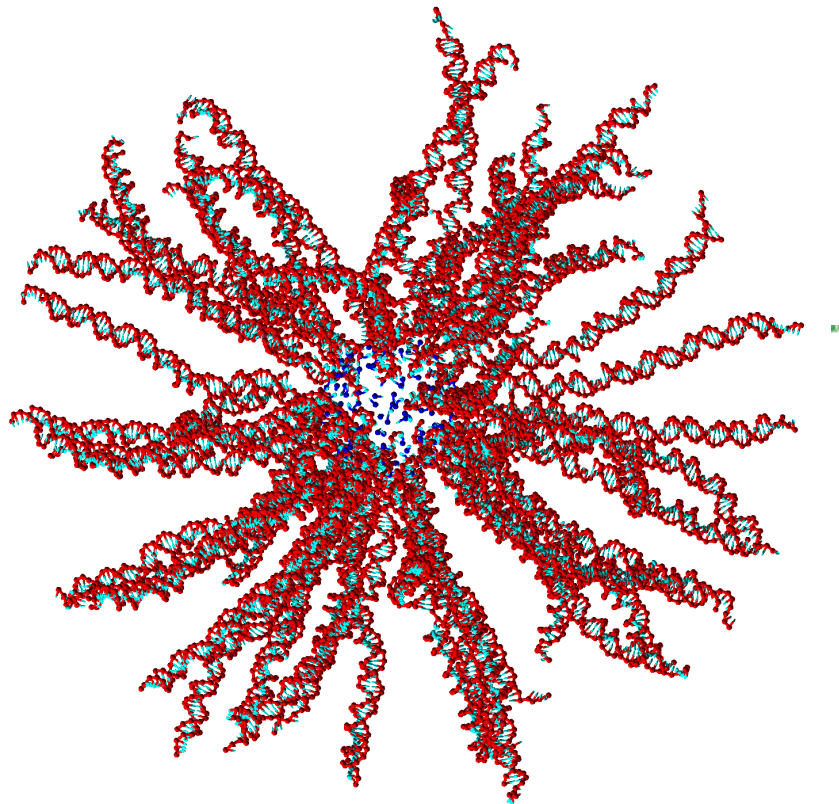
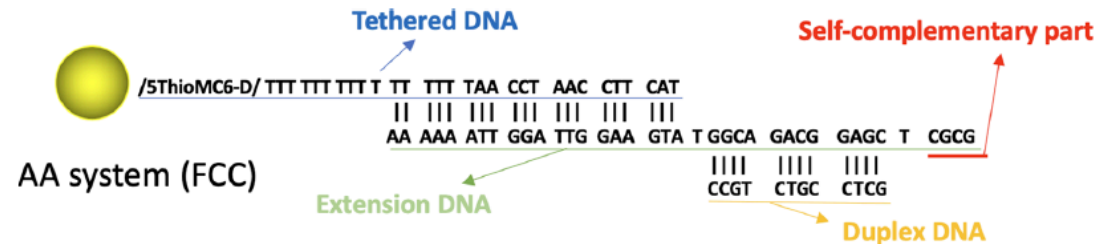
Entropic Phase Separation in Polymer-Microemulsion Networks

A. Zilman,¹ J. Kieffer,² F. Molino,² G. Porte,² and S. A. Safran¹

¹Department of Materials and Interfaces, Weizmann Institute of Science, 76100 Rehovot, Israel

²Groupe de Dynamique des Phases Condensées, Université de Montpellier II, 34095 Montpellier Cedex 05, France
(Received 27 January 2003; published 3 July 2003)





Oleg Gang (Brookhaven and Columbia)

