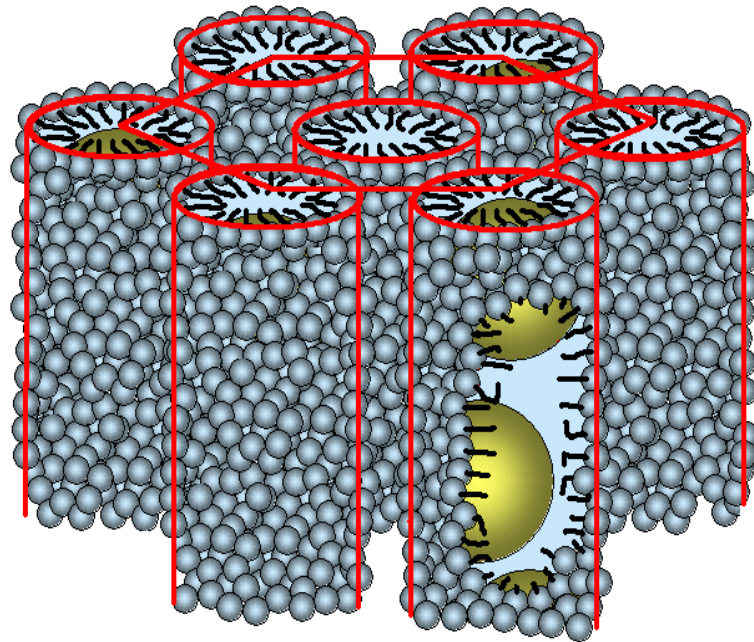


# ***SELF ASSEMBLY A BOTTOM UP APPROACH***



La Sapienza, Rome, June 2015

# OUTLINE

## ***Lecture 1&2***

- ⊙ What do we mean with Self Assembly (SA)?
- ⊙ What is the difference to aggregation?
- ⊙ Surfactants – Typical SA materials.
- ⊙ Thermodynamics
- ⊙ Molecular geometry determining the SA structures.
- ⊙ Examples
- ⊙ Other SA systems

## ***Lecture 3&4 (next week)***

- ⊙ Thermodynamics of DNA hybridization
- ⊙ Programmable SA using DNA functionalized colloids
- ⊙ Designing new colloidal materials

# WHAT IS SELF ASSEMBLY?

- ⊙ Self assembly is a type of spontaneous aggregation of (macro)molecules into well-defined mesoscopic structures.
- ⊙ Examples are micelles, vesicles, lamellae,....
- ⊙ Also referred to as **micro-phase separated systems**.
- ⊙ These are **equilibrium structures** assuming the lowest Gibbs free energy at a given temperature.

$$\Delta G = \Delta H - T\Delta S$$

- ⊙ **Aggregation (e.g. flocculation & gelation) are NON-equilibrium structures in terms of thermodynamics!**

# Surfactants =

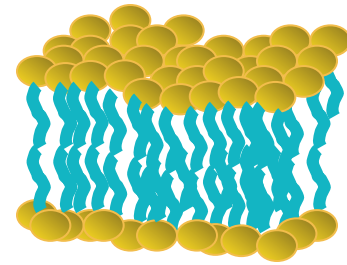
## Surface Active Molecules = Amphiphiles

- ① Surfactants are molecules with **amphiphilic** character.
- ① This means the molecules consist of a **hydrophobic** (tail) and **hydrophilic** (head group) part.

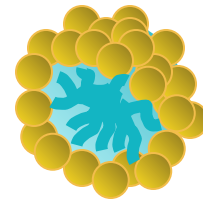




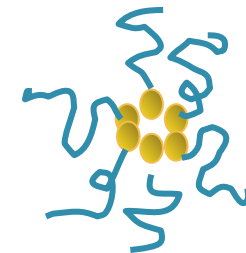
*In solution:*  
Spontaneous  
self-aggregation  
into well defined  
structures



**bilayer membrane**



**micelle**



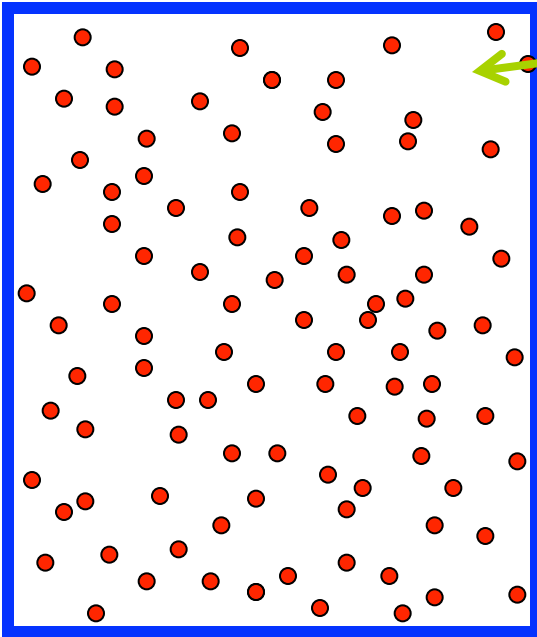
**inverted micelle**

... and many other assemblies!

# WHAT ARE THE CRITERIA FOR SELF ASSEMBLY?

# CHEMICAL POTENTIAL

**Consider:**



$N$  = number of particles

$V$  = volume (= constant)

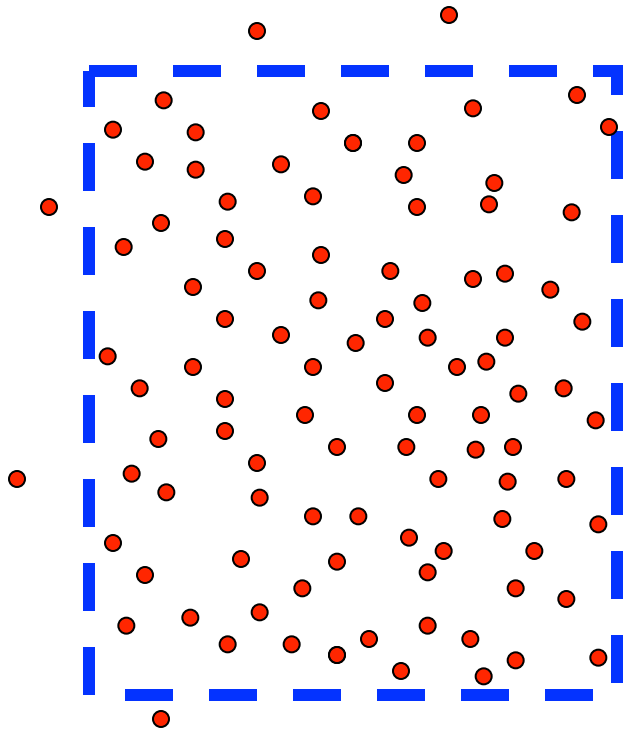
$T$  = temperature (= constant)

Gibbs free energy:

$$(G = G(T, p, N_1, N_2, \dots, N_\alpha, \dots))$$

$$G = \sum_{\alpha} \mu_{\alpha} N_{\alpha}$$

# CHEMICAL POTENTIAL



If  $V$  has permeable walls, such that particles can enter or leave, while  $T$  &  $V = \text{const.}$ :

$$\mu_\alpha = -T \left( \frac{dS}{dN_\alpha} \right)_{E_{kin}} - \epsilon \left( \frac{dS}{dE_{kin}} \right)_{N_\alpha}$$

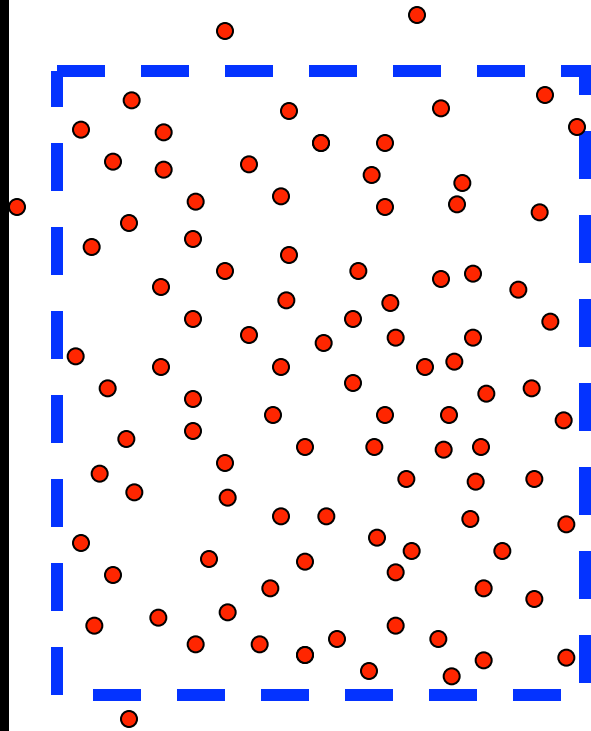
$\epsilon$  = internal energy of a particle

$N/V$  = number density

$$E_{kin} / N = (3kT)/2$$



# CHEMICAL POTENTIAL



for dilute solutions and gases

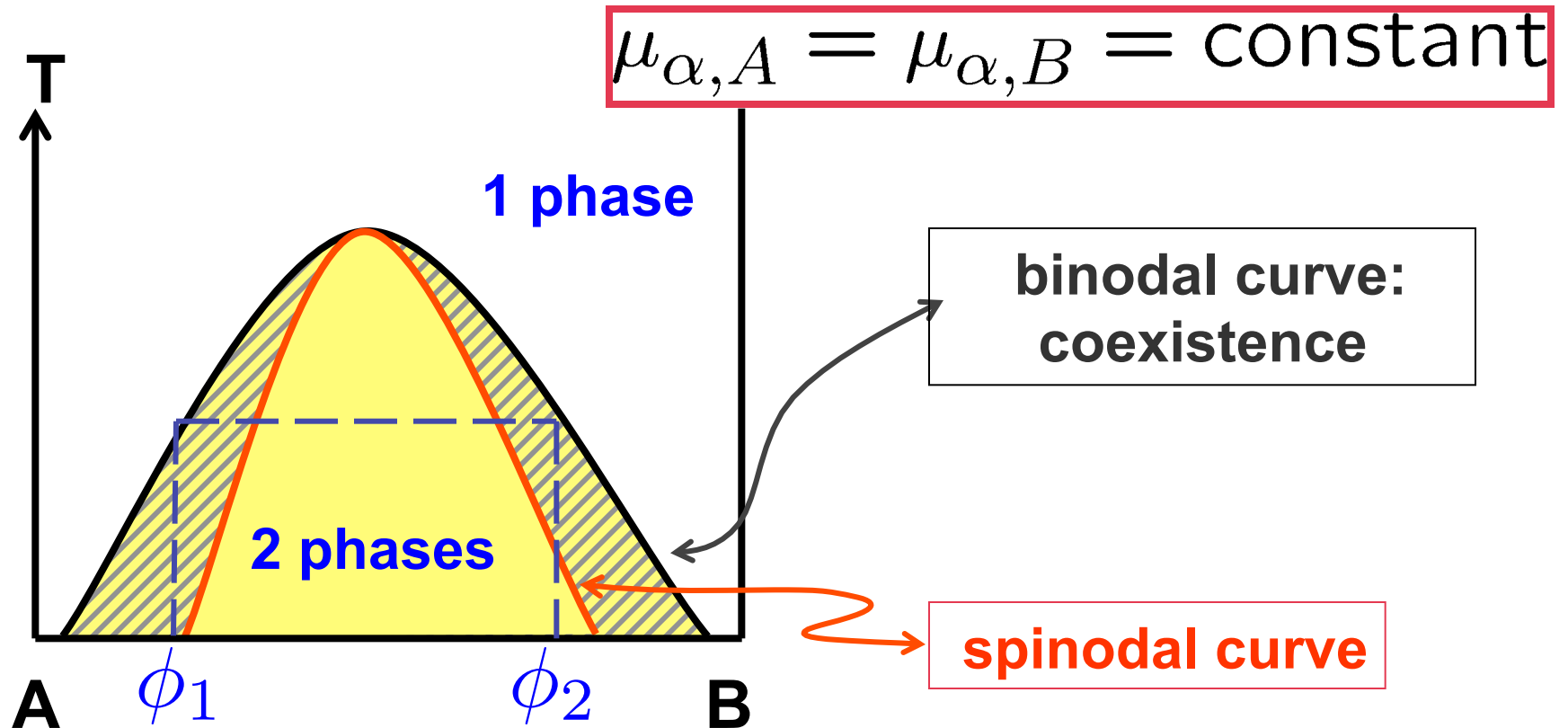
$$\mu = kT \ln \left( \frac{c}{c_0} \right) + \mu^0(T)$$