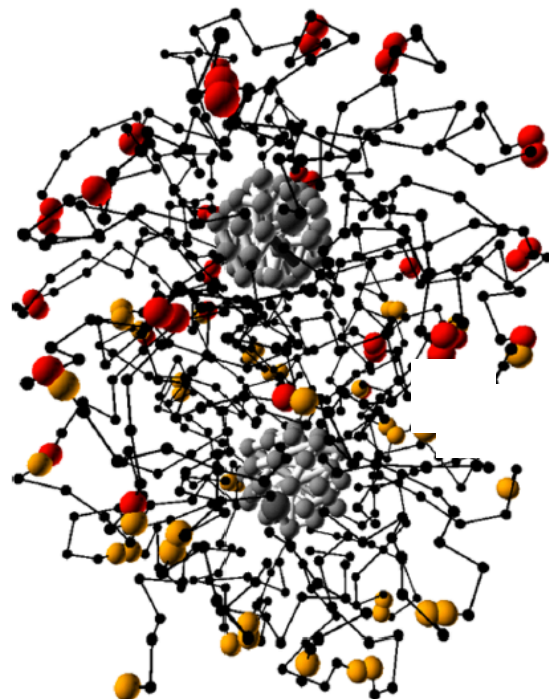


Combinatorial-Entropy-Driven Aggregation in DNA-Grafted Nanoparticles

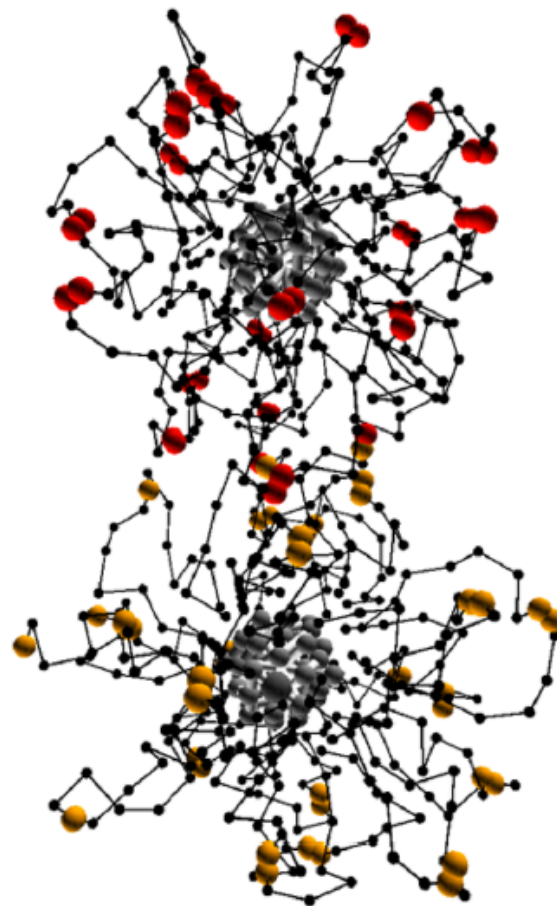
Francesco Sciortino,^{*} Yugang Zhang, Oleg Gang, and Sanat K. Kumar