translational entropy

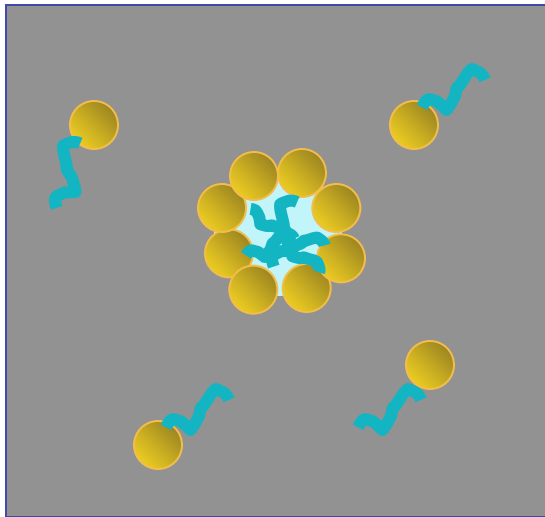
“internal”  
molecular free  
energy

# CHEMICAL POTENTIAL

Important: in chemical equilibrium ...



# WHAT IS THE CONNECTION TO SELF-ASSEMBLY?



## Thermodynamic equilibrium:

$\mu$  of identical molecules must be the same in all possible aggregates.

$$\mu = \underbrace{\mu_1^0}_{\text{monomers}} + k_B T \ln X_1 = \underbrace{\mu_2^0}_{\text{dimers}} + k_B T \frac{1}{2} \ln \frac{X_2}{2} = \underbrace{\mu_3^0}_{\text{trimers}} + k_B T \frac{1}{3} \ln \frac{X_3}{3} = \dots$$

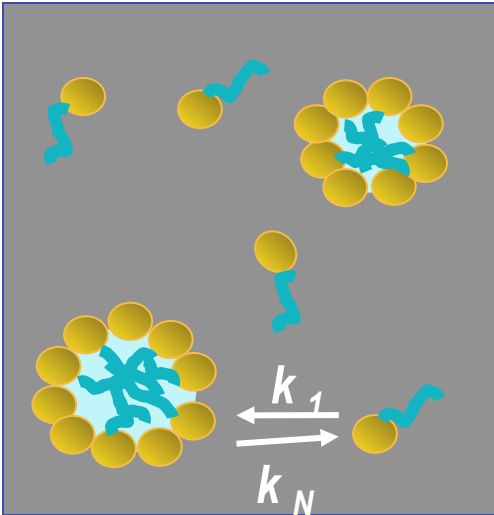
Or for an  $n$ -mer: 
$$\mu_n = \mu_n^0 + \frac{k_B T}{n} \ln \frac{X_n}{n} \quad \text{with } n = 1, 2, 3, \dots$$

$\mu_n$  = average chem. pot. of a molecule in an aggregate of  $n$  molecules

$\mu_n^0$  = energy needed to bring a molecule from infinity to the system

$X_n$  = volume fraction of molecules in an aggregate of  $n$  molecules

# SELF ASSEMBLY



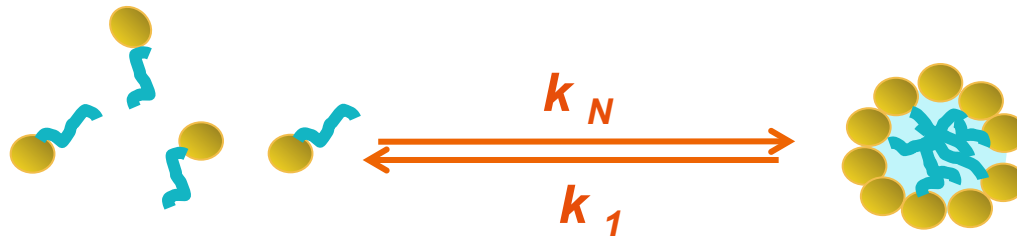
**Driving force for aggregation:**  
difference in cohesive energies  
between molecules in the  
aggregated and dispersed state.

$$K_{\text{eq}} = \frac{c}{c_0} = \exp \left[ -n \frac{\mu_n^0 - \mu_1^0}{k_B T} \right]$$
$$= \exp \left[ -\frac{\Delta G^0}{k_B T} \right]$$

**Condition to form large stable aggregates:**

$$\mu_1^0 > \mu_n^0$$

# CRITICAL MICELLE CONCENTRATION CMC

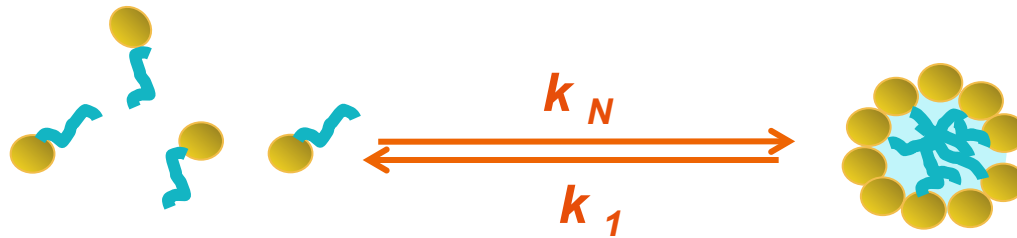


Flow in **forward** direction:  $j_F = k_n [c_1]^n$

Flow in **backward** direction:  $j_B = k_1 [c_n]$

equil.  $j_F = j_B$

# CRITICAL MICELLE CONCENTRATION CMC

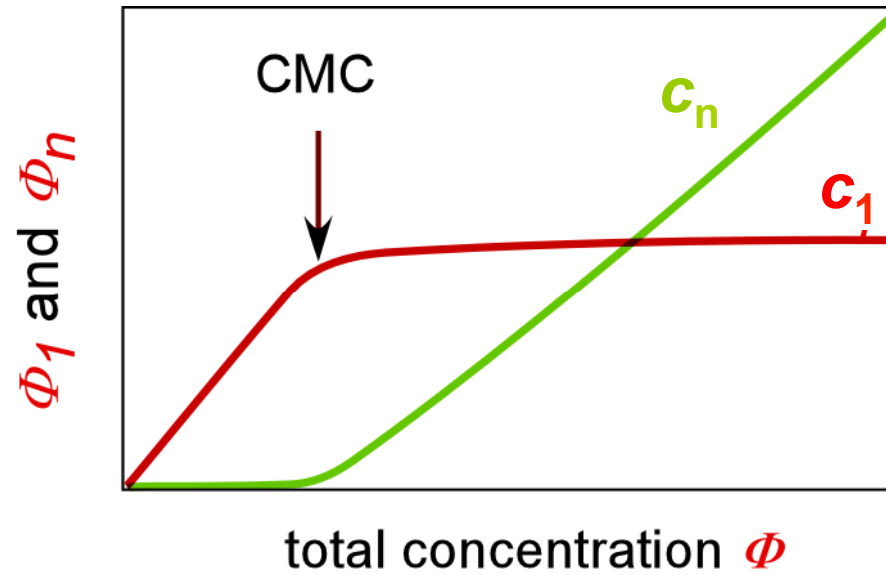
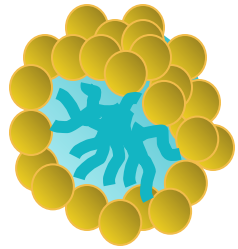


$$j_F = j_B$$

→  $k_n [c_1]^n = k_1 [c_n]$

or  $[c_n] = \frac{k_n}{k_1} [c_1]^n$

# CRITICAL MICELLE CONCENTRATION CMC

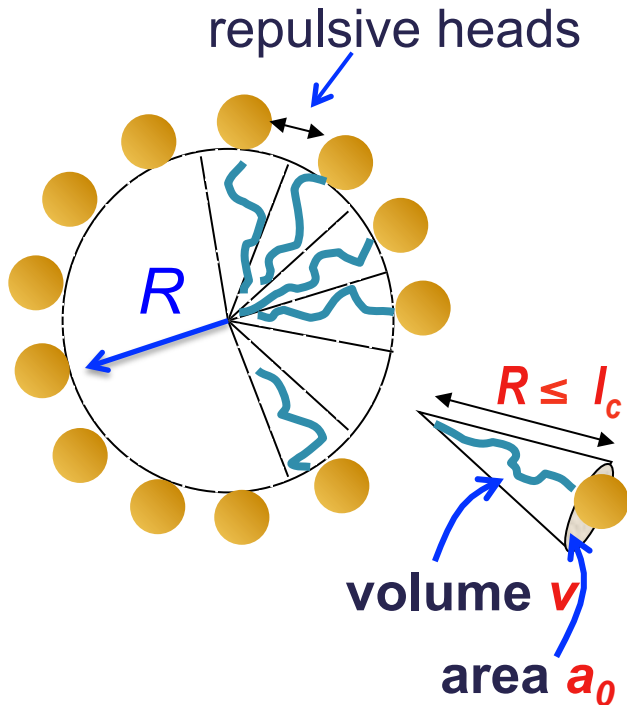


$$[c_n] = \frac{k_n}{k_1} [c_1]^n$$



# INFLUENCE OF MOLECULAR GEOMETRY ON THE TYPE OF AGGREGATES

# SA STRUCTURE & SPONTANEOUS CURVATURE



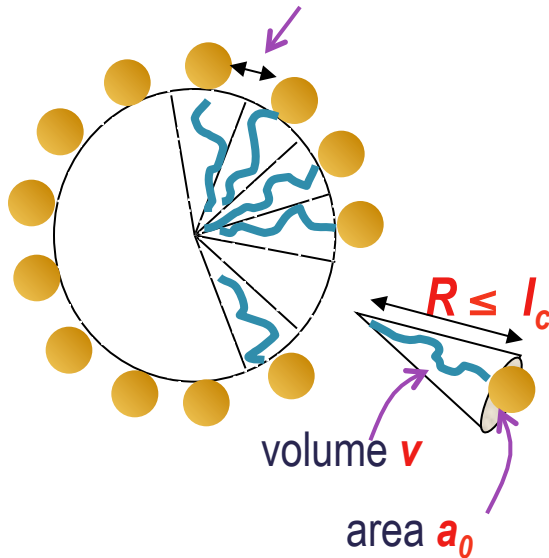
**Spontaneous curvature  $1/R$**  depends on:

- the effective head-group size  $a_0$
- the length  $l$  of the hydrophobic tail.

Note:  $a_0$  can vary strongly with  $T$ . In case of aqueous solutions the  $pH$  and  $salinity$  of the solvent also can change  $a_0$ .

# AS-STRUCTURE & SPONTANEOUS CURVATURE

repulsive heads



$a_0$  fixed (constant  $T$  and  $pH$ )

the packing geometry is determined by:

$v$  and  $l_c$

parameter  $v/(a_0 l_c)$  determines the self-assembled structures :

$$\frac{v}{a_0 l_c} < \frac{1}{3}$$

spherical micelles

$$\frac{1}{2} < \frac{v}{a_0 l_c} < 1$$

plane lamellas

$$\frac{1}{3} < \frac{v}{a_0 l_c} < \frac{1}{2}$$

non-spherical micelles

$$1 < \frac{v}{a_0 l_c}$$

inverted micelles

$$\frac{v}{a|} < \frac{1}{3}$$



$$\frac{1}{3} < \frac{v}{a|} < \frac{1}{2}$$



$$\frac{v}{a|} \sim 1$$



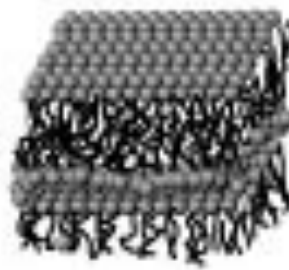
$$\frac{v}{a|} > 1$$



Micelle ( $L_1$ )



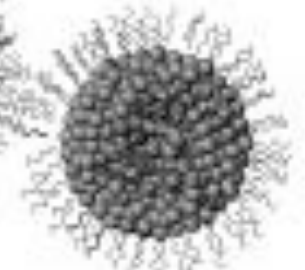
Hexagonal ( $H_1$ )



Lamellar ( $L_\alpha$ )



Inverse Hexagonal ( $H_2$ )



Inverse Micelle ( $L_2$ )

Cubic ( $V_1$ )

Cubic ( $V_1$ )

Cubic ( $V_2$ )

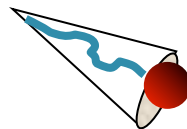
Mirror Plane



Cubic ( $V_2$ )

# A WORD ABOUT DRIVING FORCES

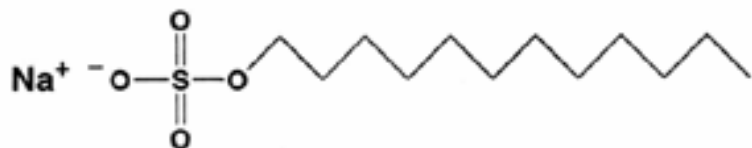
- ① In many surfactant systems the driving force for spontaneous self-assembly are the 'hydrophobic' effect combined with the Coulomb interactions of a polar or charged head groups.
- ① These Coulomb interactions are also related to the entropy of water packing around the head group.
- ① In general we need some net attraction.



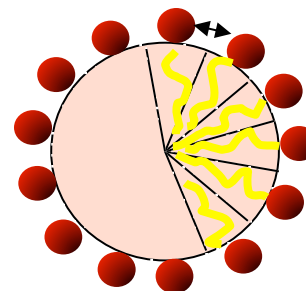
- ① If the net-attraction is too strong (on the order of  $10 k_B T$ ) irreversible aggregation takes place – hence, no equilibrium can be found. These systems are often aggregating irreversibly.

# HOW TO GO FROM SPHERICAL TO WORMLIKE MICELLES?

Sodium dodecyl sulfate (SDS)



+ Water

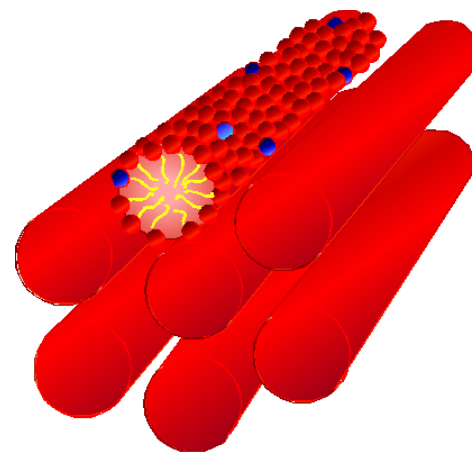
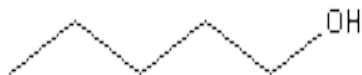


*only spherical micelles form*

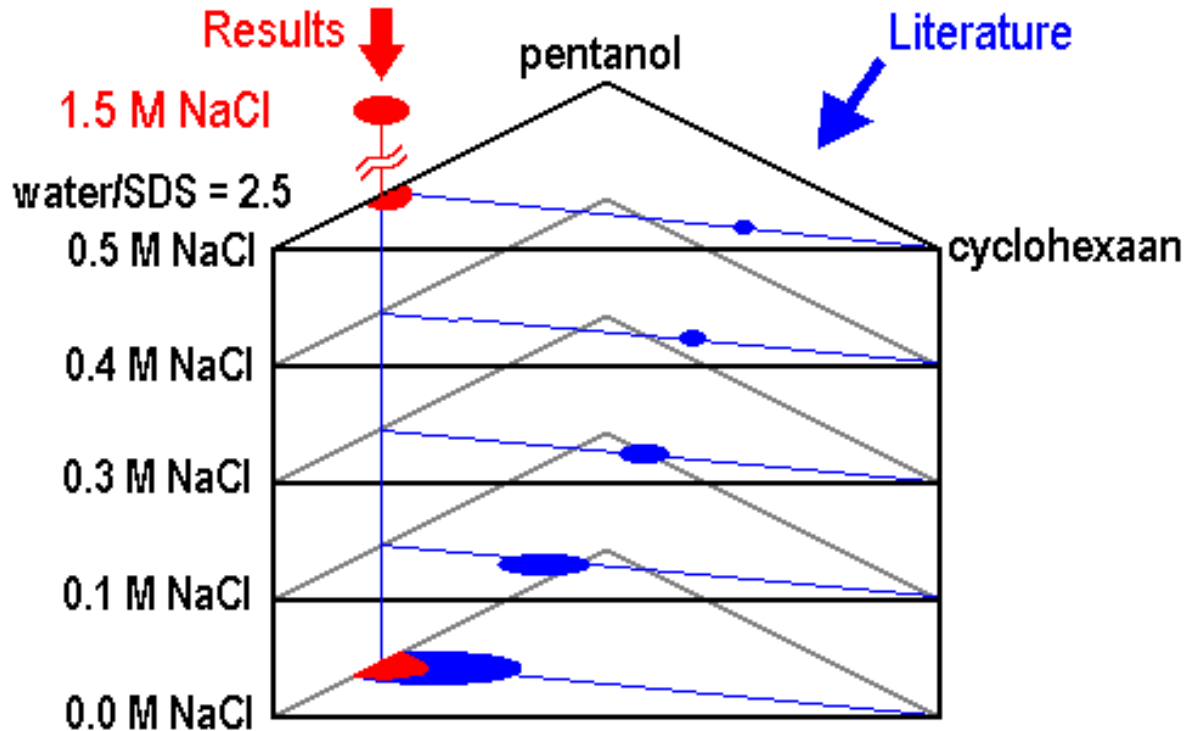
*adding a co-surfactant  
changes spontaneous curvature*



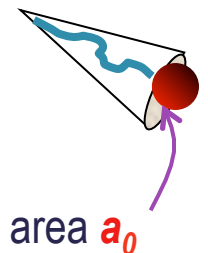
+ Pentanol



# PHASE DIAGRAM



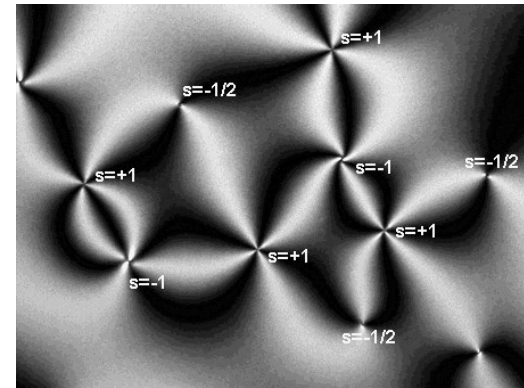
- ⊙ One can swell the hexagonal phase with organic solvent by further decreasing the spontaneous curvature  $1/R$  by adding salt (which decreases the effective head-group size  $a_0$ )



# HOW DO WE KNOW WHAT STRUCTURE WE HAVE?

*There are simple lab techniques:*

- ⊙ Birefringence
- ⊙ Microscopy under **crossed polarizers** – the resulting texture gives indications about the type of liquid crystalline properties
- ⊙ Flow properties & Shear birefringence



<http://www.personal.kent.edu/~bisenyuk/liquidcrystals/textures1.html>

*For exact structural analysis we need:*

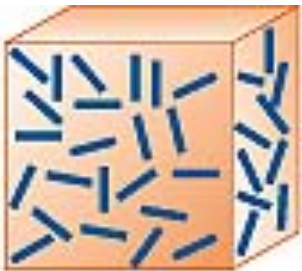
- ⊙ SAXS – Small Angle X-ray Scattering
- ⊙ SANS – Small Angle Neutron Scattering
- ⊙ Combination of Rheology & SAXS