Cite This: *ACS Nano* 2020, 14, 5628–5635

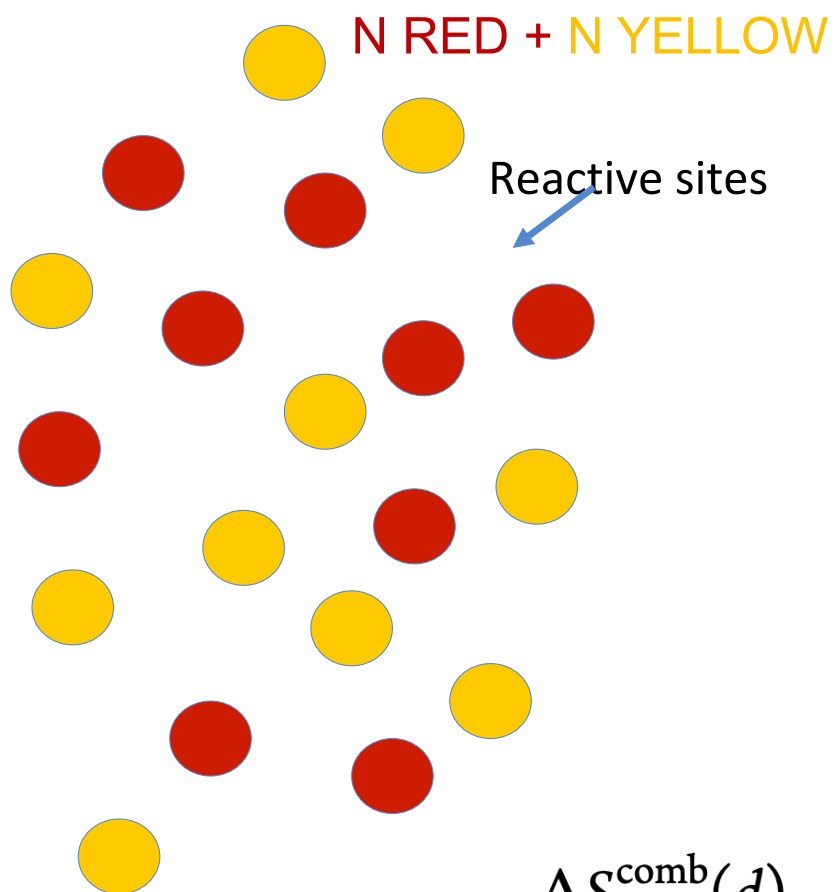
Read Online



A coarse-grained version of the DNA-decorated gold nanoparticle



Can we quantify the entropic gain ?



$$\Omega = (N - 1)!!$$

$$\Omega = (N - 1)!!$$

$$\Omega = (2N - 1)!!$$

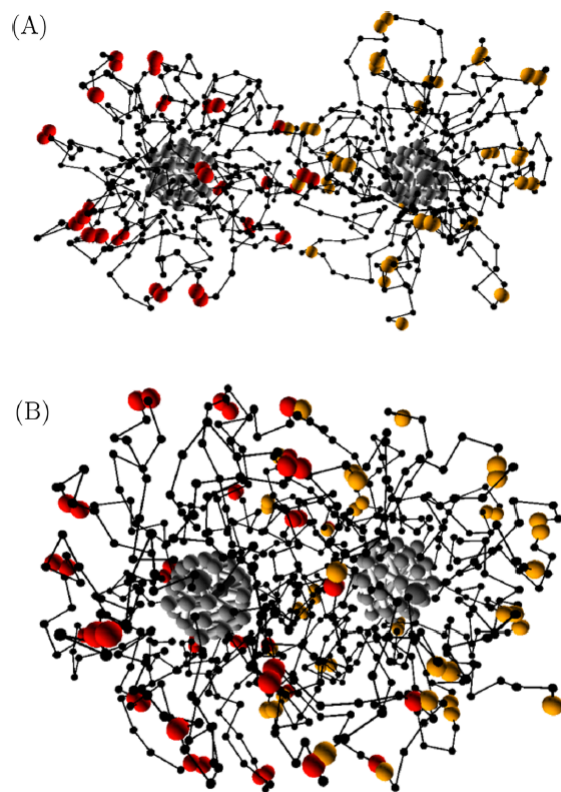
$$\frac{\Delta S^{\text{comb}}(d)}{k_B} = \ln \left[\frac{(2N(d) - 1)!!}{[(N(d) - 1)!!]^2} \right]$$

Combinatorial-Entropy-Driven Aggregation in DNA-Grafted Nanoparticles

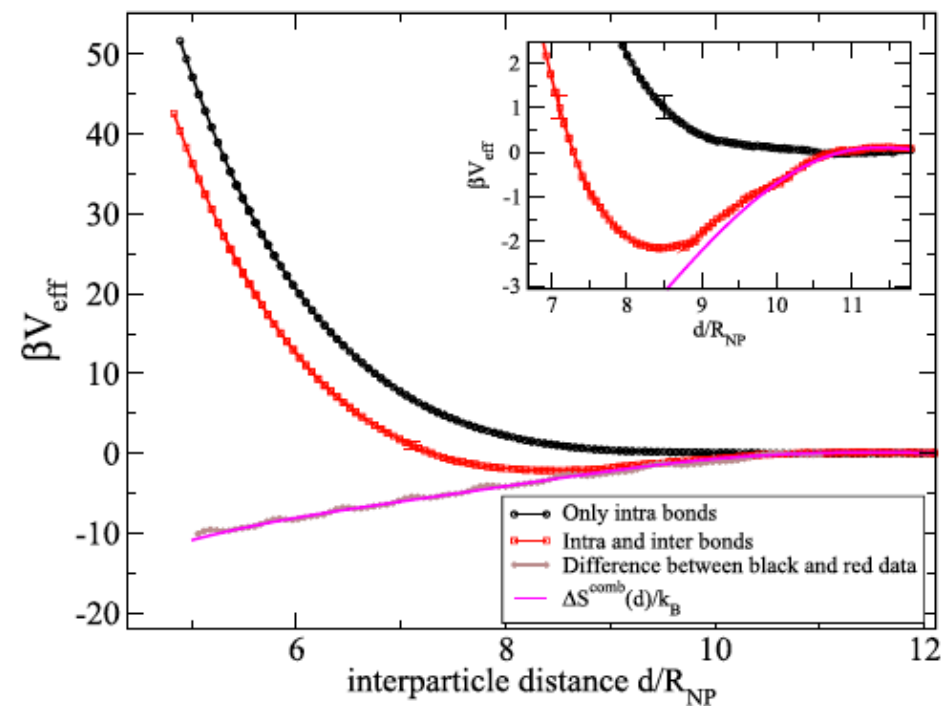
Francesco Sciortino,* Yugang Zhang, Oleg Gang, and Sanat K. Kumar

Cite This: *ACS Nano* 2020, 14, 5628–5635

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Umbrella sampling (+swap)
evaluation of the effective
potential



$$\frac{\Delta S^{\text{comb}}(d)}{k_B} = \ln \left[\frac{(2N(d) - 1)!!}{[(N(d) - 1)!!]^2} \right]$$

The late stage: mumbling Entropy Attracts !

“Patchy” polymers

■

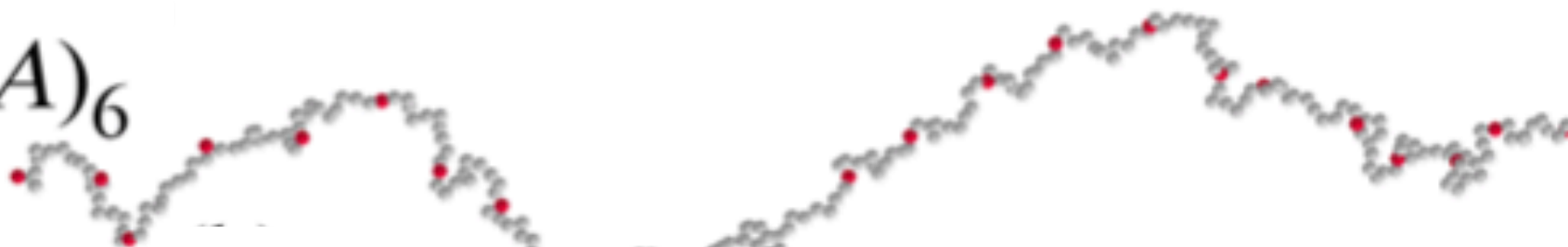
Useful for students:

FS

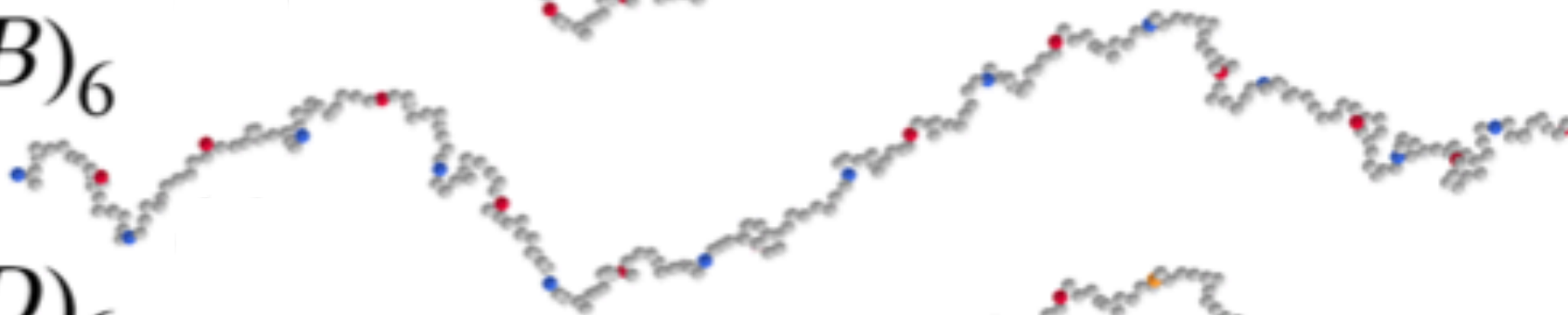
[Entropy in self assembly](#)