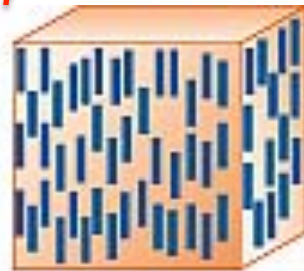
# LIQUID CRYSTALS

isotropic

non-isotropic



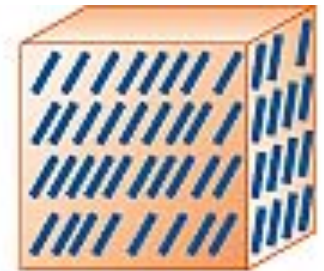
(a) Normal liquid



(b) Nematic liquid crystal



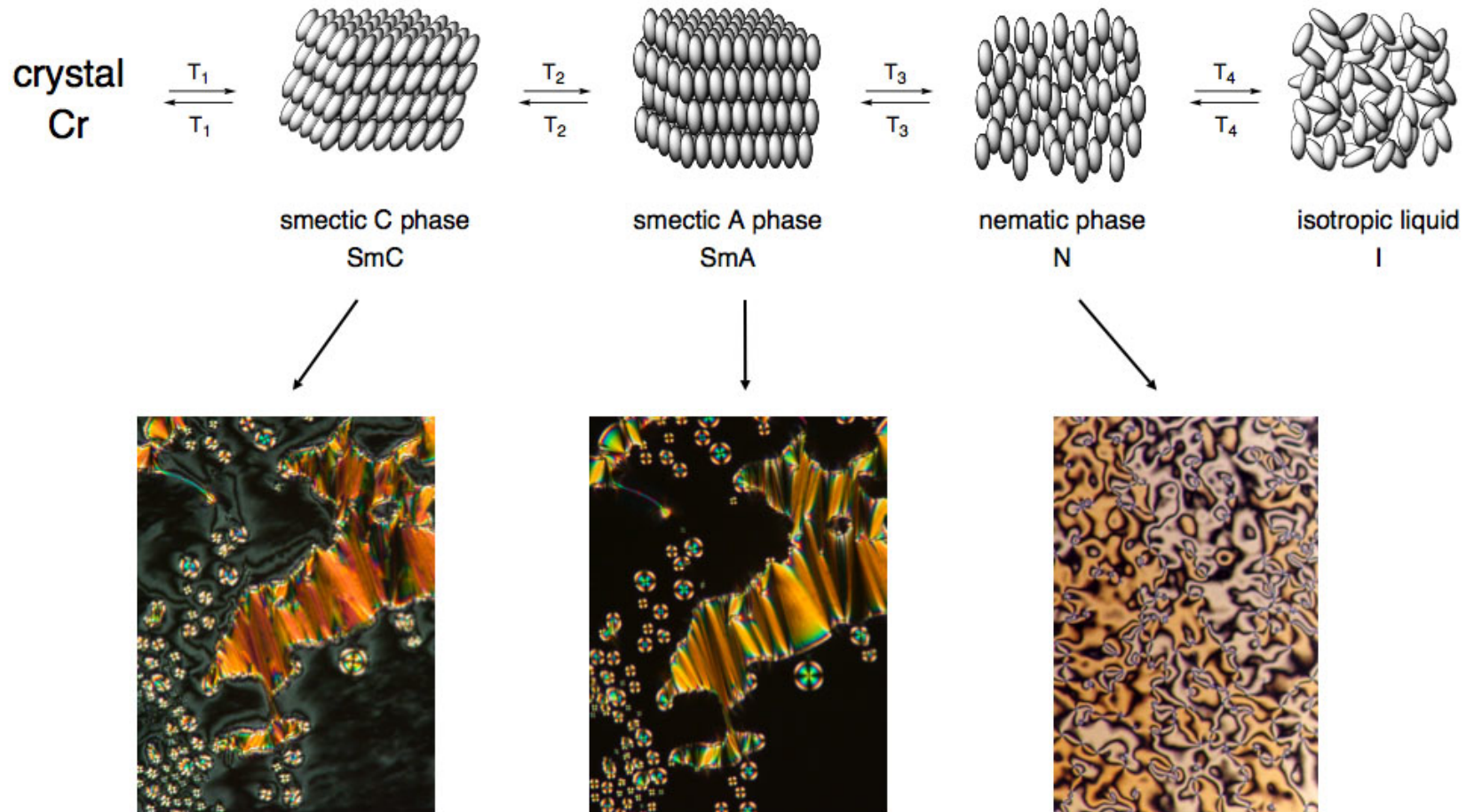
(c) Smectic A liquid crystal



(d) Smectic C liquid crystal

- ⊙ Under crossed polarizers **anisotropic** samples allow light passing through
- ⊙ **Isotropic** samples do not let light pass through when placed between crossed polarizers.

# LIQUID CRYSTALS

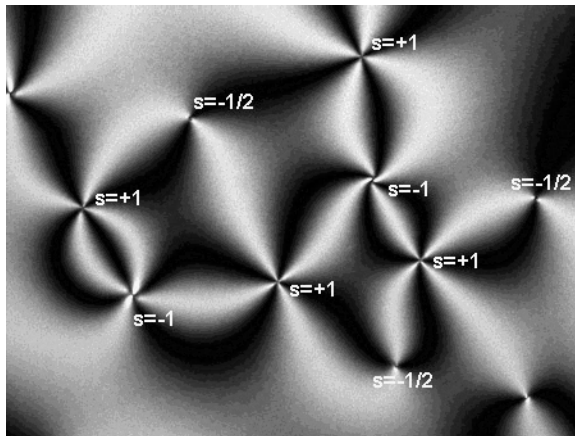


<http://faculty.chem.queensu.ca/people/faculty/lemieux/images/web-Fig.%201.jpg>

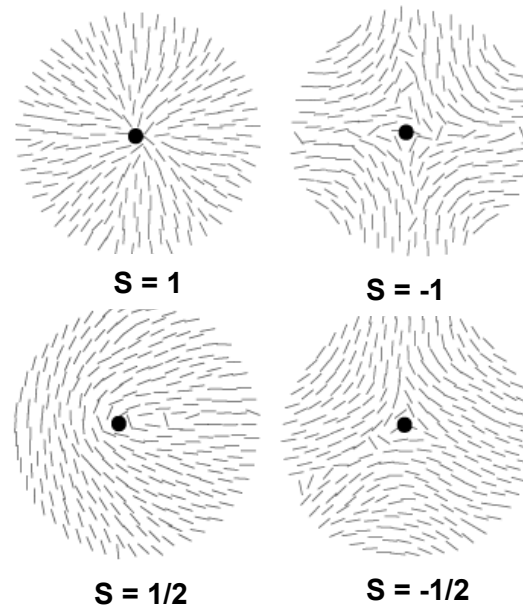
# POLARIZED BRIGHT-FIELD MICROSCOPY

*In polarized microscopy we cannot see the micelles but we do see **defects** or disclination lines*

- ⊙ To see birefringence (meaning different axial refractive indices, the sample needs to show **anisotropy**.
- ⊙ The specific textures can give us a hint to what type of LC texture we have.



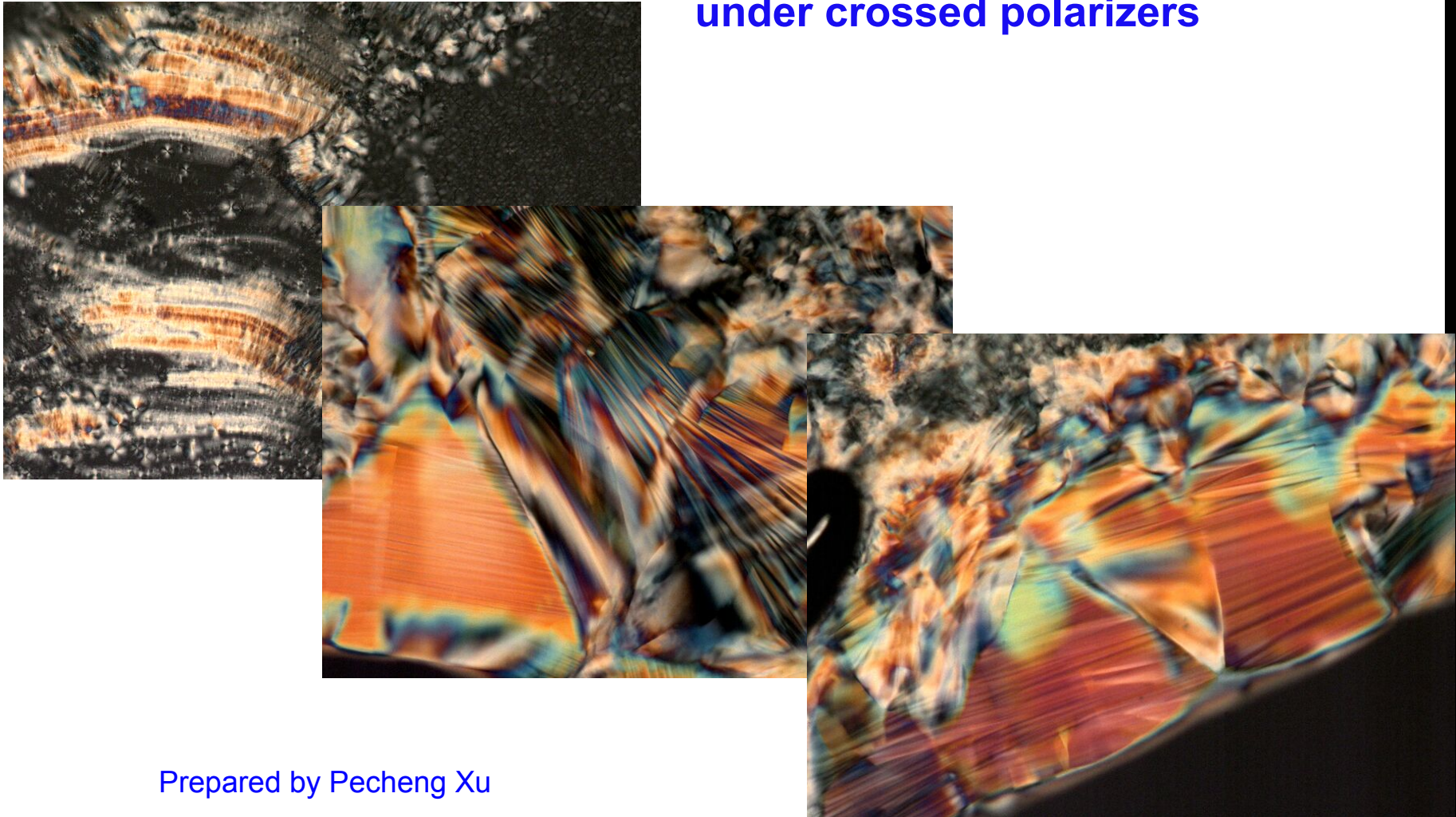
<http://www.personal.kent.edu/~bisenyuk/liquidcrystals/textures1.html>



# CROSSED POLARIZER MICROSCOPY

*Pure SDS + pentanol in water - hexagonal phase, freshly prepared*

**under crossed polarizers**



Prepared by Pecheng Xu

# CROSSED POLARIZER MICROSCOPY

*Pure SDS + pentanol in water - hexagonal phase*

**under crossed polarizers**



Freshly  
prepared

2 h

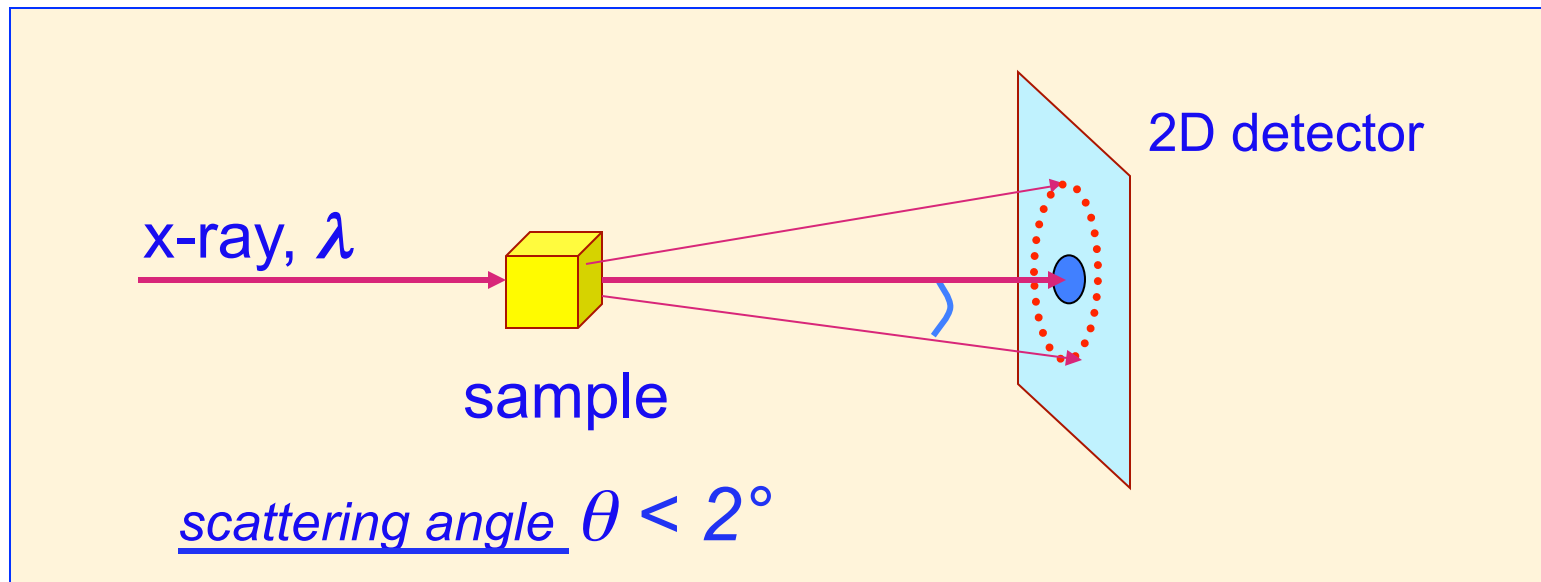
1 day

2 days

**Growth of crystals in time**

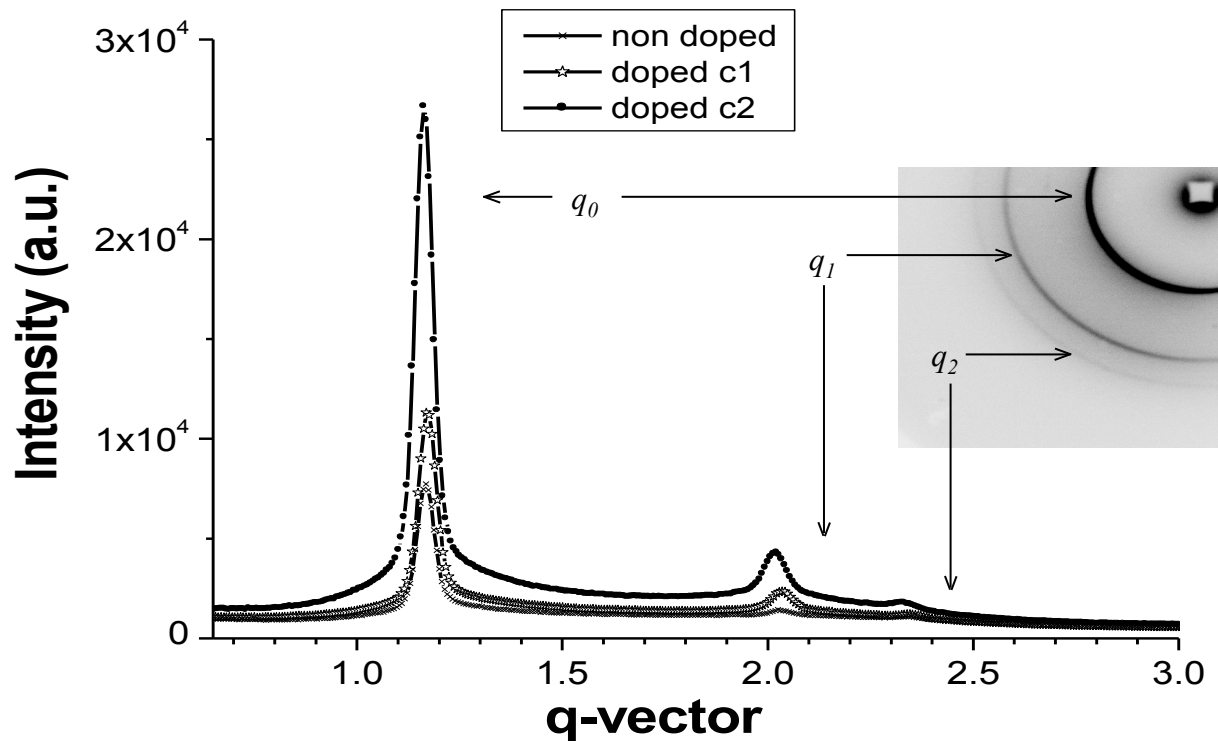
**Because the end-cap energy is high small crystals shrink**

# SMALL ANGLE X-RAY SCATTERING



- ⊙ Home made setup ( $\lambda = 1.54 \text{ \AA}$ )
- ⊙ Synchrotron ESRF : DUBBLE beam line BM26  
*sample-to-detector distance = 4 m*

# SAXS: SIGNATURE OF A HEXAGONAL PHASE



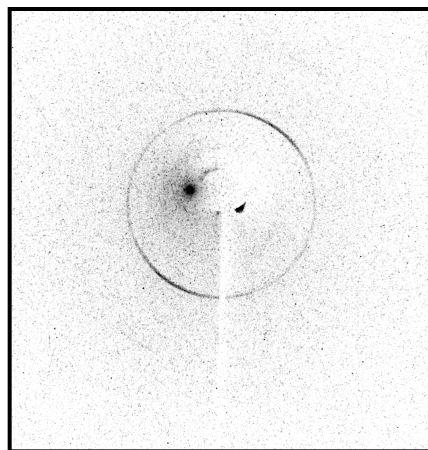
Powder spectrum of a hexagonal phase:

$$\frac{q_i}{q_0} = 1 : \sqrt{3} : 2 : \sqrt{7} : \dots$$

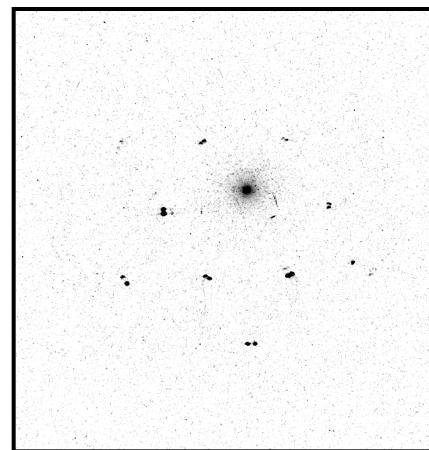
E. Eiser, F. Bouchama, M.B. Thathagar, and G. Rothenberg, "Trapping Metal Nanoclusters in "Soap and Water" Soft Crystals," *Chem. Phys. Chem.*, **4**, 526 (2003).

# SAXS: SIGNATURE OF A HEXAGONAL PHASE

## Ruthenium nanoclusters in hexagonal phase



a) 2 hours



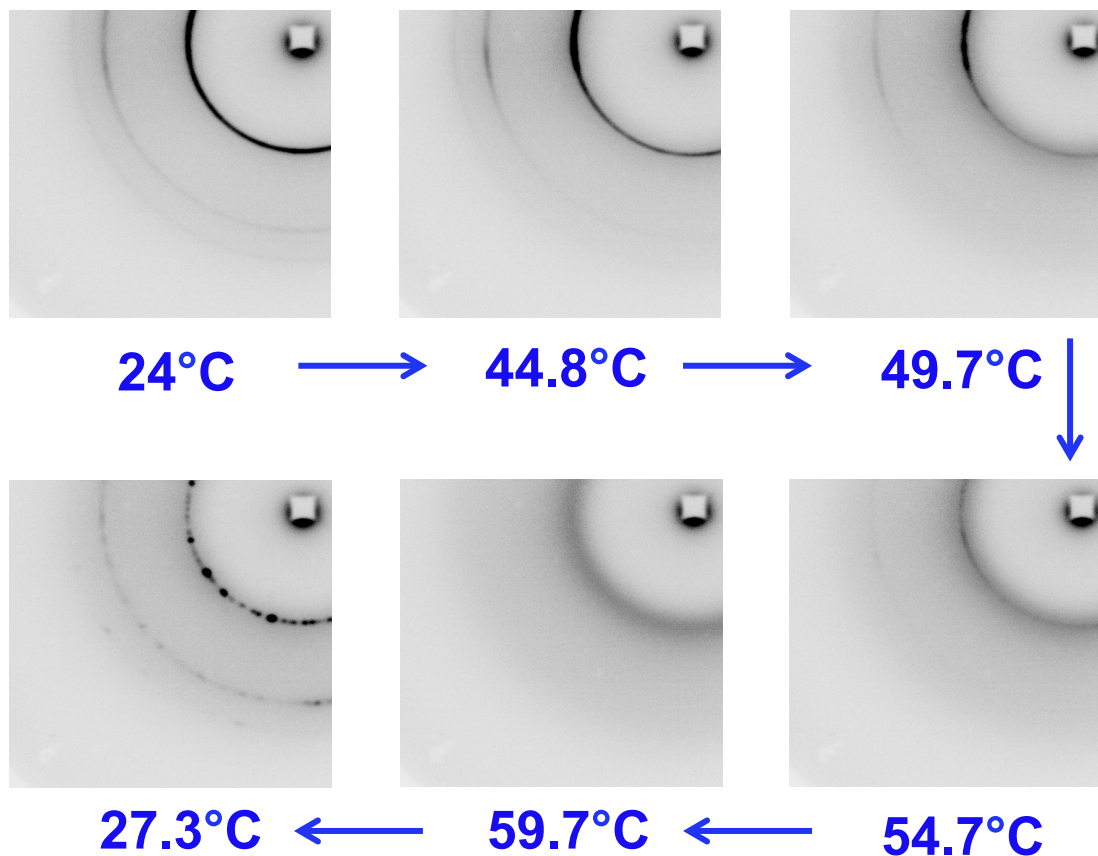
b) 60 days

- ⊙ Measured with a home made setup ( $\lambda = 1.54 \text{ \AA}$ )
- ⊙ *After 2h*: rings indicates a powder crystalline sample
- ⊙ *After 60 days*: small crystals are 'eaten up' leaving a single crystal.

E. Eiser, F. Bouchama, M.B. Thathagar, and G. Rothenberg, "Trapping Metal Nanoclusters in "Soap and Water" Soft Crystals," *Chem. Phys. Chem.*, **4**, 526 (2003).



# SAXS: MELTING OF THE HEXAGONAL PHASE

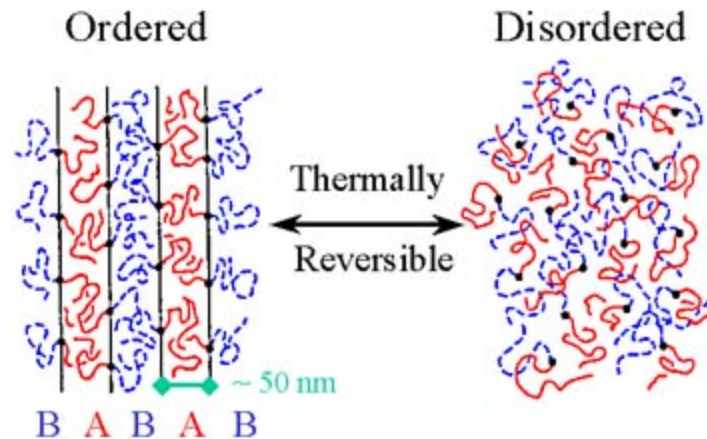
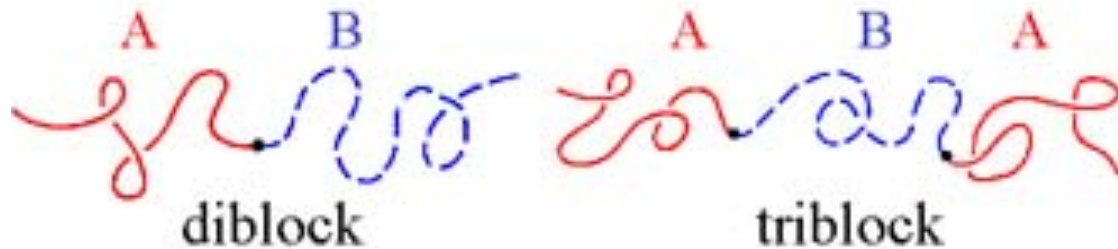


Bouchama, Thathagar, Rothenberg, Turkenburg, Eiser, "Self-Assembly of a Hexagonal Phase of Wormlike Micelles Containing Metal Nanoclusters," *Langmuir*, 20, 477 (2004)

# NOTE: THERE ARE MANY OTHER SELF-ASSEMBLING SYSTEMS

- ⊙ Block-copolymers – melts & solutions
- ⊙ Biological surfactants and macromolecules
  
- ⊙ 2D self-assembly at interfaces
  
- ⊙ And we need to consider the different driving energies:  
hydrophobic effect,  $\pi$ - $\pi$  interactions, H-bonds, ...