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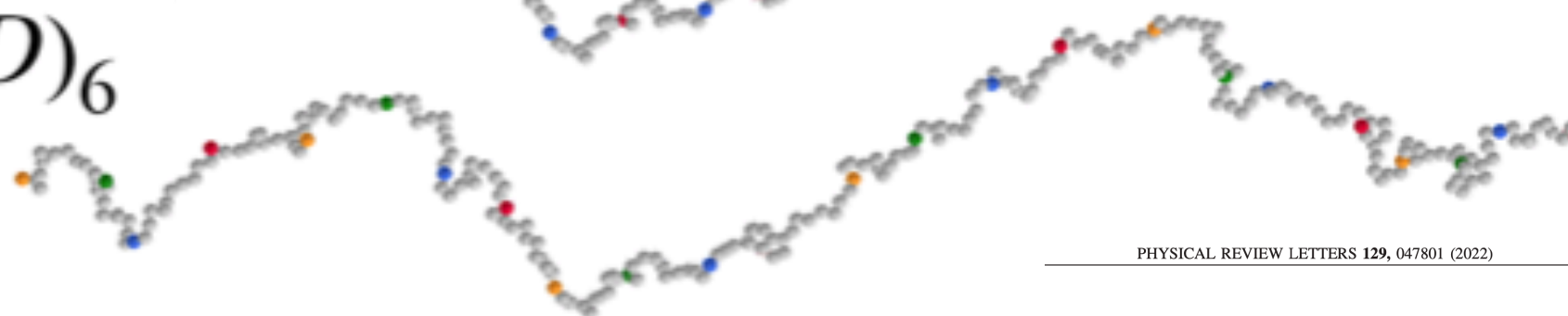
$(AAAA)_6$



$(ABAB)_6$



$(ABCD)_6$



PHYSICAL REVIEW LETTERS **129**, 047801 (2022)