# POLYMERIC SURFACTANTS



<http://www.princeton.edu/~polymer/block.html>

# PHASE DIAGRAM

A in B matrix



cubic



hexagonal cylindrical



bicontinuous gyroid



lamellar



bicontinuous gyroid

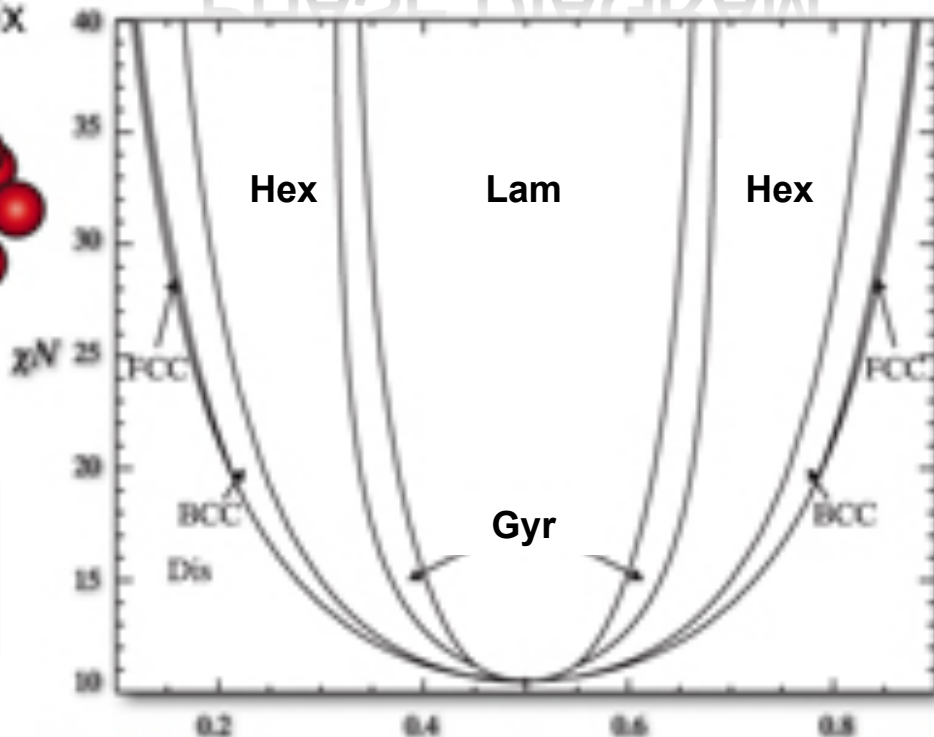
B in A matrix



cubic

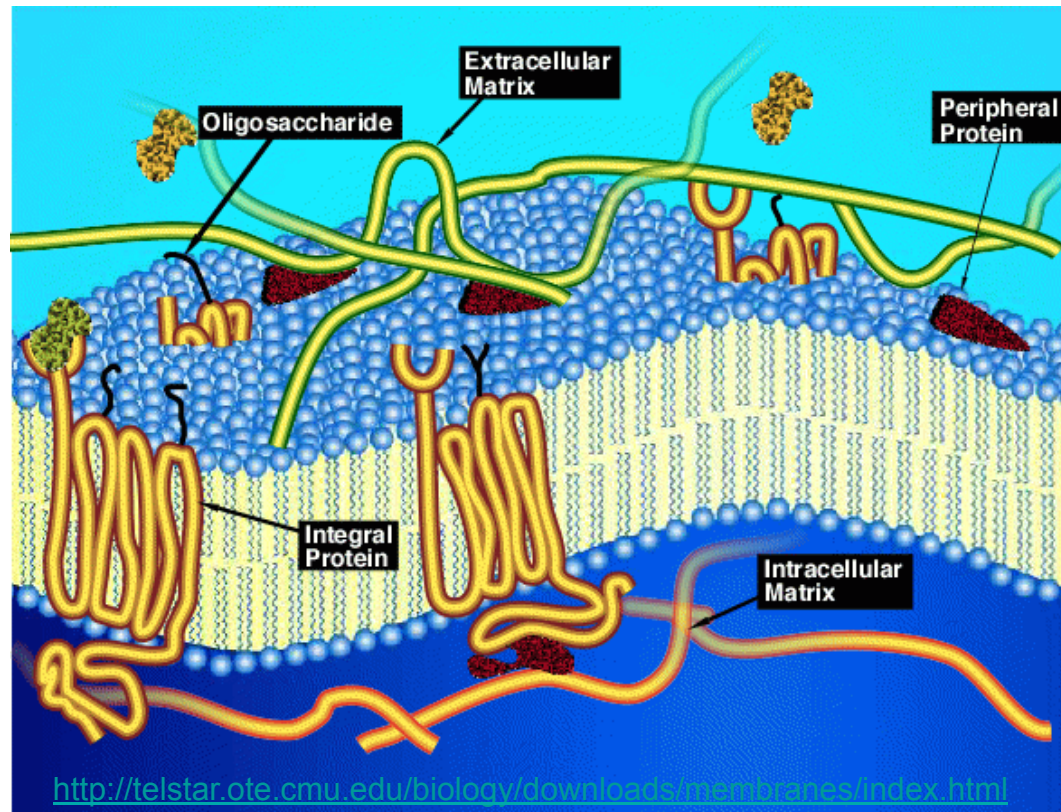


hexagonal cylindrical

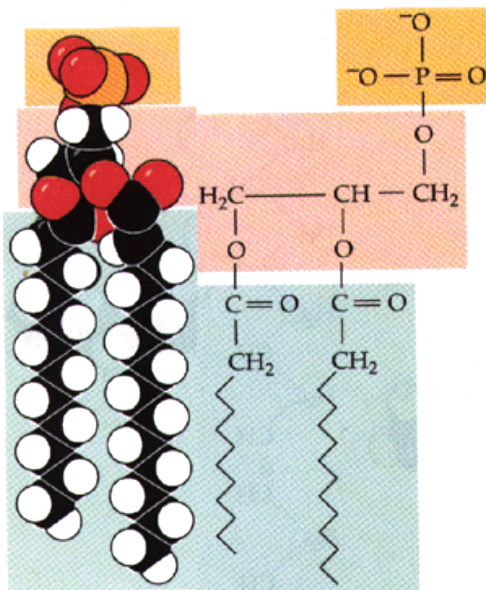


<http://www.physics.nyu.edu/pine/research/nanocopoly/CopolyPhases.jpg>

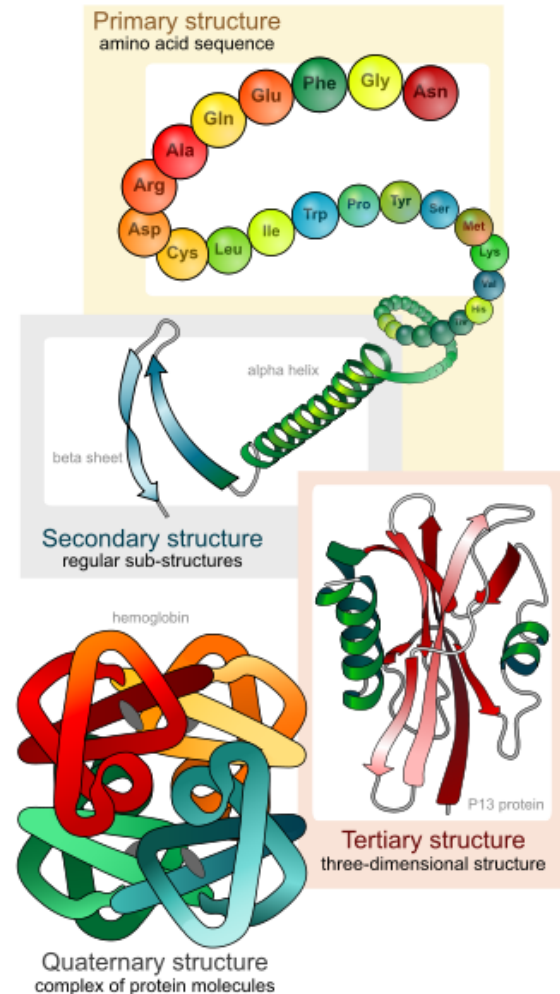
# BIOLOGICAL EXAMPLES



# CELL MEMBRANES & PROTEINS



phospholipids

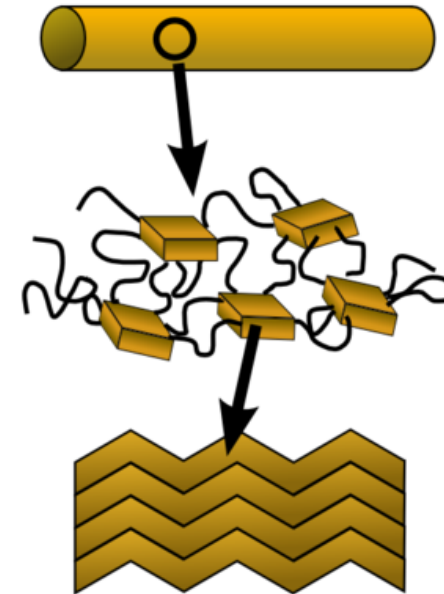




# PROTEIN FOAMS



# NON-DISEASED AMYLOID



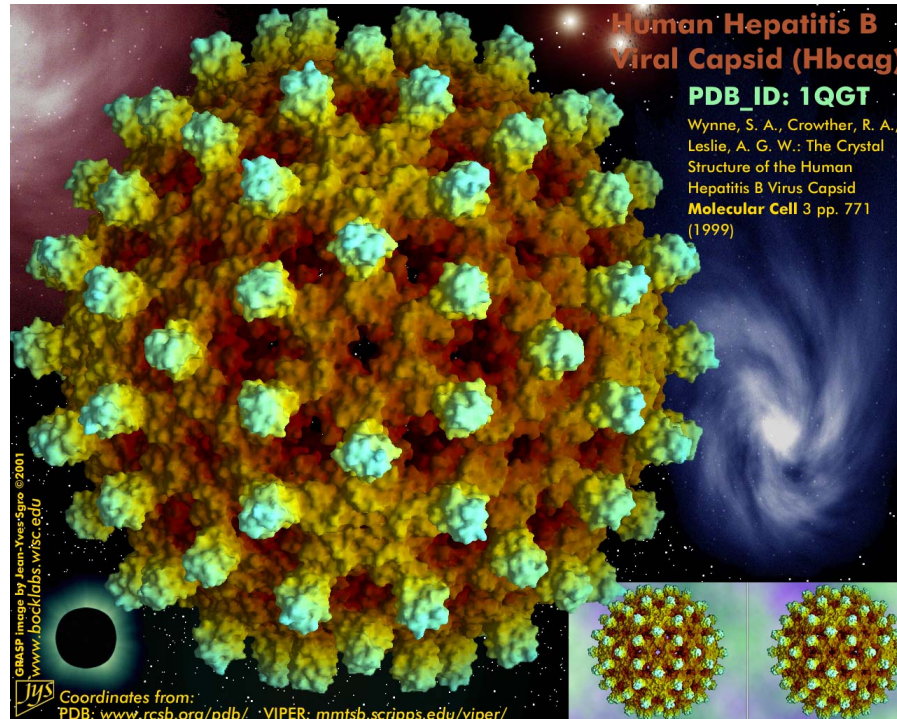
Structure of spider silk: crystalline regions (beta-sheets) are separated by amorphous linkages.



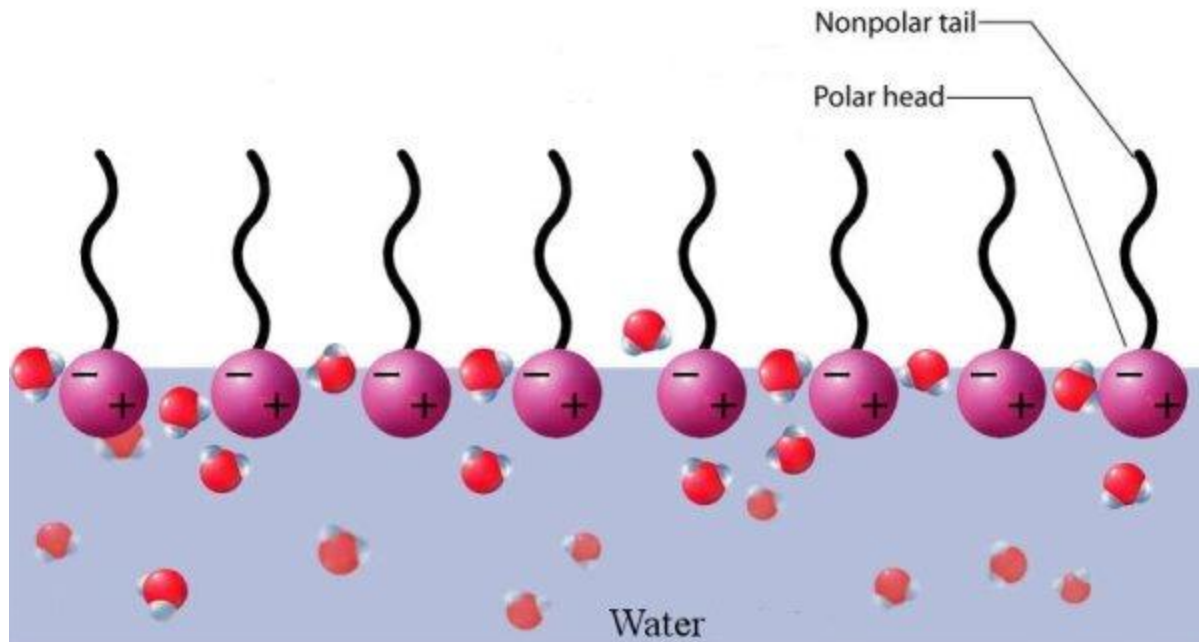
It took more than one million spiders, five years and £300,000 to create the world's largest and rarest shawl made entirely from spider silk



# VIRUS CAPSIDS



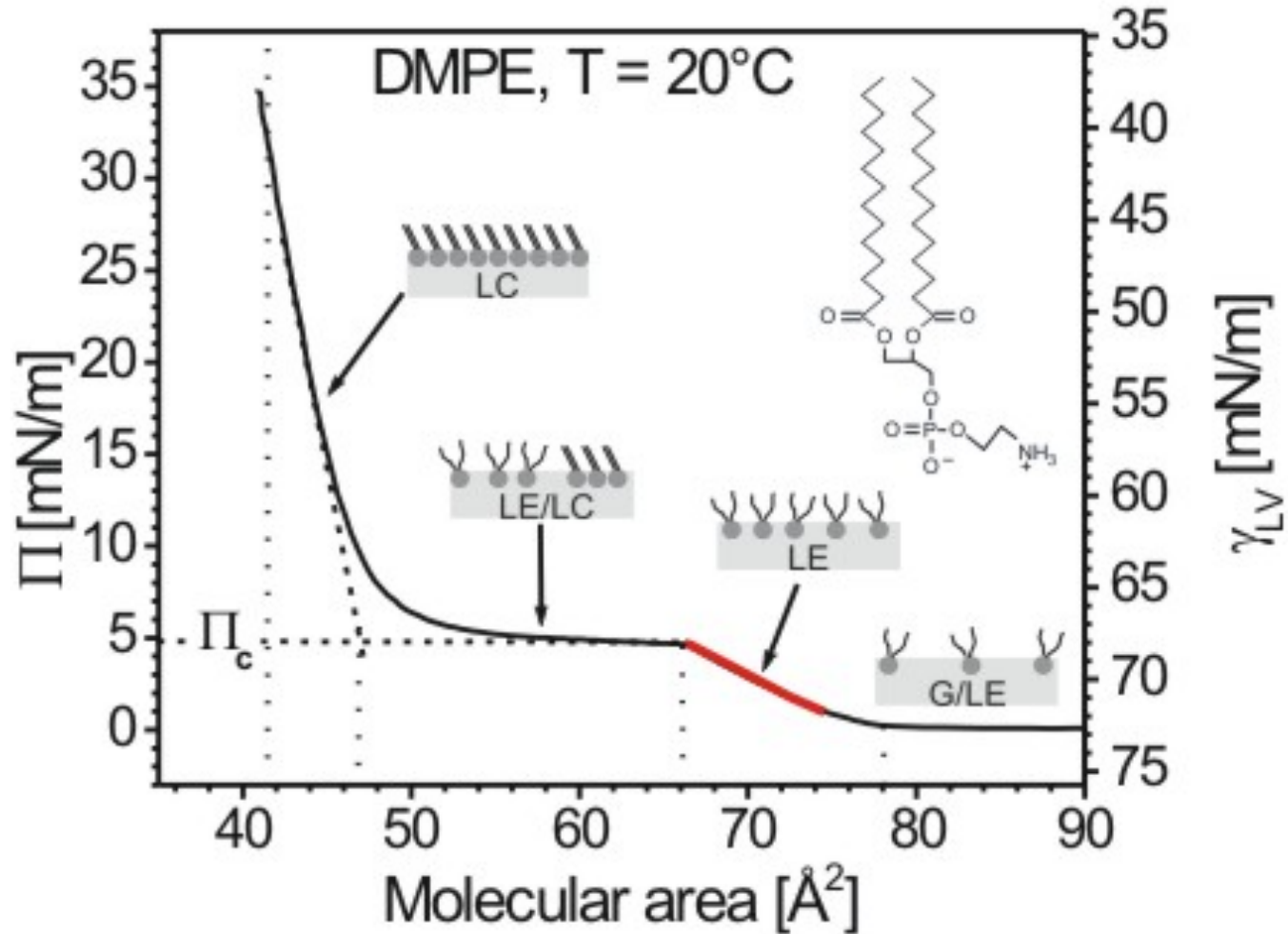
# MEMBRANES AT THE AIR-WATER INTERFACE



<http://www.answers.com/topic/langmuir-blodgett-film>

# LANGMUIR-BLODGETT FILMS

lipid DMPE (1,2-Dimyristoyl-*sn*-glycero-phosphoethanol-amine)



[http://www.mpip-mainz.mpg.de/~grafk/Monolayer\\_LB.html](http://www.mpip-mainz.mpg.de/~grafk/Monolayer_LB.html)

# LANGMUIR-BLODGETT FILMS

## Surface pressure – area isotherms...

...are the best method to study monolayers.

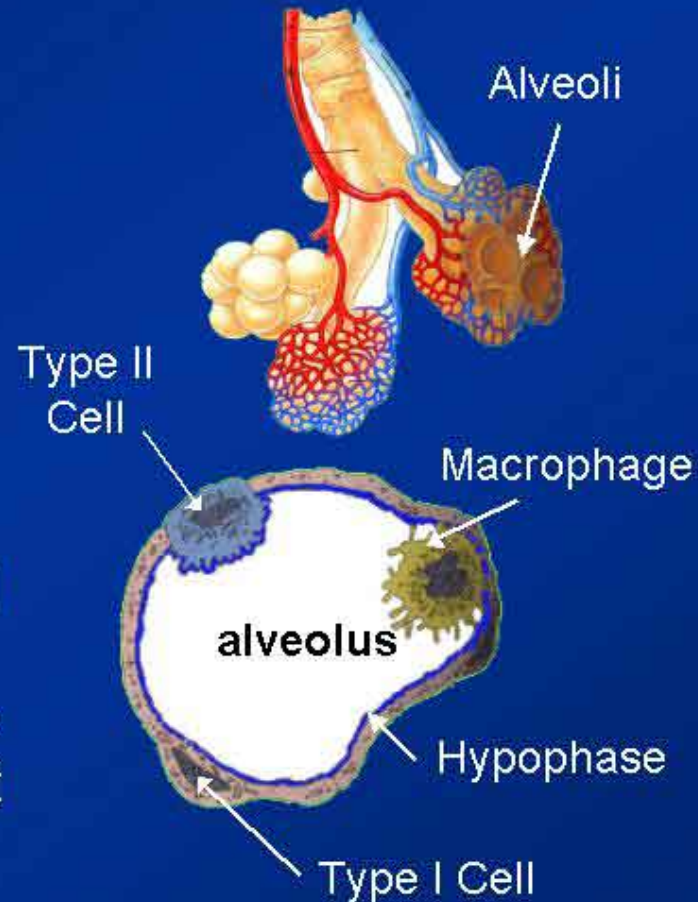
$$\pi = \gamma_0 - \gamma$$

= pressure that opposes the normal contracting tension of the surfactant free interface.