Designing Enhanced Entropy Binding in Single-Chain Nanoparticles

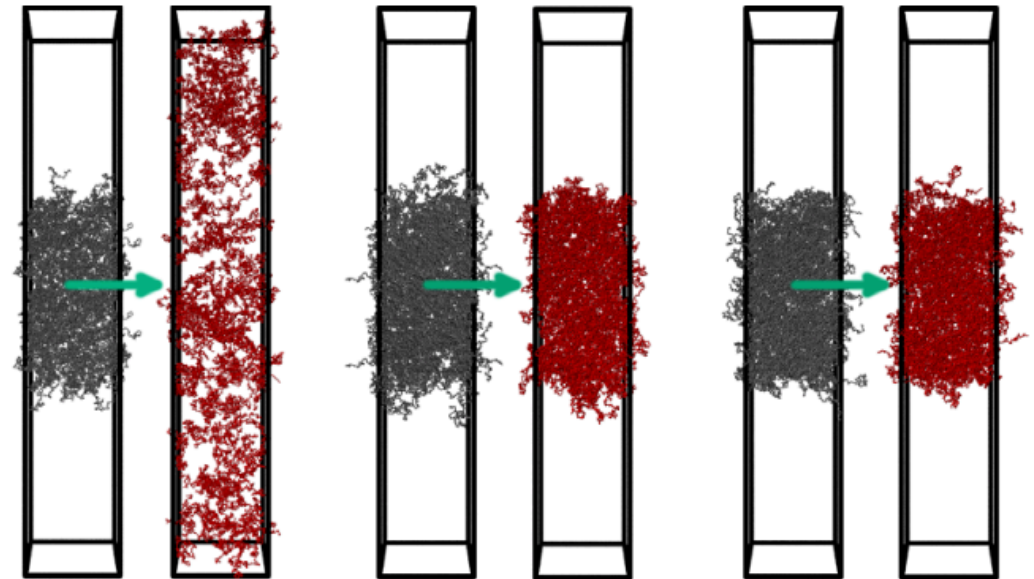
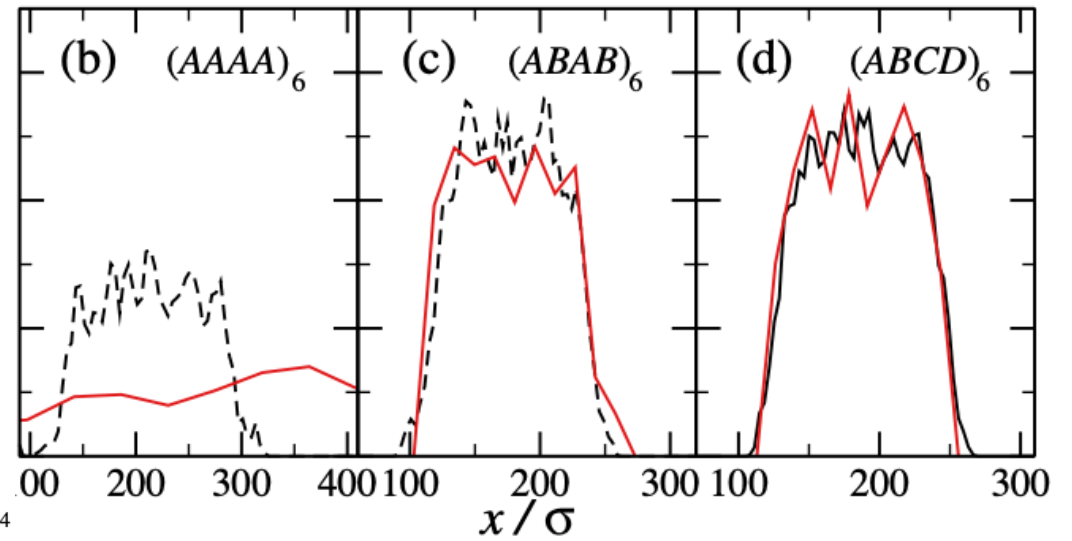
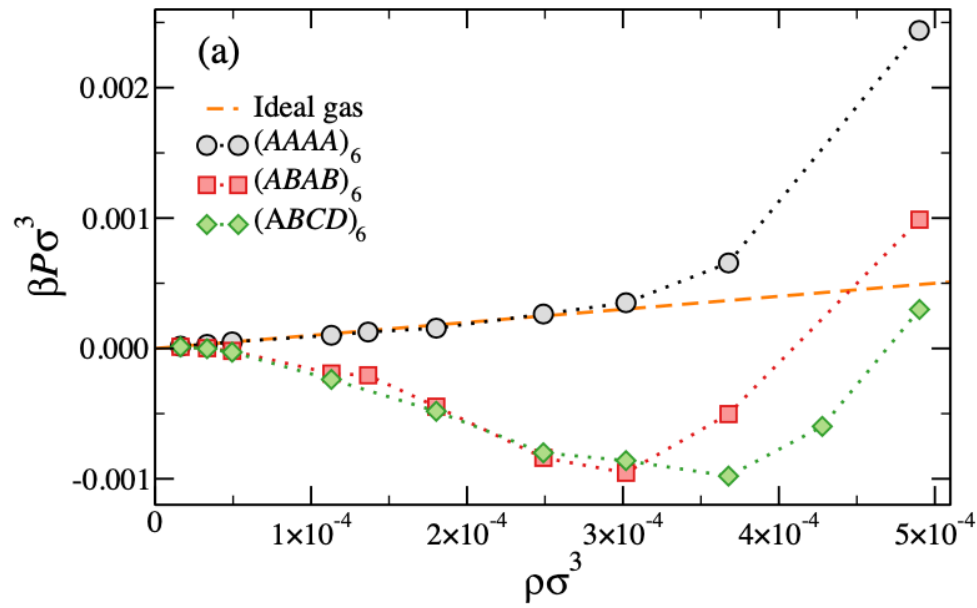
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and CNR-ISC Uos Sapienza, Piazzale A. Moro 2, IT-00185 Roma, Italy

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Phase behavior

PHYSICAL REVIEW LETTERS **129**, 047801 (2022)

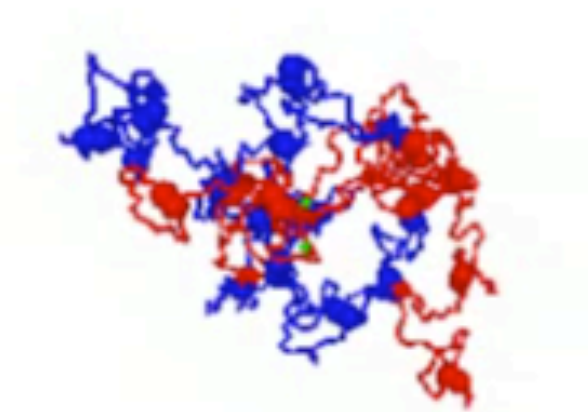
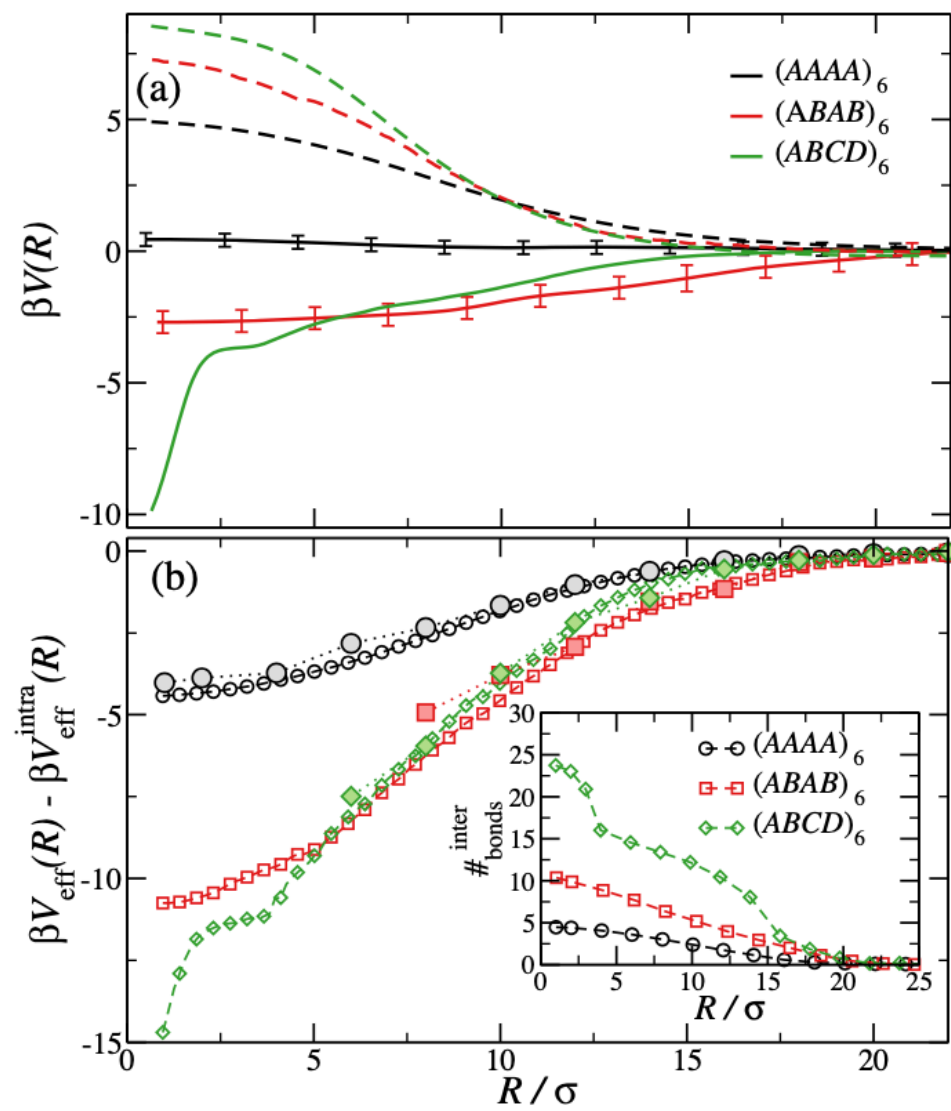
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Thank you Daan for infecting me (and many others)!