# LUNG SURFACTANTS

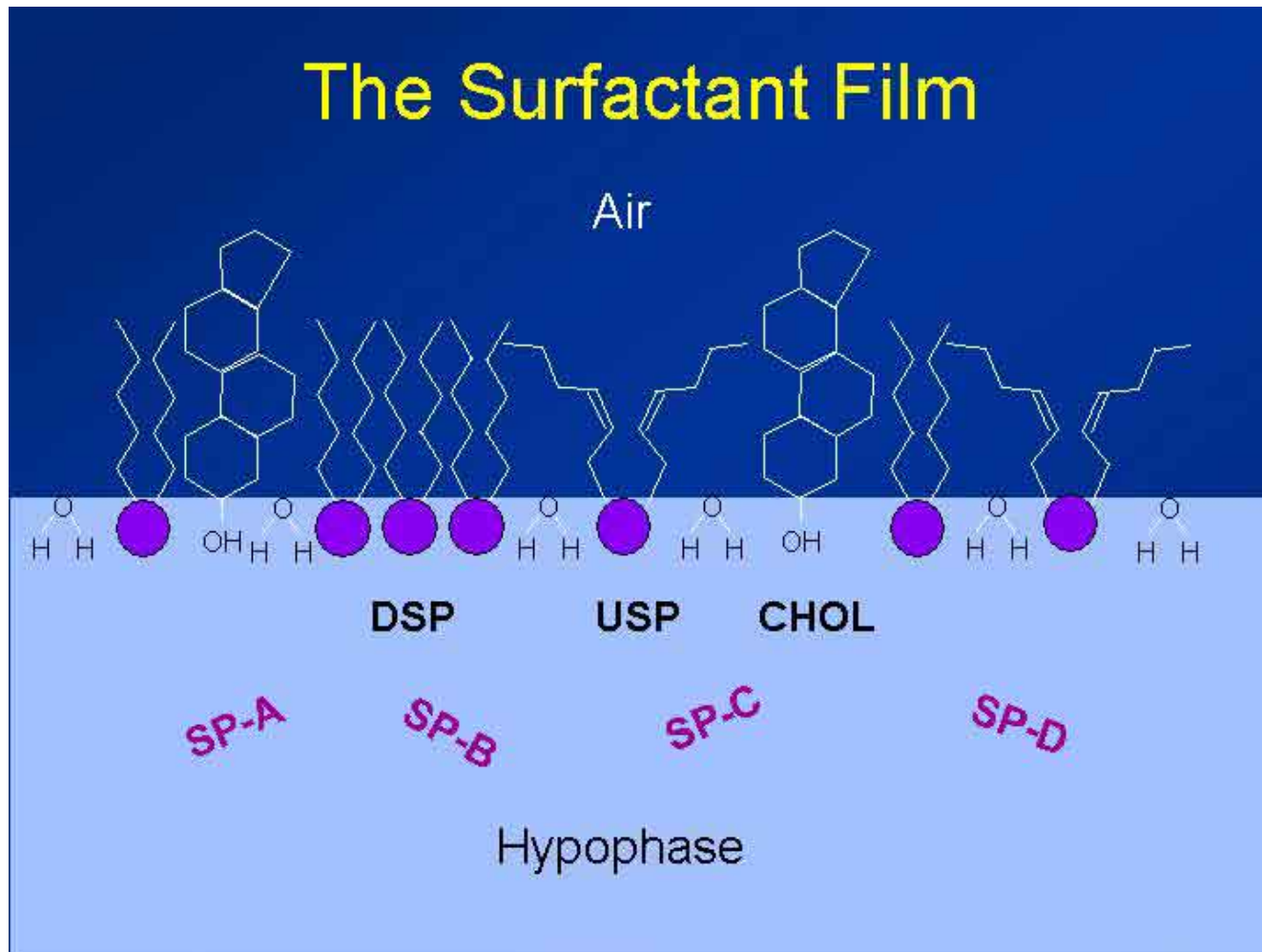
## The Alveolus

- Alveoli are lined with an aqueous hypophase
- The hypophase generates a high surface tension, which threatens lung function
- Type II cells produce pulmonary surfactant



<http://www.science.org.au/events/frontiers2003/orgeig.htm>

# LUNG SURFACTANTS



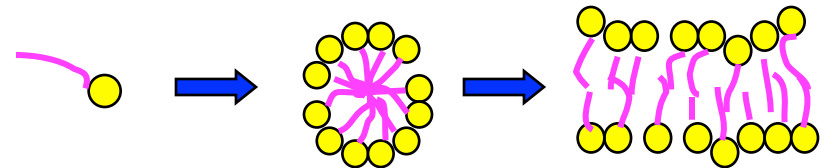
<http://www.science.org.au/events/frontiers2003/orgeig.htm>

# OTHER TYPES OF SELF ASSEMBLY



# VARIOUS TYPES OF SA IN SOLVENTS

I. **hydrophobic effect** → surfactant molecules



→ Protein aggregation

II. **attractive  $\pi$ - $\pi$  interactions** → typically aromatic rings with delocalized  $\pi$  -orbitals

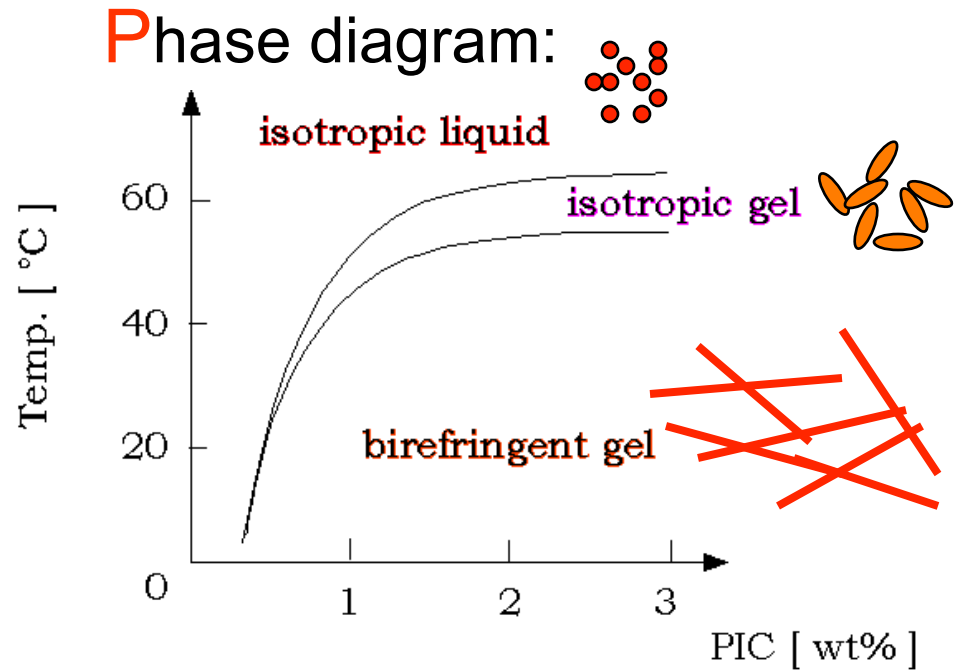
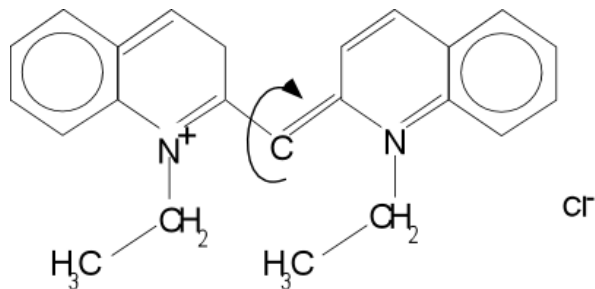
III. **H-bridges in DNA**





# ATTRACTIVE $\Pi$ - $\Pi$ INTERACTIONS

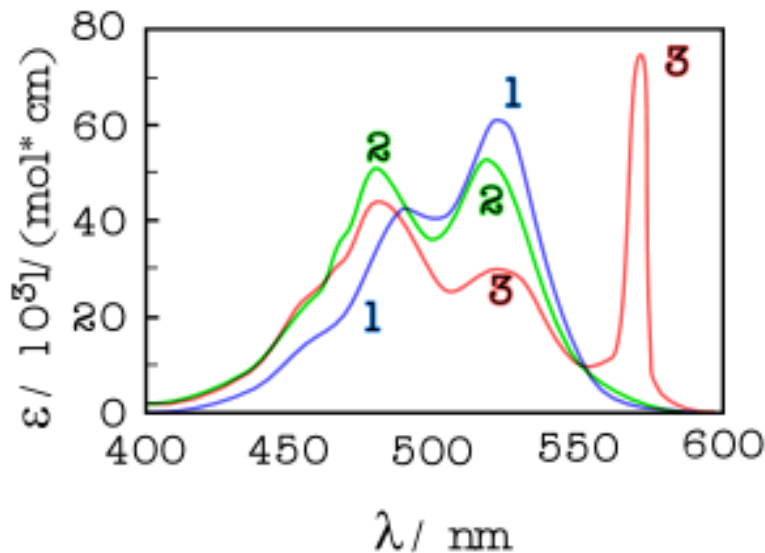
- **PIC** pseudoisocyanine chloride



# J AGGREGATES



- shift the adsorption band towards longer  $\lambda$  (H-aggregates  $\rightarrow$  shift to smaller **wavelengths**)



## UV/Vis-spectrometry:

1.  $8.6 \times 10^{-6}$  mol/l,  $25^\circ\text{C}$   $\rightarrow$  monomers
2.  $8.6 \times 10^{-4}$  mol/l,  $25^\circ\text{C}$   $\rightarrow$  mono + dimers
3.  $1.08 \times 10^{-2}$  mol/l,  $31^\circ\text{C}$   $\rightarrow$  dimers + **J**-aggregates



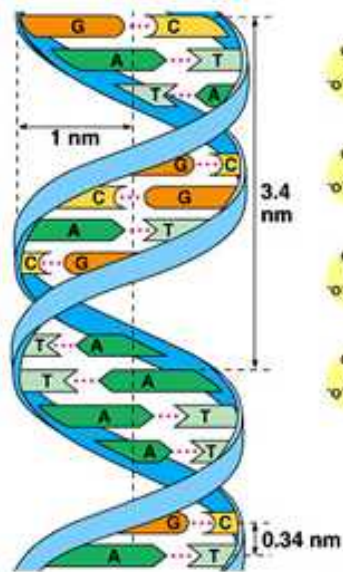
Light harvesting complex II viewed from above, showing chlorophyll and carotenoid pigments

<http://www.steve.gb.com/science/photosynthesis.html>

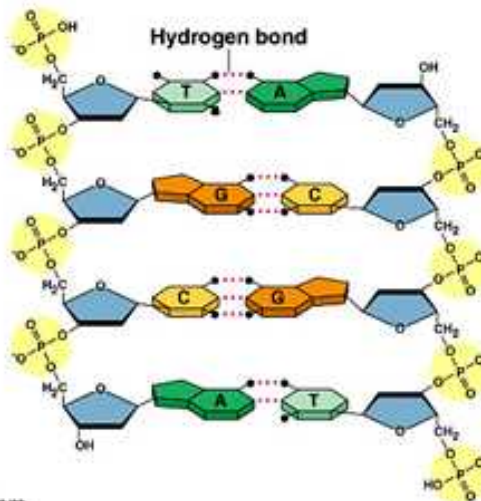
Next time

# DNA

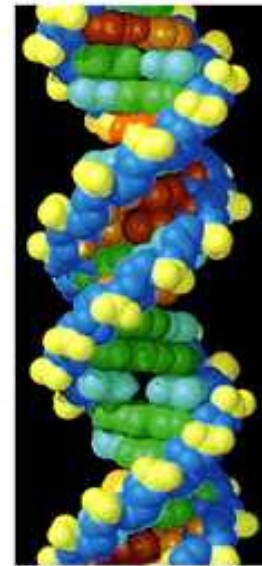
## A SELECTIVE & REVERSIBLE GLUE



(a)



(b)



(c)

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# Questions?

